

# Chlorine Decay Modeling and Water Age Predictions

Marvin Gnagy, P.E., President



PMG Consulting, Inc.

OTCO Water Workshop

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# Agenda

- Residual Decay in Water
- Experimental Data Collection
- Data Evaluations
- Adjustment for Temperature Variations
- Decay Model Development
- Applications for Decay Evaluations
- Water Age Predictions for Water Systems
- Questions

# Residual Decay in Water

- Residual decay generally follows first order reaction

$$C_t = C_o e^{-kt}$$

$C_t$  = concentration at time t

$C_o$  = initial concentration

$k$  = residual decay coefficient

$t$  = decay time in days

- Calculate decay coefficient ( $k$ ) from experimental data using reaction equation
- Decay models developed using identified coefficients for free chlorine, total chlorine, and monochloramine

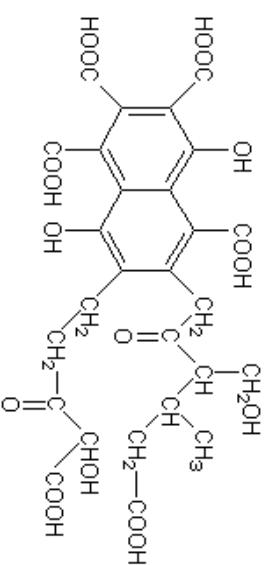


# Decay Coefficients

- Decay coefficient ( $k$ ) contains 2 components
  - $k_t = k_b + k_w$
  - $k_w$  - decay coefficient pipe wall
  - $k_b$  - decay coefficient bulk water
- $k_w$  impacted by contact at pipe wall and presence of biofilms, deposits, corrosion materials
- $k_b$  affected by demand-causing substances in distribution system (water quality)
- $k_t$  dependent on water quality and pipe conditions, site specific

# Items Influencing Residual Decay

- Initial residual concentration
- Equilibrium reactions
- Residual half-life
- Water temperature
- Water pH
- Presence of reducing substances
- Water age or residence time
- S/V ratio (surface to volume ratio in pipelines, tanks)



# Equilibrium reactions

- Changes residual concentrations based on pH and temperature variations

- Free chlorine

$$K_i = \frac{[H^+][OCl^-]}{[HOCl]} \quad HOCl = \frac{[H^+][OCl^-]}{K_i}$$

- Hypochlorous acid (HOCl) and hypochlorite ion (OCl<sup>-</sup>) remain in solution, but their content may change with pH and temperature according to solubility relationships based on equilibrium chemistry

- Monochloramine

- Equilibrium chemistry can shift monochloramine levels by simple pH and temperature changes

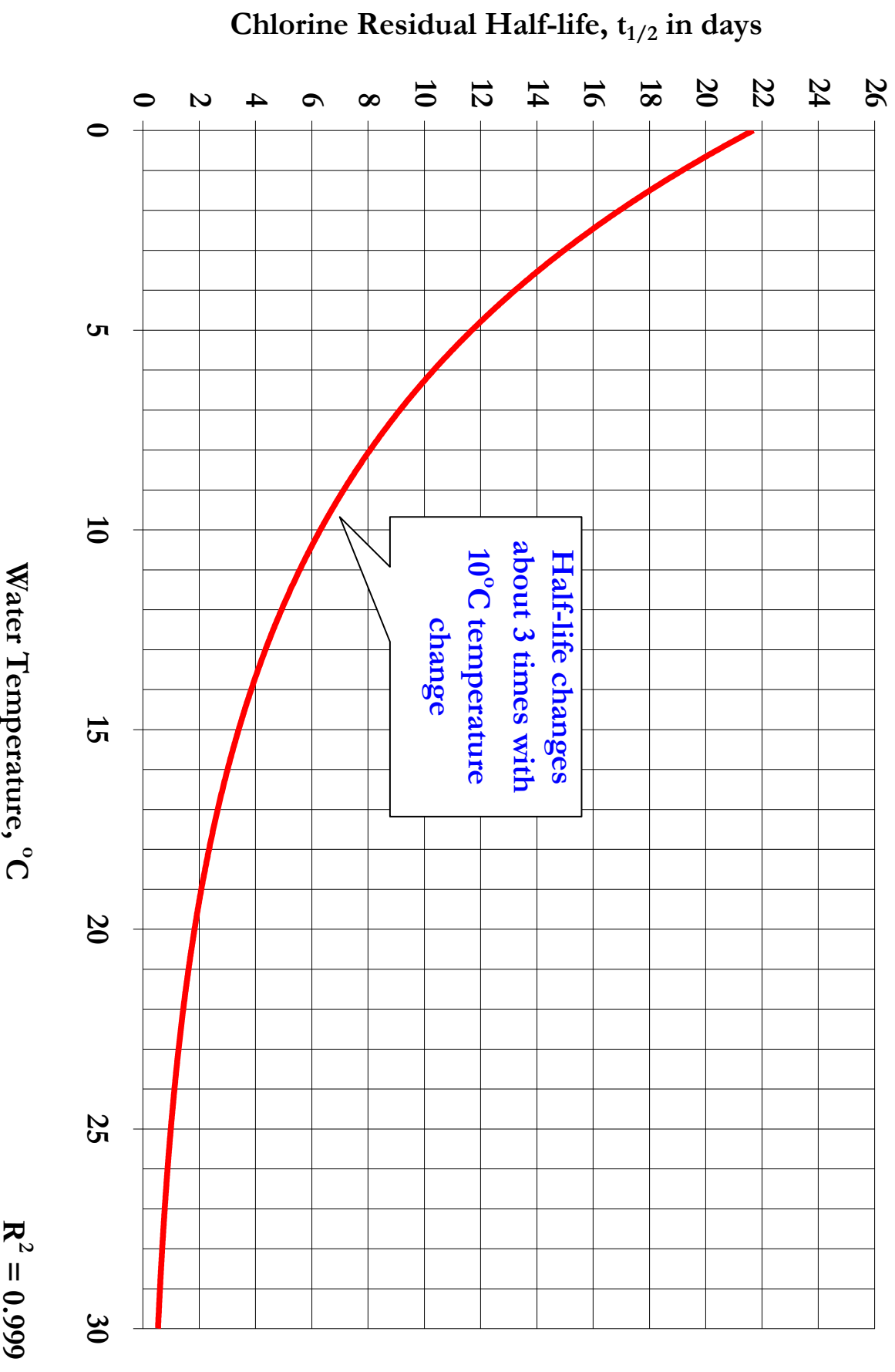


# Residual half-life

- Residual reduces according to half-life reactions for the type of residual
  - $1/2$  concentration reduction each half-life
- Results in depletion over time in distribution and storage



# Residual half-life (free chlorine)

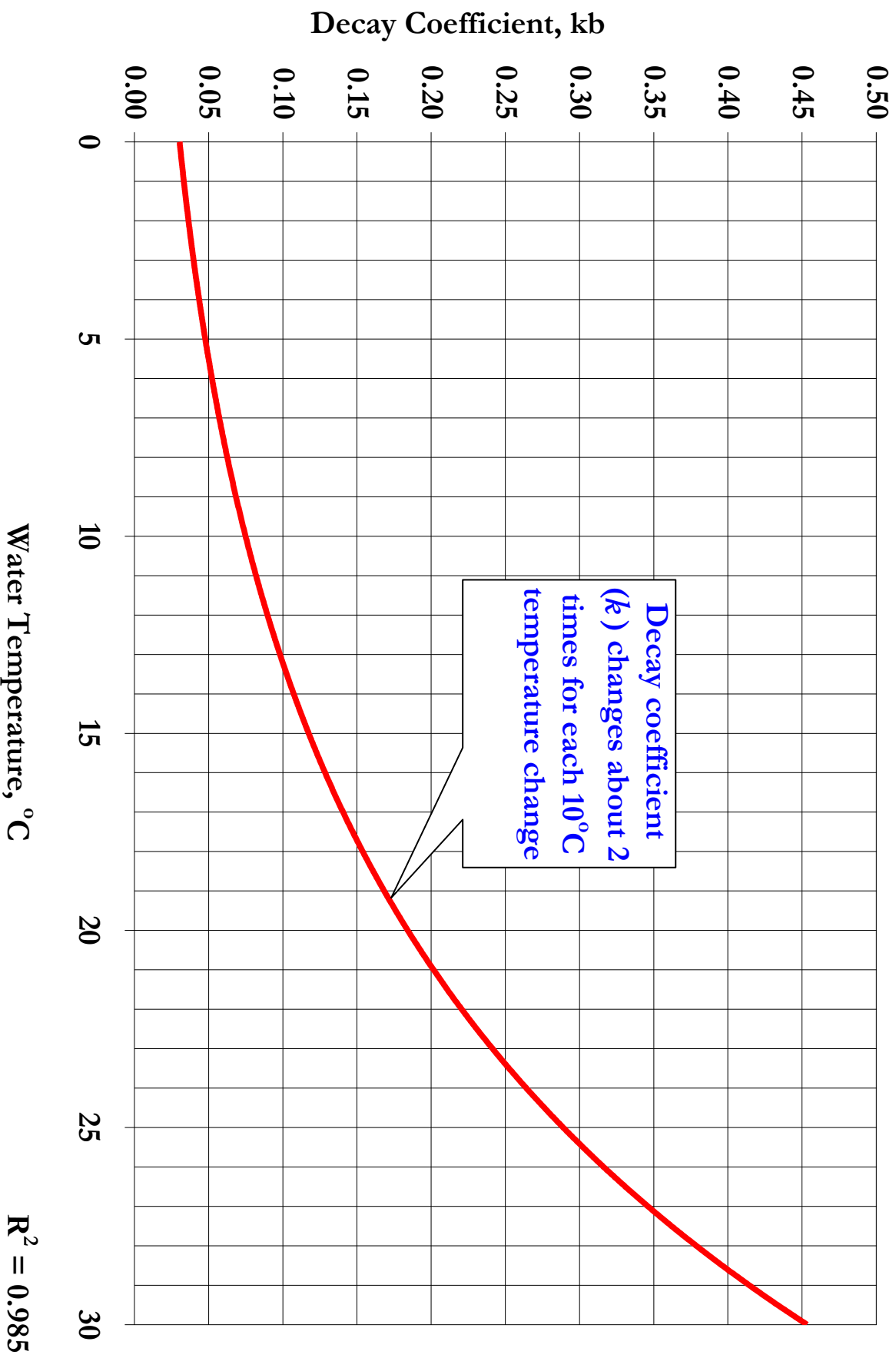




## Water temperature impacts

- Generally two fold change  $k$  each 10°C change in temperature
- Affects  $k$  and residual decay reactions
- Temperature affects type of free chlorine residual (HOCl or OCl<sup>-</sup>)
  - Equilibrium impacts for free chlorine and monochloramine shown earlier
- Increasing temperature increases auto-decomposition of chloramine residuals

