

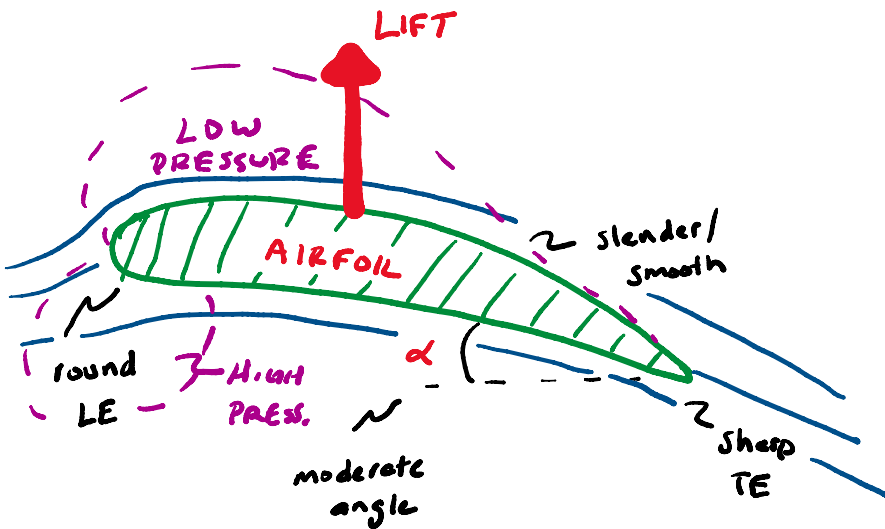
Up to this point:



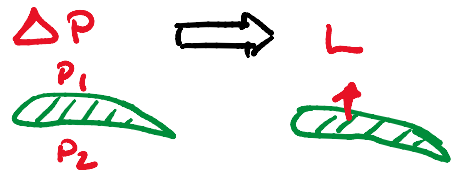
- KUTTA - JOUKOWSKI  $L' = \rho u_\infty \Gamma$
- BERNOULLI  $u \uparrow P \downarrow$

Today: where does **LIFT** come from?

MASS      MOMENTUM      ENERGY



Bodies in AERO feel force through  $P \cdot \tau$



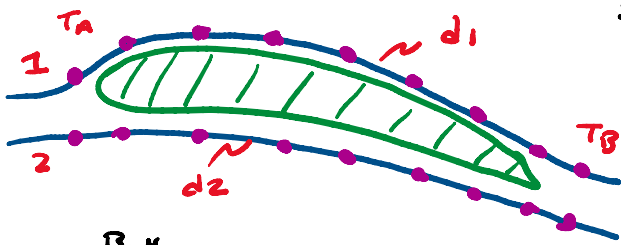
But How?

Common misconceptions:

**1. EQUAL TIME**



since  $d_1 > d_2$  then  $u_1 > u_2$  through Bernoulli:



Both particles meet at TE

since  $d_1 > d_2$  then  $u_1 > u_2$  through Bernoulli:

$P_1 < P_2$  then  $\Delta P \rightarrow L$

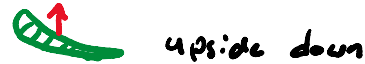
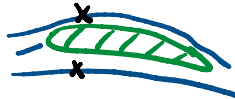
No!

issues:  $d_1 > d_2 \neq u_1 > u_2$

1. the particles don't need to meet

2.  $u_1 > u_2 \Rightarrow P_1 < P_2$  is Bernoulli

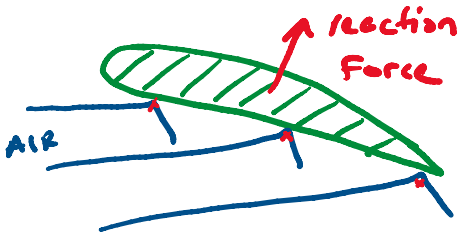
OFF a streamline



special cond. IRROTATIONAL

BUT along PATH 1  $u \uparrow \Rightarrow P \downarrow$  |  $\frac{1}{2}$  | generally  $u_1 > u_2$  ✓

## 2. AIR PUSHES



Air bounces off **FOIL** creating a **REACTION FORCE**

issues: that's not how **AIR** behaves (not bouncy balls)

