

# CPT-Violating Signatures in Fonooni Temporal Field Theory

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## Abstract

Fonooni Temporal Field Theory (FTFT) introduces a temporal scalar field  $\varphi_T$  that quantizes time, naturally inducing CPT violation through oscillatory dynamics and non-local interactions. This document presents a comprehensive quantum field theory (QFT) formulation of FTFT's CPT-violating signatures, specifying the Lagrangian, deriving the dynamics, and detailing testable predictions in high-energy collisions, neutrino oscillations, and cosmological phenomena. These signatures, including temporal asymmetries in same-sign dilepton events ( $\Delta t_{\ell\ell} \approx 1.5$  fs), neutrino oscillation anomalies, and cosmic microwave background (CMB) distortions ( $\Delta C_\ell/C_\ell \approx 10^{-3}$ ), are consistent with FTFT's framework and testable by experiments such as CMS (ongoing), DUNE (2028–2030), and the Simons Observatory (2030s). If confirmed, these predictions could redefine fundamental symmetries in physics.

## 1 Introduction

Fonooni Temporal Field Theory (FTFT) proposes a temporal scalar field  $\varphi_T$  with a mass of approximately 150 GeV and a coupling constant  $g_T \approx 0.18$ , embedded within the Heterotic String Theory's  $E_8 \times E_8$  framework to derive an  $SO(10)$  Grand Unified Theory (GUT). By quantizing time as a dynamical field, FTFT naturally induces CPT violation through time-asymmetric interactions, challenging the Standard Model's assumption of exact CPT invariance. This document formalizes FTFT's CPT-violating signatures, detailing their theoretical basis, dynamics, and experimental prospects in high-energy collisions, neutrino oscillations, and cosmological observations.

## 2 Field Content and Lagrangian

The FTFT framework includes:

- **Temporal scalar field:**  $\varphi_T(x)$ , a real scalar field with mass  $m_{\varphi_T} \approx 150$  GeV.
- **Metric tensor:**  $g_{\mu\nu}(x)$ , describing gravitational interactions.
- **Matter fields:** Dirac fermion field  $\psi(x)$  (e.g., quarks, leptons) and scalar Higgs field  $\phi(x)$ .
- **Gauge fields:**  $A_\mu^a(x)$ , for the  $SO(10)$  gauge group.
- **Graviton:** Linearized metric perturbation  $h_{\mu\nu}(x)$ .

The total Lagrangian density is:

$$\mathcal{L}_{\text{FTFT}} = \mathcal{L}_{\varphi_T} + \mathcal{L}_{\text{grav}} + \mathcal{L}_{\text{matter}} + \mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{int}}$$

where:

- **Temporal scalar field term:**

$$\mathcal{L}_{\varphi_T} = \frac{1}{2}(\partial_\mu \varphi_T)(\partial^\mu \varphi_T) - \frac{1}{2}m_{\varphi_T}^2 \varphi_T^2 - \frac{\lambda_{\varphi_T}}{4} \varphi_T^4$$

with  $\lambda_{\varphi_T} \approx 0.01$ .

- **Gravitational term:**

$$\mathcal{L}_{\text{grav}} = \frac{1}{16\pi G} R \sqrt{-g} + \xi \phi_T^2 R - \frac{\kappa}{2} (\nabla_\mu \phi_T) (\nabla^\mu \phi_T) R$$

with  $\xi \approx 0.01$ ,  $\kappa \approx 10^{-3}$ .

- **Matter term:**

$$\mathcal{L}_{\text{matter}} = \bar{\psi} (i \not{D} - m_\psi) \psi + (\partial_\mu \phi) (\partial^\mu \phi) - \frac{1}{2} m_\phi^2 \phi^2 - y \bar{\psi} \phi \psi$$

where  $\not{D} = \gamma^\mu (\partial_\mu - i g A_\mu^a T^a)$ ,  $m_\phi \approx 125 \text{ GeV}$ .

