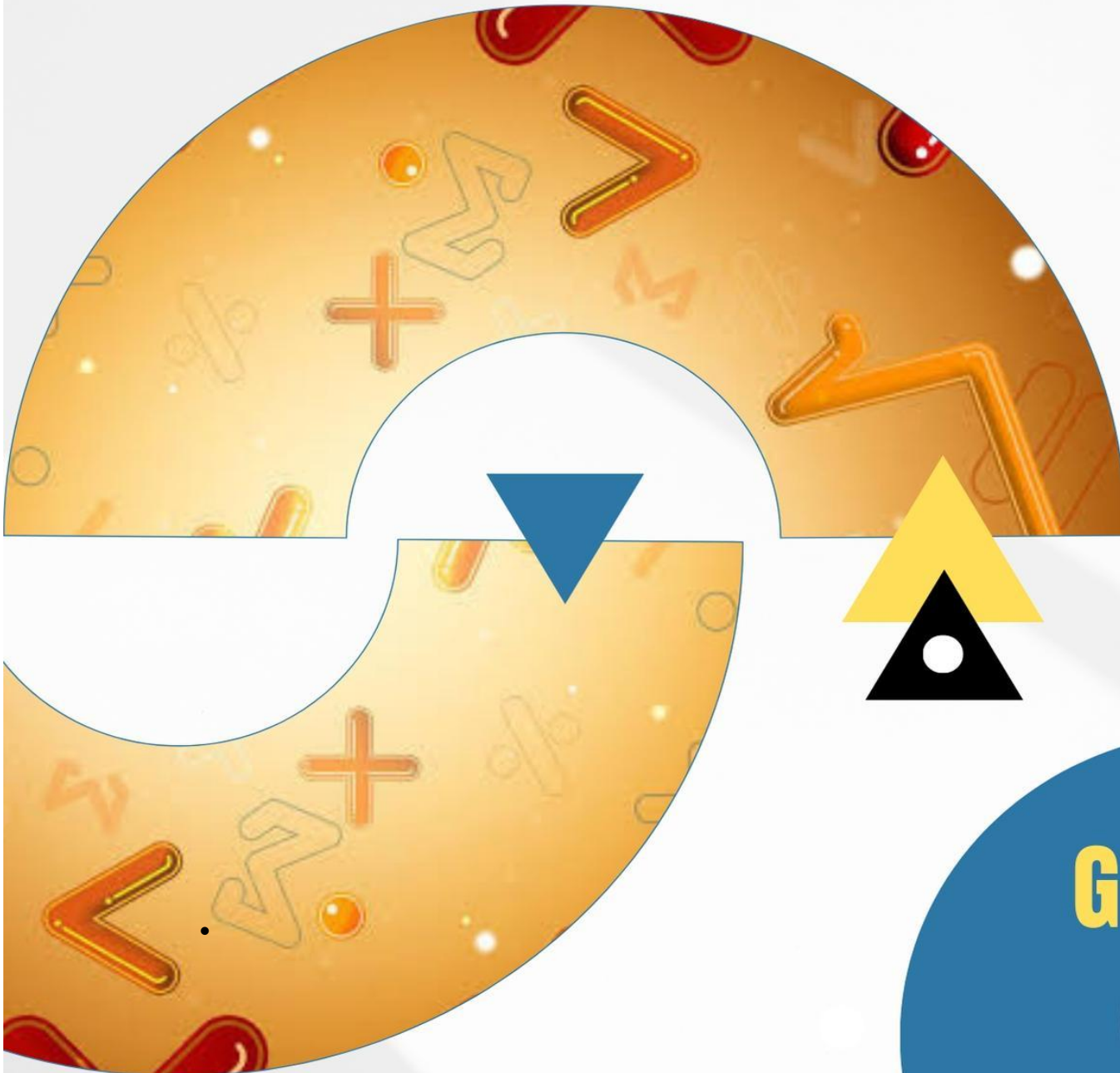


# Mathematics

## FINANCE: FINANCIAL MATHEMATICS

Study guide & worksheets



GRADE

9

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## Introduction:

Welcome to the **Grade 9 Mathematics: Finance Study Guide**! This guide is designed to help you develop a strong understanding of financial mathematics, a key part of everyday life. Whether you are calculating interest, budgeting your money, or understanding VAT, finance plays an essential role in making informed decisions about money management.