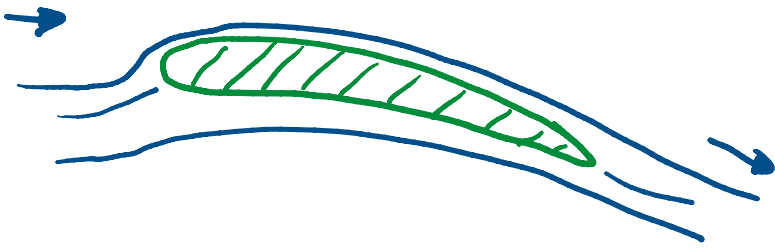


BUT **AIR** is being turned which requires a **FORCE (LIFT)**

## 3. AIR IS TURNED / ROTATED

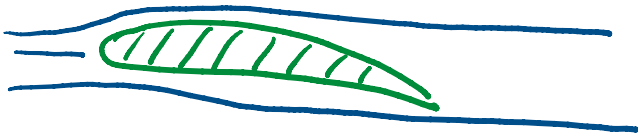


**FLOW** is redirected DOWN ↓

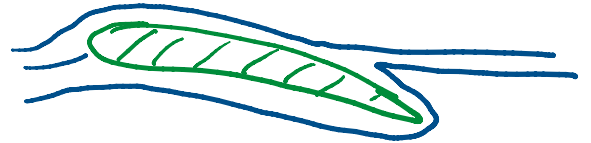


FLOW is redirected DOWN ↓  
therefore FORCE UP ↑

Yes! But, this isn't a WHY... just a FOOTPRINT



or



All concepts have something correct, but incomplete...

In reality:

CONSERVATION OF...