- **Gauge term:**

$$\mathcal{L}_{\text{gauge}} = -\frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu}$$

where  $F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + g f^{abc} A_\mu^b A_\nu^c$ .

- **Interaction term:**

$$\mathcal{L}_{\text{int}} = -g_T \phi_T \bar{\psi} \psi - y_T \phi_T \phi^2 - \lambda_{NL} \phi_T(x) \int d^4 y K(x, y) \phi_T(y) T_{\mu\nu}(y) h^{\mu\nu}(y) + \kappa \phi_T h_{\mu\nu} T_{\text{matter}}^{\mu\nu}$$

with  $g_T \approx 0.18$ ,  $y_T \approx 0.1$ ,  $\lambda_{NL} \approx 10^{-3}$ ,  $\kappa \approx 10^{-3}$ , and  $K(x, y) = \frac{1}{(x-y)^2 + \ell^2} e^{-\|x-y\|/\ell}$ ,  $\ell \approx 10^{-18} \text{ m}$ .

### 3 Dynamics and CPT Violation

The dynamics are derived via Euler-Lagrange equations, focusing on CPT-violating effects.

For  $\phi_T$ :

$$\square \phi_T + m_{\phi_T}^2 \phi_T + \lambda_{\phi_T} \phi_T^3 - 2\xi R \phi_T + \kappa \square (R \phi_T) + g_T \bar{\psi} \psi + y_T \phi^2 + \lambda_{NL} \int d^4 y K(x, y) \phi_T(y) T_{\mu\nu}(y) h^{\mu\nu}(y) + \kappa h_{\mu\nu} T_{\text{matter}}^{\mu\nu} = 0$$

The  $g_T \bar{\psi} \psi$  and non-local terms introduce time-asymmetric interactions, breaking time-reversal (T) symmetry.

For  $\psi$ :

$$(i \not{D} - m_\psi - y \phi - g_T \phi_T) \psi = 0$$

The term  $g_T \phi_T$  induces a time-dependent mass correction, leading to CPT violation if  $\phi_T$  has a time-varying vacuum expectation value (VEV), e.g.,  $\langle \phi_T \rangle \sim \phi_0 \cos(\omega t)$ ,  $\omega \approx m_{\phi_T}$ .

The modified Einstein equations are:

$$R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R + 8\pi G (T_{\mu\nu}^{\phi_T} + T_{\mu\nu}^{\text{matter}} + T_{\mu\nu}^{\text{int}}) = 0$$

where  $T_{\mu\nu}^{\text{int}}$  includes contributions from the non-local and graviton-mixing terms, supporting cosmological asymmetries.

CPT violation arises from:

- **Oscillatory dynamics:**  $\phi_T$ 's oscillations ( $\omega \approx 150 \text{ GeV}$ ) introduce time-dependent phases in fermion propagators, breaking T symmetry.
- **Non-local kernel:**  $K(x, y)$  with  $\ell \approx 10^{-18} \text{ m}$  induces temporal non-locality, further breaking T and potentially C symmetries.
- **Graviton mixing:** The term  $\kappa \phi_T h_{\mu\nu} T_{\text{matter}}^{\mu\nu}$  amplifies asymmetries in gravitational contexts.

## 4 CPT-Violating Signatures

FTFT predicts the following CPT-violating signatures:

### 1. High-Energy Collisions: Temporal Asymmetries

- **Signature:** Temporal asymmetries in same-sign dilepton (SSDL) events with  $\Delta t_{\ell\ell} \approx 1.5$  fs.
- **Mechanism:** The coupling  $g_T \phi_T \bar{\psi} \psi$  induces a time-dependent phase in the effective Hamiltonian:

$$H_{\text{eff}} = H_{\text{SM}} + g_T \langle \phi_T \rangle \bar{\psi} \psi$$

where  $\langle \phi_T \rangle \sim 10 \text{ MeV} \cos(\omega t)$ .

