

## 2.05 Difference of Squares/ Perfect Square Trinomials

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**REVIEW EXERCISES.** Use the **F OI L** method to multiply each of the following:

1.  $(x - 2)(x + 2)$

2.  $(x - 3)(x + 3)$

3.  $(x - 1)(x + 1)$

4.  $(x - 6)(x + 6)$

5.  $(2x - 3)(2x + 3)$

6.  $(3x - 5)(3x + 5)$

7.  $(x + 2)^2$

8.  $(x + 5)^2$

9.  $(x - 5)^2$

$= (x + 2)(x + 2)$

$=$

$=$

$= \underline{\quad} + \underline{\quad} + \underline{\quad}$

$=$

$=$

10.  $(x - 7)^2$

11.  $(2x + 3)^2$

12.  $(3x - 5)^2$

As in the previous section, in each of these exercises, you were given a **product** of two **binomials**. Now, as before, the problem will be to reverse the process, and factor the **difference of two squares** or factor a **perfect square trinomial**.

**EXERCISES.** In each of the following, factor the difference of squares:

1.  $x^2 - 9$

$(x - \underline{\hspace{1cm}})(x + \underline{\hspace{1cm}})$

2.  $x^2 - 16$

$(x - \underline{\hspace{1cm}})(x + \underline{\hspace{1cm}})$

3.  $x^2 - 49$

$(x - \underline{\hspace{1cm}})(x + \underline{\hspace{1cm}})$

4.  $x^2 - 64$

$(x - \underline{\hspace{1cm}})(x + \underline{\hspace{1cm}})$

5.  $x^2 - 100$

6.  $x^2 - 81$

7.  $x^2 - 25$

8.  $x^2 - 121$

9.  $x^2 - 144$

10.  $x^2 - 169$

11.  $x^2 - a^2$

12.  $x^2 - b^2$

13.  $4x^2 - 9$

$(2x - \underline{\hspace{1cm}})(2x + \underline{\hspace{1cm}})$

14.  $9x^2 - 16$

$(3x - \underline{\hspace{1cm}})(3x + \underline{\hspace{1cm}})$

15.  $16x^2 - 49$

$(\underline{\hspace{1cm}} - \underline{\hspace{1cm}})(\underline{\hspace{1cm}} + \underline{\hspace{1cm}})$

16.  $25x^2 - 64$

17.  $9x^2 - 100$

18.  $49x^2 - 81$

$19. \quad 9x^2 - 25y^2$

$20. \quad 49x^2 - 121y^2$

$21. \quad 25x^2 - 144a^2$

$22. \quad 16x^2 - 81b^2$

$23. \quad 9y^2 - 169x^2$

$24. \quad 36y^2 - 49x^2$

Don't forget that the first step in any factoring problem is to **factor the common factor first**. This means that each of the following exercises requires two steps. Again, this is the "**factoring two-step**."