### Why is Financial Mathematics Important?

Financial mathematics helps you:

- **Manage money wisely** by understanding income, expenses, savings, and budgeting.
- **Make smart financial decisions** when dealing with profit and loss, interest rates, and exchange rates.
- **Apply math to real-life situations**, such as shopping, banking, and investing.

### What You Will Learn in This Guide

This study guide covers the essential topics in Grade 9 Finance Mathematics, including:

- **Income, expenses, and budgeting**
- **Profit, loss, and percentage calculations**
- **Simple and compound interest calculations**
- **VAT (Value-Added Tax) and its application**
- **Exchange rates and currency conversions**
- **Exam preparation and problem-solving strategies**

### How to Use This Guide

- **Read through each topic carefully** and understand the key concepts.
- **Practice regularly** using the examples and exercises provided.
- **Use the formula sheet in the appendix** to help with calculations.
- **Attempt past exam questions** to test your understanding and improve your problem-solving skills.

## Introduction to Finance in Mathematics

Finance in Mathematics focuses on managing money, making calculations related to earnings, savings, and expenses, and understanding financial concepts like interest, tax, and budgeting. These skills help in making informed financial decisions in real life.

### Income and Expenses

Income: Money earned from different sources, such as:

- **Salary/Wages:** Earnings from employment
- **Commission:** Earnings based on sales percentage
- **Interest:** Money earned from savings
- **Rent Received:** Money earned from renting property

Expenses: Money spent on various needs, such as:

- **Fixed Expenses:** Constant costs like rent and school fees
- **Variable Expenses:** Costs that change, like groceries and entertainment

**Formula:**

$\text{Net Income} = \text{Total Income} - \text{Total Expenses}$

## **Profit and Loss**

Profit and loss are calculated in business transactions.

Profit: When income is greater than expenses.

Profit=Selling Price–Cost Price

Loss: When expenses are greater than income.

Loss=Cost Price–Selling Price

**Example:** If a shop buys a book for R50 and sells it for R70, the profit is:

Profit=R70–R50=R20

## **Simple and Compound Interest**

Simple Interest (SI)

Interest earned on the original amount (principal) only.

**Formula:**

$SI = P \times r \times t$

Where:

- **P** = Principal amount (initial money)
- **r** = Interest rate (in decimal form)
- **t** = Time (in years)

**Example:** If R2,000 is invested at 5% per year for 3 years:

$SI = 2000 \times 0.05 \times 3 = R300$

### Compound Interest (CI)

Interest earned on both the principal and previously earned interest.

#### **Formula:**

$$A = P \times (1 + r)^t$$

Where:

- **A** = Final amount
- **P** = Principal amount
- **r** = Interest rate per period
- **t** = Time (in years)

**Example:** If R2,000 is invested at 5% per year for 3 years:

$$A = 2000 \times (1 + 0.05)^3$$

$$A = 2000 (1 + 0.05)^3$$

$$A = 2000 \times 1.157625 = R2315.25$$

**Compound interest earned:**  $R2315.25 - R2000 = R315.25$

### **VAT (Value-Added Tax)**

VAT is a tax added to the price of goods and services. In South Africa, the standard VAT rate is **15%**.

#### **Formula:**

$$\text{VAT} = \text{Price} \times 0.15$$

$$\text{Total Price} = \text{Price} + \text{VAT}$$

**Example 1:** If an item costs R200 before VAT:

$$\text{VAT} = 200 \times 0.15 = \text{R}30$$

$$\text{Total Price} = 200 + 30 = \text{R}230$$

Example 1:

A store sells a pair of shoes for **R850** before VAT. In South Africa, VAT is charged at **15%**.

Calculate:

1. Calculate the VAT amount.
2. Find the total price after VAT.

Solution:

#### **Step 1: Calculate VAT Amount**

$$\text{VAT} = \text{Price} \times 15\%$$

$$= 850 \times 0.15$$

$$= \text{R}127.50$$

#### **Step 2: Find the Total Price Including VAT**

$$\text{Total Price} = \text{Price} + \text{VAT}$$

$$= 850 + 127.50$$

=R977.50

- **VAT Amount = R127.50**
- **Total Price After VAT = R977.50**

### **Exchange Rates**

Exchange rates determine the value of one currency compared to another.

