[This question paper contains 4 printed pages.]

Your Roll No2.

Sr. No. of Question Paper: 1206

Unique Paper Code : 2222011201

Name of the Paper : Mathematical Physics - II

(DSC - 4)

Name of the Course : B.Sc. (Hons.) Physics- core

Semester : II

Duration: 2 Hours Maximum Marks: 60

Instructions for Candidates

 Write your Roll No. on the top immediately on receipt of this question paper.

- 2. Attempt FOUR questions in all
- 3. Question No. 1 is compulsory.
- 4. Use of non-programmable scientific calculator is allowed.

- 1. Attempt ALL questions. Each question carries equal marks. (3×5=15)
 - (a) Let u_1 , u_2 , u_3 be orthogonal coordinates. Prove that $|\nabla u_p| = h_p^{-1}$, p = 1, 2, 3
 - (b) Write the expression only of the general solution near x = -1 using Frobenius method of

$$y'' + x y' + (2x-1) y = 0$$

- (c) Using the expression of the generating function of the Legendre Polynomials $P_n(x)$ find the expression for $P_2(x)$ and $P_3(x)$.
- (d) Evaluate using Beta function property $\int_0^\infty \frac{z^{m-1}}{1+z} dz = \frac{m}{\sin m\pi} \text{ the integral } \int_{-\infty}^\infty \frac{e^{2u}}{1+e^{3u}} du$
- (e) Is the given function periodic, $f(t) = \sin (10 + \pi)t.$ If yes, what is its period?

- (a) Find the Fourier series expansion of the function $f(x) = x^2 \quad , \quad 0 < x < 2\pi$ (10)
 - (b) Plot the even and odd components of a function defined by $f(t) = \begin{cases} e^{-t}, t > 0 \\ 0, t < 0 \end{cases}$
- Derive the expression for $abla^2 \varphi$ in cylindrical coordinates. (10)
 - (b) Represent the vector $\vec{A} = z\hat{\imath} 2x\hat{\jmath} + y\hat{k}$ cylindrical coordinates (ρ, ϕ, z) . Thus determine A_o, A_ϕ and A_z (5)
- \checkmark 4. (a) Prove that $P_n(x)$ is the coefficient of t^n in the expansion of $\frac{1}{\sqrt{1-2xt+t^2}}$ in the ascending powers of t. Hence find the value of $P_n(1)$ (10)
 - (b) Evaluate using the orthonormalization property of Legendre polynomial
 - (i) $\int_{-1}^{1} P_3(x) P_4(x) dx$,

(5)

(ii)
$$\int_{-1}^{1} [P_2(x)]^2 dx$$
 (5)

5. (a) Find the general solution near x = 0 using Frobenius method of:

$$xy'' + (1-2x)y' + (x-1)y = 0$$
 (10)

(b) Identify and name the nature of singularities

$$(1-x^2)^2 y'' + x(1-x)y' + (1+x)y = 0 (5)$$