

Aim: How do we rewrite expressions involving radicals and rational exponents using the properties of exponents? (Section 6-1)

Do now:

Simplify each expression. Use only positive exponents.

take note

Properties Properties of Exponents

- $a^0 = 1, a \neq 0$
- $\frac{a^m}{a^n} = a^{m-n}$

- $a^{-n} = \frac{1}{a^n}$
- $(ab)^n = a^n b^n$
- $(a^m)^n = a^{mn}$

- $a^m \cdot a^n = a^{m+n}$
- $\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$

1. $(2a^3)(5a^4)$

2. $(-3x^2)(-4x^{-2})$

3. $(3x^2y^3)^2$

4. $(3x^{-4}y^3)^2$

5. $\frac{4a^0}{2a^4} = \frac{2 \cdot 2 \cancel{a^0 a^0 a^0 a^0 a^0}}{2 a^4 a^4}$

6. $\frac{12x^5y^3}{4x^{-1}}$

Answers:

1) $10a^7$

2) $+12x^0 = 12$

5) $2a^4$

6) $3x^6y^3$

3) $9x^4y^6$

4) $9x^{-8}y^6$

$(3x^{-4}y^3)^2 = (3x^{-4}y^3)(3x^{-4}y^3)$

$x^{-4} \cdot x^{-4} = x^{-4+(-4)} = x^{-8}$

$\frac{9y^6}{x^8}$

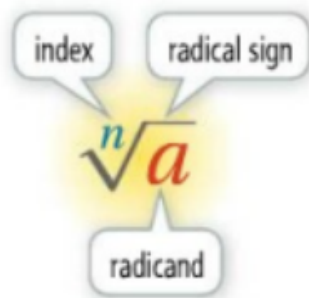
Reasoning Your friend tells you that $(k^2)^{-5} = -k^{10}$. Did she apply the properties of exponents correctly? Explain why or why not.

NO CORRECT

CORRECT k^{-10} OR $\frac{1}{k^{10}}$

I- Finding all real roots

1)



2)

Find all the real square roots of each number.

1. 625

$$\sqrt{625} = \pm 25$$

$$\left\{ \begin{array}{l} 25 \times 25 = 625 \\ -25 \times -25 = 625 \end{array} \right.$$

2. -1.44 =

No Real

$$\left. \begin{array}{l} \text{Root} \leftarrow \\ \sqrt{-1.44} \end{array} \right\}$$

3. $\frac{16}{81}$

$$\sqrt{\frac{16}{81}} = \pm \frac{4}{9}$$

3)

Find all the real cube roots of each number.

4. -216

5. $\frac{1}{64}$

6. 0.027

$$\sqrt[3]{-216} = -6$$

$$\sqrt[3]{\frac{1}{64}} = \frac{1}{4}$$

$$\sqrt[3]{0.027} = 0.3$$

II- Simplifying Radical Expressions

1)

Take note

Property n th Roots of n th Powers

For any real number a , $\sqrt[n]{a^n} = \begin{cases} a & \text{if } n \text{ is odd} \\ |a| & \text{if } n \text{ is even} \end{cases}$

Piecewise equations
(choice)

2) Simplify each radical expression. Use absolute value symbols when needed. To start, write the factors of the radicand as perfect squares, cubes, or fourths.

1. $\sqrt{25x^6}$

$$\hookrightarrow \sqrt{(5)^2(x^3)^2} = \sqrt{(5x^3)^2}$$

$$\begin{aligned} \sqrt{=} &= 5|x^3| &= |5x^3| \\ &= 5x^3 \end{aligned}$$

2. $\sqrt[3]{343x^9y^{12}} = \text{No problem}$

3. $\sqrt[4]{16x^{16}y^{20}} = \sqrt[4]{(2x^4y^5)^4}$

$$2x^4|y^5|$$

III- Using Radical Expressions

Academics Some teachers adjust test scores when a test is difficult. One teacher's formula for adjusting scores is $A = 10\sqrt{R}$, where A is the adjusted score and R is the raw score. If the raw scores on one test range from 36 to 90, what is the range of the adjusted scores?

on your own!