Notes: Operations with Radicals

Do Now: Simplify each expression.

1)
$$7x + 9x$$

2)
$$7x^2 + 9x$$

3)
$$7\sqrt{2} + 9\sqrt{2}$$

4)
$$7\sqrt{3} + 9\sqrt{2}$$

When ADDING or SUBTRACTING radicals, you must have

LIKE TERMS

Simplify each of the following radical expressions:

A)
$$10\sqrt{11} + 2\sqrt{11}$$

B)
$$4\sqrt{2} + 3\sqrt{2}$$

C)
$$5\sqrt{13} + 3\sqrt{7}$$

D)
$$\sqrt{3} - 8\sqrt{3}$$

But what if we have ...

UNLIKE TERMS

$$5\sqrt{3} - \sqrt{12}$$

- 1) **SIMPLIFY** all radicals.
- 2) Combine all like terms.

$$3\sqrt{27} + 2\sqrt{12}$$

Checkpoint:

Completely simplify each of the following expressions.

A)
$$2\sqrt{32} + 7\sqrt{98}$$

B)
$$10\sqrt{27} - 9\sqrt{18}$$

C)
$$\frac{2}{3}\sqrt{27} - 3\sqrt{108} + 1.2\sqrt{75}$$

D)
$$\sqrt{98} - 4\sqrt{8} + 3\sqrt{128}$$

MULTIPLYING

 $\sqrt{5}(\sqrt{10})$

- 1) **MULTIPLY** coefficients.
- 2) MULTIPLY radicands.
- 3) If possible, simplify the result.

 $2\sqrt{15}(3\sqrt{3})$

Checkpoint:

Completely simplify each of the following expressions.

1)
$$3\sqrt{27} \cdot 5\sqrt{2}$$

$$2) \left(\frac{1}{2} \sqrt{3}\right)^2$$

3)
$$-4\sqrt{a}(3\sqrt{a})$$

4)
$$(4 - \sqrt{6})(3 + \sqrt{6})$$

Dividing Radicals

We must first RATIONALIZE THE DENOMINATOR!

$$\frac{\sqrt{3}}{\sqrt{7}}$$

$$\frac{2\sqrt{3}}{\sqrt{5}}$$

$$\frac{5\sqrt{3}}{2\sqrt{5}}$$

$$\frac{5\sqrt{3}}{2+\sqrt{5}}$$

$$\frac{9-2\sqrt{3}}{\sqrt{3}+6}$$

Classwork: Operations with Radicals

Completely simplify each expression.

1)
$$\sqrt{5} + 6\sqrt{5}$$

2)
$$-8.7\sqrt{3} - 3\sqrt{3}$$

3)
$$2\sqrt{72} + 3\sqrt{98}$$

4)
$$\sqrt{7}(24 + \sqrt{7})$$

5)
$$3\sqrt{18}(-4\sqrt{8})$$

$$6)\sqrt{75} - 4\sqrt{12} + 3\sqrt{192}$$

7)
$$\sqrt{81x} + \sqrt{16x}$$

$$8)\left(\frac{1}{3} + \sqrt{18}\right)^2$$

9)
$$(\sqrt{3} - \sqrt{6})(\sqrt{3} + \sqrt{6})$$

Completely simplify each expression.

$$10)\,\frac{\sqrt{27}}{\sqrt{15}}$$

$$11) \frac{4 - \sqrt{768}}{4}$$

12)
$$\frac{2-\sqrt{5}}{-3+\sqrt{5}}$$

13) The length of a rectangle is $(3\sqrt{8} + 2)$ and the width is $(2\sqrt{2} + 1)$. Express the perimeter of the rectangle in simplest radical form. Express the area of the rectangle in simplest radical form.

14) If $A = -3 + 8\sqrt{5}$ and $B = \sqrt{5} - 9$, then A - B equals

$$(1) -12 + 7\sqrt{5}$$

(2)
$$6 + 7\sqrt{5}$$

$$(3) -12 + 8\sqrt{5}$$

$$(4) 6 + 8\sqrt{5}$$

15) Dominque is installing a rectangular window in his neighbor's house. If the width of the window is $\frac{8+2\sqrt{10}}{3+\sqrt{5}}$ in. and the length is $\frac{5-\sqrt{5}}{\sqrt{3}}$ in. Find the window's total area, keeping your answer in simplest radical form.