

# **ADHIKAANSH**

## **ACADEMY**

### **(IITJEE NEET IX X XI XII)**

**RUN BY:**

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# **MATHS NOTES**

## **(CLASS 11<sup>TH</sup>)**



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## Chapter 13

### LIMITS AND DERIVATIVES

#### Some standard results on limits

- 1)  $\lim_{x \rightarrow c} f(x) = l$       iff  $\lim_{x \rightarrow c-} f(x) = \lim_{x \rightarrow c+} f(x) = l$
- 2)  $\lim_{x \rightarrow a} k = k$       where  $k$  is a fixed real number.
- 3)  $\lim_{x \rightarrow c} f(x) = f(c)$       where  $f(x)$  is a real polynomial in  $x$ .
- 4)  $\lim_{x \rightarrow c} x^n = c^n$       for all  $n \in \mathbb{N}$
- 5)  $\lim_{x \rightarrow c} |x| = |c|$

#### Algebra of limits

Refer : NCERT Textbook page no: 292.

#### Evaluation of algebraic limits

##### Type I ( Direct substitution method)

Eg: Evaluate  $\lim_{x \rightarrow 1} (x^3 - x^2 + 1) = 1^3 - 1^2 + 1 = 1$

Evaluate the following limits:

NCERT Textbook Exercise 13.1 Q 1,2,3,4,5,9,11,12.

##### Additional Questions and HOT Questions

\*\* 1)  $\lim_{x \rightarrow -1} (1 + x + x^2 + \dots + x^{10})$       Ans: 1

\*\* 2)  $\lim_{x \rightarrow -1} (x^5 + 2x^8)^{60}$       Ans: 1

\*\* 3)  $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} + \sqrt{1-x}}{1+x}$       Ans:2

##### Type II (Factorisation method)

Eg : Evaluate :  $\lim_{x \rightarrow 1} \frac{x^3 - 1}{x - 1}$

$$\begin{aligned} \lim_{x \rightarrow 1} \frac{x^3 - 1}{x - 1} \quad \left(\frac{0}{0} \text{ form}\right) &= \lim_{x \rightarrow 1} \frac{(x-1)(x^2 + x + 1)}{x-1} \\ &= \lim_{x \rightarrow 1} (x^2 + x + 1) \\ &= 1^2 + 1 + 1 = 3 \end{aligned}$$

Evaluate the following limits.

NCERT Textbook Exercise 13.1 Q 7,8 , Example 2.

**Evaluate:**

$$** \ 1) \ \lim_{x \rightarrow 1} \frac{(2x-3)(\sqrt{x}-1)}{2x^2+x-3} \quad \text{ans: } \frac{-1}{10}$$

$$** \ 2) \ \lim_{x \rightarrow \sqrt{2}} \frac{x^4-4}{x^2+3\sqrt{2}x-8} \quad \text{ans: } \frac{8}{5}$$

$$** \ 3) \ \lim_{x \rightarrow 2} \frac{x^3-4x^2+4x}{x^2-4} \quad \text{ans: } 0$$

### Type III

For any positive integer n,  $\lim_{x \rightarrow a} \frac{x^n - a^n}{x - a} = n a^{n-1}$  ( This is applicable for any rational number n and for  $a > 0$ .)

Evaluate :  $\lim_{x \rightarrow 2} \frac{x^4-16}{x-2}$

$$\text{Ans: } \lim_{x \rightarrow 2} \frac{x^4-16}{x-2} = \lim_{x \rightarrow 2} \frac{x^4-2^4}{x-2} = 4 \cdot 2^{4-1} = 4 \cdot 2^3 = 32$$

Evaluate the following limits.

NCERT Textbook Exercise 13.1 Q 10 , Example 3.

1) Evaluate :  $\lim_{x \rightarrow 2} \frac{x^{10}-1024}{x^5-32}$       Ans: 64

2) If  $\lim_{x \rightarrow -a} \frac{x^9+a^9}{x+a} = 9$  , find the value of a.

### Type IV

Evaluate  $\lim_{x \rightarrow 0} \frac{\sqrt{1+x}-1}{x}$

$$\text{Ans: } \lim_{x \rightarrow 0} \frac{\sqrt{1+x}-1}{x} = \lim_{x \rightarrow 0} \frac{\sqrt{1+x}-1}{1+x-1}$$

Put  $y = 1+x$  when  $x \rightarrow 0$  ,  $y \rightarrow 1$

$$\therefore \text{ value} = \lim_{y \rightarrow 1} \frac{\sqrt{y}-1}{y-1}$$

$$= \lim_{y \rightarrow 1} \frac{y^{1/2} - 1^{1/2}}{y-1}$$

$$= \frac{1}{2}$$

### Evaluate

1) NCERT Ex 13.1 Q 6

$$2) \lim_{x \rightarrow 0} \frac{(1-x)^{n-1}}{x} \quad \text{ans} = -n$$

$$3) \lim_{x \rightarrow 0} \frac{(1+x)^6 - 1}{(1+x)^5 - 1} \quad \text{ans} = \frac{6}{5}$$

$$4) \lim_{x \rightarrow 0} \frac{(x+8)^{1/3} - 2}{x} \quad \text{ans} = \frac{1}{12}$$

### Type V

Concepts :  $\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$

$$\lim_{x \rightarrow 0} \cos x = 1$$

$$\lim_{x \rightarrow 0} \frac{\tan x}{x} = 1$$

NCERT Exercise 13.1 : Q 13, 14, 16, 18, 19, 20, 21

Evaluate :  $\lim_{x \rightarrow 0} \frac{\tan 8x}{\sin 3x} \quad \text{ans: } \frac{8}{3}$