# Water temperature impacts

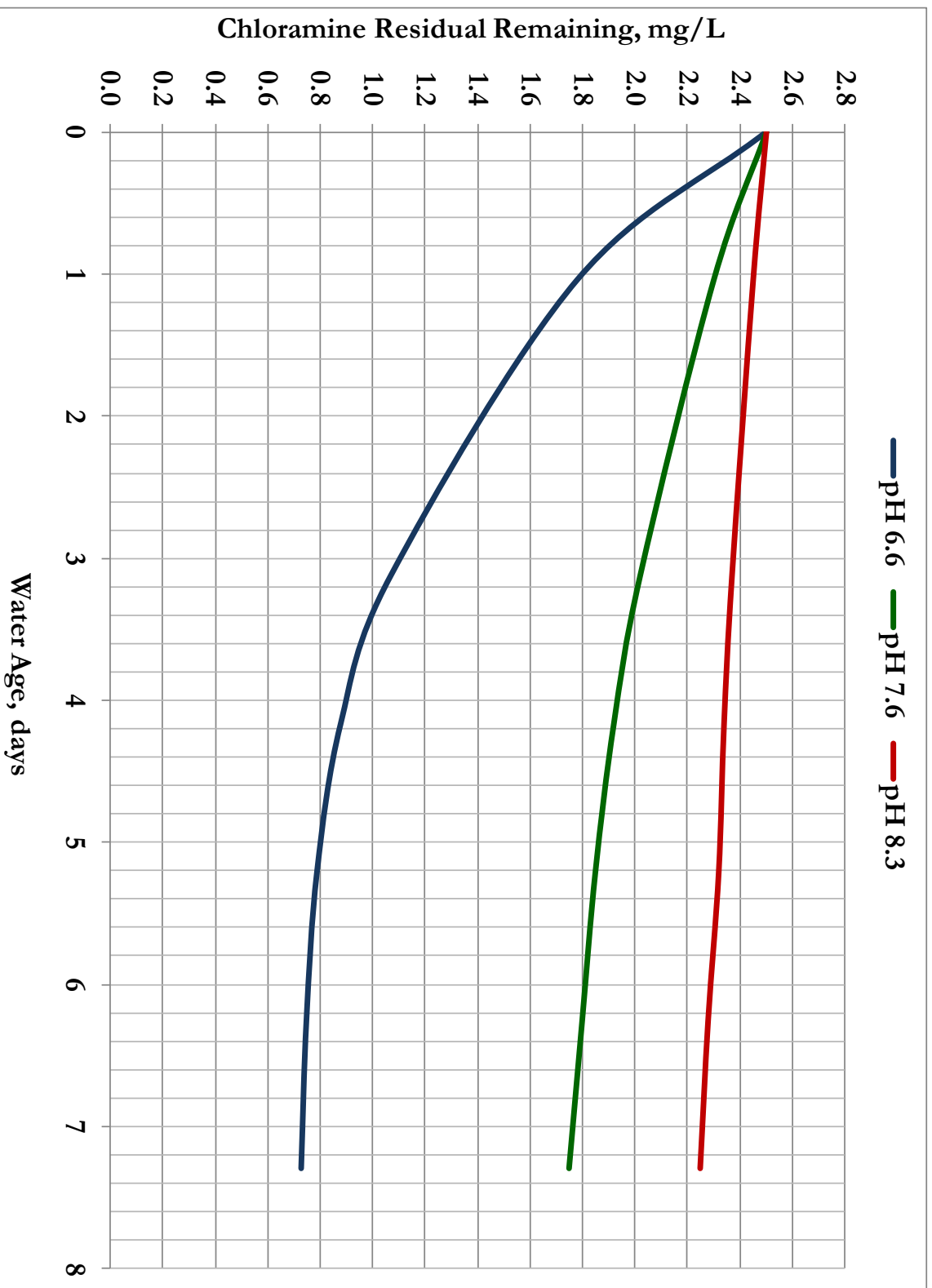


# Water pH effects

- pH affects type of residual based on equilibrium
  - Free chlorine ( $\text{HOCl}$  or  $\text{OCl}^-$ )
  - Monochloramine balance with ammonia and free chlorine
- Decay of system residuals dependent on pH level and type of residual
  - pH levels above 8 slow auto-decomposition of chloramine residuals
  - pH levels above 8 predominantly  $\text{OCl}^-$  rather than  $\text{HOCl}$



# Water pH effects

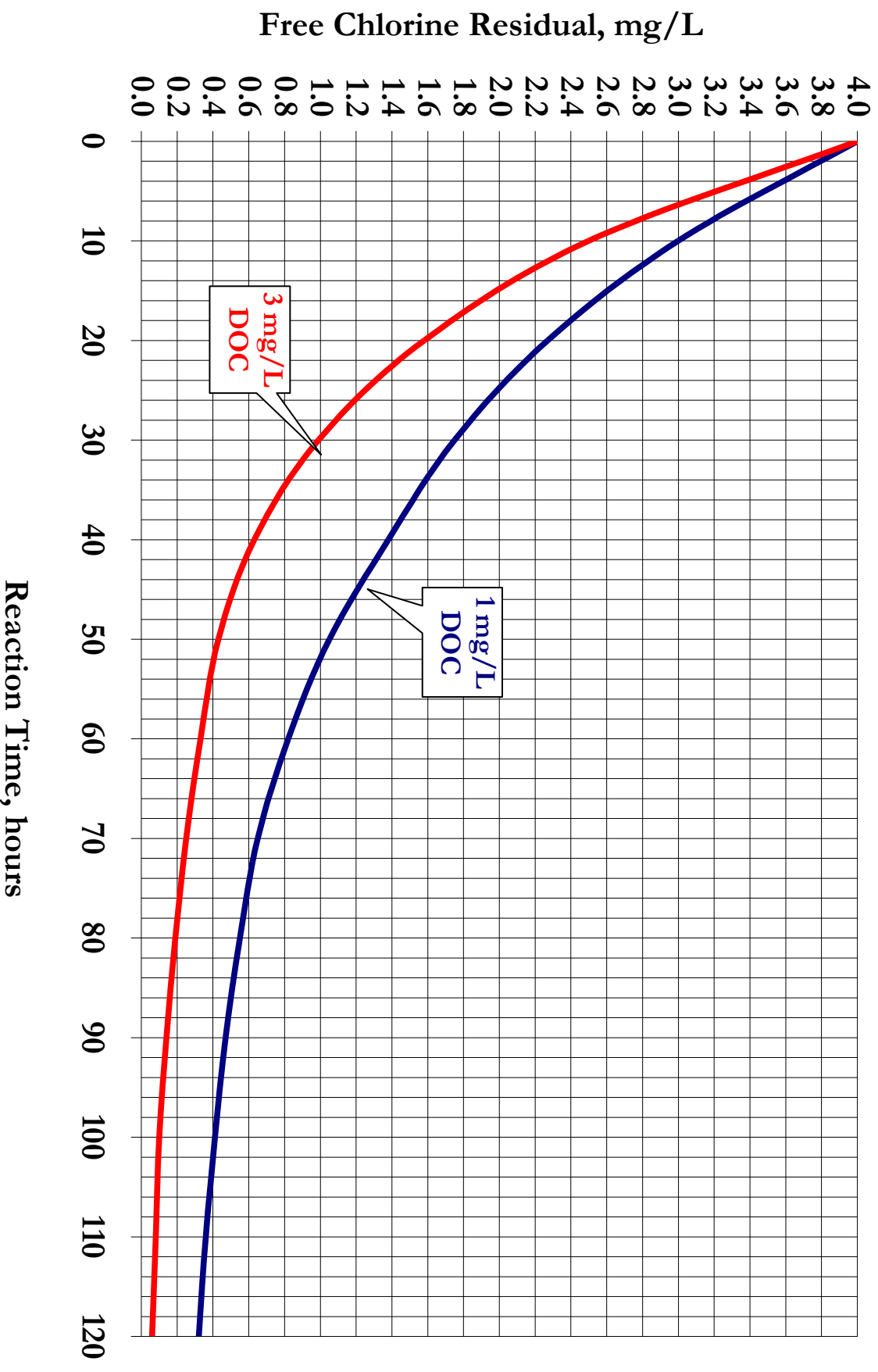


# Reducing substances

- **Water quality parameters cause depletion of residual**
  - Iron, manganese, ammonia, sulfides, bromide, organic matter, nitrite, cyanide
- **Reactions at pipe wall cause depletion of residual**
  - Pipe Deposits
  - Corrosion Reactions
  - Biofilms



# Reducing substances - DOC



# Water age / residence time

- **Most significant effects on residual decay**
  - Exponent in first order reaction
  - Longer residence time reduces residuals
    - More reaction time with reducing substances
    - More decay reaction based on time
    - More reaction with pipe wall materials
  - Water storage affects water age and residence times
- Affects water temperature variations in storage tanks
  - Water temperature impacts given earlier
  - Stagnant water conditions erode residual concentrations



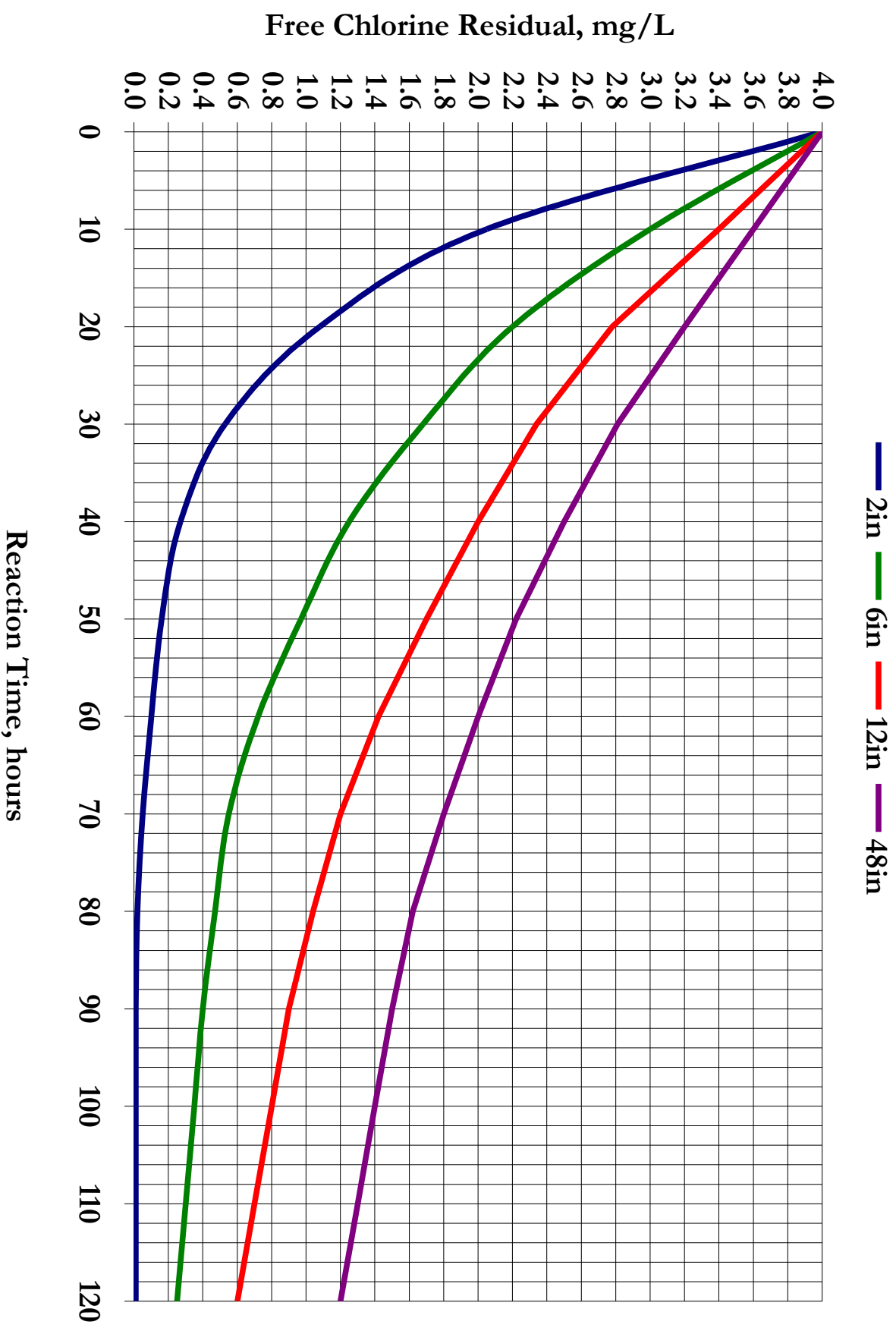
# S/V ratio

- Affects volume of water reacting with pipe wall or tank wall
- Smaller diameter increases bulk volume of water contacting pipe surface
  - Increases residual decay ( $k_{r(w)}$ )
- Affected by flow velocity
- Increased Reynolds number increases residual decay ( $k_{r(w)}$ )
- Affects volume to surface area ratio in pipelines increasing decay ( $k_{r(w)}$ )