**MASS**

↳ Flow accel



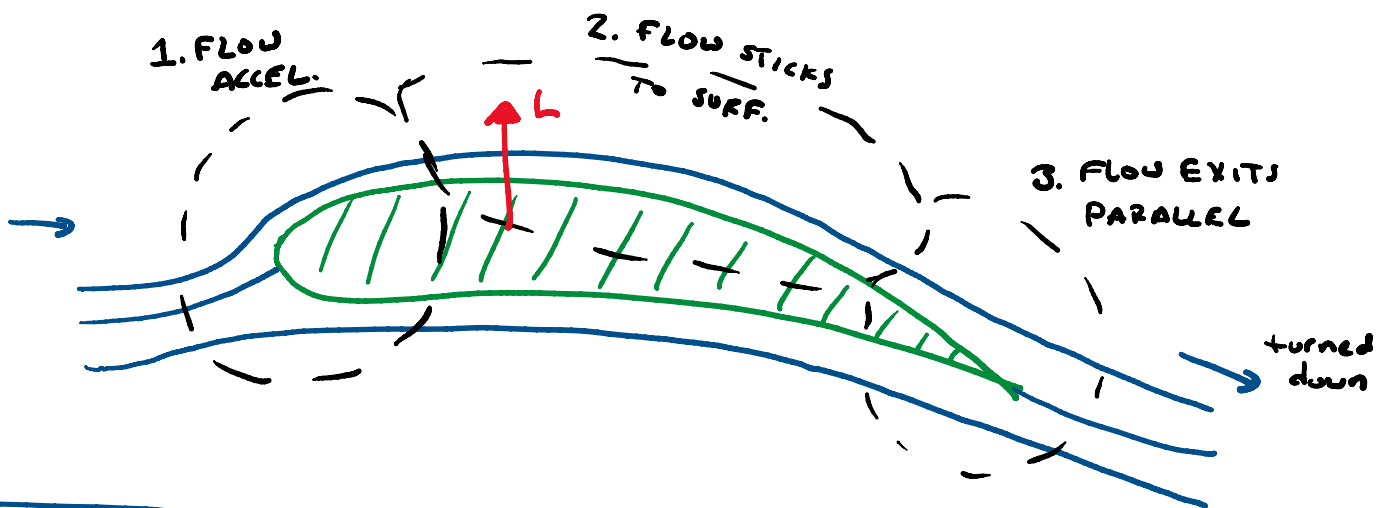
**ENERGY**

↳ accel becomes force



**MOMENTUM**

↳ explains force from flow rotation



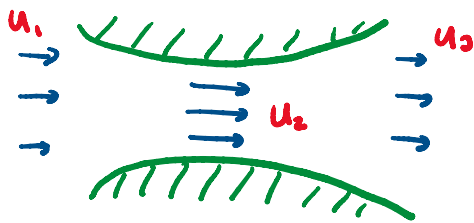
**AT THE NOSE**

flow acceleration



$$u_1 = u_2$$

CONSERVATION OF MASS

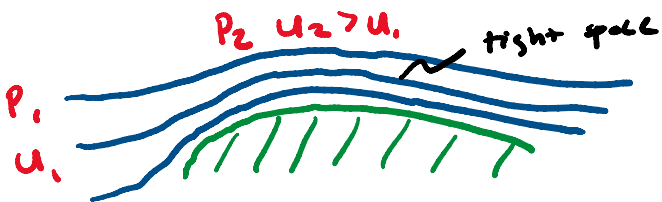


$u_1 = u_3$   
 $u_2 > u_1, u_3$

CONSERVATION OF MASS

$\dot{m} = \text{const.} \Rightarrow \rho u_1 A_1 = \rho u_2 A_2$   
 $A \downarrow \Rightarrow u \uparrow$

Same happens on a foil



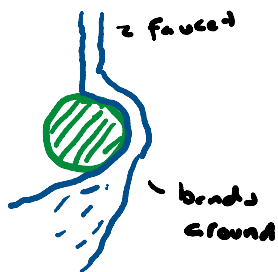
Rapid changes in curvature  
 CAUSE ACCELERATION

BERNOULLI:  $P + \frac{1}{2} \rho u^2 = \text{const.} \Rightarrow P_2 < P_1$

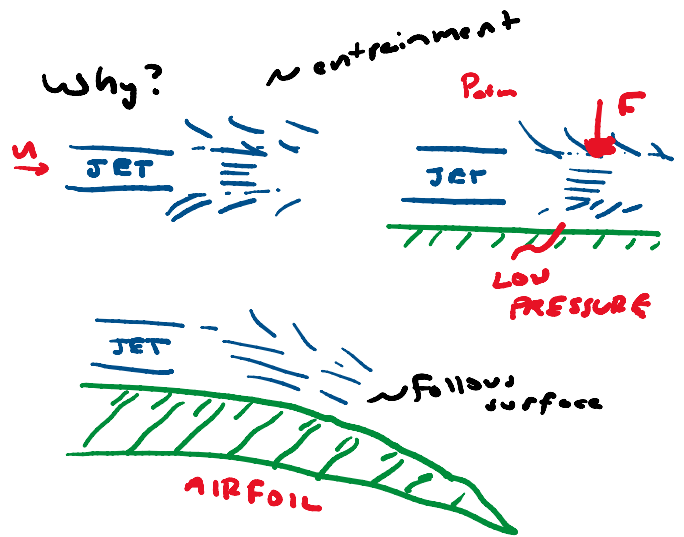
**ON THE SURFACE**

flow sticks

COANDA EFFECT



Flow tends to prefer to stay on surface



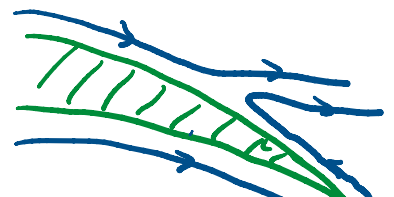
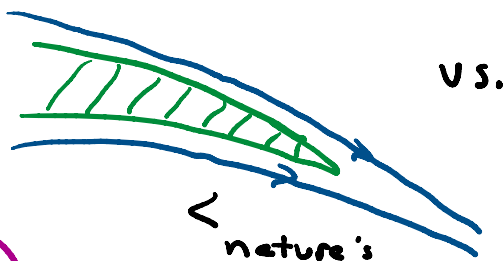
So flow doesn't do this:

**AT THE TIP**

easy flow exit

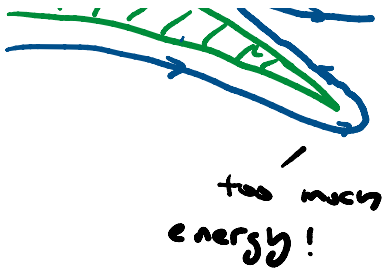
KUTTA-CONDITION

Flow smoothly leaves

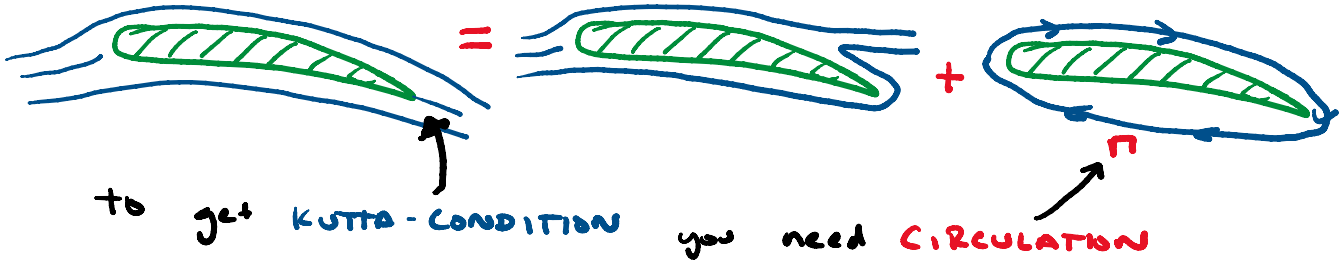


Flow smoothly leaves Top/Bottom at the TE

< nature's preference



recall ELEMENTARY FLOWS

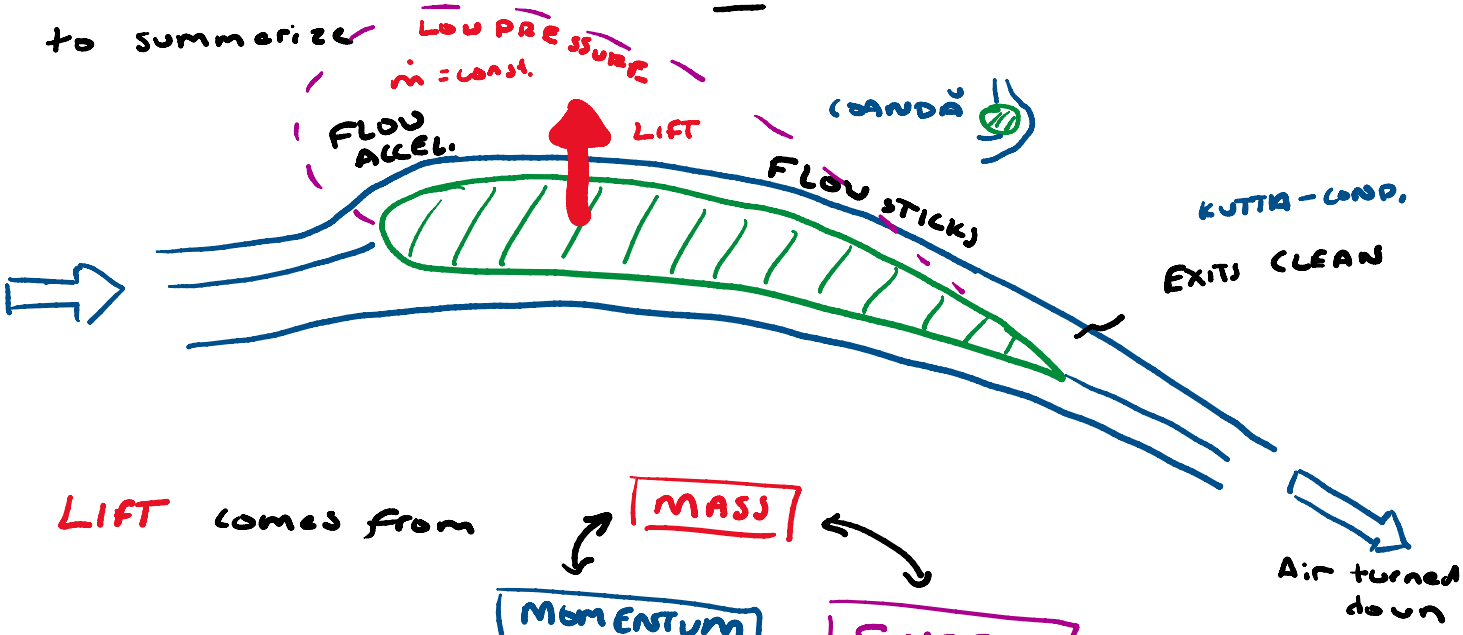


$$L' = \rho U_{\infty} \Gamma$$

circ. leads to LIFT

KUTTA-JOUKOWSKI THEOREM

to summarize



LIFT comes from

