KEY STAGE 2 GRADES 3-5

Mathematical Treasure Hunt

Mathematical Treasure Hunt

Instructions for Teachers

Introduction

The mathematical treasure hunt is a great activity for fun and engaging mathematics lessons: the pupils follow a trail of clues and mathematical problems around the school site; each clue contains a hint to where the next clue is hidden.

This document includes clues and questions intended for Key Stage 2 (UK) or grades 6–8 (US).

The treasure hunt works best when the class is divided into groups of about 5 children of different abilities. Working in a team, and in a competition, supports team working skills, and even children with difficulties in mathematics can participate.

The questions are taken from a wide range of different topics, and often not directly related to the mathematics curriculum. Some of the problems lend themselves to further discussion afterwards; often there is an article on that topic in the Mathigon World of Mathematics.

The answer to each problem is an integer, and all the answers – once decoded into letters – spell the location of the treasure.: the library.

The Questions

	Name	Locations	Solution	0	rder	of '	Геан	ns
A	Cryptography		18	1	9	7	5	3
B	Combinatorics		18	2	10	8	6	4
С	Graph Theory	A Martin	2	3	1	9	7	5
D	Number Pyramid	ALL VILLEY	9	4	2	10	8	6
E	Pascal's Triangle		8	5	3	1	9	7
F	Prime Numbers		25	6	4	2	10	8
G	Probability	A REAL PROPERTY AND	20	7	5	3	1	9
Η	Platonic Solids		12	8	6	4	2	10
Ι	Tangram		1	9	7	5	3	1
J	Secret Numbers		5	10	8	6	4	2

Preparation

First choose 10 locations in your school where to hide the different questions (see previous table). Either use the prepared clues (pages 9–10) or come up with your own clues (pages 11–12) to lead to these questions. Print the clues once for each team.

Make sure that the class is able to solve all the problems. Print the introductory sheets and questions (pages 3–8) once for every team and cut them in the middle. Print and cut the additional materials for various problems (pages 13–15).

Put the questions, materials as well as the clues leading to the *next* question into an envelope, and hide the 10 envelopes around the school site. Keep the two introductory sheets for each team, as well as a different clue for each team – the ones leading to their first problem.

At the beginning of the lesson, divide the class into a couple of teams and give each team the two introductory sheets, as well as their first clue. The treasure is hidden in the library – usually chocolate works well...

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Page 3	Introductory Sheets
Pages 4–8	Problems
Pages 9–10	Clues
Pages 11–12	Customisable Clues
Pages 13–15	Additional Materials

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INSTRUCTIONS

Professor Integer was one of the world's most famous mathematicians, who made discoveries that changed the world forever: from algorithms for computers and internet to statistical calculations and quantum mechanical predictions.

When he died, he had no relatives or close friends but a very large fortune. He believed that only the best mathematicians deserved to find his treasure and created a trail of puzzles and problems.

Many of his diary pages, notes and letters are archived at the University of Cantortown, and they all include clues and hints regarding the location of the treasure.

This treasure hunt will require you to move around your school, find the hidden clues and solve mathematical problems. Each question will contain a clue about where the next problem will be hidden, but every team solves the problems in a different order.

When you find an envelope, take <u>one</u> problem page and <u>one</u> clue. Try to solve the problem, sometimes using additional materials in the envelope; then look for the next problem. You may not find the problems in the correct order!

There are many other children in the school, so avoid any unnecessary noise. Don't leave your solutions behind for the next team to see, and don't take more than one copy of each problem – otherwise following teams might not be able to solve the problem.

You are now ready to receive the first clue and a copy of the last letter written by Professor Integer.

Good luck!

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2	Item (

The Integer Files

Archive of the University of Cantortown Item 0: Last letter of Prof. Integer Item 0 Catalogue Nr. 0010

Peat Mathematicians,

When you tead this letter, f will be dead, and my treasure will be hidden in a bery safe location. Only the best mathematicians deserve to find it.

fn my notes and diaties, f habe left 10 problems which you need to solbe. (The answer to every problem is a single number, which you can write down here:

A B C D E F G H I J

Once you have sofved all problems, turn the numbers into letters (1-a, 2-6,3-c and so on) and bring the letters into the correct order to spell the location of the treasure:

Rutty, though, because othet teams may be onto it as well ...