#### **Formula:**

Foreign Currency=Local Currency÷Exchange Rate

Local Currency=Foreign Currency×Exchange Rate

**Example 1:** If 1 US Dollar = R18, then R360 can be exchanged for:

$$360 \div 18 = 20 \text{ US Dollars} \quad 360 \div 18 = 20$$

#### **Example 2:**

##### **Question:**

Lebo is traveling to the United States. She exchanges **R3,600** into US dollars. The exchange rate is **1 USD = R18**. How much money will she receive in US dollars?

##### **Solution:**

##### **Answer:**

Lebo will receive **200 US dollars**.

##### **Workings:**

## **Budgeting and Financial Planning**

A **budget** is a plan that tracks income and expenses. It helps individuals and businesses manage their money effectively.

### **Steps to Create a Budget:**

1. Identify sources of income.
2. List all expenses (fixed and variable).
3. Subtract total expenses from income.
4. Adjust spending if expenses exceed income.

### **Example Budget:**

Category	Amount (R)
Income	5,000
Rent	2,000
Groceries	1,200
Transport	500
Savings	300
Entertainment	500
<b>Total Expenses</b>	<b>4,500</b>
<b>Balance (Savings)</b>	<b>500</b>

## Study Tips for Grade 9 Mathematics: Finance

### 1. Understand the Concepts First

- Before memorizing formulas, make sure you **understand the meaning** behind them.
- Relate finance concepts to **real-life situations** (e.g., calculating VAT while shopping or interest on savings).

### 2. Master Key Formulas

- Write down all important formulas for **Simple Interest, Compound Interest, VAT, Exchange Rates, Profit & Loss, and Budgeting** on a formula sheet.
- Practice applying these formulas in different types of questions.

### 3. Practice Regularly

- Solve **at least 5-10 finance questions daily** to improve accuracy and speed.
- Start with **easy questions** and gradually move to **challenging word problems**.

### 4. Show All Steps in Calculations

- Always **write down formulas before substituting numbers** in your calculations.
- Check your work step-by-step to avoid unnecessary mistakes.

### 5. Use Past Papers and Worksheets

- Attempt previous exam papers to **familiarize yourself with the format and types of questions**.
- Time yourself while answering to **improve speed and efficiency**.

### 6. Identify and Correct Mistakes

- Review incorrect answers to **understand where you went wrong**.
- Ask teachers or peers for **explanations if you don't understand something**.

### 7. Create Summary Notes

- Use **mind maps, tables, and flashcards** to summarize key concepts.
- Highlight important points like **common errors and useful shortcuts**.

## 8. Apply Finance to Real Life

- Practice finance concepts in daily life (e.g., **calculate the VAT on purchases, estimate interest on savings, or convert currency when traveling**).
- This makes the subject **more practical and easier to remember**.

## 9. Group Study and Discussion

- Study with friends to **explain concepts to each other**.
- Teaching someone else helps you **remember better**.

## 10. Stay Calm and Manage Exam Stress

- Get **enough rest before exams** to improve concentration.
- Read each question carefully before solving.
- If stuck on a question, **move on and come back later** to save time.

## Exam Practice Questions & Answers

### Multiple Choice Questions (MCQs)

1. If a shop buys an item for R150 and sells it for R200, what is the profit?  
A) R50  
B) R150  
C) R200  
D) R100

**Answer:** A) R50

2. If R5,000 is invested at 6% simple interest for 2 years, how much interest is earned?  
A) R600  
B) R300  
C) R150  
D) R1,200

**Answer:** A) R600

### Word Problems

#### 1. Calculate VAT on an item priced at R500 before VAT.

- $\text{VAT} = \text{R}500 \times 0.15 = \text{R}75$
- $\text{Total price after VAT} = \text{R}500 + \text{R}75 = \text{R}575$

#### 2. A person invests R10,000 at an interest rate of 8% per year, compounded annually for 3 years. Calculate the final amount.

- $A = 10,000 \times (1 + 0.08)^3$
- $A = 10,000 \times 1.2597 = \text{R}12,597$

## Exam Practice Questions

### Section A

#### Question 1: Multiple-Choice Questions (*Choose the correct answer.*)

1.1 If a person earns R8,000 per month and spends R6,500, how much is their savings?

- A) R1,500
- B) R6,500
- C) R8,000
- D) R2,500

○ **Answer:** A) R1,500

1.2 A shop buys a product for R120 and sells it for R150. What is the profit?

- A) R30
- B) R270
- C) R150
- D) R120

○ **Answer:** A) R30

1.3 The VAT on an item is R45, and the total price after VAT is R345. What was the original price before VAT?

- A) R390
- B) R300
- C) R345
- D) R255

○ **Answer:** B) R300

1.4 A person deposits R5,000 in a bank account with a simple interest rate of 5% per year. How much interest is earned after 3 years?