$25. \quad 9x^2 - 9$

$26. \quad 3x^2 - 12$

$27. \quad 5x^2 - 45$

$9(\quad)$

$3(\quad)$

$\underline{\quad}(\quad)$

$9(\quad)(\quad)$

$3(\quad)(\quad)$

$\underline{\quad}(\quad)(\quad)$

$28. \quad 4x^2 - 64$

$29. \quad 4x^2 - 100$

$30. \quad 8x^2 - 72$

$31. \quad 25x^2 - 25$

$32. \quad 7x^2 - 700$

$33. \quad x^3 - 16x$

$$34. \quad 3x^3 - 75x$$

$$35. \quad 5x^3 - 80x$$

$$36. \quad 2x^3 - 50x$$

$$37. \quad 16x^4 - 16x^2y^2$$

$$38. \quad 9y^4 - 9x^2y^2$$

$$39. \quad 81y^4 - 9x^2y^2$$

$$40. \quad 64x^4 - 4x^2y^2$$

$$41. \quad 12y^4 - 12x^2y^2$$

$$42. \quad 79y^4 - 79x^2y^2$$

**Factor each of the following perfect square trinomials:**

$$43. \quad x^2 + 4x + 4$$

$$44. \quad x^2 + 6x + 9$$

$$45. \quad x^2 + 2x + 1$$

$$= ( \quad )( \quad )$$

$$= ( \quad )^2$$

$$46. \quad x^2 + 12x + 36$$

$$47. \quad x^2 + 14x + 49$$

$$48. \quad x^2 + 20x + 100$$

49.  $x^2 - 8x + 16$

50.  $x^2 - 4x + 4$

51.  $x^2 - 10x + 25$

52.  $x^2 - 12x + 36$

53.  $x^2 - 18x + 81$

54.  $x^2 - 24x + 144$

**Remember to factor the common factor first:**

55.  $5x^2 - 20x + 20$

56.  $2x^2 - 20x + 50$

57.  $3x^2 + 6x + 3$

$\underline{\quad}(\quad)$

$\underline{\quad}(\quad)(\quad)$

$\underline{\quad}(\quad)^2$

58.  $3x^2 - 60x + 300$

59.  $6x^2 - 36x + 54$

60.  $4x^2 + 32x + 64$

61.  $x^3 + 4x^2 + 4x$

62.  $x^3 - 12x^2 + 36x$

63.  $9x^3 - 18x^2 + 9x$

$$64. \quad 6x^4 - 36x^3 + 54x^2$$

$$65. \quad 12y^4 - 48y^3 + 48y^2$$

$$66. \quad 2y^4 - 28y^3 + 98y^2$$

In the next exercises, it turns out that sum of squares, such as  $x^2+9$  or  $x^2+4$ , does NOT factor by this method. Do you think you can factor  $x^2+9$ ? (You can try if you like, but no matter what you try, it WON'T work! The answer is NO!)

$$67. \quad x^4 - 16$$

$$68. \quad x^4 - 1$$

$$= (x^2 - \underline{\hspace{2cm}})(x^2 + \underline{\hspace{2cm}})$$

$$= (x - \underline{\hspace{2cm}})(x + \underline{\hspace{2cm}})(x^2 + \underline{\hspace{2cm}})$$

$$69. \quad x^4 - 81$$

$$70. \quad x^4 - y^4$$

$$71. \quad 81x^4 - 16y^4$$

$$72. \quad 16x^4 - 81$$

$$= (4x^2 - \underline{\hspace{2cm}})(4x^2 + \underline{\hspace{2cm}})$$

$$= (2x - \underline{\hspace{2cm}})(2x + \underline{\hspace{2cm}})(4x^2 + \underline{\hspace{2cm}})$$

$$73. \quad x^4 + 10x^2 + 9$$

$$74. \quad x^4 + 13x^2 + 36$$

$$75. \quad x^4 - 13x^2 + 36$$

$$76. \quad x^4 - 5x^2 + 4$$

$$77. \quad x^4 - 29x^2 + 100$$

$$78. \quad y^4 + 5y^2 - 36$$

$$79. \quad y^4 - 8y^2 + 16$$

$$80. \quad y^4 - 18y^2 + 81$$

## ANSWERS 2.05

**p.157:** 1.  $x^2 - 4$ ; 2.  $x^2 - 9$ ; 3.  $x^2 - 1$ ; 4.  $x^2 - 36$ ; 5.  $4x^2 - 9$ ; 6.  $9x^2 - 25$ ; 7.  $x^2 + 4x + 4$ ; 8.  $x^2 + 10x + 25$ ; 9.  $x^2 - 10x + 25$ ; 10.  $x^2 - 14x + 49$ ; 11.  $4x^2 + 12x + 9$ ; 12.  $9x^2 - 30x + 25$ .

