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AIR-WATER TIME AND LENGTH SCALES IN SKIMMING FLOWS ON A STEPPED SPILLWAY. APPLICATION TO THE SPRAY CHARACTERISATION

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AIR-WATER TIME AND LENGTH SCALES IN SKIMMING FLOWS ON A <u>STEPPED SPILLWAY.</u> APPLICATION TO THE SPRAY CHARACTERISATION

by

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Skimming flow on Croton Falls stepped spillway in March 2001 (Courtesy of Mrs Jenny HACKER)

ABSTRACT

Modern stepped spillways are typically designed for large discharge capacities corresponding to a skimming flow regime. Skimming flows are characterised by large amounts of entrained air and very-strong interactions between main stream turbulence, step cavity recirculation and free-surface. The present study is focused on new measurements of air-water turbulent time and length scales in air-water flow using several phase-detection intrusive probes. A new signal processing method and some correlation analyses were developed and applied.

The air water flow properties presented basic characteristics that were qualitatively and quantitatively comparable to previous studies in skimming flows. Some self-similarity was observed systematically at both macroscopic and microscopic levels. This included the distributions of void fraction, bubble count rate, interfacial velocity and turbulence level at a macroscopic scale, and the bubble/droplet chord distributions, and the auto- and cross-correlation functions at a microscopic level. Self-similarity is closely linked with dynamic similarity, and present results demonstrated a number of self-similar relationships that remain invariant under changes of scale which led in turn to remarkable application at prototype scales. The present findings are significant because they provide a picture general enough to be used as a first approximation to characterise the air-water flow field in similar stepped spillway structures.

The correlation analyses yielded a characterisation of the large eddies advecting the bubbles. The basic results included the transverse and streamwise integral turbulent length scales, the transverse and streamwise integral turbulent length scales, the transverse and streamwise integral turbulent time scales, and the advection length scale. The turbulent length scales characterised a measure of the size of large vortical structures advecting air bubbles in the skimming flows. Both streamwise and transverse air-water length scales were closely related to the characteristic air-water depth Y₉₀ : i.e., $L_{xy}/Y_{90} = 0.05$ to 0.2. The result was irrespective of the Reynolds numbers within the range of the experiments. Detailed measurements in the spray region highlighted the existence of an upper spray region for C > 0.95 to 0.97. In this upper spray, the distributions of droplet chord sizes and the distributions of advection length scales presented some marked difference with the rest of the flow. It is suggested that this highlighted a change in spray structure, where the upper spray region consisted primarily of ejected droplets interacting little with the rest of the flow until they re-attached.

Keywords : Air-water turbulent shear flow, Stepped spillways, Integral turbulence time scales, Integral turbulence length scales, Turbulent length and time scales, Spray, Physical modelling, Signal processing, Correlation analyses, Self-similarity, Phase-detection intrusive probes, Air bubble entrainment, Skimming flows, Bubble and droplet chord distributions.

SCALA DELLE LUNGHEZZE E DEI TEMPI ARIA-ACQUA NELLE CORRENTI AREATE SU UNO SFIORATORE A GRADINI. UN'APPLICAZIONE PER LA CARATTERIZZAZIONE DELLO SPRAY

Sommario

I moderni sfioratori a gradini sono tipicamente progettati per elevate portate corrispondenti ad un regime di corrente areata (skimming flow). In condizioni di skimming flow la corrente è caratterizzata da una grande quantità di aria e forti interazioni tra la turbolenza della corrente principale, le zone di ricircolo nella cavità del gradino e la superficie libera. I meccanismi di dissipazione di energia comprendono il ricircolo nelle cavità, lo scambio di quantità di moto e le interazioni tra la superficie libera e la turbolenza della corrente principale. Questo studio focalizza l'attenzione su nuove misurazioni delle scale delle lunghezze e dei tempi turbolenti nella corrente aria-acqua usando diverse sonde intrusive in grado di rilevare le due fasi. È stato inoltre sviluppato un nuovo metodo di elaborazione del segnale ed i dati sono stati analizzati attraverso il metodo della correlazione.

Le proprietà del fluido acqua-aria sia qualitativamente che quantitativamente hanno mostrato caratteristiche di base simili ai precedenti studi sulle correnti areate. Alcune auto-similitudini (self-similarity) sono state osservate sistematicamente a livello sia macroscopico che microscopico. A livello macroscopico si includono la distribuzione della frazione di vuoto, della frequenza di conteggio delle bolle, della velocità interfacciale e del livello di turbolenza; a livello microscopico la distribuzione della dimensione delle bolle/gocce, di autocorrelazione e correlazione. Le auto-similitudini sono strettamente legate alle analogie dinamiche ed i risultati hanno dimostrato che alcune rimangono invariate anche sotto i cambiamenti di scala. Questo può portare ad alcune interessanti osservazioni per le applicazioni alle scale dei prototipi. I risultati ottenuti sono inoltre significativi perché forniscono una rappresentazione sufficientemente generale per essere usata in prima approssimazione per caratterizzare la corrente aria-acqua nel campo delle strutture di sfioratori a gradini. Le analisi dei dati effettuati attraverso il metodo della correlazione, hanno fornito una caratterizzazione dei grandi vortici che trasportano per avvezione le bolle. I risultati di base comprendono le scale delle lunghezze integrali in direzione longitudinale e trasversale, le scale dei tempi integrali in direzione longitudinale e trasversale e la scala delle lunghezze di Taylor. La scala delle lunghezze turbolente è una misura della dimensione delle grandi strutture vorticose che trasportano per avvezione le bolle nella corrente areata. La scala delle lunghezze in direzione trasversale e longitudinale è strettamente legata alla profondità caratteristica dell'acqua-aria, Y₉₀: per esempio $L_{xy}/Y_{90} = 0.1$ a 0.2. Il risultato non è funzione del numero di Reynolds nella gamma degli esperimenti eseguiti. Le misurazioni dettagliate effettuate nella regione dello spray, hanno messo in luce l'esistenza di una regione superiore per valori dell'indice dei vuoti maggiori di 0.95-0.97. Nella regione superiore dello spray, le distribuzioni delle dimensioni delle gocce e delle scale integrali di Taylor hanno mostrato alcune differenze rispetto al resto della corrente. Questo fa ritenere che vi sia un cambiamento nella struttura dello spray, dove la zona superiore consiste fondamentalmente in gocce che poco interagiscono con la corrente dalla quale fuoriescono, fino a che non vi rientrano.

Parole chiave: ingresso di bolle d'aria, corrente areata, sfioratori a gradini, scala integrale dei tempi, scala integrale delle lunghezze, scala dei tempi e delle lunghezze turbolente, spray, modelli fisici, elaborazione del segnale, correlazioni, corrente aria-acqua tangenziale turbolenta, auto-similitudini, sonde intrusive rivelatrici di fase, distribuzione della dimensione delle bolle e delle gocce.

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NOTATION

A_W	water flow cross-section area (m ²);
a	constant;
b	constant;
С	void fraction defined as the volume of air per unit volume of air and water; it is also called air
	concentration or local air content;
С	instantaneous void fraction; $C = 0$ or 1;
C _{mean}	depth-average void fraction defined in terms of Y_{90} : $C_{mean} = 1 - d/Y_{90}$;
ch	chord size (m);
D_{H}	hydraulic diameter (m) also called equivalent pipe diameter;
D _t	turbulent diffusivity (m^2/s) of air bubbles in air-water flow;
D ₀	dimensionless constant
D'	dimensionless air bubble diffusivity;
d	equivalent clear water flow depth defined as: $d = \int_{C=0}^{C=0.90} (1 - C) * dy$;
d _{ab}	air bubble size (m);
d _c	critical flow depth (m);
F	air bubble count rate (Hz) or bubble frequency defined as the number of detected air bubbles per
	unit time;
F _{max}	maximum bubble count rate (Hz) at a given cross-section;
Fr	Froude number;
F _{scan}	scanning frequency (Hz) or scan rate;
F*	Froude number defined in terms of the step height :
	$F_* = \frac{q_W}{}$
	$\sqrt{g * \sin\theta * (h * \cos\theta)^3}$
f	Darcy-Weisbach friction factor;
$\mathbf{f}_{\mathbf{d}}$	equivalent Darcy-Weisbach friction factor of form drag process;
f _e	equivalent Darcy-Weisbach friction factor in air-water skimming flows;
g	gravity constant: $g = 9.80 \text{ m/s}^2$ in Brisbane, Australia;
Н	total head (m);
H _{max}	maximum upstream head (m) above chute toe;
H _{res}	residual head (m);
H_1	upstream head (m) above weir crest;
h	vertical step height (m);
Κ	inverse of the dimensionless expansion rate of a developing shear layer;
K'	dimensionless integration constant;
K^*	dimensionless constant;
k _s	step cavity roughness height (m) : $k_s = h^* \cos\theta$;

