

MRS21-LESSON-5

Mr. Pineda

Aim: What are complex numbers? (Section 4-8)

Do Now: What are the roots for  $5x^2+20$ ?

$$5x^2 + 20 = 0$$

$$5x^2 = -20$$

$$x^2 = \frac{-20}{5}$$

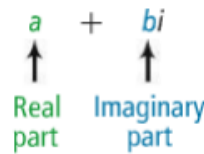
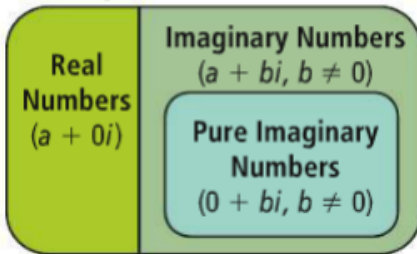
$$x^2 = -4$$

$$x = \pm \sqrt{-4}$$

ERROR FOR REAL numbers.

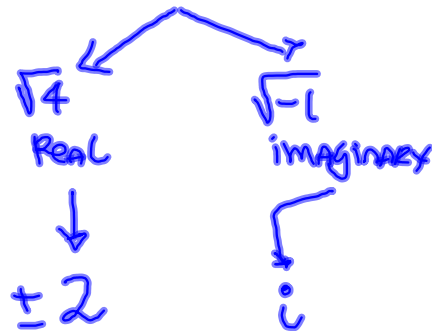
I- Complex Numbers

Complex Numbers ( $a + bi$ )



EXAMPLE

$$\sqrt{-4}$$



$$= \boxed{\pm 2i}$$

Rewrite it

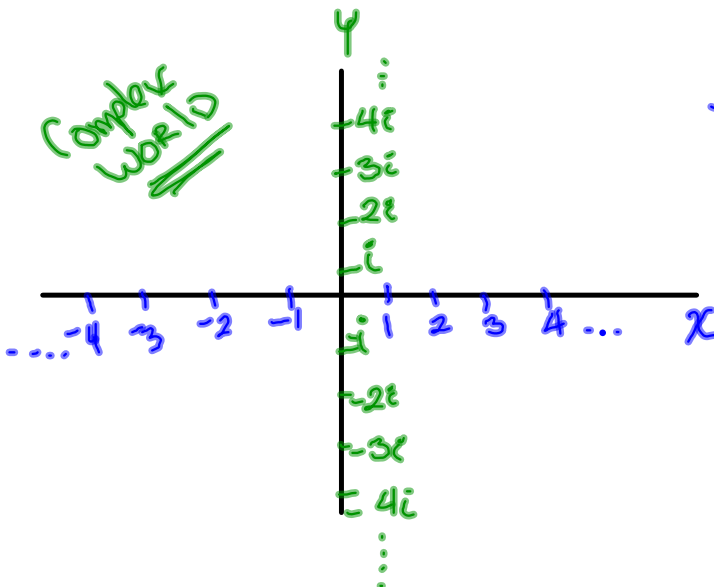
$$0 \pm 2i$$

Real            Imaginary

Complex Number

$$\sqrt{-1} = i$$

Complex World



1- Powers i

$$\sqrt{2} \cdot \sqrt{2} = 2$$

$$\sqrt{x} \cdot \sqrt{x} = x$$

$$\sqrt{6} \cdot \sqrt{6} = 6$$

$$\sqrt{36}$$

$$\sqrt{-1} \cdot \sqrt{-1} = -1$$

The **imaginary unit**  $i$  is the complex number whose square is  $-1$ . So,  $i^2 = -1$ , and  $i = \sqrt{-1}$ .

2) Circle of answers

$$\sqrt{-1} = i$$

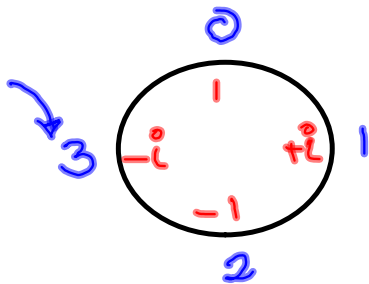
$$\sqrt{-1} \cdot \sqrt{-1} = i^2 = -1$$

$$\sqrt{-1} \cdot \sqrt{-1} \cdot \sqrt{-1} = i^3 = i \cdot i^2 = -i$$

$$\underbrace{\sqrt{-1} \cdot \sqrt{-1}}_{-1} \cdot \underbrace{\sqrt{-1} \cdot \sqrt{-1}}_{-1} = i^4 = +1$$

$$= i^5 = i \cdot i^4 = i$$

$$= i^6 = -1 = i \cdot i^5 = -1$$



$$i^4 = 1 \rightarrow 4 \div 4 = \text{Remainder } 0$$

$$i^6 = -1 \rightarrow 6 \div 4 = \text{Remainder } 2$$

$$i^3 = -i \rightarrow 3 \div 4 = \text{Remainder } 3$$

$$i^{99} = -i \rightarrow 99 \div 4 = \text{Remainder } 3$$

$$\begin{array}{r} 24 \\ 4 \overline{) 99} \\ \underline{-8} \phantom{0} \\ 19 \\ \underline{-16} \\ 3 \text{ Remainder} \end{array}$$

3) Simplify each number by using the imaginary number  $i$ .