- A) R250
- B) R750
- C) R1,500
- D) R2,000

○ **Answer:** B) R750

( $SI = 5000 \times 0.05 \times 3 = 750$ )

1.5 If 1 US Dollar = R19, how much is R380 worth in US Dollars?

- A) 10
- B) 15

C) 20

D) 25

1.6 **Answer:** C) 20

$$(380 \div 19 = 20 \text{ USD})$$

## Section B: Short Answer Questions

6. A jacket costs R800 before VAT. Calculate:

a) The VAT amount (15%).

b) The final price after VAT.

○ **Answer:**

a)  $\text{VAT} = \text{R}800 \times 0.15 = \text{R}120$

b)  $\text{Final price} = \text{R}800 + \text{R}120 = \text{R}920$

7. Calculate the profit or loss if a business buys a product for R350 and sells it for R280.

○ **Answer:**

$\text{Loss} = \text{R}350 - \text{R}280 = \text{R}70$  (Since the selling price is lower, it's a loss.)

8. An investment of R12,000 earns simple interest at a rate of 7% per year for 5 years. Calculate the total interest earned.

○ **Answer:**

$\text{SI} = 12,000 \times 0.07 \times 5 = \text{R}4,200$

## Section C: Word Problems

9. **Budgeting Problem:**

Thabo earns R10,000 per month. He spends:

- Rent: R3,500
- Groceries: R2,000
- Transport: R1,500
- Savings: R1,200
- Entertainment: R800

a) Calculate Thabo's total expenses.

b) How much money does he have left after expenses?

○ **Answer:**

a)  $\text{Total expenses} = 3,500 + 2,000 + 1,500 + 1,200 + 800 = \text{R}9,000$

b)  $\text{Remaining money} = \text{R}10,000 - \text{R}9,000 = \text{R}1,000$

10. **Compound Interest Problem:**

Sipho deposits R5,000 in a bank account at an interest rate of 6% per year, compounded annually for 2 years. Calculate the total amount after 2 years.

○ **Answer:**  $A = 5000 \times (1 + 0.06)^2$   
 $A = 5000 \times 1.1236 = \text{R}5,618$   
 $5000 \times 1.1236 = \text{R}5,618$  **Total amount after 2 years = R5,618**

11. A business sells a product for R400. The profit margin is 25%. Calculate the cost price of the product.

- **Answer:** (Cost Price) = (Selling Price)(1 + Profit %) =  $400(1.25) = R500$
12. A cellphone is priced at R6,500. A store offers a payment plan where customers can pay in **12 monthly installments** with a **10% total interest** applied to the original price.
- a) Calculate the total amount to be paid.
  - b) Find the monthly installment.
- **Answer:**
    - a) **Total amount =  $6,500 \times 1.10 = R7,150$**
    - b) **Monthly installment =  $7,150 \div 12 = R595.83$**

## Finance Worksheet

### Instructions:

- Answer all questions.
  - Show all calculations.
  - Round off answers where necessary.
- 

### Section A: Multiple-Choice Questions (*4 marks*)

Choose the correct answer.

1.1 If a person earns R12,000 and spends R9,500, how much is their savings?

- A) R3,500
- B) R2,500
- C) R9,500
- D) R12,000

1.2 A shop buys an item for R180 and sells it for R250. What is the profit?

- A) R80
- B) R70
- C) R250
- D) R180

1.3 Calculate the VAT amount on an item that costs R600 before VAT (15%).

- A) R90
- B) R100
- C) R120
- D) R150

1.4 If the exchange rate is **1 US Dollar = R18**, how much is **R540** worth in US Dollars?

- A) 20 USD
- B) 30 USD
- C) 40 USD
- D) 50 USD

## Section B

### Question 2: Short Answer Questions (12 marks)

2.1 A dress costs R750 before VAT. Calculate:

a) The VAT amount (15%).

b) The final price after VAT.

2.2 Calculate the profit or loss if a business buys a product for R420 and sells it for R390.

2.3 A person deposits R8,000 in a bank account at a simple interest rate of 5% per year for 4 years. Calculate the total interest earned.