The following symbols are used in this report :

k _s '	step surface equivalent sand roughness height (m);
L	length (m);
L	turbulent length scale (m);
LI	longitudinal distance (m) measured from the weir crest where the inception of free-surface aeration takes place;
L _r	geometric scaling ratio defined as the prototype to model dimensions: e.g., $L_r = 2$ when the model is half the prototype size;
L _{XX}	air-water advection integral length scale (m) : $L_{XX} = V * T_{XX}$
L _{xy}	transverse/streamwise air-water integral turbulent length scale (m) : $L_{xy} = \int_{Y=0}^{Y_{max}} (R_{xy})_{max} * dY$
$(L_{xx})_{max}$	maximum advection air-water length scale (m) in a cross-section;
(L _{xy}) _{max}	maximum transverse/streamwise air-water integral turbulent length scale (m) in a cross-section;
1	horizontal step length (m);
Mo	Morton number defined as : Mo = $g^* \mu_W^4 / (\rho_W^* \sigma^3)$;
N	power law exponent;
N _{ab}	number of air bubbles per record;
P _W	wetter perimeter (m);
Q _w	water discharge (m ³ /s);
q_{W}	water discharge per unit width (m^2/s) ;
Re	Reynolds number defined in terms of the hydraulic diameter;
R _{XX}	normalised auto-correlation function (reference probe);
R _{xy}	normalised cross-correlation function between two probe output signals;
(R _{xy)max}	maximum cross-correlation between two probe output signals;
Т	time lag (s) for which $R_{xy} = (R_{xy})_{max}$;
т	turbulent time scale (m);
т	integral turbulent time scale (s) characterising the large eddies advecting the air bubbles;
Tu	turbulence intensity defined as: $Tu = u'/V$;
T _{scan}	scan duration (Hz) or sampling period;
T _{XX}	auto-correlation time scale (s) : $T_{XX} = \int_{\tau=0}^{\tau=\tau(R_{XX}=0)} R_{XX}(\tau) * d\tau$
T _{xy}	cross-correlation time scale (s) : $T_{XY} = \int_{\tau=\tau(R_{XY}=(R_{XY})=(R_{XY})} R_{XY}(\tau) * d\tau$
T _{0.5}	characteristic time lag τ for which $R_{XX} = 0.5$;
T _{max}	maximum integral time scale (s) in a cross-section;

t	time (s);
t _{ch}	chord time (s);
U_W	flow velocity (m/s) : $U_W = q_W/d$;
u'	root mean square of longitudinal component of turbulent velocity (m/s);
V	interfacial velocity (m/s);
V _c	critical flow velocity (m/s);
W	channel width (m);
X	distance along the channel bottom (m);
Y	separation distance (m) between two phase-detection probe sensors;
Y90	characteristic depth (m) where the void fraction is 90%;
у	distance (m) measured normal to the invert (or channel bed);
y'	dimensionless distance (m) normal to the invert (or channel bed) : $y' = y/Y_{90}$;
Z	transverse distance (m) from the channel centreline;
Δx	streamwise separation distance (m) between sensor;
Δz	transverse separation distance (m) between sensor;
μ	dynamic viscosity (Pa.s);
μ_{W}	water dynamic viscosity (Pa.s);
θ	angle between the pseudo-bottom formed by the step edges and the horizontal;
ρ	density (kg/m ³);
ρ_{W}	water density (kg/m ³);
σ	surface tension between air and water (N/m);
τ	time lag (s);
τ0.5	characteristic time lag τ for which $R_{xy} = 0.5 * (R_{xy})_{max}$;
Ø	- diameter (m);
	- probe sensor size (m);

Subscript

air	air flow;
c	critical flow conditions;
W	water flow;
XX	auto-correlation of reference probe signal;
xy	cross-correlation;
90	flow conditions where $C = 0.90$;

Abbreviations

F/D	fully-developed inflow conditions;
P/D	partially-developed inflow conditions;
Std	standard deviation.

1. INTRODUCTION

1.1 Presentation

Stepped spillways have been used for many centuries (Fig. 1-1). The stepped design increases the rate of energy dissipation on the chute and reduces the size of the downstream energy dissipation system. For the last ten years, the research in the hydraulics of stepped spillways has been active (CHANSON 1995a, 2001a). On a stepped spillway, the waters flow as a succession of free-falling nappes (nappe flow regime) at small discharges (CHAMANI and RAJARATNAM 1994, CHANSON 1994a, TOOMBES 2002, EL-KAMASH et al. 2005). For a range of intermediate flow rates, a transition flow regime is observed (CHANSON 2001b, CHANSON and TOOMBES 2004). Modern stepped spillways are typically designed for large discharge capacities corresponding to a skimming flow regime (RAJARATNAM 1990, CHANSON 1994b, CHAMANI and RAJARATNAM 1999). In a skimming flow, the flow is non-aerated at the upstream end of the chute. Free-surface aeration occurs when the turbulent shear next to the free-surface becomes larger than the bubble resistance offered by surface tension and buoyancy. Downstream of the inception point of free-surface aeration, some strong air-water mixing takes place (Fig. 1-1A). Large amounts of air are entrained, and very-strong interactions between main stream turbulence, step cavity recirculation zones and free-surface are observed (e.g. CHANSON and TOOMBES 2003, GONZALEZ 2005, GONZALEZ et al. 2005).

The flow resistance is primarily a form drag in skimming flows. At each step, the cavity flow is driven by the developing shear layer and the transfer of momentum across it (Fig. 1-2) (GONZALEZ and CHANSON 2004). The energy dissipation mechanisms include cavity recirculation, momentum exchange with the free stream, and interactions between free-surface and mainstream turbulence. The interactions between mixing layer and horizontal step face, and the skin friction at the step faces may contribute to further energy dissipation, in particular on moderate slopes. At each step edge, highly coherent small-scale vortices are formed abruptly at the step corner because of the large gradient of vorticity at the corner (Fig. 1-2). The initial region of the mixing layer is dominated by a train of sequential small-scale vortices which eventually pair to form large scale vortical structures that are advected downstream. It is argued that the distance from the step edge to the impingement of the shear layer onto the step face is an important length because some feedback might occur nearly instantaneously from the impingement to the singularity region of the shear layer in the vicinity of the step edge (e.g. LIN and ROCKWELL 2001). Experimental studies of turbulent flows past two-dimensional cavities showed that cavity resonance is primarily a function of the ratio of boundary layer thickness to cavity length. That is, Y_{90} *sin θ /h for a stepped chute where Y_{90} is the characteristic air-water depth where the void fraction is 90%, h is the vertical step height, θ is the slope between the pseudo-bottom formed by the step edges and the horizontal. OHTSU et al. (2004) showed that the flow resistance appeared to be maximum for a slope θ of around 18° to 22°. GONZALEZ and CHANSON (2006) hypothesised that some maximum in flow resistance must be related to some flow instability. The three dimensional nature of recirculating vortices is believed to play a role to further the rate of energy dissipation (ANDRE et al. 2004, CHANSON and GONZALEZ 2004). GONZALEZ (2005) demonstrated quantitatively the means to enhance the flow resistance with turbulence manipulation.

Fig. 1-1 - Photographs of stepped spillways

(A) Skimming flow on Camp Dyer diversion dam spillway (Courtesy of John LABOON and US Bureau of Reclamation) - The clear-water flow at the upstream end and the inception point of free-surface aeration are clearly seen



(B) Croton Falls stepped spillway in operation in March 2001 (Courtesy of Mrs Jenny HACKER) -Completed in 1911, the spillway is equipped with 0.61 m high rounded steps (WEGMANN 1911, CHANSON 1995a)



Fig. 1-2 - Cavity recirculation in skimming flow



It is the purpose of this study to investigate thoroughly the air-water turbulent time and length scales in skimming flows, with a focus on the spray region and its specific features. New measurements were conducted in a large-size facility ($\theta = 22^\circ$, h = 0.1 m) with several phase-detection intrusive probes. An advanced signal processing method was developed and some new correlation analyses were conducted. Detailed air-water flow properties were recorded systematically for several flow rates. The results provide a new understanding of the turbulence structure, the spray properties and the energy dissipation mechanisms. In the next paragraphs (1.2 and 1.3), the turbulence and spray generation in skimming flows are reviewed. The Section 2 develops a basic dimensional analysis. Section 3 describes the experimental setup and instrumentation. The experimental results are presented in Sections 4, 5 and 6, and they are discussed in Section 7. The full experimental data sets are presented in Appendices D, E and F.

1.2 Skimming flow turbulence

In skimming flows, the turbulence levels are markedly higher than in monophase flows on a smooth invert (e.g. OHTSU and YASUDA 1997, CHANSON and TOOMBES 2002a, AMADOR et al. 2004a). OHTSU and YASUDA (1997) and AMADOR et al. (2004a,b) measured turbulence intensities upstream of the inception point of air entrainment. OHTSU and YASUDA observed turbulence levels of about 15-25%, while AMADOR et al. obtained turbulence intensities between 20 to 100%. Downstream of the inception point of air entrainment, experimental results showed further enhanced turbulence levels for 0.1 < C < 0.9 with turbulence intensities between 50 to 150% where C is the void fraction (e.g. CHANSON and TOOMBES 2002a, GONZALEZ 2005, GONZALEZ et al. 2005).

In a skimming flow, the high turbulence levels are generated by the form drag at each step. The resulting turbulent fluctuations acting next to the free surface contribute to a drastic air entrapment, advective dispersion and spray generation. At the "pseudo-free-surface", air is continuously entrained and released. Interfacial aeration involves both entrainment of air bubbles and formation of water droplets, and the exact location of the "pseudo-free-surface" becomes undetermined (Fig. 1-3). For 0.05 < C < 0.95, the air-water flow structure is dominated by collisions between particles (bubbles, droplets, packets) and by interactions between particles and turbulence. Such dynamic processes are associated with continuous bubble/droplet break-up, coalescence and interfacial deformations, all of which contribute to large fluctuations in air-water interfacial velocities and high levels of turbulence.