Evaluate :  $\lim_{x \rightarrow 0} \frac{\sin 2x + 3x}{2x + \sin 3x} \quad \text{ans: } 1$

### Type VI

NCERT Exercise 13.1 : Q 17

Evaluate :  $\lim_{x \rightarrow 0} \frac{1 - \cos 5x}{1 - \cos 6x}$

### Type VII

Evaluate :  $\lim_{x \rightarrow \pi} \frac{\sin(\pi-x)}{\pi(\pi-x)}$

Let  $x = \pi + h$

$$\begin{aligned} \therefore \lim_{x \rightarrow \pi} \frac{\sin(\pi-x)}{\pi(\pi-x)} &= \lim_{h \rightarrow 0} \frac{\sin[\pi-(\pi+h)]}{\pi[\pi-(\pi+h)]} \\ &= \frac{1}{\pi} \lim_{h \rightarrow 0} \frac{\sin h}{h} = \frac{1}{\pi} \end{aligned}$$

Textbook Q no: 22

Evaluate 1)  $\lim_{x \rightarrow \pi/2} \frac{\tan 2x}{x - \frac{\pi}{2}}$  ans: 2

2)  $\lim_{x \rightarrow 1} \frac{\cos \frac{\pi}{2}x}{1-x}$  ans :  $\frac{\pi}{2}$

3)  $\lim_{x \rightarrow \pi} \frac{\sin x}{x-\pi}$  ans : (-1)

4)  $\lim_{x \rightarrow \pi/2} \frac{1+\cos 2x}{(\pi-2x)^2}$  ans :  $\frac{1}{2}$

### Type VIII

Applying  $\sin C \pm \sin D$  formulae

Evaluate 1)  $\lim_{x \rightarrow 0} \frac{\sin 2x + \sin 6x}{\sin 5x - \sin 3x}$

2)  $\lim_{x \rightarrow a} \frac{\sin x - \sin a}{x-a}$  ans :  $\cos a$

### Type IX

$$\lim_{x \rightarrow c^-} f(x) = \lim_{x \rightarrow c^+} f(x) = l$$

\*\* NCERT Exercise 13.1 -

1) Q 23

2) Q 24

3) Q 25

4) Q 26

\*\* 5) If  $f(x) = \begin{cases} \frac{|x-2|}{2-x}, & x \neq 2 \\ -1, & x = 2 \end{cases}$ , find  $\lim_{x \rightarrow 2} f(x)$

6) If  $f(x) = \begin{cases} x, & x > 0 \\ 1, & x = 0 \\ -x, & x < 0 \end{cases}$ , find  $\lim_{x \rightarrow 0} f(x)$

## Type X

\*\* NCERT Exercise 13.1 -

1) Q 28

2) Q 30

3) Q 32

4) Let  $f(x) = \begin{cases} 4x - 5, & x \leq 2 \\ x - k, & x > 2 \end{cases}$  . Find k if  $\lim_{x \rightarrow 2} f(x)$  exists. **Ans : k = -1**

## Type XI

### Exponential Limits

$$\lim_{x \rightarrow 0} \frac{e^x - 1}{x} = 1$$

NCERT Exercise 13.2 Q1 , Q2, Q4, Q6.

## Type XII

NCERT Exercise 13.2 Q3 , Q5

## Type XIII

$$\lim_{x \rightarrow 0} \frac{\log_e(1+x)}{x} = 1$$

NCERT Exercise 13.2 Q7 , Q8

## DIFFERENTIATION

### Type I

Find the derivatives of the following functions from first principle.

1)  $x$

2)  $\frac{1}{x}$

3)  $-x$

4)  $(-x)^{-1}$

5)  $x^n$

6) NCERT Ex 13.2 Q4

\*\* 7)  $\sin x$

\*\* 8)  $\cos x$

- \*\* 9)  $\tan x$
- \*\* 10)  $\sec x$
- \*\* 11)  $\operatorname{cosec} x$
- \*\* 12)  $\sin 2x$
- \*\* 13)  $\cos 3x$
- 14)  $x \sin x$
- 15)  $\sin^2 x$
- 16)  $\sin(x+1)$
- 17) Misc Example 19

### **Type II**

Find the derivatives of the following

- \* 1)  $3 \cot x + 5 \operatorname{cosec} x$
- 2)  $5 \sin x - 6 \cos x + 7$
- 3)  $2 \tan x - 7 \operatorname{cosec} x$
  
- 4)  $x^3 - 27$
- 5)  $2x - \frac{3}{4}$
- \* 6)  $x^2 + \sin x + \frac{1}{x^2}$

### **Type III**

- Ex 13.2 Q1
- Ex 13.2 Q2
- Ex 13.2 Q3
- Ex 13.2 Q5



### Type IV

$$\frac{d}{dx}(uv) = u \cdot \frac{dv}{dx} + v \cdot \frac{du}{dx}$$

NCERT Ex 13.2

\* 1) Q7 (1),(2)

\* 2) Q9 (2),(3),(4),(5)

\* 3) Q11 (1)

\* 4) Example 18

\*\* 5) Misc Ex Q 15, Q22, Q25, Q29.

### Type V

$$\frac{d}{dx} \left( \frac{u}{v} \right) = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$$

Misc Exercise Q 5,6,7,8,9,16,17,18,20,26.

### Additional questions and HOT Questions

1. Find the derivatives of the following functions

a)  $\frac{\sec x + \tan x}{\sec x - \tan x}$

\*\* b)  $(x^2 - 3x + 2)(x + 2)$

\*\* c)  $\frac{\sin x - x \cos x}{x \sin x + \cos x}$

2. If  $y = 1 + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$ , show that  $\frac{dy}{dx} = y$ .

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