Ecgards - and good Luck! Hrof. Integer



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The Integer Files	
Archive of the University of Cantortown	Item 1
Item 1: Lined Paper, Cards	Catalogue Nr. 7644

	Prob	LEM A: CRYPTOGRAPHY							
0	I think somebo	ody has broken into my study and stolen important docu-							
	ments and calc	ilations. It is a disaster that I have lost my notes, but it							
	is even worse th	hat the thief can read my discoveries and ideas.							
	In the future.	I need to decisher my notes, so that only I can read							
	them. A very	easy method was invented by Julius Caesar: you just							
	shift ever letter	shift ever letter along the alphabet, for example							
	a b c d e j t u n w x y	t o h i j k l m n o p q r s t n n w x y z i z a b c d e f g h i j k l m n o p q r s							
	The word 'mat	hematician' for example would be shifted to							
0	ftmaxftmbrbtg'.								
	To decipher the	is code, one wonld have to try all 24 possibilities to shift							
	the letter, whic	h could take a very long time. This should keep my notes							
	safe in the futu	re!							
		at mathematics about finding							
		Note: Cryptography is the area of important in wars: dur-							
11-1-1-1	A. A. 10	and breaking codes. It was the Cambridge Mathematician Alter							
	TAX	ing the second telly built one of the first computers to the							
TCL	PYKK	German Enigma coding machine. This could the allied victory.							
-10	INN D	single most important achievement of single most important achievement of							
XB	CAMXX	There are many much more complicated methods be unbreakable and							
0		sentences today, some of which (we use							
		without which internet bunking that mathematical results.							
		prime numbers and many my							

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Read Street	Item 2:
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The Integer Files

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m 2: Spiral Bound Notebook 1, piece of cardbord

Item 2 Catalogue Nr. 0556

PROB	LEM B: COM	MBINATORICS
Yesterday wa 6 presents f packing, a c me: How many for me to un	ns Christmas a From my friend curious quest different o ppack them?	and I received ds. When un- ion occurred to rders are there
For example, bered A, B, possible ord	if the 6 pro C, D, E and 1 ders would be	esent are num- F, then a few
A B B C C D	C D E F E F D A A F E B	Twonder whether you can use simile
but there ar How many are total?	e many more. there in	ideas to calculate the probability to win in lotta. H
I don't thin practical to all possibil	hk it is write down ities -	many ways are the to choose 6 number
500. Maybe t clever metho using mathem	there is a od to do it natics!	out of 49. Chis is related to an area of maths called
To get the key	number	Combinatorics.
for this probler the result by 4	n, divide 0!	



The Integer Files	
Archive of the University of Cantortown	Item 3
Item 3: Spiral Bound Notebook No 2	Catalogue Nr. 5478



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<u> </u>	Archive of the U
2 mars	Item 4: Old piec

Files Iniversity of Cantortown Item 4 ce of paper 1 Catalogue Nr. 1271

PROBLEM D: NUMBER PYRAMID

Last night I was thinking about a large number pyramid. Unfortunately I spilled my coffee, and I lost many of the numbers - only 6 remained legible. I was thinking about it for some time, and I think it is possible to reconstruct the whole pyramid using only those 6 numbers!





The Integer Files	
Archive of the University of Cantortown	Item 5
Item 5: Old piece of paper 2, Pascal's Triangle	Catalogue Nr. 9912

P Orthogonality || Pascal's Triangle

Two lines or curves are <u>orthogonal</u> if they are perpendicular at their point of intersection. Two vectors are orthogonal if and only if their dot product is zero.

Pascal's Triangle

In mathematics, Pascal's triangle is a triangular array of binomial coefficients. It is named after the French mathematician Blaise Pascal, but other mathematicians studied it centuries before him in India and China.

A simple construction of the triangle proceeds in the following manner. In the first row, write only the number 1. Then, to construct the elements of following rows, add the two numbers above a cell to make the number in the new cell. For example, the first number in the first row is $0 \oslash I =$ I, whereas the numbers I and 3 in the third row are added to produce the number 4 in the fourth row.



PROBLEM E: Pascal's Triangle

I tried colouring in all cells divisible by 3 in Pascal's triangle with 16 rows. Guess how long the base of the largest coloured triangle was ...

Pascal's triangle has many interesting properties. It is symmetric, the diagonals are all 1s, the second diagonals are the integers 1, 2, 3, ... and the third diagonal are the triangle numbers 1, 2, 6, 10, ... Many other interesting number sequences and patterns can be found if you look more closely.

A particularly interesting thing happens when you colour in all cells that are divisible by 2 or 3. The result will be a pattern of many more triangles of various sizes. As you try this with bigger and bigger versions of Pascal's triangle, it starts looking like a fractal, a shape which repeats itself on

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6 6 2	A
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Item 6: Diary, 100-tables

Item 6 Catalogue Nr. 7964

How many prime Numb	of the 100-tables in the envelope.	sieve of Eratosthenes. You will need one	numbers less than 100. It is called the	found an easy way to calculate all the prime	Fratacthenes a Greek mathematician	numbers.	any further. They are like the "atoms" of	in mathematics, since they can't be divided	Prime numbers play a very important role	however that 1 itself is not a prime number!	1 and itself is called a prime number. Note	A number which has no factors apart from	factor of 21 since, $21 = 7 \times 3$.	y with another number For example, 7 is a	number x if you can make x by multiplying	We say that a number y is a factor of a		PROBLEM F: PRIME NUMB
ers are there less than 100?	are prime numbers.	Then all remaining circled numbers	may be crossed out several times:).	circled or crossed out (some of them	continue until all numbers are either	the remaining multiples of 5. We	ber we circle is 5 and we cross out	since 4 is crossed out, the next num-	these numbers can't be prime.	cross out all multiples of 3; again	isn't crossed out, in this case <mark>3,</mark> and	Now we circle the next number which	bers, since they are divisible by 2.	these numbers can't be prime num-	all multiples of 2 less than 100 –	prime number, <mark>2.</mark> Then we cross out	We start by circling the smallest	ERS