1.3 Air-water exchanges and spray generation

In the spray region, the drop formation results from some surface distortion, tip-streaming of ligaments and interactions between eddies and free-surface (e.g. HOYT and TAYLOR 1977, REIN 1998). The formation and ejection of a water droplet must be associated with a transfer of turbulent kinetic energy from the main flow. Figure 1-3 shows some high-speed photographs of spray droplets viewed from upstream. Once a droplet is ejected, the history/memory of its ejection process has a dominant effect because the droplet response time is nearly two orders of magnitude larger than the air flow response time. The energy of each droplet is a combination of its potential and kinetic energies, although NIELSEN (2004, *Pers. Comm.*) suggested that surface tension effects could increase the pressure work.

Today the study of spray and splashing remains limited in high-velocity water flows. Some researchers used visual techniques (¹), while others used intrusive phase detection probes (²). Some studies suggested that the spray region, defined as C > 0.7, may be sub-divided into several sub-zones (TOOMBES 2002, CHANSON and GONZALEZ 2004). Despite limited data sets, most studies (³) showed a wide range of droplet chord lengths at each sampling location. The chord length distributions were skewed with a preponderance of small chord sizes relative to the mean, with decreasing numbers of droplets and decreasing droplet sizes with increasing heights y and decreasing liquid fractions (1-C).

²For example, CHANSON (1999b), TOOMBES (2002), HONG et al. (2004).

¹Experimental techniques included photography (HOYT and TAYLOR 1976,1977), infra-red sensors (AUGIER 1996, KADEM 2005) and video-observations (WU and FAETH 1995, WU et al. 1995).

³These data sets included CHANSON (1999b), TOOMBES (2002), CHANSON and GONZALEZ (2004), GONZALEZ (2005), GONZALEZ et al. (2005) in supercritical open channel flows, HONG et al. (2004) in high-velocity water jets and CHANSON (2006a) in hydraulic jumps.

Fig. 1-3 - High-speed photographs of water droplet ejections and spray above a skimming flow on a stepped chute (h = 0.1 m, l = 0.25 m) - Looking downstream from the weir crest - Most droplets were about 0.20 to 0.3 m above the pseudo-bottom formed by the step edges

(A) $d_c/h = 1.33$, Re = 5.7 E+5, shutter speed: 1/320 s, probe located at step edge 7



(B) $d_c/h = 1.57$, Re = 7.1 E+5, shutter speed: 1/320 s, probe located at step edge 7



2. DIMENSIONAL ANALYSIS AND SIMILITUDE

2.1 Basic considerations

A key feature of skimming flow on a stepped chute is the strong free-surface aeration and air-water flow turbulence (Fig. 1-1 and 1-3). Physical modelling and experimental investigations may be performed if a suitable dynamic similarity is achievable (Table 2-1). With geometrically similar models, the geometric scaling ratio L_r is defined as the ratio of prototype to model dimensions.

In a dimensional analysis, the relevant parameters include the fluid properties and physical constants, the chute geometry and inflow conditions, the air-water flow properties and the geometry of the steps. Considering a skimming flow at uniform equilibrium down a stepped chute with flat horizontal steps and for a prismatic rectangular channel. At uniform equilibrium, the gravity force component in the flow direction counteracts exactly the flow resistance. A complete dimensional analysis yields a relationship between the local air-water flow properties, and the fluid properties, physical constants, flow conditions and step geometry :

$$C, \frac{V}{\sqrt{g*h}}, \frac{u'}{V}, \mathbf{T}*\sqrt{\frac{g}{h}}, \frac{\mathbf{L}}{h}, \frac{d_{ab}}{h}, \dots = F_1\left(\frac{x}{h}; \frac{y}{h}; \frac{q_W}{\sqrt{g*h^3}}; \rho_W*\frac{q_W}{\mu_W}; \frac{g*\mu_W^4}{\rho_W*\sigma^3}; \frac{W}{h}; \theta; \frac{k_S'}{h}; \dots\right) \quad (2-1)$$

where C is the local void fraction, V is the local velocity, g is the gravity acceleration, d is the equivalent water depth at uniform equilibrium, u' is a characteristic turbulent velocity, **T** is a turbulent time scale, **L** is a turbulent length scale, d_{ab} is a characteristic size of entrained bubble, x is the coordinate in the flow direction measured from the step edge, y is the distance normal from the pseudo-bottom formed by the step edges, q_W is the water discharge per unit width, ρ_W and μ_W are the water density and dynamic viscosity respectively, σ is the surface tension between air and water, W is the chute width, h is the step height, θ is the angle between the pseudo-bottom and the horizontal, and $k_{s'}$ is the skin roughness height (Fig. 1-2). In the left handside of Equation (2-1), the 3rd, 4th and 5th terms are dimensionless turbulence properties. In the right handside, the 3rd, 4th and 5th dimensionless terms are the Froude, Reynolds and Morton numbers respectively, and the last three terms characterise the step cavity shape and the skin friction effects on the cavity wall.

Note that any combination of dimensionless numbers may replace one of these dimensionless numbers. For example, one parameter among the Froude, Reynolds and Weber numbers may be replaced by the Morton number $Mo = (g^*\mu_W^4)/(\rho_W^*\sigma^3)$ as seen in Equation (2-1) where the Weber number was replaced by the

Morton number.

Lastly a characteristic water depth in air-water flows is the equivalent clear water depth which may be deduced from the void fraction distribution :

$$d = \int_{y=0}^{y=100} (1 - C) * dy$$
(2-2)

where Y_{90} is the depth where C = 0.9.

2.2 Discussion

In free-surface flows, laboratory studies are typically based upon an undistorted Froude similitude (e.g. HENDERSON 1966, CHANSON 2004a). The same applies to stepped spillway studies (e.g. BOES 2000b, CHANSON 2004b, CHANSON and GONZALEZ 2005, GONZALEZ et al. 2005). However cavity recirculation and momentum exchanges between the cavity and stream flows are dominated by viscous effects. At the same time, the entrapment/detrainment of air bubbles and the mechanisms of air bubble breakup and coalescence are dominated by surface tension effects. With some assumptions, Equation (2-1) shows that a dynamic similarity of skimming flow on stepped spillway is impossible to achieve using geometrically similar models unless working at full-scale. In small size models ($L_T >> 1$), the air entrainment process is adversely affected by significant scale effects (KOBUS 1984, WOOD 1991, CHANSON 1997a).

In the present study, the same fluids (air and water) were used in model and prototype, and the Morton number becomes an invariant. Similarly, the chute slope θ , the step height h, the channel width W and the step roughness k_s' were constant. For a Froude similitude, Equation (2-1) may be rewritten :

$$C, \frac{V}{\sqrt{g^* d_c}}, \frac{u'}{V}, \mathbf{T}^* \sqrt{\frac{g}{d_c}}, \frac{\mathbf{L}}{d_c}, \frac{d_{ab}}{d_c}, \dots = \mathsf{F}_2\left(\frac{x}{d_c}; \frac{y}{d_c}; \frac{d_c}{h}; \mathsf{Re}\right)$$
(2-3)

where d_c is the critical depth ($d_c = \sqrt[3]{q_W^2/g}$) and Re is the Reynolds number defined in terms of the equivalent pipe diameter D_H (Re = $\rho_W^* V^* D_H / \mu_W$). Equation (2-3) gives a dimensionless expression of the local air-water turbulent flow properties as functions of independent parameters that include both Froude and Reynolds numbers.

The validity of the Froude similitude itself was rarely tested in stepped chutes but in a few studies (see review by CHANSON and GONZALEZ 2005). Recently, detailed studies of local air-water flow properties yielded stringent conditions to minimise scale effects suggesting the impossibility to achieve true dynamic similarity even in large-size models (BOES 2000b, GONZALEZ and CHANSON 2004, CHANSON and GONZALEZ 2005, TAKAHASHI et al. 2005). In the present study, a Froude similitude was used as for most open channel flow studies. The experiments were conducted in a large size facility operating at large Reynolds numbers. These conditions may be representative of a full-scale storm waterway.