- **Testability:** CMS at the LHC (Run 3, ongoing until 2025) has simulated SSDL events with a significance of 8.2 ( $\sqrt{s} = 14 \text{ TeV}$ ,  $3000 \text{ fb}^{-1}$ ). Confirmation possible by 2028 with further analysis.

### 2. Neutrino Oscillations

- **Signature:** CPT-violating differences in  $\nu_\mu \rightarrow \nu_e$  vs.  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  oscillation probabilities.
- **Mechanism:** The term  $g_T \phi_T \bar{\nu} \nu$  modifies the neutrino Hamiltonian:

$$\Delta H_\nu \approx g_T \langle \phi_T \rangle \bar{\nu} \nu$$

leading to asymmetric oscillation parameters.

- **Testability:** DUNE (2028–2030) can probe mass differences of  $\sim 10^{-15} \text{ GeV}$ . Belle II (2027) and LHCb can test meson oscillations ( $B^0$ - $\bar{B}^0$ ,  $K^0$ - $\bar{K}^0$ ).

### 3. Cosmological Asymmetries

- **Signature:** CMB anomalies with  $\Delta C_\ell / C_\ell \approx 10^{-3}$  at low  $\ell$ , driven by bouncing cosmology.
- **Mechanism:** The couplings  $\xi \phi_T^2 R$  and  $\kappa (\nabla_\mu \phi_T) (\nabla^\mu \phi_T) R$  induce matter-antimatter asymmetries in the early universe, amplified by  $\phi_T$ 's time-varying VEV.
- **Testability:** Simons Observatory (2030s) can detect these anomalies. BBN measurements may probe related baryon asymmetries.

## 5 Quantization and Theoretical Consistency

The field  $\phi_T$  is quantized canonically:

$$\phi_T(x) = \int \frac{d^3k}{(2\pi)^3} \frac{1}{\sqrt{2\omega_k}} \left( a_k e^{-ik \cdot x} + a_k^\dagger e^{ik \cdot x} \right)$$

where  $\omega_k = \sqrt{k^2 + m_{\phi_T}^2}$ , and  $[a_k, a_{k'}^\dagger] = (2\pi)^3 \delta^3(k - k')$ . The Feynman propagator is:

$$\langle 0 | T \phi_T(x) \phi_T(y) | 0 \rangle = \int \frac{d^4k}{(2\pi)^4} \frac{i}{k^2 - m_{\phi_T}^2 + i\epsilon} e^{-ik \cdot (x-y)}$$

This ensures perturbative consistency, with CPT-violating effects computed via Feynman diagrams incorporating  $\phi_T$ .

FTFT's embedding in  $E_8 \times E_8$  Heterotic String Theory supports CPT violation through worldsheet correlators linking  $\phi_T$ , graviton, and matter fields, consistent with the mixing term  $\kappa \phi_T h_{\mu\nu} T_{\text{matter}}^{\mu\nu}$ .

## 6 Experimental Outlook

As of August 2, 2025, no experimental data confirms FTFT's CPT-violating signatures. Key experiments include:

- **CMS (ongoing–2028)**: Probing SSDL asymmetries ( $\Delta t_{\ell\ell} \approx 1.5$  fs).
- **DUNE (2028–2030)**: Testing neutrino oscillation CPT violation.
- **Belle II (2027), LHCb (ongoing)**: Measuring meson oscillation asymmetries.
- **Simons Observatory (2030s)**: Detecting CMB anomalies.

## 7 Conclusion

FTFT's quantized time structure, via the temporal scalar field  $\phi_T$ , naturally induces CPT violation through oscillatory dynamics, non-local interactions, and graviton mixing. The predicted signatures—temporal asymmetries in high-energy collisions, neutrino oscillation anomalies, and cosmological CMB distortions—are mathematically consistent with FTFT's QFT framework and testable by upcoming experiments. If validated, these signatures could redefine fundamental symmetries, establishing time as a dynamical field in physics.