The Integer Files	
Archive of the University of Cantortown	Item 7
Item 7: Old notebook, box of marbles	Catalogue Nr. 4652



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CA ?	Archive of the
Contraction of the	Item 8: Old pi

The Integer Files	
Archive of the University of Cantortown	Item 8
tem 8: Old piece of paper 2, Icosahedron	Catalogue Nr. 5512

PROBLEM H: PLATONIC SOLIDS

This shape is called an Icosahedron. All faces are equilateral triangles, and it looks the same from every direction. Therefore it is called a Platonic Solid, named after the Greek mathematician Plato. Plato showed that there are only five solids of this kind. He though that they corresponded to the four classical elements fire, air, earth and fire, as well as the universe. Here is a table showing all 5 platonic solids. Can you find a pattern and fill in the gaps?

Fame	H.odel	Faces	Vertices	Edges	6
Tetrahedron		4		6	1
Cube		6	8	12	
Octahedron		8	6		
Dodecahedron		0	20	30	
Icosahedron		20	0	30	
MAYBE THI	NK ABOU	T FACE	S + VE	KTCES!	1



The Integer Files	
Archive of the University of Cantortown	Item 9
Item 9: Two letters by Prof. Integer, Tangram	Catalogue Nr. 1972

PROBLEM I: TANGRAM

Today when browsing a shop in Chinatown, I discovered a fantastic game, called Tangram: it consists of geometric shapes which can be combined to make new ones.

You are given a certain shape, like a square, and you have to use all of the tiles available to make that shape.

Unfortunately I mixed up two games and couldn't figure out which tile didn't belong there. 8 of the tiles on the back can be used to make a square: find the one that is left over.



The Integer Files

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Item 10: Spiral Bound Notebook No 2

	Ite	m	10
Catalogue	Nr.	96	12





























Pascal's Triangle

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0

Pascal's Triangle Print several times for each group, cut out and add to problem E

	2			(
1/2/	2	3	1/1/21	5	1/1	7	19831	9	1/2001
11	1/1/24	13	1/1/2/	15	Man 1	17	1/1/23/	19	1/2/0)
21	142A	23	12/AI	25	1915A	27	1/2/81	29	13/2)
31	1/1/24	33	"MA	35	3/51	37	12/3/	39	1/10
41	1424	43	"HA	45	4/5/	47	4481	49	130
51	1/1/2/4	53	"SA	55	5/201	57	1/1/8/	59	160
61	1/1/24	63	"BEAT	65	6%	67	18	69	1/10
71	1/1/24	73	"MA	75	1/201	77	1/251	79	1840
81	1/8/24	83	18 A	85	81/21	87	12/8/	89	1/3/2)
91	1/102	93	1/st A	95	19/6	97	198	99	tiog

100 Number Table Print several times for each group, cut out and add to problem F

	2			1					
					$\overline{}$				
1/1	2	3	"Man	5	11/1	7	1/10/	9	1/1/201
11	1/104	13	1/1/	15	Man 1	17	1/1/8/	19	1/2/201
21	1/1/24	23	"MAI	25	1/2/21	27	1/1/281	29	1/2/201
31	19/24	33	13/A	35	3/21	37	13/81	39	140
41	14/24	43	"HA	45	4451	47	4481	49	1/201
51	19924	53	15 A	55	5/5/	57	1/3/8/	59	18401
61	10024	63	184A	65	(they	67	10181	69	1/101
71	1/1/24	73	MA.	75	1/5/	77	1/181	79	18/201
81	19924	83	184A	85	81/21	87	18 By	89	1/2/2/
91	1/22	93	191A	95	19/61	97	198	99	100



Tangram Print once (on coloured cardboard), cut out and add to problem I

PROBLEM D: MAGIC SQUARES

Do you know what a magic square is? A quadratic grid of integers, so that the sum of the numbers in every row, every column and the two diagonals is always the same. Here is a 3×3 magic square with the numbers from 1 to 9. The rows, columns and diagonals all add up to 15:

2	2	7	6	
	9	5	1	
1	4	3	8	

Magic squares have also played an important role in Chinese and Arabic mathematics: they were believed to have magical powers and a supernatural meaning.

I found this 4×4 magic square in a book, except that some numbers are missing. Can you fill in the gaps and find the number in the bottom left corner?



Note: Maybe you should first determine what the sum of the numbers in every row and column is.

KS4
Big Caesar Code 18
Combinatorics: Lotto 8
Graph Theory: Bridges 2
Magic Square 9
Sequences Hard 20
Sieve of Eratosthenes 25
Probability 18
Symmetry Groups: $13 - 1 = 12$
Geometry 1
Modular Arithmetic 5