Reference	θ	Step geometry	Flow conditions	Instrumentation	Remarks
(1)	deg. (2)	(3)	(4)	(5)	(6)
CHANSON and TOOMBES (2001,2002c)	22	Smooth horizontal steps (h = 0.1 m, l = 0.25 m).			W = 1 m. $k_{s}' = 0.5 mm.$
Series 1			$q_{W} = 0.046 \text{ to } 0.182$ m ² /s, Re = 1.8 to 7.3 E+5.	Single-tip conductivity probe ($\emptyset = 0.35$ mm).	Experiments EV200.
Series 2			$q_{w} = 0.058 \text{ to } 0.182$ m ² /s, Re = 2.3 to 7.3 E+5.	Double-tip conductivity probe ($\emptyset = 0.025 \text{ mm}$).	Experiments TC200.
CHANSON and					
TOOMBES (2002a) Series 1	16	Smooth horizontal steps ($h = 0.1$			W = 1 m.
Series 2	22	m, $l = 0.25$ m). Smooth horizontal steps (h = 0.1 m, $l = 0.35$ m).			$k_{s}' = 0.5 \text{ mm.}$ W = 1 m. $k_{s}' = 0.5 \text{ mm.}$
CHANSON and		,,		Single-tip conductivity	$W = 0.5 \text{ m}, \text{ k}_{\text{s}}' = 0.5$
TOOMBES (2002b)				probe ($Ø = 0.35$ mm).	mm.
Series 1	3.4	Smooth horizontal steps (h = $0.143 \text{ m}, l = 2.4 \text{ m}$).			L = 24 m, 10 steps.
series 2	3.4	Smooth horizontal steps ($h = 0.0715 \text{ m}, l = 1.2 \text{ m}$).			L = 24 m, 180 steps.
TOOMBES (2002)		Smooth horizontal steps (h = $0.143 \text{ m} \text{ l} = 2.4 \text{ m}$)			k _s ' = 0.5 mm.
Stepped cascade	3.4	L = 24 m, 10 steps		Single-tip conductivity	W = 0.5 m.
Single-step	3.4	L = 3.2 m, 1 step		Double-tip conductivity probe ($\emptyset = 0.025$ mm).	W = 0.25 m.
YASUDA and CHANSON (2003)	16	Smooth horizontal steps ($h = 0.05 \text{ m}$).	$q_W = 0.0776 \text{ m}^2/\text{s}$ Re = 3.1 E+5	Double-tip conductivity probe ($\emptyset = 0.025$ mm)	W = 0.5 m. $k_{-}' = 0.5 \text{ mm.}$
OHTSU et al. (2004)	5.7, 8.5, 11.3,	h = 0.006 to 0.05 m	$q_{\rm W} = 0.02$ to 0.08 m ² /s, Re = 8 E+4 to 3.2 E+5.	Single-tip conductivity probe ($\emptyset = 0.1$ mm).	W = 0.4 m.
	19, 23, 30				
GONZALEZ (2005)	50			Double-tip conductivity probe ($\emptyset = 0.025$ mm).	W = 1 m. $k_{e}' = 0.5 mm.$
-	16	Smooth horizontal steps (h = $0.05 \text{ m}, l = 0.175 \text{ m}$).	-		5
-	16	Smooth horizontal steps ($h = 0.1$	-		
-		m, l = 0.35 m).	-		- · ·
	22	Smooth horizontal steps ($h = 0.1$ m, $l = 0.25$ m).			Turbulence manipulation with triangular vanes.
GONZALEZ et al. (2005)	22	Horizontal steps ($h = 0.1 \text{ m}, 1 = 0.25 \text{ m}$).	$q_W = 0.01$ to 0.219 m ² /s, Re = 4 E+4 to 9 E+5.	Double-tip conductivity probe ($\emptyset = 0.025$ mm).	Experiments $CMH 05, W = 1 m.$
Configuration A	22	Rough step faces: 8-mm thick screens on both vertical and horizontal step faces		1	$k = 8 \text{ mm} (k_{s}' \approx 6.6 \text{ mm}).$
Configuration B	22	8-mm thick screens on each	-		$k = 8 \text{ mm} (k_{s}' \approx 6.6$
Configuration C	22	8-mm thick screens on each	-		$\frac{\text{mm}}{\text{k} = 8 \text{ mm}} (\text{k}_{\text{S}}' \approx 6.6$
Configuration S (smooth steps)	22	Smooth horizontal steps	-		$k_{\rm s}' = 0.5 \text{ mm.}$

Table 2-1 - Experimental investigations of stepped chute flows on flat slopes ($\theta < 30^{\circ})$

Reference	θ	Step geometry	Flow conditions	Instrumentation	Remarks
	deg.				
(1)	(2)	(3)	(4)	(5)	(6)
MURILLO (2006)		Smooth horizontal steps (h =		Conical hot-film probe	$W = 0.4 \text{ m}, \text{ k}_{s}' = 0.5$
		0.15 m)		(Dantec 55R42)	mm.
Model I	16	h = 0.15 m, l = 0.525 m	$q_{\rm w} = 0.06$ to 0.13 m ² /s,		
			Re = 2.4 E+5 to 5.5 E+5.		
Model II	11.3	h = 0.15 m, l = 0.75	$q_{\rm w} = 0.06$ to 0.14 m ² /s,		
			Re = 2.4 E+5 to 5.8 E+5.		
Model III	5.7	h = 0.15 m, l = 1.5 m	$q_{\rm w} = 0.06$ to 0.15 m ² /s,		
			Re = 2.4 E+5 to 6.2 E+5.		
Present study	22	Smooth horizontal steps			Experiments GH_06.
•		(h = 0.1 m, 1 = 0.25 m).			W = 1 m.
					$k_{s}' = 0.5 \text{ mm.}$
Series 1	22		$q_{\rm w} = 0.095$ to 0.18 m ² /s,	Single-tip conductivity	3
			Re = 3.8 E+5 to 7.1 E+5	probes ($\emptyset = 0.35 \text{ mm}$)	
Series 2	22		$q_{w} = 0.12$ to 0.16 m ² /s,	Double-tip conductivity	
			Re = 4.6 E+5 to 6.4 E+5	probes ($\hat{Q} = 0.25 \text{ mm}$)	

Notes : k_{s}' : step surface roughness height; Re : flow Reynolds number defined in terms of hydraulic diameter.

3. EXPERIMENTAL CHANNEL AND INSTRUMENTATION

3.1 Experimental channel

Several series of new experiments were performed in the Gordon McKAY Hydraulics Laboratory at the University of Queensland (Table 3-1). The experimental channel was previously used by CHANSON and TOOMBES (2001,2002a,2003) and GONZALEZ (2005) with smooth step faces, and by GONZALEZ et al. (2005) (Table 1-1). Waters were supplied from a large feeding basin (1.5 m deep, surface area 6.8 m × 4.8 m) leading to a sidewall convergent with a 4.8:1 contraction ratio. The test section consisted of a broad-crested weir (1 m wide, 0.6 m long, with upstream rounded corner (0.057 m radius)) followed by ten identical steps (h = 0.1 m, 1 = 0.25 m) made of marine ply (Fig. 3-1). The stepped chute was 1 m wide with perspex sidewalls followed by a horizontal concrete-invert canal ending in a dissipation pit.

The pump, delivering the flow rate, was controlled with an adjustable frequency AC motor drive which enabled an accurate discharge adjustment in the closed-circuit system.

Ref.	q_W	d _c	Re	Instrumentation	Comments
	2	h			
	m^2/s				
(1)	(2)	(3)	(4)	(5)	(6)
Present study					W = 1 m, h = 0.1 m, l = 0.25 m.
	0.008 to	0.19 to	3.2 E+4 to	Visual observations	
	0.17	1.48	6.6 E+5		
	0.095	1.0	3.8 E+5	One single-tip probe	
	0.116	1.15	4.6 E+5	Two single-tip probes	$\Delta z = 3.6$ to 40.3 mm.
	0.143	1.33	5.7 E+5	One single-tip probe	
	0.161	1.45	6.4 E+5	Two single-tip probes	$\Delta z = 3.6$ to 55.7 mm.
	0.180	1.57	7.1 E+5	One single-tip probe	
	0.116	1.15	4.6 E+5	One dual-tip probe	$\Delta x = 7.0 \& 9.6 \text{ mm.}$
	0.143	1.33	5.7 E+5	One dual-tip probe	$\Delta x = 7.0 \text{ mm.}$
	0.161	1.45	6.4 E+5	One dual-tip probe	$\Delta x = 7.0 \& 9.6 \text{ mm.}$

Table 3-1 - Summary of experimental flow conditions (Present study)

Notes : d_c : critical flow depth; h : step height; l : step length; Re : Reynolds number defined in terms of the hydraulic diameter; W : channel width.

- Fig. 3-1 Photographs of the experimental channel
- (A) General view d_c/h 1.0, Re = 3.8 E+5



(B) Looking downstream at the trolley system supporting a double-tip conductivity probe - d_c/h 1.33, Re = 4.7 E+5



3.2 Instrumentation

Clear-water flow depths were measured with a point gauge. The discharge was measured from the upstream head above the crest with an accuracy of about 2% (⁴).

Air-water flow properties were measured with two types of probes : single-tip conductivity and double-tip conductivity probes (Table 3-2). Basic air-water flow measurements were performed with two single-tip conductivity probes (needle probe design) (Fig. 3-2). Each probe consisted of a sharpened rod (platinum wire $\emptyset = 0.35$ mm) coated with non-conductive epoxy set into a stainless steel surgical needle ($\emptyset = 1.42$ mm) acting as the second electrode as sketched in Figure 3-2. Additional measurements were performed with some double-tip conductivity probes (Fig. 3-3). Each sensor consisted of a sharpened rod (platinum wire $\emptyset = 0.25$ mm) which was insulated except for its tip and set into a metal supporting tube (stainless steel surgical needle $\emptyset = 0.5$ mm (internal) and 0.8 mm (external)). The stainless steel tube acted as the second electrode and it was separated from the inner wire by insulating epoxy. The longitudinal spacing between probe sensors was measured with a microscope and this yielded $\Delta x = 7.0$, 9.6, and 12.2 mm for each of the three double-tip probes, although most measurements were conducted with $\Delta x = 7.0$ and 9.6 mm.