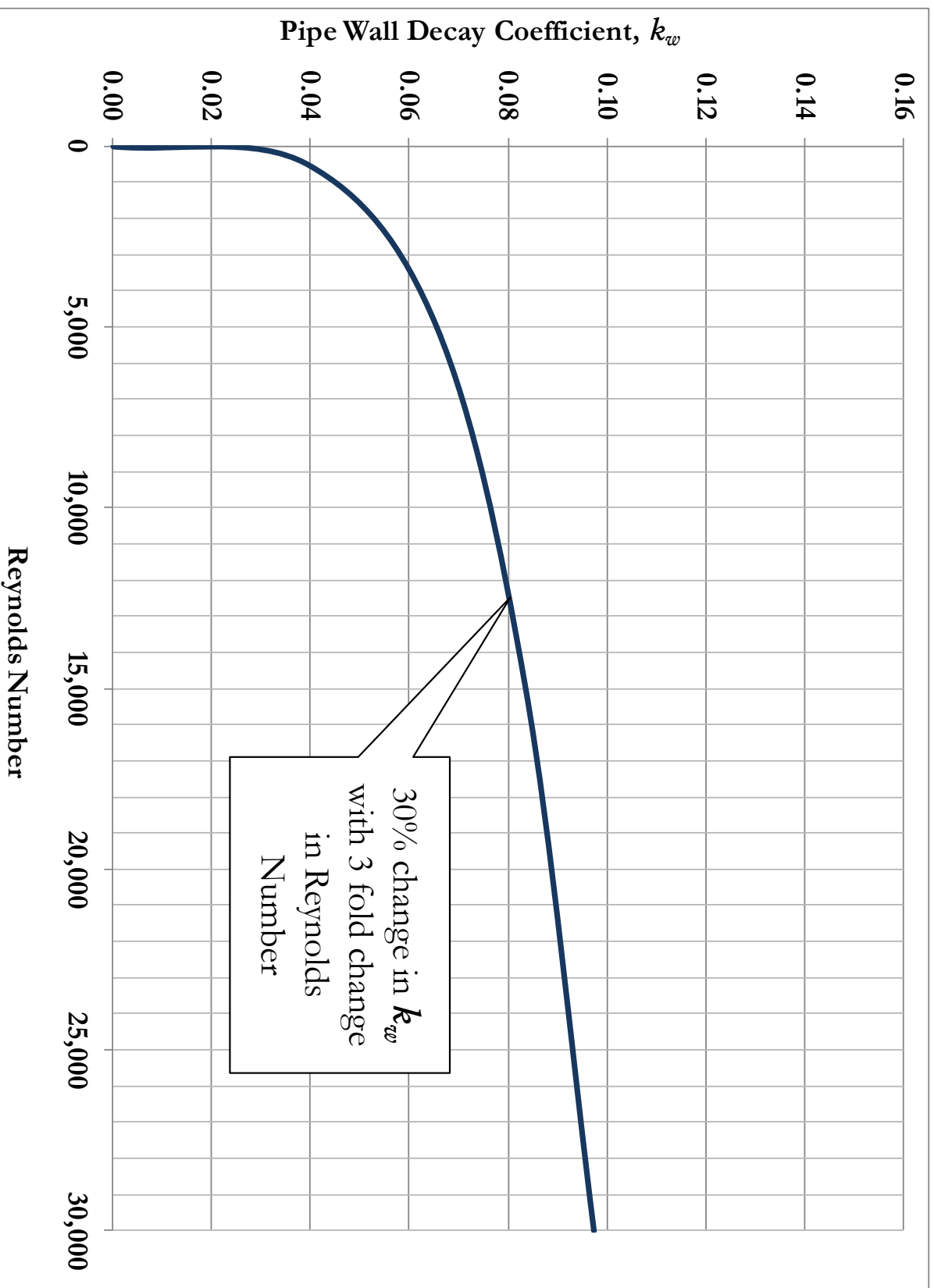




# S/V ratio



# Flow velocity effects



# Experimental Data Collection

# Experimental Data Collection

- **Representative sample with known residual concentration**
  - Plant tap collected for experimental evaluation
    - Single sample for entire test period
    - May need to spike sample with disinfectant for evaluation
  - Glass container, brown or amber
    - Rinsed with chlorine and lab water to remove demand on container wall
    - Dried prior to decay evaluation testing
    - Stored in dark conditions
  - Sample capped to simulate pipe conditions
    - No evaporation or off gassing
- Maintained at room temperature or incubator controlled

# Daily observations

- Time, temperature, residual concentration
  - Record observations at nearly same time each day
- Conduct decay testing until maximum residence time achieved
  - Estimate of water system residence time (8 days to 21 days common)
    - OR -
  - Until residual falls below 0.2 mg/L free chlorine or 1.0 mg/L total chlorine
- Record observations for evaluation and  $k$  determination

# Data Evaluations

Day 0	1.82
Day 1	1.37
Day 2	1.01
Day 3	0.76
Day 4	0.58
Day 5	0.42
Day 6	0.34
Day 7	0.24
Day 8	0.19

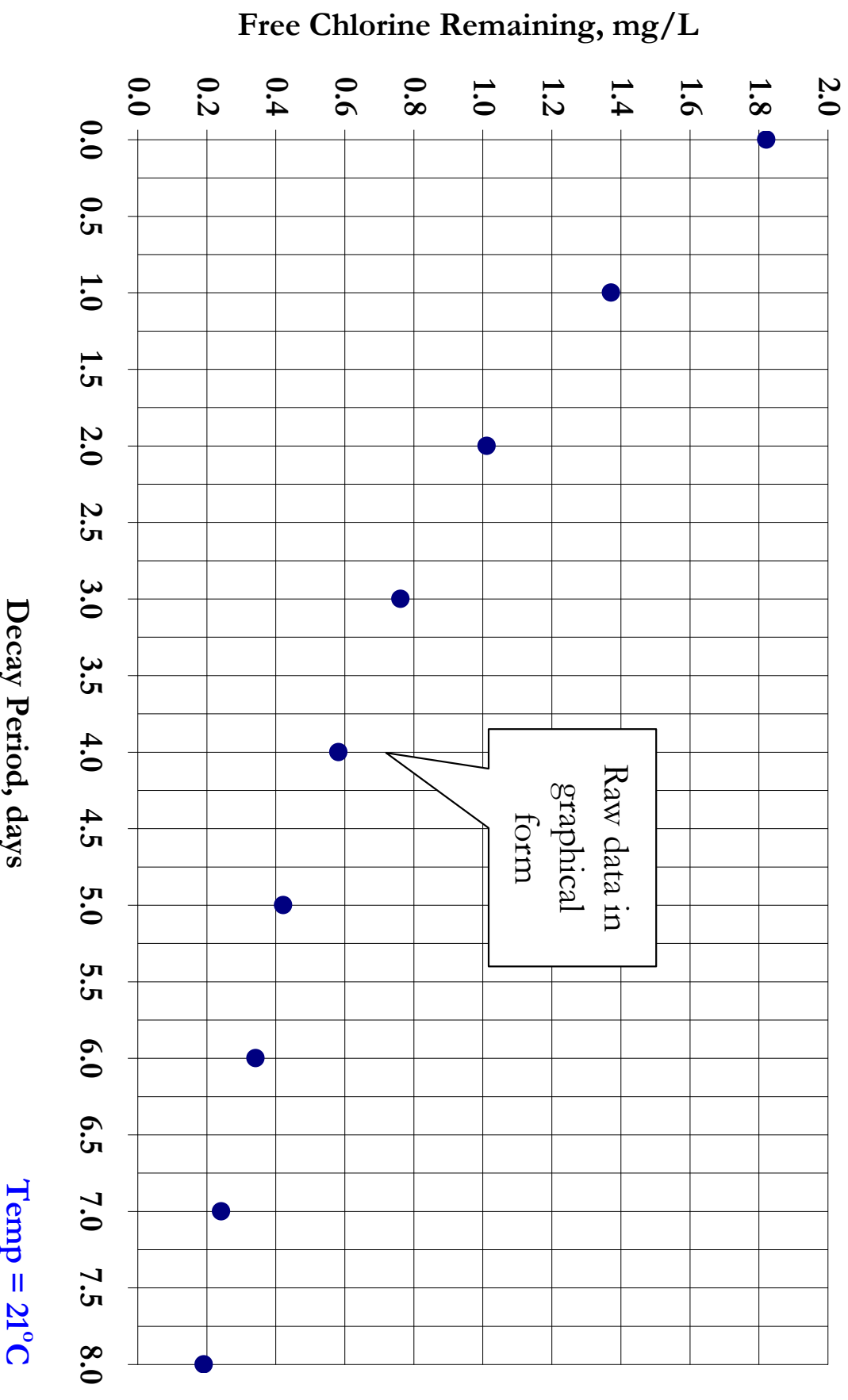
## Water System A

- Free chlorine decay for 8 days (max residence time)
- Graph data in Excel™
  - Select scatter graph
  - Add trend line to data points
  - Select exponential graph type
  - Display equation and R<sup>2</sup> options
- Determine decay coefficient ( $k$ ) from equation