## Section C

### 3 Question 3: Word Problems (14 marks). **Budgeting Problem:**

A family earns R20,000 per month. They spend:

3.1 Rent: R6,500

3.2 Food: R4,000

3.3 Transport: R2,500

3.4 School fees: R3,000

3.5 Entertainment: R2,000

a) Calculate the total monthly expenses. (3)

b) How much money is left after expenses? (2)

### 4 **Compound Interest Problem:**

A person deposits R10,000 in a bank account at an interest rate of 7% per year, compounded annually for 3 years. Calculate the final amount. (5)

### 5 A store sells a laptop for R9,000. A payment plan allows customers to pay in **12 monthly installments**, with a **10% total interest** applied to the original price.

a) Calculate the total amount to be paid. (3)

b) Find the monthly installment. (2)

## MEMORANDUM

### Section A

#### Question 1: Multiple-Choice Questions (4 marks, 1 mark each)

**1.1 B) R2,500** Savings=Income–Expenses=12,000–9,500=R2,500

**1.2 B) R70** Profit=Selling Price–Cost Price=250–180=R70

**1.3 C) R90** VAT=600×0.15=R90

**1.4 B) 30 USD** USD=54018=30

### Section B

#### Question 2: Short Answer Questions (12 marks)

**2.1 a) VAT = R750 × 0.15 = R112.50 (2)**

**2.2 b) Final price = R750 + R112.50 = R862.50 (1)**

**2.3 Loss = R420 - R390 = R30 (3)**

#### **Simple Interest:**

$$SI = P \times r \times t$$

$$= 8000 \times 0.05 \times 4$$

$$= R1,600 SI$$

**Total interest earned = R1,600 (3)**

#### Word Problems (14 marks)

#### **4. a) Total expenses:**

$$a) 6,500 + 4,000 + 2,500 + 3,000 + 2,000 = R18,000 (3)$$

$$b) \text{Remaining money: } 20,000 - 18,000 = R2,000 (2)$$

#### **6. Compound Interest Calculation:**

$$A = P(1 + r)^t \quad A = 10,000(1 + 0.07)^3 \quad A = 10,000(1.225043) \quad A = 10,000(1.225043)$$

$$A = R12,250.43. \quad A = R12,250.43$$

**Final amount = R12,250.43 (5)**

## Appendix

### A. Financial Formulas

#### 1. Simple Interest

$$\mathbf{SI = P \times r \times t}$$

Where:

- **SI** = Simple Interest
- **P** = Principal Amount (Initial Money)
- **r** = Interest Rate (as a decimal)
- **t** = Time (in years)

#### 2. Compound Interest

$$\mathbf{A = P (1 + r)^t}$$

Where:

- **A** = Final Amount
- **P** = Principal Amount
- **r** = Interest Rate (as a decimal)
- **t** = Time (in years)

#### 3. Profit and Loss

- **Profit = Selling Price - Cost Price**
- **Loss = Cost Price - Selling Price**

#### 4. Value-Added Tax (VAT) (15%)

- **VAT Amount = Price  $\times$  0.15**
- **Price Including VAT = Price + VAT**
- **Price Before VAT = Total Price  $\div$  1.15**

#### 5. Budgeting Formula

$$\mathbf{Savings = Income - Expenses}$$

## B. Important Definitions

### 1. Interest

The extra money earned or paid on a principal amount.

- **Simple Interest:** Earned only on the original principal.
- **Compound Interest:** Earned on both the principal and previously earned interest.

### 2. VAT (Value-Added Tax)

A tax added to goods and services at 15% in South Africa.

### 3. Profit and Loss

- **Profit:** When selling price is greater than cost price.
- **Loss:** When selling price is less than cost price.

### 4. Exchange Rate

The value of one currency compared to another (e.g., 1 USD = R19).

### 5. Budget

A plan that shows income and expenses to help manage money effectively.

## C. Common Mistakes and How to Avoid Them

### 1. Forgetting to convert percentages to decimals

- Example: 5% should be written as **0.05** in calculations.

### 2. Incorrectly applying VAT

- Always **add** VAT to the original price when finding the total.
- Always **divide by 1.15** when finding the price before VAT.

### 3. Misusing Exchange Rates

- Always **check if you are converting from local to foreign or vice versa.**

### 4. Not showing steps in calculations

- Always **write down formulas before substituting values.**

### 5. Skipping word problems

- **Underline important numbers and key terms** before solving.