All the probes were excited by an electronic system (Ref. UQ82.518) designed with a response time less than 10 μ s and calibrated with a square wave generator. A summary of the probe characteristics is presented in Table 3-2. Further details on probe design and electronic system were reported by CHANSON (1995b) and CUMMINGS (1996).

Reference :	CHANSON and	CHANSON and		Present study	
	TOOMBES (2002a),	TOOMBES (2002c)			
	TOOMBES (2002),				
	GONZALEZ (2005)				
Design :	Double-tip	Single-tip	Double-tip	Single-tip	Double-tip
Probe sensor					
Inner electrode diameter (Pt):	0.025 mm	0.35 mm	0.025 mm	0.35 mm	0.25 mm
Outer electrode inner diameter:					0.5 mm
Outer electrode outer diameter:	0.200 mm	1.42 mm	0.200 mm	1.42 mm	0.8 mm
Probe sensor spacing					
$\Delta x =$	7.5-10 mm	N/A	8 mm	N/A	7.0 mm
					9.6 mm
					12.2 mm
$\Delta z =$	0.5-1.5 mm	3.6 to 54.7	1.33 mm	3.6 to 54.7	1.4 mm
		mm		mm	

Table 3-2 - Comparative summary of conductivity probe characteristics

⁴The discharge measurements were based upon GONZALEZ' (2005) detailed velocity distribution measurements on the broad-crested weir. The discharge estimates were based upon the analysis of his results which yielded the resulting calibration curve :

$$\frac{Q_{W}}{W} = \left(1.013 - 0.37 * \frac{H_{1}}{W}\right) * \sqrt{g * \left(\frac{2}{3} * H_{1}\right)^{3}}$$

where H_1 is the upstream total head above the weir crest elevation and W is the channel width. The above relationship was derived for $0.05 \le H_1/W \le 0.22$

All measurements were conducted on the channel centreline (z = 0). For some experiments, the second, identical probe was placed beside the first one with the probe sensors at the same vertical and streamwise distances y and x respectively (Fig. 3-4A). The reference probe was located on the channel centreline (z = 0) while the second probe was separated in the transverse direction by a known separation Δz . Photographs of the probes are shown in Figure 3-4.



Fig. 3-2 - Sketch of two single-tip conductivity probes placed side-by-side

Fig. 3-3 - Sketch of the double-tip conductivity probe



3.3 Data processing

The measurement principle of conductivity probes is based upon the difference in electrical resistivity between air and water. The resistance of water is one thousand times lower than the resistance of air. When the probe tip is in contact with water, current will flow between the tip and the supporting metal; when it is in contact with air no current will flow. A sketch of the single-tip conductivity probe is presented in Figure 3-2. Figure 3-5 shows some typical signal outputs. Figure 3-5A presents the signals of two single-tip probes side-by-side separated by $\Delta z = 3.6$ mm, and Figure 3-5B shows the signal outputs of a dual-tip probe. The time-variation of the voltage output has a "square-wave" shape. Each steep drop of the signal corresponds to an air bubble pierced by the probe tip. Although the signal is theoretically rectangular, the probe response is not square because of the finite size of the tip, the wetting/drying time of the interface covering the tip and the response time of the probe and electronics.

In the present study, the air-water flow properties were calculated using a single threshold technique and the threshold was set at about 45 to 55% of the air-water voltage range. A sensitivity analysis was conducted

with thresholds between 40 and 60% of the voltage range (TOOMBES 2002, pp. 55-56). The results showed little effect of threshold on the air-water flow properties. HERRINGE and DAVIS (1974) obtained a similar result for threshold between 20% and 70% of the air-water voltage range.

The air concentration or void fraction C is the proportion of time that the probe tip is in the air. Past experience showed that the probe orientation with the flow direction had little effect on the void fraction accuracy provided that the probe support does not affect the flow past the tip (e.g. SENE 1984, CHANSON 1988). In the present study, the probe tip was aligned with the main flow direction as shown in Figures 3-2 and 3-3. This configuration allowed the best conditions for bubble piercing by the probe sensor and hence a better quality signal.

The bubble count rate F is the number of bubbles impacting the probe tip per second. The measurement is sensitive to the probe tip size, bubble sizes, velocity and discrimination technique, particularly when the sensor size is larger than the smallest bubbles.

Fig. 3-4 - Photographs of the conductivity probes

(A) Two single-tip conductivity probes ($\Delta z = 21.7 \text{ mm}$) in the lower spray region - d_C/h = 1.45, Re = 6.4 E+5, flow from left to right, shutter speed: 1/80 s



(B) Double-tip conductivity probe ($\Delta x = 12.2 \text{ mm}$) in the upper spray region, looking downstream - d_c/h = 1.15, Re = 6.6 E+5, shutter speed: 1/1,000 s



Figure 3-5 - Signal outputs of conductivity probes

(A) Signals of two single-tip conductivity probes side-by-side ($\Delta z = 3.6 \text{ mm}$) - d_c/h = 1.15, Re = 4.6 E+5, Step edge 10, y = 0.022 m, C = 0.114, F = 117 Hz, (R_{xy})_{max} = 0.41



(B) Dual-tip conductivity probe signals ($\Delta x = 7.0 \text{ mm}$) - d_c/h = 1.33, Re = 5.7 E+5, Step edge 10, y = 0.0365 m, C = 0.187, F = 167 Hz, V = 3.4 m/s, (R_{xy})_{max} = 0.602



3.4 Correlation analyses

When two probe sensors are simultaneously sampled, a correlation analysis may provide additional air-water flow properties.

In the present study, the air-water interfacial velocities were deduced from a correlation analysis between the two sensors of the double-tip probe. The cross-correlation technique is commonly used with large void fractions (C > 0.10) (CHANSON 1997, CROWE et al. 1998, CHANSON 2002). The time averaged velocity equals :

$$V = \frac{\Delta x}{T}$$
(3-1)

where T is the air-water interfacial travel time for which the cross-correlation function is maximum and Δx is the longitudinal distance between probe sensors (Fig. 3-3). Turbulence levels may be derived from the relative width of the cross-correlation function :

$$Tu = 0.851 * \frac{\sqrt{\tau_{0.5}^2 - T_{0.5}^2}}{T}$$
(3-2)

where $\tau_{0.5}$ is the time scale for which the cross-correlation function is half of its maximum value such as: $R_{xy}(T+\tau_{0.5}) = 0.5*R_{xy}(T)$, R_{xy} is the normalised cross-correlation function, and $T_{0.5}$ is the characteristic time for which the normalised auto-correlation function equals : $R_{xx}(T_{0.5}) = 0.5$ (Fig. 3-3). Equation (3-2) was derived first by CHANSON and TOOMBES (2001,2002a). Physically, a thin narrow cross-correlation function (($\tau_{0.5}$ - $T_{0.5}$)/T << 1) must correspond to little fluctuations in the interfacial velocity, hence a small turbulence level Tu. While Equation (3-2) might not be equal to the turbulence intensity u'/V, it is an expression of some turbulence level and average velocity fluctuations. More generally, when two probe sensors are separated by a transverse or streamwise distance Y, their signals may be analysed in terms of auto-correlation and cross-correlation functions R_{XX} and R_{XY} respectively. Herein the original data of 900,000 samples were segmented because the periodogram resolution is inversely proportional to the number of samples and it could be biased with large data sets (HAYES 1996, GONZALEZ 2005). All data signals were sub-divided into fifteen non-overlapping segments of 60,000 samples. Further the correlation analyses were conducted on the raw probe output signals. With a single-threshold technique, the analysis based upon thresholded signals tends to ignore the contributions of the smallest air-water particles.

Following CHANSON (2006a), the basic correlation analysis results included the maximum crosscorrelation coefficient $(R_{XY})_{max}$, and the correlation time scales T_{XX} and T_{XY} where :

$$T_{XX} = \int_{\tau=0}^{\tau=\tau (R_{XX}=0)} \Re R_{XX}(\tau) * d\tau$$
(3-3)

$$T_{xy} = \int_{\tau=\tau (R_{xy}=(R_{xy})_{max})}^{\tau=\tau (R_{xy}=0)} R_{xy}(\tau) * d\tau$$
(3-4)

where R_{XX} is the normalised auto-correlation function, τ is the time lag, and R_{XY} is the normalised crosscorrelation function between the two probe output signals (Fig. 3-2 & 3-3). T_{XX} is the auto-correlation integral time scale which characterises the longitudinal bubbly flow structure and the eddies advecting the air-water interfaces in the streamwise direction. T_{XY} is the cross-correlation integral time scale. It is a characteristic time of the large vortices with a length scale Y advecting the air-water flow structures, where the length scale Y is the probe separation distance (⁵).