$$C_t = C_o e^{(-kt)}$$

# Water System A

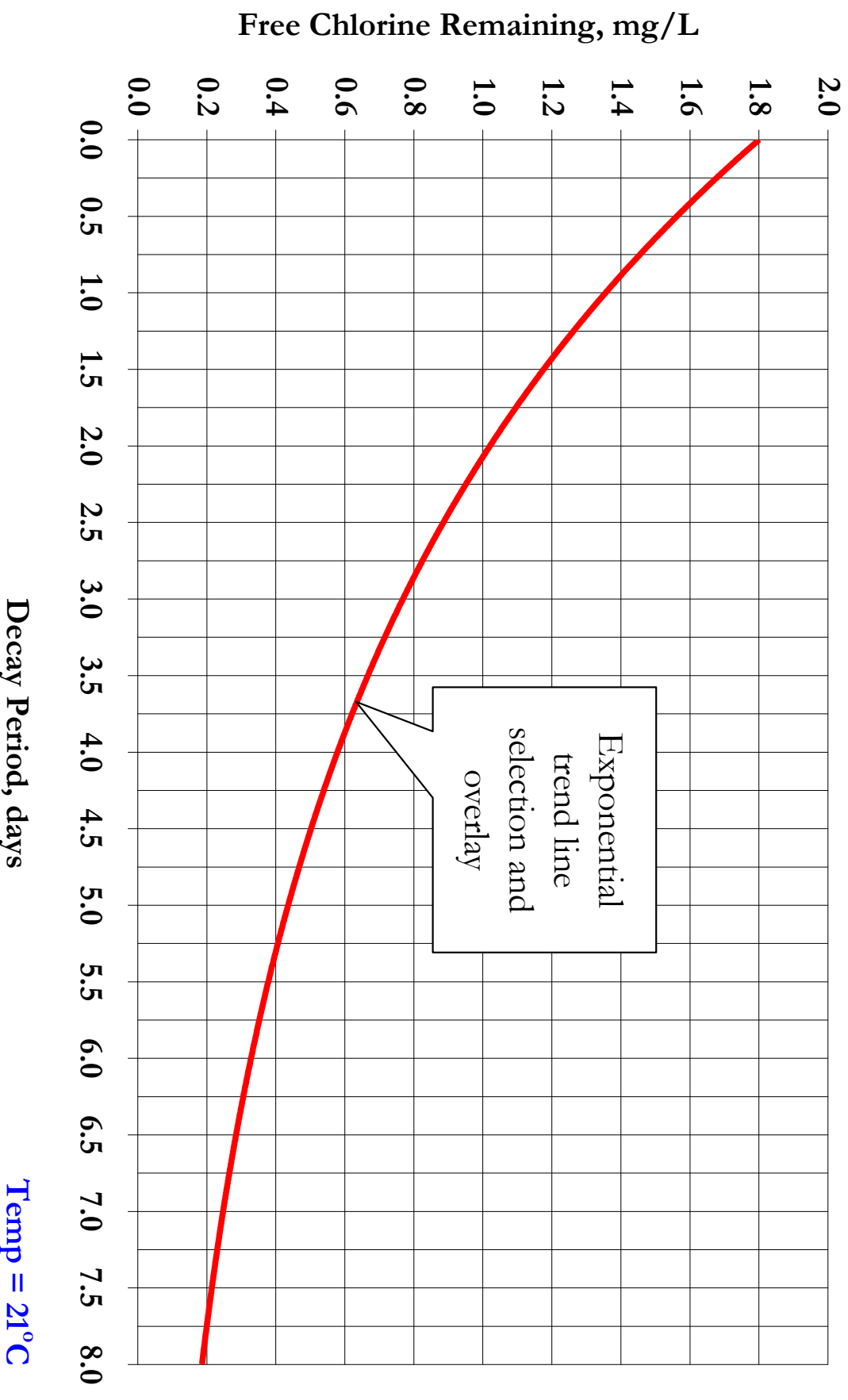
## Water System A





# Water System A

Water System A

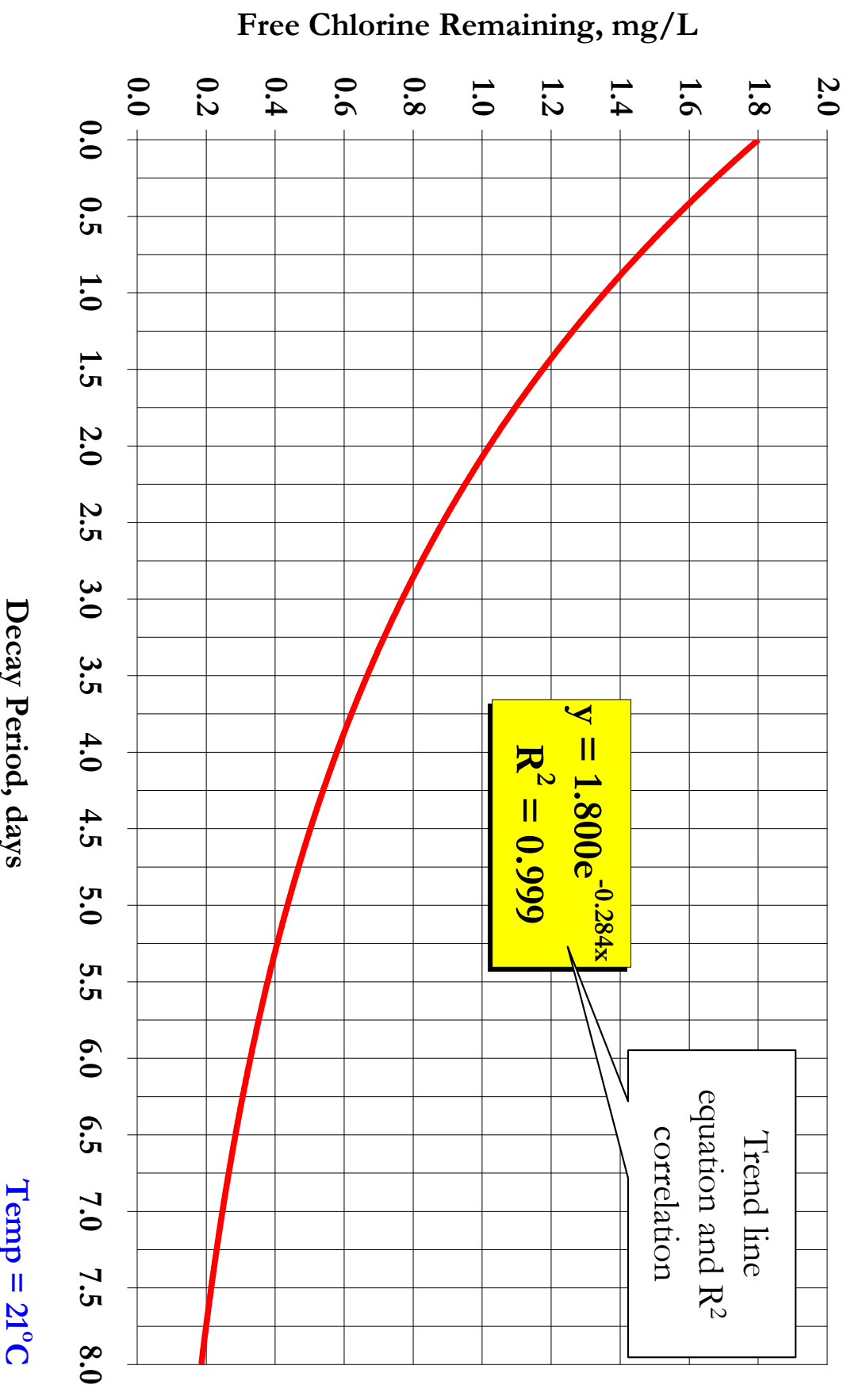


Decay Period, days

Temp = 21°C

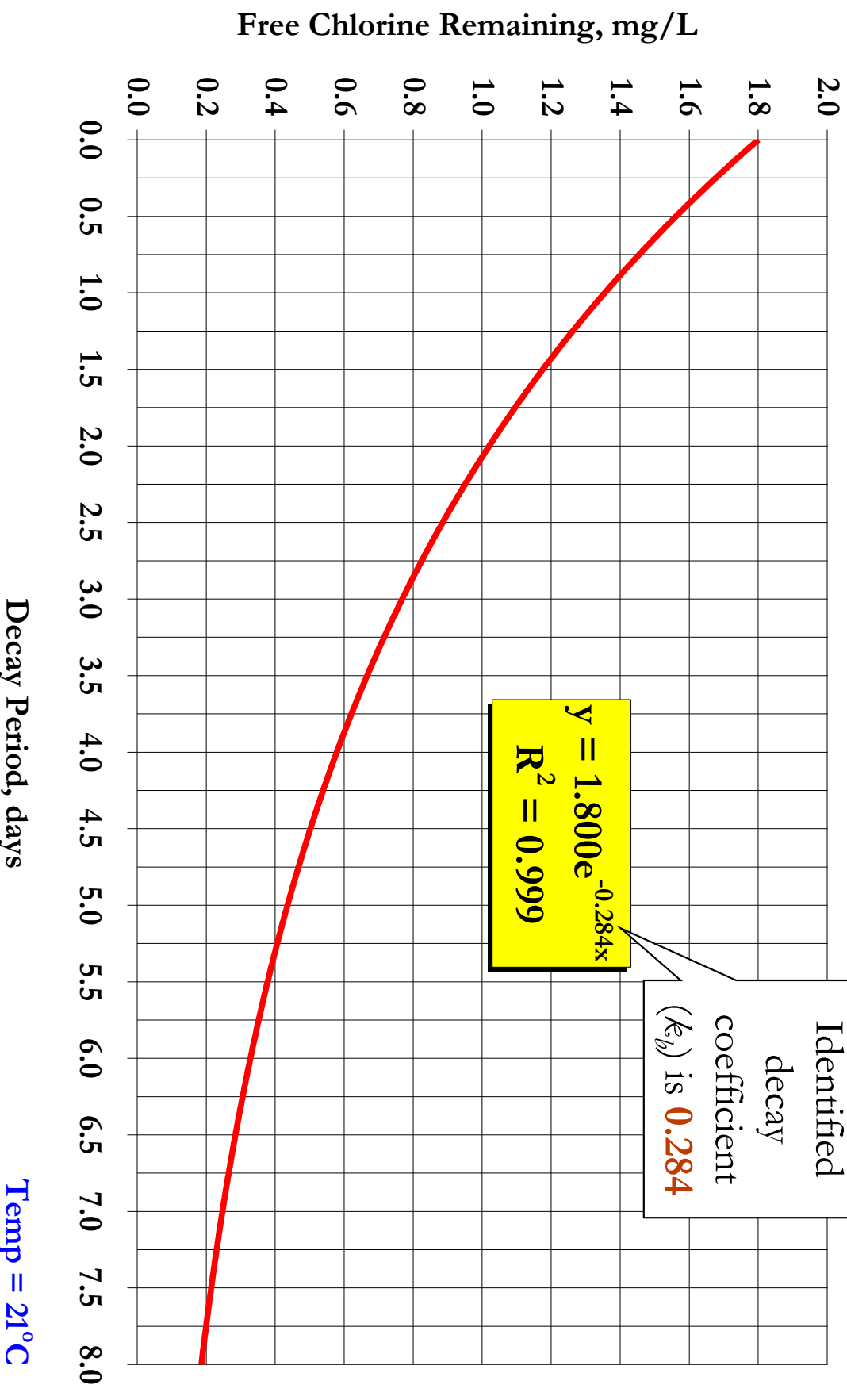
# Water System A

Water System A



# Water System A

Water System A



Day 0	3.05	Day 11	2.20
Day 1	2.70	Day 13	2.15
Day 3	2.55	Day 15	2.05
Day 5	2.45	Day 17	2.00
Day 7	2.38	Day 19	1.95
Day 9	2.30	Day 21	1.90