**p. 158-163:** (NOTE: Factors may be given in any order!)

1.  $(x-3)(x+3)$ ; 2.  $(x-4)(x+4)$ ; 3.  $(x-7)(x+7)$ ; 4.  $(x-8)(x+8)$ ; 5.  $(x-10)(x+10)$ ;
6.  $(x-9)(x+9)$ ; 7.  $(x-5)(x+5)$ ; 8.  $(x-11)(x+11)$ ; 9.  $(x-12)(x+12)$ ; 10.  $(x-13)(x+13)$ ;
11.  $(x-a)(x+a)$ ; 12.  $(x-b)(x+b)$ ; 13.  $(2x-3)(2x+3)$ ; 14.  $(3x-4)(3x+4)$ ; 15.  $(4x-7)(4x+7)$ ;
16.  $(5x-8)(5x+8)$ ; 17.  $(3x-10)(3x+10)$ ; 18.  $(7x-9)(7x+9)$ ; 19.  $(3x-5y)(3x+5y)$ ;
20.  $(7x-11y)(7x+11y)$ ; 21.  $(5x-12a)(5x+12a)$ ; 22.  $(4x-9b)(4x+9b)$ ; 23.  $(3y-13x)(3y+13x)$ ;
24.  $(6y-7x)(6y+7x)$ ; 25.  $9(x-1)(x+1)$ ; 26.  $3(x-2)(x+2)$ ; 27.  $5(x-3)(x+3)$ ;
28.  $4(x-4)(x+4)$ ; 29.  $4(x-5)(x+5)$ ; 30.  $8(x-3)(x+3)$ ; 31.  $25(x-1)(x+1)$ ; 32.  $7(x-10)(x+10)$ ;
33.  $x(x-4)(x+4)$ ; 34.  $3x(x-5)(x+5)$ ; 35.  $5x(x-4)(x+4)$ ; 36.  $2x(x-5)(x+5)$ ;
37.  $16x^2(x-y)(x+y)$ ; 38.  $9y^2(y-x)(y+x)$ ; 39.  $9y^2(3y-x)(3y+x)$ ; 40.  $4x^2(4x-y)(4x+y)$ ;
41.  $12y^2(y-x)(y+x)$ ; 42.  $79y^2(y-x)(y+x)$ ; 43.  $(x+2)^2$ ; 44.  $(x+3)^2$ ; 45.  $(x+1)^2$ ; 46.  $(x+6)^2$ ;
47.  $(x+7)^2$ ; 48.  $(x+10)^2$ ; 49.  $(x-4)^2$ ; 50.  $(x-2)^2$ ; 51.  $(x-5)^2$ ; 52.  $(x-6)^2$ ; 53.  $(x-9)^2$ ; 54.  $(x-12)^2$ ;
55.  $5(x-2)^2$ ; 56.  $2(x-5)^2$ ; 57.  $3(x+1)^2$ ; 58.  $3(x-10)^2$ ; 59.  $6(x-3)^2$ ; 60.  $4(x+4)^2$ ; 61.  $x(x+2)^2$ ;
62.  $x(x-6)^2$ ; 63.  $9x(x-1)^2$ ; 64.  $6x^2(x-3)^2$ ; 65.  $12y^2(y-2)^2$ ; 66.  $2y^2(y-7)^2$ ; 67.  $(x-2)(x+2)(x^2+4)$ ;
68.  $(x-1)(x+1)(x^2+1)$ ; 69.  $(x-3)(x+3)(x^2+9)$ ; 70.  $(x-y)(x+y)(x^2+y^2)$ ;
71.  $(3x-2y)(3x+2y)(9x^2+4y^2)$ ; 72.  $(2x-3)(2x+3)(4x^2+9)$ ; 73.  $(x^2+9)(x^2+1)$ ; 74.  $(x^2+9)(x^2+4)$ ;
75.  $(x-3)(x+3)(x-2)(x+2)$ ; 76.  $(x-2)(x+2)(x-1)(x+1)$ ; 77.  $(x-5)(x+5)(x-2)(x+2)$ ;
78.  $(y^2+9)(y-2)(y+2)$ ; 79.  $(y-2)^2(y+2)^2$ ; 80.  $(y-3)^2(y+3)^2$ .