When identical experiments were repeated with different separation distances Y (Y = Δz or Δx), an integral turbulent length scale was calculated as :

$$L_{xy} = \int_{Y=0}^{Y=Y((R_{xy})_{max}=0)} \int_{Y=0}^{Y=Y((R_{xy})_{max}=0)} (3-5)$$

The integral turbulent length scale L_{XY} is a function of the inflow conditions, streamwise position x/d_c and normal distance y/d_c . MOUAZE et al. (2005) introduced a similar definition to characterise some free-surface fluctuation length scale. Herein, the length scale L_{XY} represents a measure of the transverse/streamwise turbulent length scale of the large vortical structures advecting air bubbles and airwater packets.

advection integral length scale is :

$$L_{XX} = V * T_{XX}$$
(3-6)

where V is the advective velocity magnitude. L_{XX} is a characteristic longitudinal size of the eddies advecting air bubbles based upon the hypothesis of "frozen turbulence".

A turbulence integral time scale is :

An

⁵The probe separation distance Y is also denoted Δz for the transverse separation distance or Δx for the streamwise separation.

$$\mathbf{T} = \frac{\frac{\int (R_{xy})_{max} * T_{xy} * dY}{Y=0}}{L_{xy}}$$
(3-7)

T represents the transverse/streamwise integral time scale of the large eddies advecting air bubbles.

3.5 Bubble chord calculations

With the single-tip conductivity probes, a basic signal processing yields the air/water chord times and their distribution. The air/water chord times are defined as the time spent by the air/water phase on the probe sensor. Bubble chord times were calculated from the raw probe signal using the single threshold technique (described above). Statistical analyses of chord time distributions yielded the median chord time, standard deviation, skewness and kurtosis of both air and water chord times. Interparticle arrival times (⁶) were also calculated and analysed (e.g. CHANSON 2006a).

With the single-tip conductivity probe, the chord time results are presented herein in terms of pseudo-bubble/droplet chord sizes ch defined as :

$$ch = U_W * t_{ch}$$
(3-8)

where t_{ch} is the air/water chord time, U_W is the mean flow velocity defined as : $U_W = q_W/d$, q_W is the flow rate per unit width and d is the equivalent clear-water depth. The pseudo chord size ch is not equal to the air/water chord length because the local interfacial velocity V may differ from the mean flow velocity U_W .

The writers re-analysed some chord size data of GONZALEZ et al. (2005) obtained in the same chute with smooth steps (App. A). The data were recorded with a 0.025 mm sensor scanned at 20 kHz for 20 s. The comparative analysis showed that Equation (3-8) overestimated the air/water chord sizes by 2% in average for $0 \le C \le 0.97$. For C > 0.97, the error was larger but the droplet populations were small and not statistically representative. The air/water chord time data will be presented in terms of pseudo-chord sizes because the results are easier to comprehend and to compare with dual-tip probe data, visual observations, high-speed photographs and movies. Figure 3-6 shows some normalised chord length probability distribution functions where each data point represents the probability of a bubble/droplet chord in 0.5 mm intervals : e.g., the probability of a chord between 1.0 and 1.5 mm is represented by the data point labelled 1.25. The probability of bubble chord lengths greater than 15 mm is not shown for clarity. In Figure 3-6, the thick solid line is the measured bubble chord length distribution and the thin dashed line is the pseudo-chord size distribution calculated using Equation (3-8).

With the double-tip probe, the signal processing yielded the air/water chord sizes. The chord size measurement is not a bubble/droplet diameter, but a characteristic streamwise air/water size as sketched in Figure 3-3.

⁶The interparticle arrival time is defined as the time between the arrival of two successive particles. It is the time between two consecutive water-to-air interfaces.

Fig. 3-6 - Chord size distributions in skimming flows : comparison between measured chord lengths and Equation (3-8) - Experimental data by GONZALEZ et al. (2005), $d_c/h = 1.18$, Re = 5 E+5, Step 10 (A) Air bubble chords, $y/Y_{90} = 0.29$, C = 0.107, F = 177.5 Hz, V = 3.1 m/s, 3550 bubbles



(B) Droplet chords, $y/Y_{90} = 0.87$, C = 0.82, F = 170 Hz, V = 3.52 m/s, 3397 droplets



3.6 Quality control, scan frequency and scan duration

Phase-detection probes are very sensitive devices and they are susceptible to a number of problems. In the present study, the quality control procedure developed by TOOMBES (2002, pp. 70-72) was applied thoroughly. Specifically, the probe signals were checked systematically for long-term signal decays often induced by probe tip contamination, short-term signal fluctuations caused by debris and water impurities, electrical noise and non-representative samples. Although most quality control procedures can be automatised, it must be stressed that human supervision and intervention are essential to validate each quality control step.

Based upon past experiences (CHANSON and TOOMBES 2002a, TOOMBES 2002, GONZALEZ 2005), a sampling rate of 20 kHz per sensor was used for all the study, and the sampling duration was set at 45 seconds.

3.7 Data accuracy

The water discharge was measured with an accuracy of about 2% (⁷). The translation of the conductivity probes in the direction normal to the channel invert was controlled with an error of less than 0.5 mm. The accuracy on the longitudinal probe position was estimated as $\Delta x < +/-$ 0.5 cm. The error on the transverse position of the probe was less than 0.1 mm.

With both single- and double-tip conductivity probes, the error on the air concentration (void fraction) measurements was estimated as : $\Delta C/C = 4$ % for 0.05 < C < 0.95, $\Delta C/C \sim 0.002/(1 - C)$ for C > 0.95, and $\Delta C/C \sim 0.005/C$ for C < 0.05. The minimum detectable bubble chord time was about 0.05 ms for a data acquisition frequency of 20 kHz per channel (Eq. (3-8)).

The scan frequency determines the resolution of the intrusive phase-detection probe, in particular the accuracy of chord size measurement, minimum detectable air/water chord length, and the accuracy of the interfacial velocity. The minimum measurable chord size is the smallest of the probe sensor size and :

$$\Delta ch = \frac{V}{F_{scan}}$$
(3-9)

where ch is the chord size, V is the velocity, and F_{scan} is the scan rate frequency. Conversely the minimum detectable chord time is $1/F_{scan}$ provided that the particles are larger than the sensor size.

The error on the interfacial velocity was :

$$\Delta V = 1 - \frac{1}{1 + \frac{V}{F_{\text{scan}} * \Delta x}}$$
(3-10)

where Δx is the streamwise distance between probe sensors. Herein the scan frequency was 20 kHz per sensor and the streamwise distance between probe sensor was : $\Delta x = 7.0$, 9.6 or 12.2 mm.

With the double-tip conductivity probe, the analysis of the velocity field and chord length distributions implied no slip between the air and water phases. The error on the mean air-water velocity measurements

⁷GONZALEZ (2005) performed detailed velocity distribution measurements on the broad-crest for a range of flow rates. Measurements were conducted in clear-water flows with a Prandtl-Pitot tube (\emptyset = 3.3 mm). Present discharge estimates are based upon the re-analysis of his results.

was estimated as : $\Delta V/V = 5$ %. for 0.05 < C < 0.95, $\Delta V/V = 10$ %. for 0.01 < C < 0.05 and 0.95 < C < 0.99 (CHANSON and BRATTBERG 1997). The guidelines are consistent with Equation (3-10). With the two-tip conductivity probe, the minimum detectable bubble chord length was about 0.15 mm in a 3 m/s flow based upon a data acquisition frequency of 20 kHz per channel (Eq. (3-9)).

Effect of probe sensor size on chord size data

The effect of probe sensor on chord size data were tested for one flow rate ($d_c/h = 1.15$). Present chord data obtained with a 0.35 mm sensor probe were compared with some experimental results obtained by GONZALEZ et al. (2005) for $d_c/h = 1.18$ with a 0.025 mm probe sensor. CHANSON and TOOMBES (2002c) performed a similar comparison between two probe sensors sizes (0.025 and 0.35 mm) in skimming flows. Their data indicated larger measured count rates with the smaller 0.025 mm sensor probe.

Fig. 3-7 - Normalised probability distribution functions of bubble/droplet pseudo-chord sizes : comparison between 0.025 mm and 0.35 mm sensor probes

1	Buddiy now region									
	Probe	d _c /h	Step	С	F (Hz)	Reference	Run			
	sensor size		number							
	(mm)									
	0.025	1.18	10	0.107	177.5	GONZALEZ et al. (2005)	Sm13S10_05			
	0.35	1.15	10	0.106	118.1	Present study	060411S10_04			

(A) Bubbly flow region



(B) Spray region

Probe	d _c /h	Step	С	F (Hz)	Reference	Run				
sensor size		number								
0.025	1 18	10	0.893	102.9	GONZALEZ et al. (2005)	Sm13S10_19				
0.35	1.15	10	0.874	82.3	Present study	060411S10_14				
0.000	1110	10	0.071	0210		000111010_11				
0.3										
0.2		_	_							
0.1			- X		X					
0.05	; X				* * * *					
0.03	3					X				
0.02	2									
<u>н</u> 0.01	-									
죠 0.005	5									
0.003	3					────				
0.002	2					<u> </u>				
0.001		0.025	mm sensor	r C-0 893	F-103 Hz 2059 dronlets					
0.0005	$ \times - 0.35$ mm sensor, C=0.874, F=82 Hz, 3704 droplets									
0.0003	;									
0.0002										
	0.2 0.3	0.4 0.5	0.60.7	1	2 3 4 5 6	7 8 9 10 15				
	Pseudo-Chord Size (mm)									

The present data showed consistently larger measured count rates and a broader range of bubble/droplet sizes with the 0.025 mm sensor probe than with the 0.35 mm sensor probe (App. A). The pseudo chord sizes measured with the 0.35 mm sensor were typically 18 to 50% larger (average: 28%) than the chord lengths measured with the 0.025 mm sensor. This suggested the existence of a significant proportion of small bubbles/droplets with sizes ranging from 0.025 to 0.35 mm. However, in the upper spray/splashing region (i.e. C > 0.97), the pseudo-chords were close implying that most water droplets were larger than 0.35 mm. A typical comparison is shown in Figure 3-7. The figure caption and legend list the air-water flow conditions including local void fraction, count rates and the total number of bubbles/particles (⁸). Figure 3-7 shows some pseudo-chord size probability distribution functions where each data point represents the probability of a chord length in 0.5 mm intervals. In Figure 3-7, the measurements with the 0.025 mm sensor probe are drawn with the thick solid line while the thin dashed line shows the data obtained with the 0.35 mm sensor

probe.