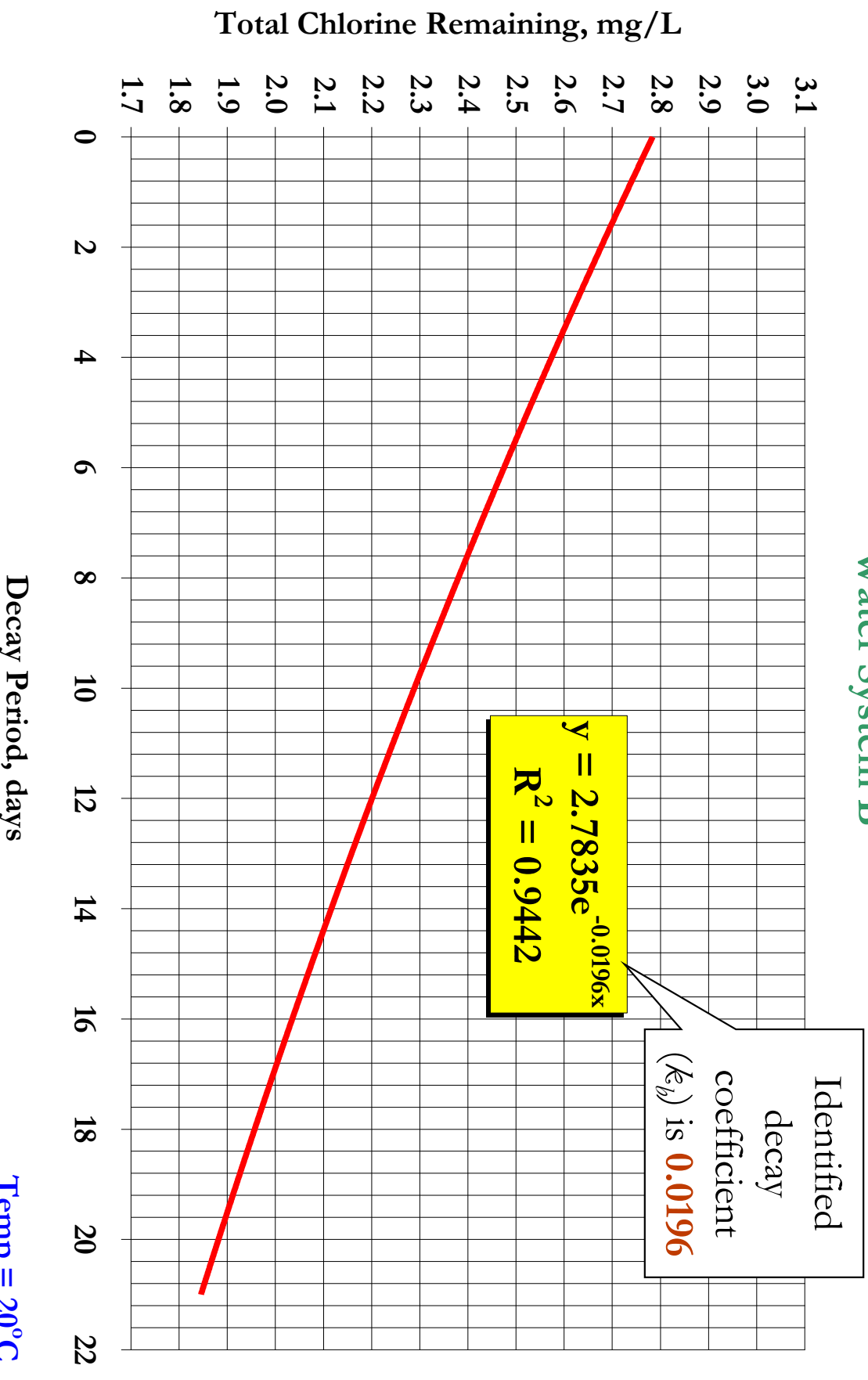
## Water System B

- Total chlorine decay for 21 days (depletion minimized)
- Graph data in Excel™
  - Select scatter graph
  - Add trend line to data points
  - Select exponential graph type
  - Display equation and R<sup>2</sup> options
- Determine decay coefficient ( $k$ ) from equation

$$C_t = C_o e^{(-kt)}$$

# Water System B

Water System B



Day 0	3.6	Day 12	1.90
Day 2	3.3	Day 14	1.80
Day 4	2.9	Day 16	1.7
Day 6	2.6	Day 18	1.7
Day 8	2.3		
Day 10	2.1		

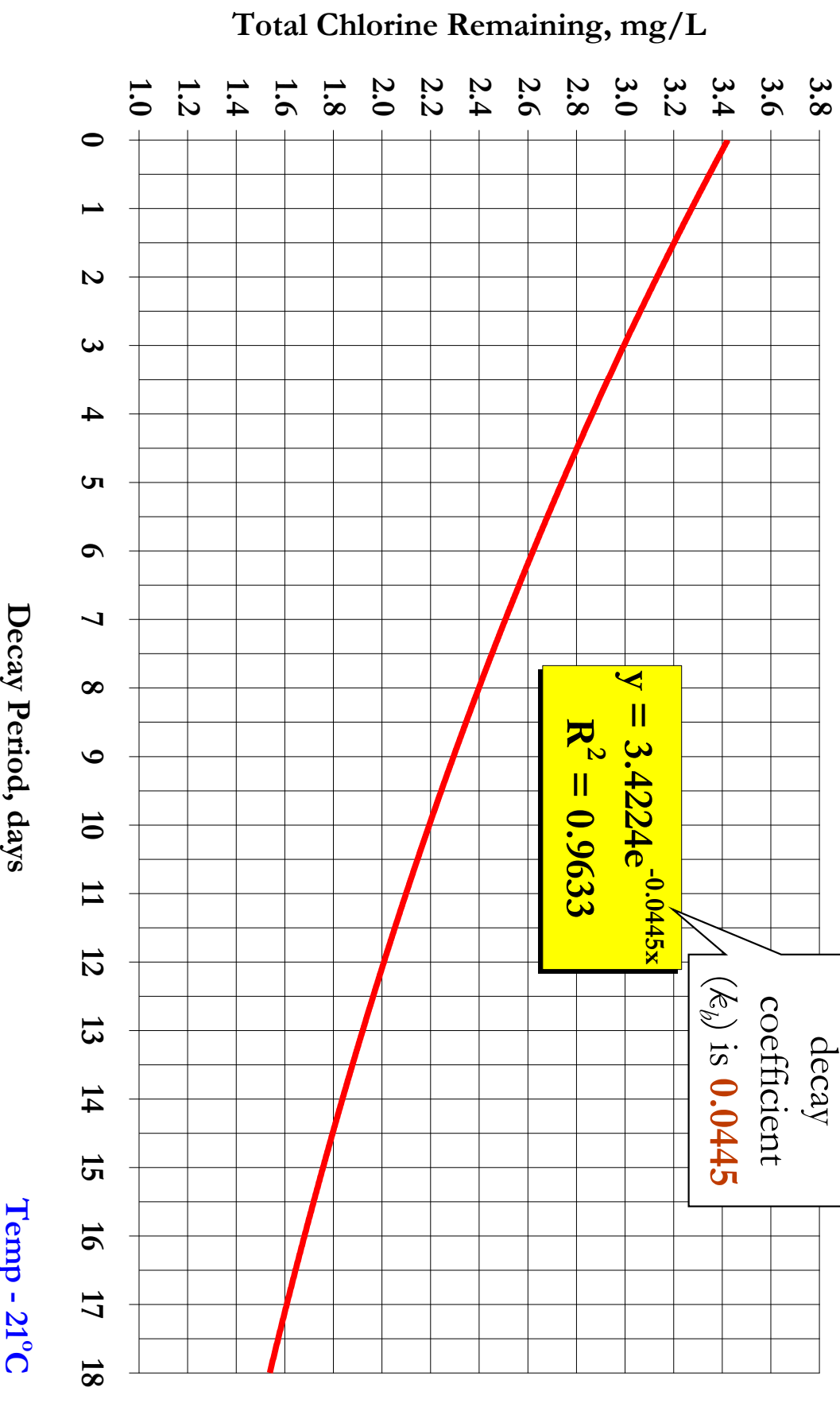
## Water System C

- Total chlorine decay for 19 days (depletion minimized)
- Graph data in Excel™
  - Select scatter graph
  - Add trend line to data points
  - Select exponential graph type
  - Display equation and R<sup>2</sup> options
- Determine decay coefficient ( $k$ ) from equation

$$C_t = C_o e^{(-kt)}$$

# Water System C

Water System C



Day 0	2.17	Day 10	1.23
Day 1	1.94	Day 12	1.12
Day 2	1.86	Day 14	1.08
Day 4	1.62	Day 15	1.07
Day 6	1.40		
Day 8	1.34		

## Water System D

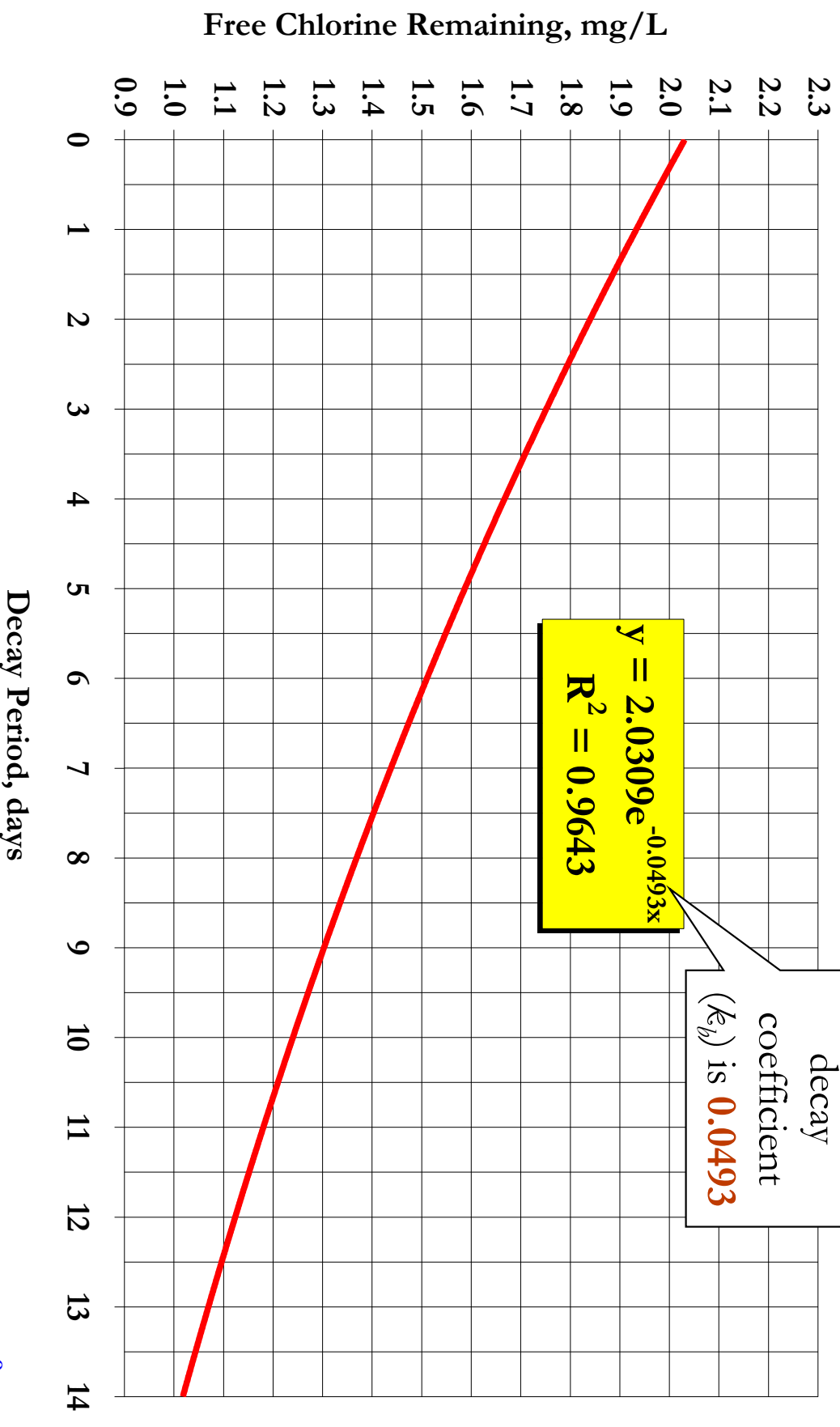
- Free chlorine decay for 15 days (depletion minimized)
  - Sample spiked with NaOCl
- Graph data in Excel™
  - Select scatter graph
  - Add trend line to data points
  - Select exponential graph type
  - Display equation and R<sup>2</sup> options
- Determine decay coefficient ( $k$ ) from equation