#### D. Additional Resources

- **Textbooks:**
  - Grade 9 Mathematics CAPS-approved textbooks
  - Financial Mathematics resources
- **Websites for Extra Practice:**
  - Khan Academy ([www.khanacademy.org](http://www.khanacademy.org))
  - Siyavula ([www.siyavula.com](http://www.siyavula.com))
- **Past Exam Papers:**
  - DBE (Department of Basic Education) website
  - School and Provincial Education Portals

## References

Below are the sources used in compiling this study guide:

Textbooks & Curriculum Guidelines:

- Department of Basic Education (DBE). *Mathematics Grade 9 CAPS Curriculum*. Pretoria: Government Printer, Latest Edition.
- Siyavula. *Mathematics Grade 9 Learner's Guide*. Available at: [www.siyavula.com](http://www.siyavula.com)

Online Educational Resources:

- Khan Academy. *Financial Mathematics and Interest Calculations*. Available at: [www.khanacademy.org](http://www.khanacademy.org)
- South African Revenue Service (SARS). *Value-Added Tax Guidelines*. Available at: [www.sars.gov.za](http://www.sars.gov.za)

Past Exam Papers & Study Material:

- National Senior Certificate (NSC) Past Papers, DBE website: [www.education.gov.za](http://www.education.gov.za)
- Provincial Education Departments' online portals for Mathematics study material.

Other References:

- Business Insider SA. *Current Exchange Rates and Economic Trends in South Africa*. Available at: [www.businessinsider.co.za](http://www.businessinsider.co.za)
- Financial Literacy SA. *Managing Personal Finance – A Guide for Students*. Johannesburg: FL South Africa, 2024.



# Mathematics

Master Financial Mathematics with Confidence

This Grade 9 Mathematics: Finance Study Guide is designed to help you understand and apply essential financial concepts with ease. Covering key topics such as income and expenses, profit and loss, interest calculations, VAT, budgeting, and exchange rates, this guide provides clear explanations, step-by-step examples, and practice questions to boost your confidence.

Inside, you'll find:

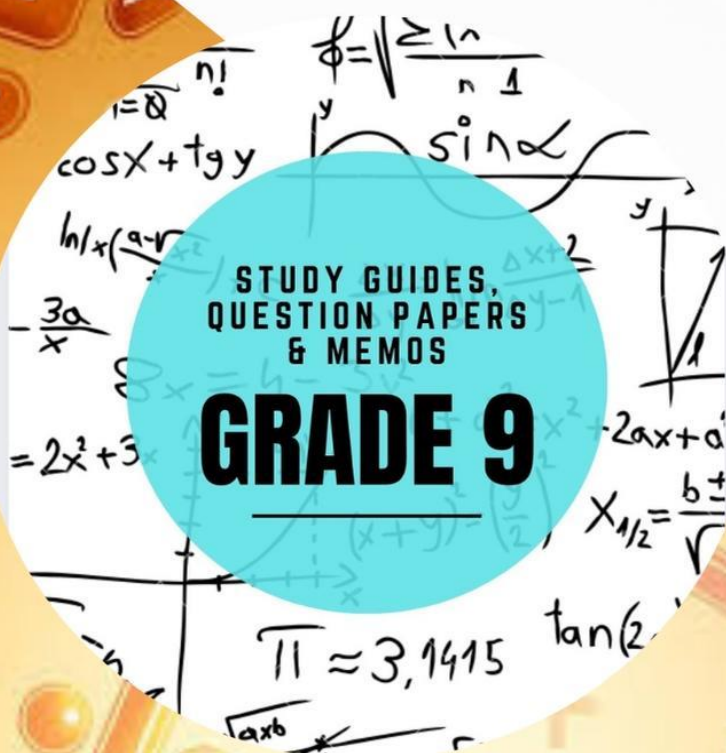
- ✓ Easy-to-understand notes with real-life applications
- ✓ Worked-out examples to guide you through calculations
- ✓ Practice exercises with answers to test your knowledge
- ✓ Study tips and exam strategies to help you perform your best

Whether you're preparing for exams or looking to improve your financial skills, this study guide is your perfect companion for success in Mathematics. Take control of your learning and achieve your best results!

[www.emmanuelsthole.co.za](http://www.emmanuelsthole.co.za)

[www.youdefineus.co.za](http://www.youdefineus.co.za)

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STUDY GUIDES,  
QUESTION PAPERS  
& MEMOS

**GRADE 9**

**GRADE**

**9**