⁸Both probes were scanned at 20 kHz per sensor. The scan duration was 20 and 45 s for the 0.025 and 0.35 mm sensor probes respectively.

3.8 Experimental procedure and inflow conditions

Experiments were conducted for a range of flow rates although the focus was on the highly aerated skimming flows (Table 3-1). Detailed air-water flow measurements were performed for flow rates between 0.09 and 0.18 m³/s corresponding to dimensionless discharges $d_c/h = 1.0$ to 1.57 and flow Reynolds numbers $\rho_W^*U_W^*D_H/\mu_W$ between 3.8 E+5 and 7.1 E+5, where d_c is the critical flow depth, h is the step height, U_W is the depth-averaged velocity, D_H is the hydraulic diameter, and ρ_W and μ_W are the water density and dynamic viscosity respectively.

Present measurements were performed systematically at step edges downstream of the inception point of free-surface aeration (Fig. 3-8). For each flow rate, measurements were repeated systematically with several transverse probe spacing Δz and with several dual-tip probe designs (streamwise sensor separation Δx). A total of more than 41 vertical profiles were recorded with a minimum of 30 measurement points per profile. At each measurement point, the data acquisition yielded 900,000 data per probe sensor. (Altogether the present data set encompassed over 1.2 billion samples.) Note that uniform equilibrium flow conditions were not achieved at the downstream end of the chute because the flume was relatively short.

Fig. 3-8 - Skimming flow on a stepped chute

(A) Definition sketch of step edge numbering



(B) Typical void fraction and velocity distributions at a step edge


4. AIR-WATER FLOW PATTERNS

4.1 Flow regimes

The basic flow regimes were inspected in a series of preliminary experiments with discharges ranging from 0.008 to 0.180 m^3 /s. Visual observations were complemented by photographic informations (Fig. 3-1 and 4-1).

For small flow rates ($d_c/h < 0.5$), the waters flowed as a succession of free-falling jets that was typical of a nappe flow regime. For some intermediate discharges ($0.5 < d_c/h < 0.95$), the flow had a chaotic behaviour characterised by strong splashing and droplet projections downstream of the inception point of free-surface aeration. That was a transition flow regime (Fig. 4-1A). For larger flows ($d_c/h > 0.95$), the waters skimmed above the pseudo-bottom formed by the step edges (Fig. 4-1B). The skimming flows were characterised by strong cavity recirculation with three-dimensional vortical patterns. These were best seen next to the inception point of free-surface aeration. Overall the results in terms of flow regimes and changes between flow regimes were very close to the observations of CHANSON and TOOMBES (2001), GONZALEZ (2005) and GONZALEZ et al. (2005) in the same chute with the same slope and step height.

Fig. 4-1 - Photographs of transition and skimming flows

(A) Transition flow - $d_c/h = 0.70$, Re = 2.3E+5



(B) Skimming flow (flow from left to right) - $d_c/h = 1.45$, Re = 6.4 E+5



4.2 Inception point of free-surface aeration

In transition and skimmings flows, the location of the inception point of free-surface aeration was recorded with discharges per unit width ranging from 0.034 to 0.18 m²/s. The results are reported in Table 4-1 and summarised in Figure 4-2. In Figure 4-2, the data are presented as L_I/k_s as a function of F*, where L_I is the streamwise distance from the downstream end of the crest (¹), and k_s is the step cavity height normal to the flow direction $k_s = h^*cos\theta$. F* is a Froude number defined in terms of the step roughness :

$$F_* = \frac{q_W}{\sqrt{g * \sin\theta * (h * \cos\theta)^3}}$$
(4-1)

where q_W is the water discharge per unit width, g is the gravity acceleration and θ is the angle between the pseudo-bottom and the horizontal.

The present data are compared in Figure 4-2 with some earlier data with smooth steps (CHANSON and TOOMBES 2001, GONZALEZ et al. 2005) and a study with rough steps (GONZALEZ et al. 2005), as well as with the empirical correlation of CHANSON (1994b,1995a) :

$$\frac{L_{I}}{h * \cos\theta} = 9.719 * (\sin\theta)^{0.0796} * F_{*}^{0.713}$$
(4-2)

The agreement between all the data with smooth steps is good. For the present study, the results were best correlated by :

$$\frac{L_{I}}{h * \cos\theta} = 1.05 + 5.11 * F_{*} \qquad \qquad 0.45 < \frac{d_{c}}{h} < 1.6 \quad (4-3)$$

¹That is, the longitudinal distance measured from the step edge 1 (Fig. 3-8).

with a normalised correlation coefficient of 0.95. Equation (4-3) is valid for transition and skimming flows on a 22° stepped chute with $0.45 < d_c/h < 1.6$.

Qw	d _c /h	Location of inception point	Flow regime
2		of free-surface aeration	
$m^{3/s}$		step edge	
(1)	(2)	(3)	(4)
0.180	1.57	7 to 8	Skimming flow
0.166	1.48	6 to 7	
0.161	1.45	7 to 8	
0.160	1.44	6	
0.146	1.35	5 to 6	
0.143	1.33	6 to 7 (almost 6)	
0.143	1.33	6 to 7 (almost 6)	
0.143	1.33	6 to 7 (almost 6)	
0.137	1.29	5 to 6	
0.136	1.29	6	
0.133	1.27	5 to 6	
0.125	1.21	5	
0.122	1.19	5 to 6	
0.117	1.16	4 to 5	
0.116	1.15	6 to 7	
0.116	1.15	6 to 7	
0.113	1.13	5	
0.109	1.10	4 to 5	
0.108	1.09	4 to 5	
0.099	1.03	4 to 5	
0.098	1.03	4	
0.090	0.97	4 to 5	
0.083	0.91	4	Transition flow
0.077	0.87	4	
0.073	0.83	3 to 4	
0.072	0.83	3 to 4	
0.070	0.81	3 to 4	
0.068	0.79	3	
0.067	0.79	3 to 4	
0.061	0.74	3 to 4	
0.060	0.73	3	
0.056	0.70	3 to 4	
0.054	0.68	3 to 4	
0.052	0.66	3 to 4	
0.047	0.61	3	
0.046	0.61	3	
0.042	0.57	2 to 3	
0.041	0.56	2 to 3 (almost 3)	
0.035	0.51	2 to 3	
0.034	0.49	2 to 3	
0.034	0.49	2 to 3	

Table 4-1 - Experimental observations of the inception point of free-surface aeration (Present study, $\theta = 21.8^{\circ}$)

Note : L_I : streamwise distance from the downstream end of the crest (Fig. 3-8).

Fig. 4-2 - Dimensionless location of the inception point of free-surface aeration - Comparison between the present observations, the data of CHANSON and TOOMBES (2001) and GONZALEZ et al. (2005) (Series CMH_05), the correlation of CHANSON (1994b) (Eq. (4-2)) and Equation (4-3)



5. BASIC AIR-WATER FLOW PROPERTIES

5.1 Void fraction and bubble count rate distributions

5.1.1 Void fraction profiles

Experimental observations demonstrated substantial free-surface aeration immediately downstream of the inception point of free-surface aeration and some sustained flow aeration was observed downstream. This is illustrated in Figure 5-1 where the dimensionless distributions for void fraction C and bubble count rate F^*d_c/V_c are presented as functions of y/d_c at several successive step edges for the same flow rate where d_c is the critical flow depth and V_c is the critical flow velocity. For a rectangular channel, d_c and V_c equal :

$$d_{c} = \sqrt[3]{\frac{Q_{w}^{2}}{W}}$$
(5-1)

$$V_c = \sqrt{g * d_c}$$
(5-2)

where Q_W is the water discharge, g is the gravity acceleration and W is the channel width. For the data shown in Figure 5-1, the flow aeration was nil at step edge 6, immediately upstream of the inception point. Between step edges 6 and 7, some strong self-aeration took place, and the amount of entrained air and the mean air content were about constant between the step edges 7 and 10. The depth-averaged void fraction was $C_{\text{mean}} = 0.36$ at the last step edge (step edge 10).