$$C_t = C_o e^{(-kt)}$$



# Water System D

Water System D



# Adjustment for Temperature Variations

# Water temperature changes

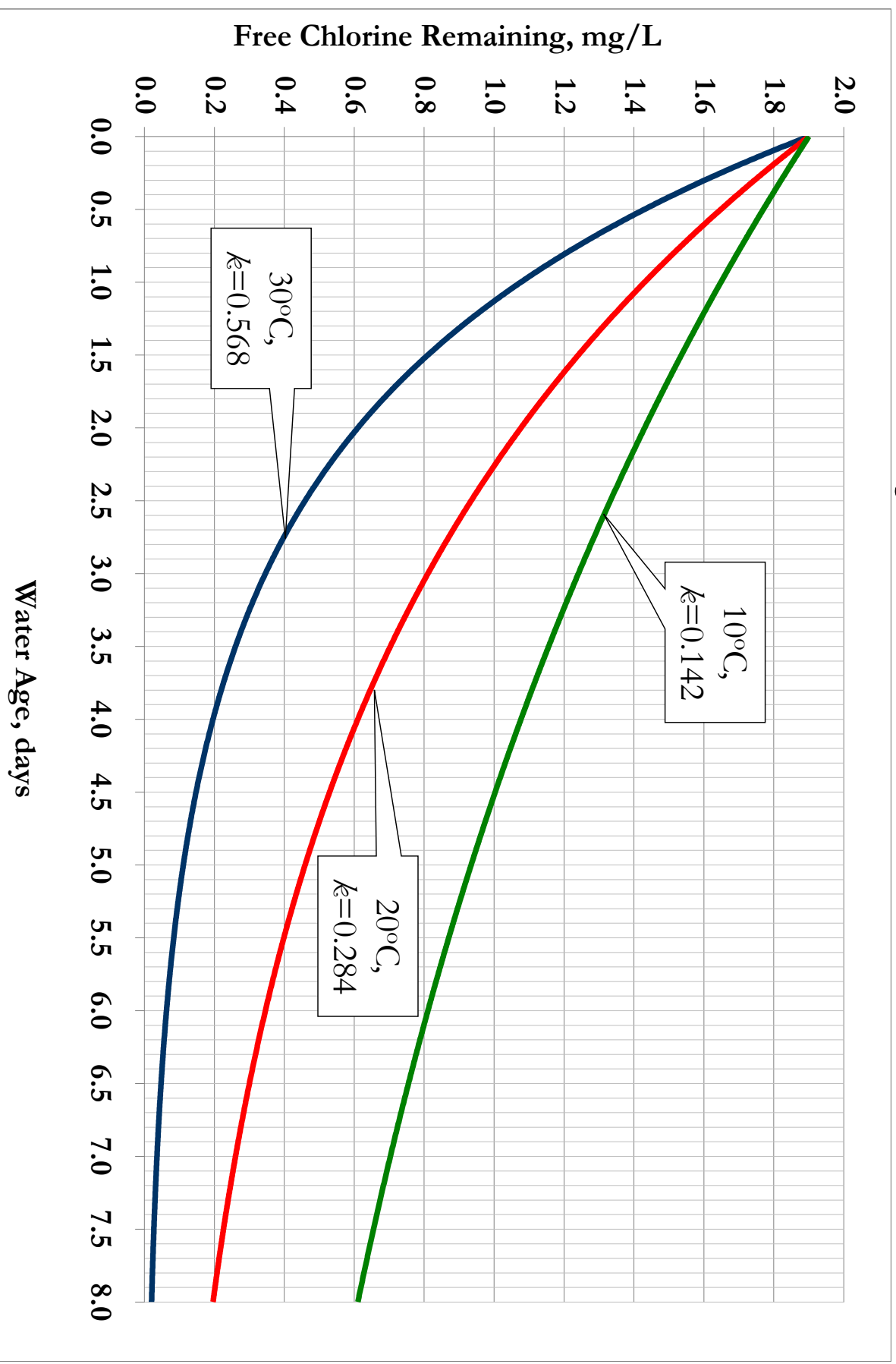
- $k$  changes by factor of 2 each 10°C change in temperature
  - Each 1°C changes  $k$  about 10%
    - Increasing temperature increases  $k$
    - Decreasing temperature decreases  $k$
  - Calculate  $k$  at various temperatures to bracket range of water temperatures experienced in distribution
- Initial experimental data System B
  - $k = 0.0196$  @20°C
  - 10°C - 0.0098
  - 20°C - **0.0196**
  - 30°C - 0.0392

# Water temperature changes

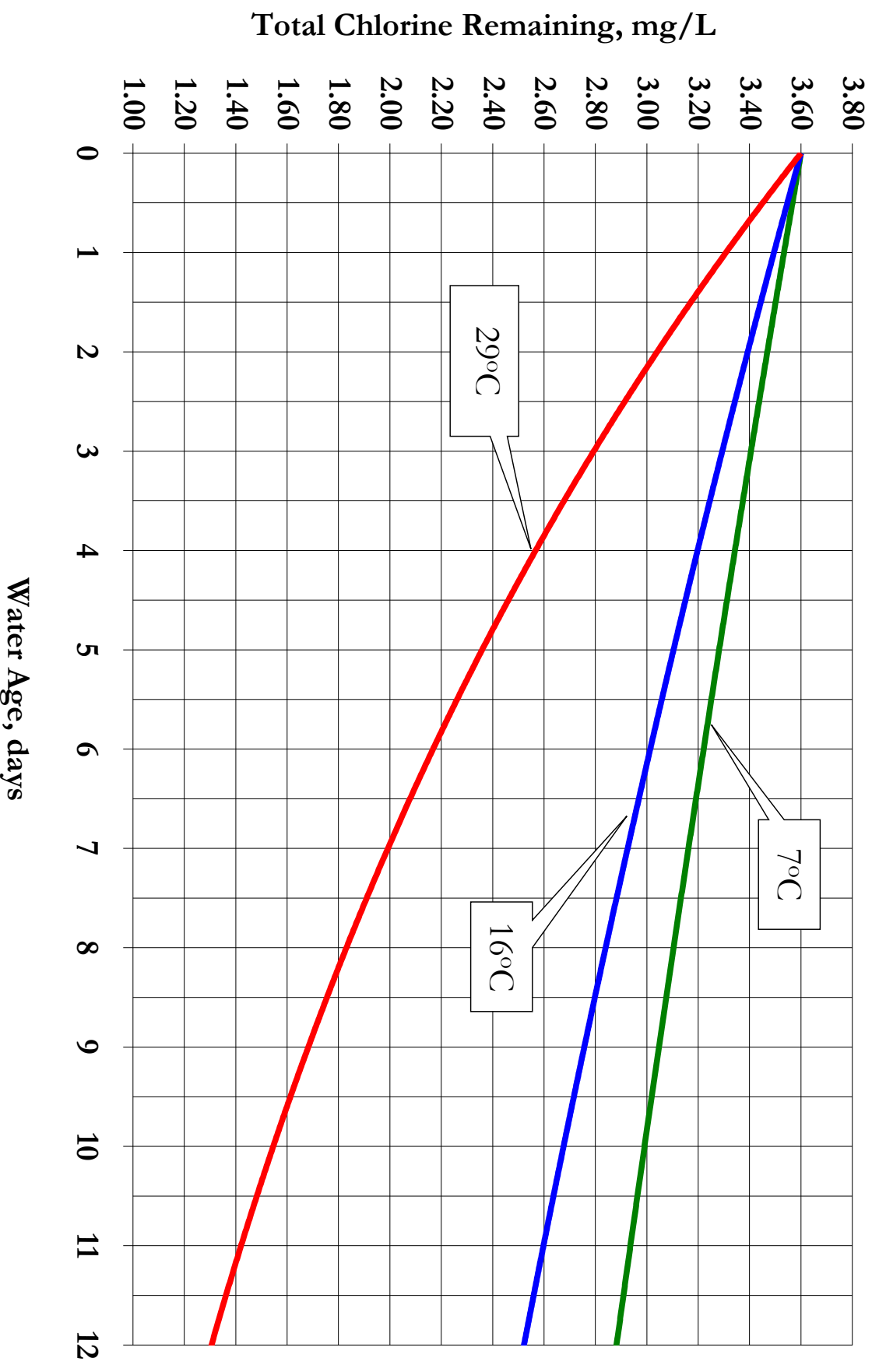
- $k$  changes by factor of 2 each 10°C change in temperature
  - Each 1°C changes  $k$  about 10%
    - Increased temp increases  $k$
    - Decreased temp decreases  $k$
  - Calculate  $k$  at various temperatures to bracket range of water temperatures experienced in distribution system
- Initial experimental data System B
  - $k = 0.0196$  @20°C
  - 10°C - 0.0098
  - 20°C - **0.0196**
  - 30°C - 0.0392

3°C	0.0070	13°C	0.115
4°C	0.0073	14°C	0.122
5°C	0.0075	15°C	0.131
6°C	0.0078	16°C	0.140
7°C	0.0082	17°C	0.151
8°C	0.0085	18°C	0.163
9°C	0.0089	19°C	0.178
10°C	0.0098	<b>20°C</b>	<b>0.0196</b>
11°C	0.0103	21°C	0.0215
12°C	0.0109	22°C	0.0225

# Seasonal Decay Variations



# Seasonal Variations Water System C



# Decay Model Development

# Decay Model Development

- Using  $k$  values established decay calculations are made using first order equation
  - $k$  varies with temperature (lookup function in Excel™)
  - Bracket water age 0 days to  $\underline{X}$  days
  - Use typical initial residuals in plant effluent ( $t=0$ )
  - Bracket residual concentration variations
  - Insert equations for each residual and water age into table
- **Table becomes decay model for individual water systems**
  - Known water age predicts residual at that location
  - Known residual concentration predicts water age at that location
  - Predict tap residuals needed to meet minimum system residuals
    - Temperature variations often illustrate loss of residual due to decay reactions