1.  $\sqrt{-100}$

$\sqrt{-1 \times 100}$

$\sqrt{-1} \times \sqrt{100}$

$$\begin{array}{c} \sqrt{-100} \\ \swarrow \quad \searrow \\ \sqrt{-1} \quad \sqrt{100} \\ \downarrow \quad \downarrow \\ i \quad \pm 10 \\ \hline \pm 10i \end{array}$$

2.  $\sqrt{-2}$

$\pm \sqrt{2} i$

3.  $\sqrt{-48}$

$$\begin{array}{c} \sqrt{-48} \\ \swarrow \quad \searrow \\ \sqrt{-1} \quad \sqrt{48} \\ \downarrow \quad \downarrow \quad \downarrow \\ i \quad \sqrt{16} \quad \sqrt{3} \\ \downarrow \quad \downarrow \\ i \quad \pm 4 \quad \sqrt{3} \\ \hline \pm 4i\sqrt{3} \end{array}$$

4.  $\sqrt{-36}$

$\pm 6i$

$$\begin{array}{c} \sqrt{-36} \\ \swarrow \quad \searrow \\ \sqrt{-1} \quad \sqrt{36} \end{array}$$

II – Graphing Complex Numbers

Plot each complex number and find its absolute value.

5.  $5i$

$(0 + 5i)$

6.  $3 + 2i$

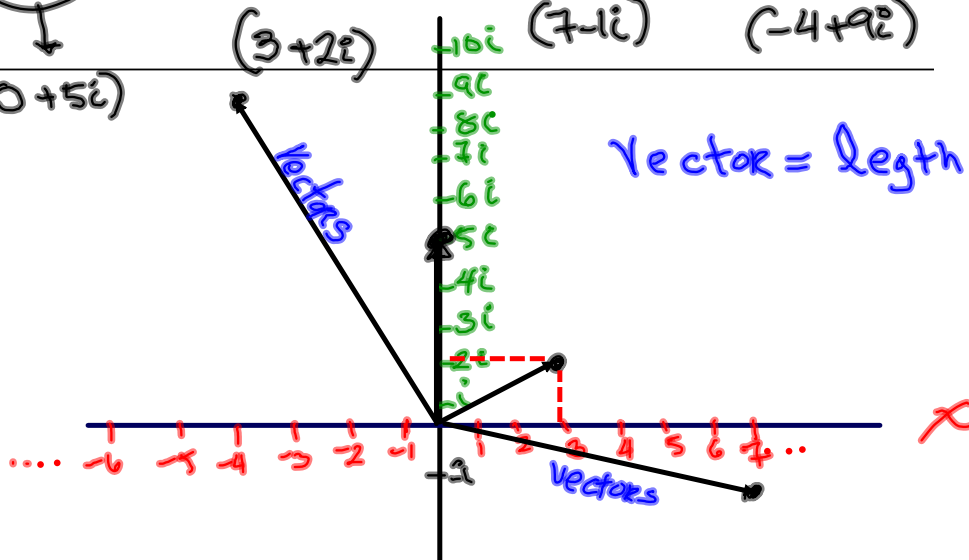
$(3 + 2i)$

7.  $7 - 1i$

$(7 - 1i)$

8.  $-4 + 9i$

$(-4 + 9i)$



## III – Operations with Complex Numbers

1- Simplify each expression.

$$9. (9 + 6i) + (2 - i)$$

$$(9 + 2) + (6i - i)$$

$$11 + 5i$$

$$10. (-12i) - (3 + 3i)$$

$$-3 - 3i$$

$$-12i$$

$$-3 - 15i$$

$$11. (-2i)(5 + 4i)$$

multiplication

$$= -10i - 8i^2$$

$$= -10i - 8(-1)$$

$$= -10i + 8$$

Don't forget

$$i^2 = (-1)$$

Write each quotient as a complex number.

12.  $\frac{5+4i}{7i}$

$$\frac{5+4i-7i}{7i} = \frac{5-3i}{7i}$$

13.  $\frac{-1+5i}{3-2i} \cdot \frac{3+2i}{3+2i} =$

14.  $\frac{2-6i}{2-3i} \cdot \frac{2+3i}{2+3i} =$

$$\frac{5+4i}{7i} \cdot \frac{-7i}{-7i} = \frac{-35i-28i^2}{-49i^2}$$

$$= \frac{-35i-28(-1)}{-49(-1)} = \frac{-35i+28}{49}$$

complex #

$$\frac{28}{49} - \frac{35i}{49}$$
  
$$\boxed{a+bi}$$
  
form

**15. Error Analysis** Robert solved the equation  $2x^2 + 16 = 0$ . His solution was  $x = \pm\sqrt{-8i}$ . What errors did Robert make? What is the correct solution?

Complete on  
your own