# Example Decay Model Table

## Chlorine Decay Model

Temp, oC	21
k	<b>0.284</b>

mg/L Tap	Residence Time, Days															
	0.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0	4.5	5.0	5.5	6.0	6.5	7.0	7.5	8.0
<b>2.8</b>	2.43	2.11	1.83	1.59	1.38	1.19	1.04	0.90	0.78	0.68	0.59	0.51	0.44	0.38	0.33	0.29
<b>2.7</b>	2.34	2.03	1.76	1.53	1.33	1.15	1.00	0.87	0.75	0.65	0.57	0.49	0.43	0.37	0.32	0.28
<b>2.6</b>	2.26	1.96	1.70	1.47	1.28	1.11	0.96	0.83	0.72	0.63	0.55	0.47	0.41	0.36	0.31	0.27
<b>2.5</b>	2.17	1.88	1.63	1.42	1.23	1.07	0.93	0.80	0.70	0.60	0.52	0.45	0.39	0.34	0.30	0.26
<b>2.4</b>	2.08	1.81	1.57	1.36	1.18	1.02	0.89	0.77	0.67	0.58	0.50	0.44	0.38	0.33	0.29	0.25
<b>2.3</b>	2.00	1.73	1.50	1.30	1.13	0.98	0.85	0.74	0.64	0.56	0.48	0.42	0.36	0.32	0.27	0.24
<b>2.1</b>	1.82	1.58	1.37	1.19	1.03	0.90	0.78	0.67	0.59	0.51	0.44	0.38	0.33	0.29	0.25	0.22
<b>2.0</b>	1.74	1.51	1.31	1.13	0.98	0.85	0.74	0.64	0.56	0.48	0.42	0.36	0.32	0.27	0.24	0.21
<b>1.9</b>	1.65	1.43	1.24	1.08	0.93	0.81	0.70	0.61	0.53	0.46	0.40	0.35	0.30	0.26	0.23	0.20
<b>1.8</b>	1.56	<b>1.35</b>	1.18	1.02	0.88	<b>0.77</b>	0.67	0.58	0.50	<b>0.44</b>	0.38	0.33	0.28	0.25	0.21	<b>0.19</b>
<b>1.7</b>	1.47	1.28	1.11	0.96	0.84	0.73	0.63	0.55	0.47	0.41	0.36	0.31	0.27	0.23	0.20	0.18

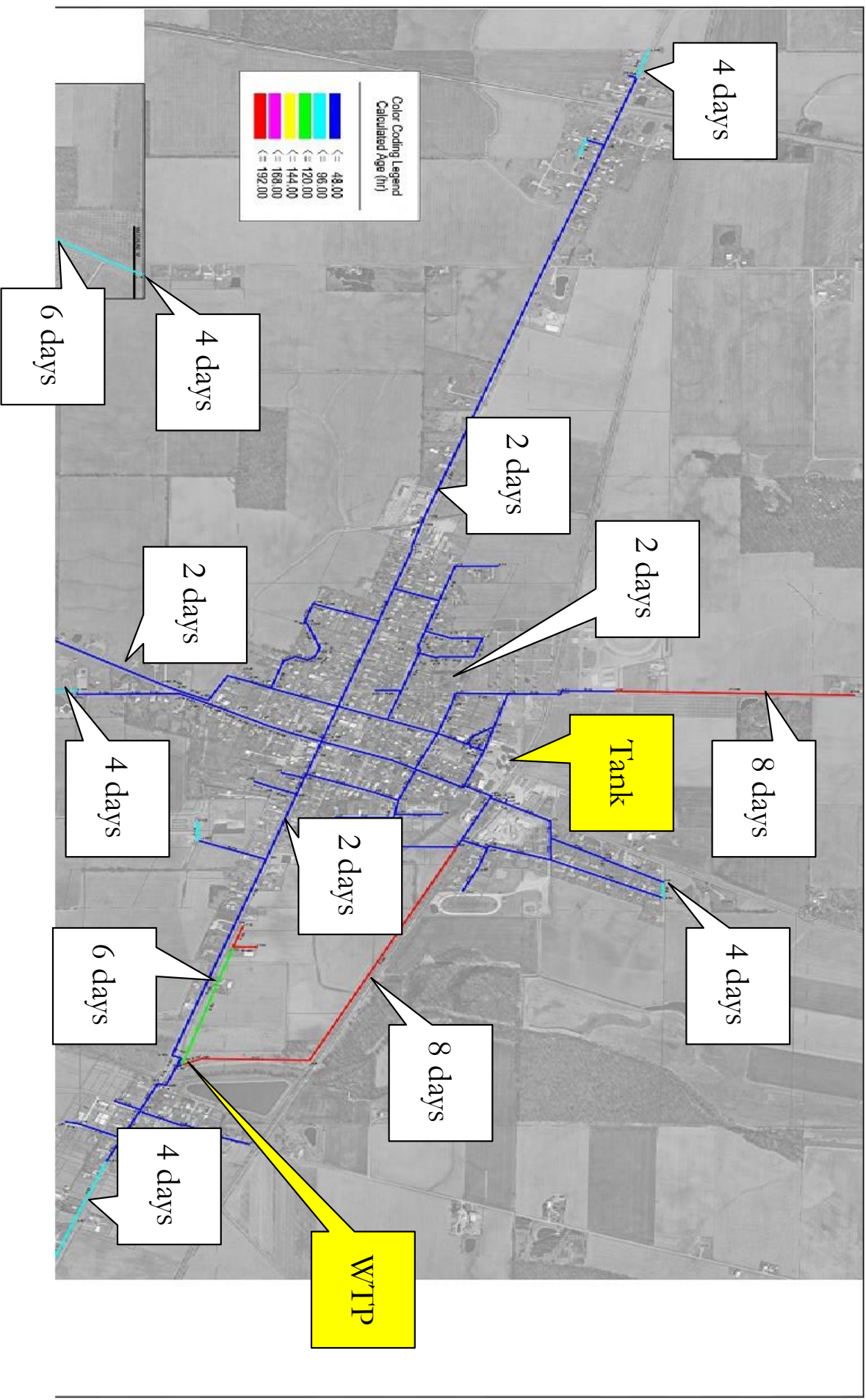
# Applications for Decay Evaluations

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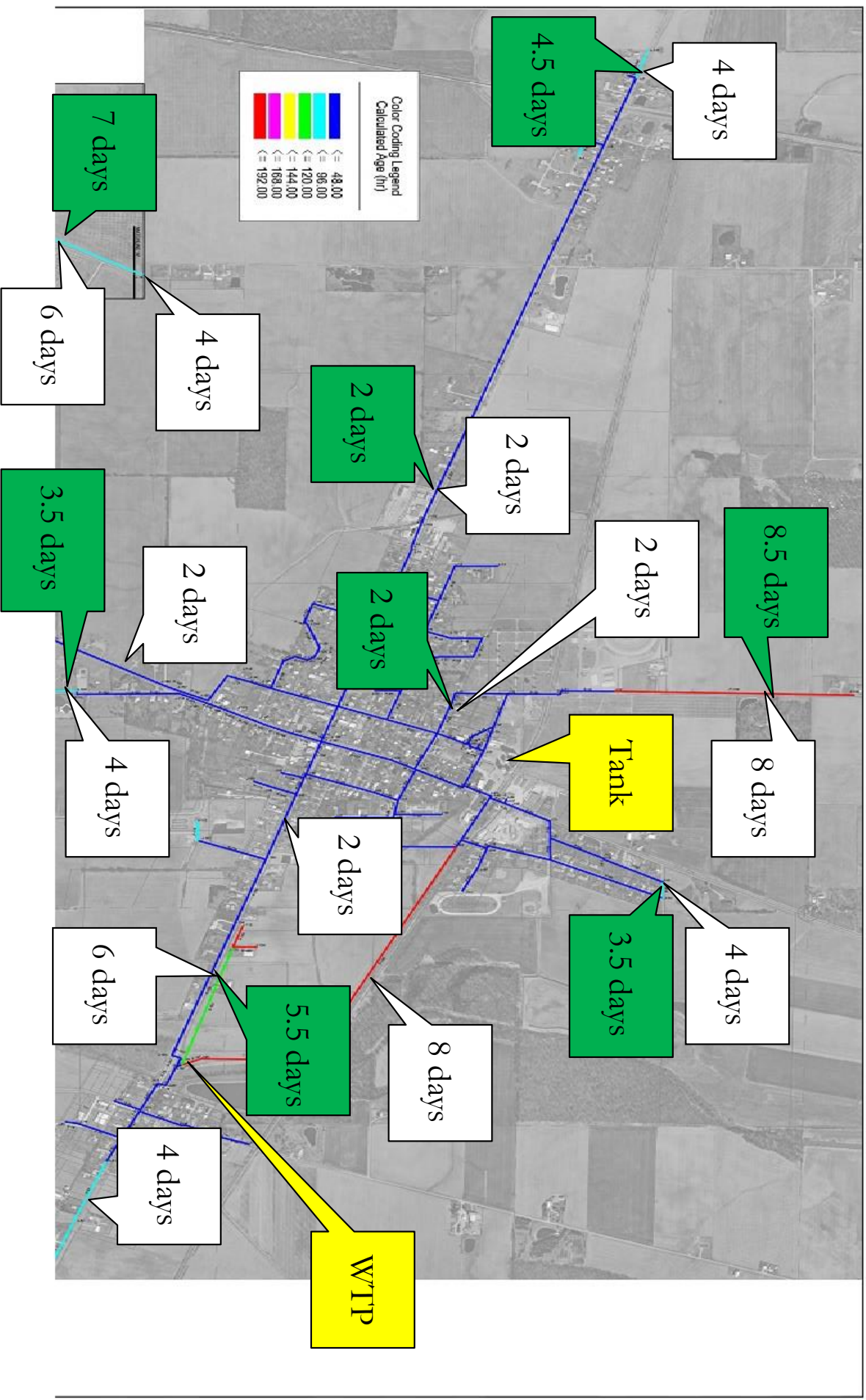
- Define residuals in areas that are not monitored
- Evaluate seasonal impacts to meet system residual requirements
- Define problem areas in storage and pipelines where persistent low residuals exist
  - Extended water age due to lack of mixing
  - Discover water age issues within distribution system
- Match decay evaluations with hydraulic modeling
- Relate other water quality issues in distribution

# Water Age Predictions

# Water System A (Hydraulic Model)

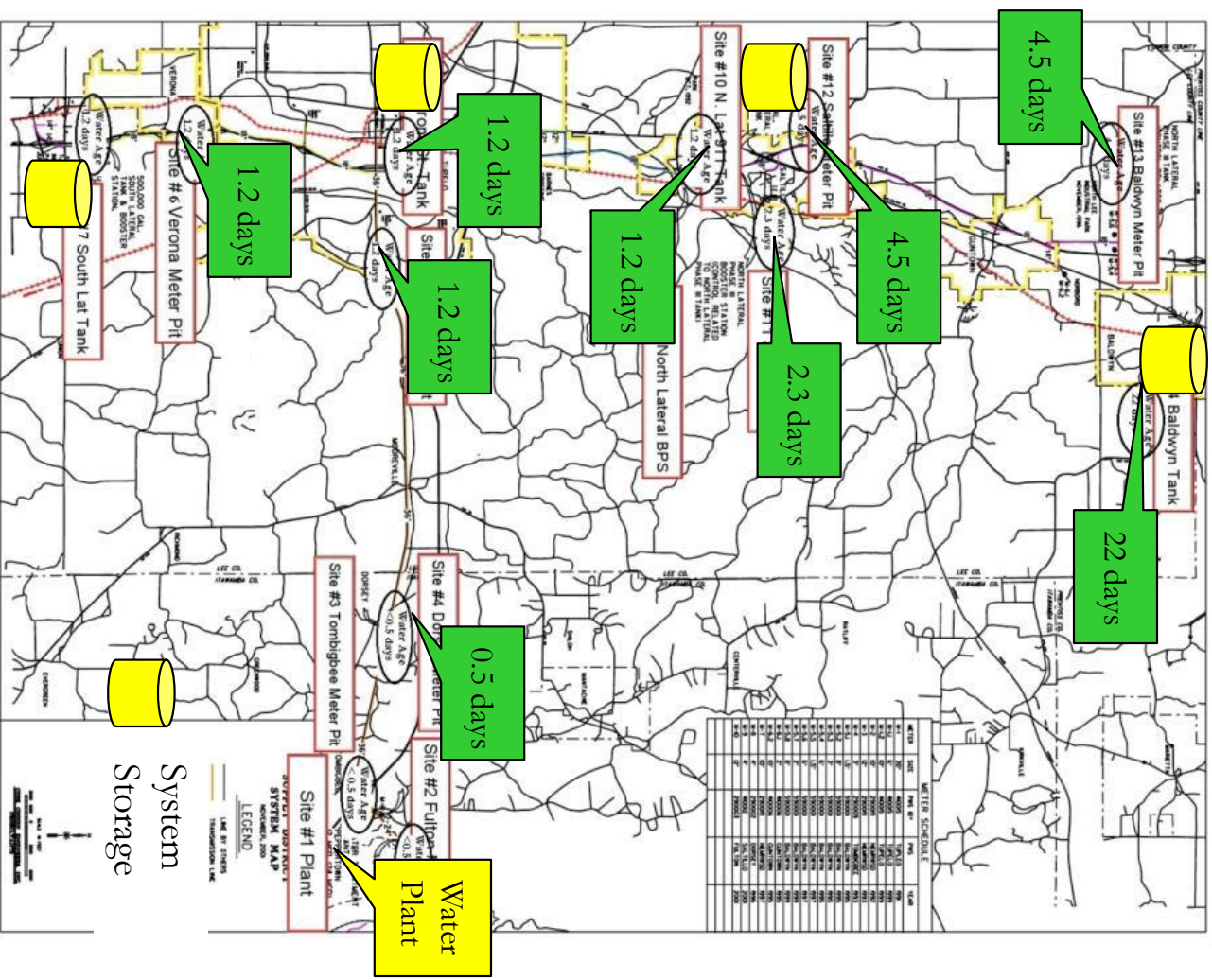


# Water System A (Hydraulic Model vs. Decay)

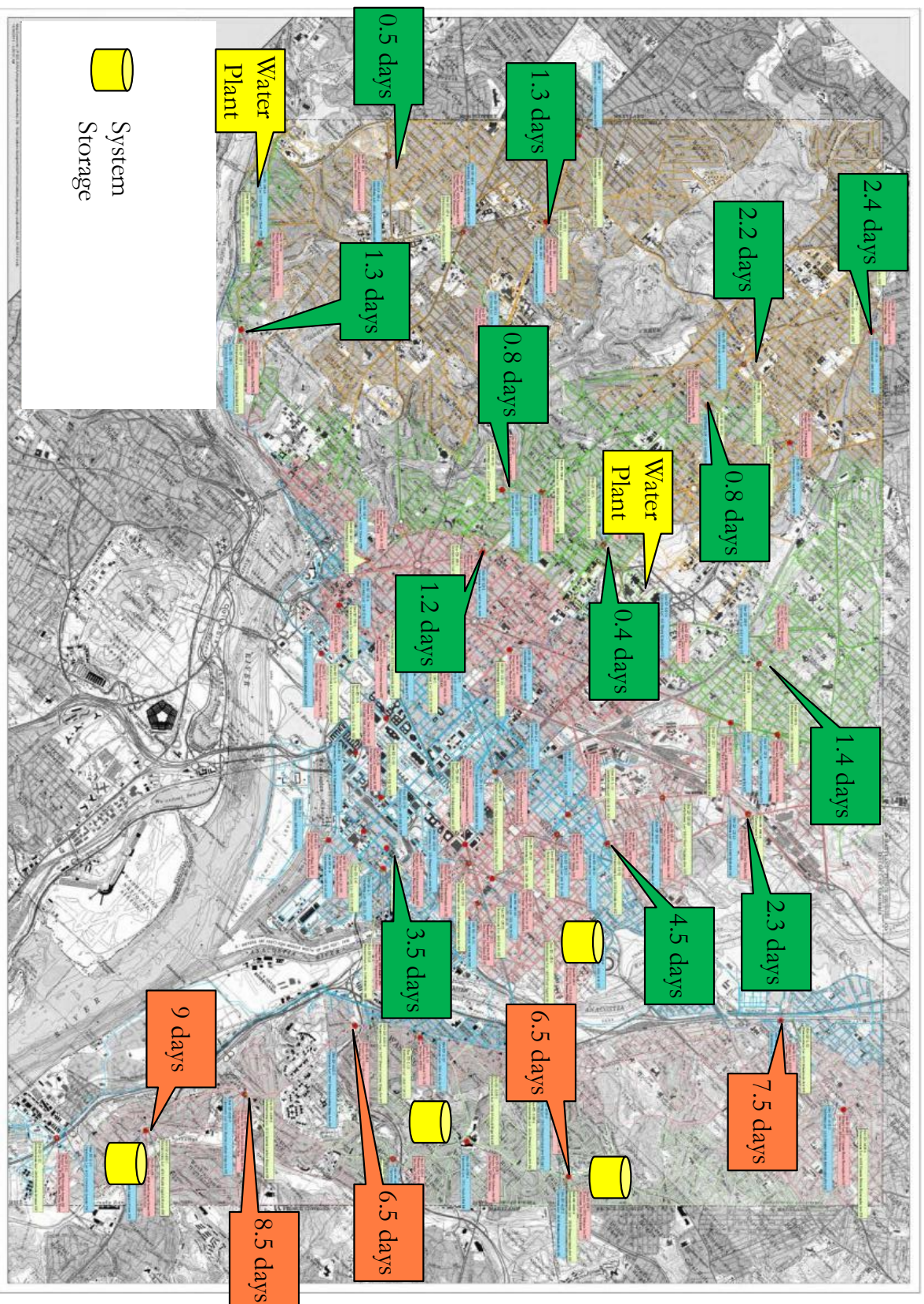


# Water System B

- Northern most tank contributes significant water age
- Total chlorine depleted less than 1.0 mg/L
- Study underway for tank mixing

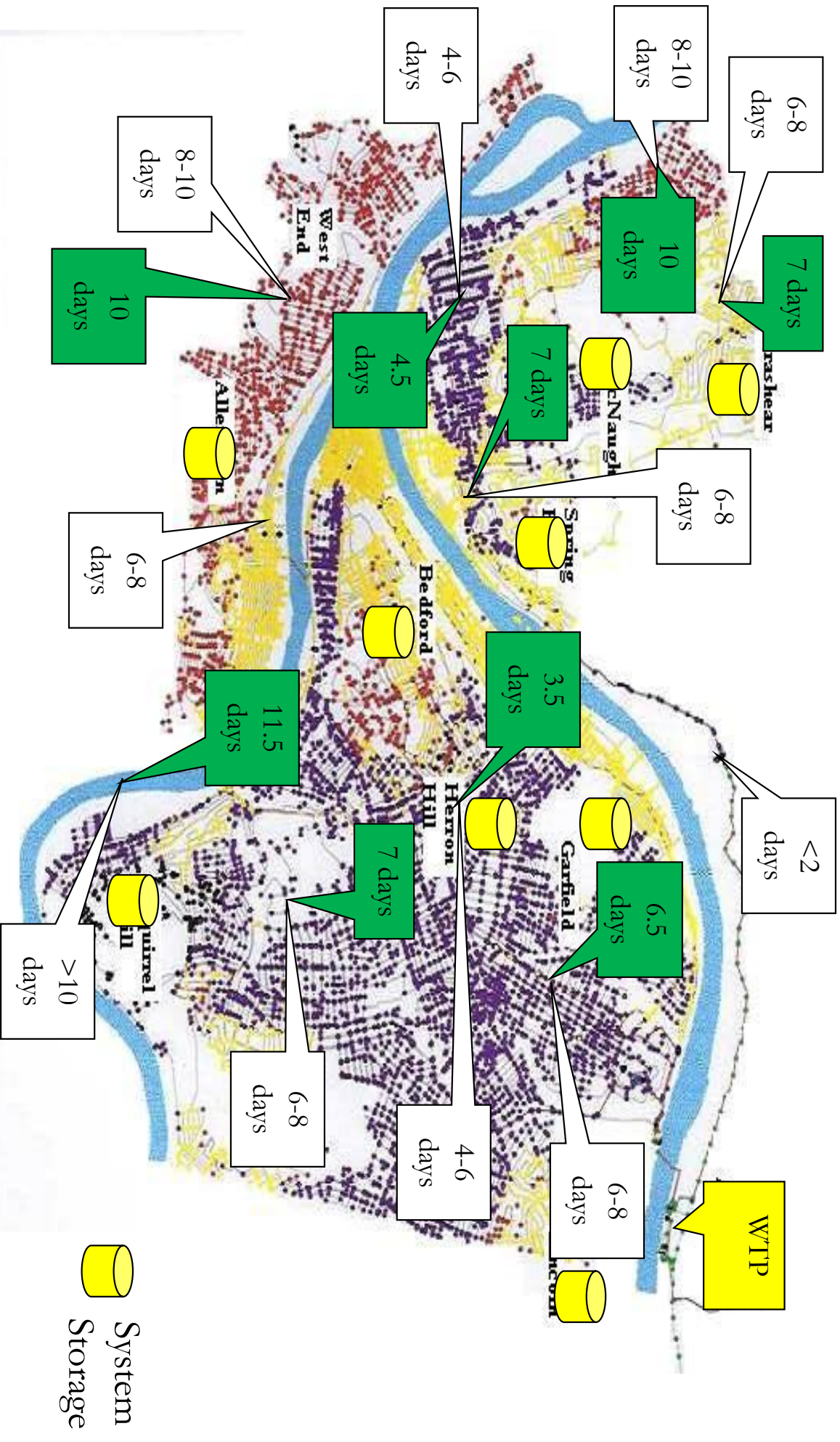


# Water System C





# Water System D-Hydraulic Model vs. Decay



# Questions

**Marvin Gnagy**

**[mcg7@bex.net](mailto:mcg7@bex.net)**

**419.450.2931**