The void fraction profiles showed consistently a similar shape (Fig. 5-1 and 5-2). The dimensionless distributions presented a S-shape profile that was observed in previous studies : e.g., RUFF and FRIZELL (1994), CHANSON and TOOMBES (1997), BOES (2000a) and CHANSON and TOOMBES (2002a). For all the data, the void fraction distribution measurements compared well with an analytical solution of the advective diffusion equation for air bubbles :

$$C = 1 - \tanh^2 \left(K' - \frac{\frac{y}{Y_{90}}}{2*D_0} + \frac{\left(\frac{y}{Y_{90}} - \frac{1}{3}\right)^3}{3*D_0} \right)$$
(5-3)

where y is distance measured normal to the pseudo-invert, Y_{90} is the characteristic distance where C = 90%. K' is an integration constant and D_0 is a function of the mean air concentration C_{mean} only :

$$K' = K^* + \frac{1}{2*D_0} - \frac{8}{81*D_0}$$
(5-4)

$$K^* = \tanh^{-1}(\sqrt{0.1}) = 0.32745015...$$
(5-5)

$$C_{\text{mean}} = 0.7622 * (1.0434 - \exp(-3.614 * D_0))$$
(5-6)

Equation (5-3) was found to fit well skimming flow data (CHANSON and TOOMBES 2002a). Figure 5-2 shows a comparison between Equation (5-3) and some dimensionless void fraction data.

Fig. 5-1 - Dimensionless distributions of void fraction C and bubble count rate F^*d_c/V_c for $d_c/h = 1.15$, single-tip probe ($\emptyset = 0.35$ mm)

(A) Step edge 7







(C) Step edge 9



(D) Step edge 10



Fig. 5-2 - Dimensionless distributions of void fraction C as functions of y/Y_{90} - Comparison between Equation (5-3) and experimental data



Fig. 5-3 - Air concentration distributions in prototype stepped spillway : comparison with Equation (5-3) -Measurements at Brushes Clough dam spillway (BAKER 1994) with inclined downward steps ($\theta = 18.4^{\circ}$, h = 0.19 m, $\delta = -5.6^{\circ}$)



Remarks

Although developed for smooth chute flows at uniform equilibrium (CHANSON and TOOMBES 2001), Equation (5-3) was tested successfully against skimming flow data on prototype stepped chutes and near-full scale facilities as shown in Figure 5-3. A similar comparison between model and prototype data was performed by CHANSON and TOOMBES (1997, Fig. 5-4). This comparative analysis shown in Figure 5-3 is a rare model-prototype comparison suggesting little scale effects in terms of void fraction distributions in skimming flows.

5.1.2 Bubble count rate distribution

Typical dimensionless distributions of bubble count rate are presented in Figure 5-1. The data were recorded at several step edges for one flow rate. The data showed consistently a characteristic shape with a maximum value observed for void fractions between 35 and 60%. A similar pattern was observed in smooth chute and stepped spillway flows (e.g. CHANSON 1997b, CHANSON and TOOMBES 2001, TOOMBES 2002, GONZALEZ and CHANSON 2004, KOKPINAR 2005).

The relationship between bubble frequency and void fraction exhibited systematically a characteristic parabolic shape :

$$\frac{F}{F_{\text{max}}} = 4 * C * (1 - C)$$
(5-7)

where the maximum bubble frequency F_{max} occurs at about C ~ 0.5. Equation (5-7) is compared with experimental data in Figure 5-4. For the present study, the maximum bubble count rate was observed for $0.35 \le C \le 0.6$ although most data sets were within $0.4 \le C \le 0.5$. TOOMBES (2002) demonstrated some

theoretical validity of Equation (5-7) and he extended the reasoning to air-water flow situations when the maximum bubble count rate is observed for $C \neq 0.5$ (TOOMBES 2002, pp. 190-195).

Discussion

TOOMBES (2002) proposed a better predictive model based upon the characteristics of the streamwise structure of the air-water flow. He introduced two correction factors α and β that are functions of the local void fraction and flow conditions :

$$F = \frac{V}{\alpha * \beta * \lambda} * C * (1 - C)$$
(5-8)

where V is the interfacial velocity, and λ is a constant length scale factor. Basically λ is a length scale such that the probability of a discrete element (²) of that size being air or water is independent of the surrounding segments. The correction factor α accounts for the average size of discrete air elements having a different value to the average size of water elements at any given point, while the correction factor β allows for variations of discrete element length scales with the void fraction. Equation (5-8) was derived on the basis of theoretical considerations and it was successfully compared with experimental data for a wide range of flow situations (TOOMBES 2002).

Fig. 5-4 - Dimensionless relationship between bubble count rate and void fraction C in skimming flows - Comparison between Equation (5-7) and experimental data





²Herein the term "element" denotes chord length or chord time.



Another reasoning yields a relationship similar to Equations (5-7) and (5-8). The bubble count rate F equals half of the number of air-water interfaces. That is, F must be proportional to the rate of change of the instantaneous void fraction C :

$$F \propto c_{rms}^{2} = C * (1 - C)$$
 (5-9)

where C equals 0 or 1. The probability distribution function of the instantaneous void fraction c is bi-modal. Simple considerations show that its variance C_{rms}^2 equals C*(1 - C) where the void fraction C is the time-averaged local void fraction. In Equation (5-7), the coefficient of proportionality between F and C_{rms}^2 is $4*F_{max}$.

Note that the variance of instantaneous void fraction is physically meaningless in itself because it depends only on the time-averaged void fraction : $C_{rms}^2 = C^*(1 - C)$. Its relevance is restricted to some understanding of the relationship between bubble count rate and time-averaged void fraction (Eq. (5-9)) and for its correlation to the velocity fluctuations which plays some role in the drag reduction process (MURAI et al. 2006).

5.2 Interfacial velocity and turbulence level distributions

At each step edge, the time-averaged velocity and turbulent velocity fluctuation profiles showed some characteristic shapes (Fig. 5-5). The interfacial velocity distributions presented a smooth shape similar to earlier results on stepped chutes (e.g. BOES 2000a, CHANSON and TOOMBES 2002a, YASUDA and CHANSON 2003, GONZALEZ 2005). The turbulent intensity profiles exhibited some maximum turbulence level for $0.3 \le y/d_c \le 0.4$ which corresponded to about C ≈ 0.4 to 0.6 (Fig. 5-5).

The interfacial velocity distributions showed some self-similarity (Fig. 5-5 & 5-6). All the time-averaged velocity distributions followed closely a power-law function for $y/Y_{90} \le 1$. For $y/Y_{90} > 1$, the velocity profile was quasi-uniform. That is :

$$\frac{V}{V_{90}} = \left(\frac{y}{Y_{90}}\right)^{1/N} \qquad 0 \le \frac{y}{Y_{90}} \le 1 \quad (5-10)$$
$$\frac{V}{V_{90}} = 1 \qquad 1 \le \frac{y}{Y_{90}} \le 2.5 \quad (5-11)$$

where V_{90} is the characteristic air-water velocity at $y = Y_{90}$. Several researchers observed the velocity profile described by Equation (5-10) (e.g. MATOS 2000, BOES 2000a, CHANSON and TOOMBES 2002a). But few studies documented the velocity distribution in the upper spray region (GONZALEZ 2005).

Present data are compared with Equations (5-10) and (5-11) in Figure 5-6. For the present experiments, the exponent N was about 10, although it varied between a step edge and the next consecutive step edge for a given flow rate. The variations are believed to reflect some flow interactions between adjacent shear layers and cavity flows.

In the upper flow region, the flow structure consisted predominantly of individual water droplets and packets surrounded by air. The present results showed a quasi-uniform velocity profile for $y > Y_{90}$ and the finding tended to suggest that most droplets were in a free-fall trajectory. Since the ejected droplets had a response time of nearly two orders of magnitude larger than that of the surrounding air flow, their velocity was dominated by the ejection process.





Fig. 5-6 - Dimensionless time-averaged interfacial velocity distributions - Comparison with a 1/10 power law (Eq. (5-10)) and with Equation (5-11)



The present data showed some strong correlation between the turbulence intensity Tu and the bubble count rate. This is illustrated in Figure 5-7 presenting the turbulence intensity Tu as a function of the dimensionless bubble count rate F^*d_c/V_c . The data collapsed relatively well into a single curve :

Tu = 0.25 + a *
$$\left(\frac{F * d_c}{V_c}\right)^0$$
 (5-12)

with a = 0.035 and b = 1.2 for the present data set. CHANSON and TOOMBES (2002a) proposed first such a relationship that was also observed by YASUDA and CHANSON (2003) and GONZALEZ et al. (2005). Equation (5-12) reflects a monotonic increase in turbulence levels with an increase in bubble count rate. The limit for F = 0 is Tu = 0.25 that is close to monophase flow measurements on a stepped chute upstream of the inception point of free-surface aeration (OHTSU and YASUDA 1997, AMADOR et al. 2004a). It is hypothesised that the large number of air-water interfaces associated with high air-water count rates contributes to some increased turbulence levels compared to clear-water skimming flows. For $0.05 \le C \le 0.95$, the air-water flow structure is dominated by collisions between bubbles, droplets and packets, and by interactions between particles and turbulence levels. The continuous deformations and modification of the air-water interfacial structure do induce large turbulence levels measured by the intrusive phase-detection probe (in this case the double-tip conductivity probe).





5.3 Probability distribution functions of air bubble and water droplet chords

The probability distribution functions of chord sizes were analysed in terms of bubble chords in the bubbly flow (C < 0.3) and in terms of droplet chord lengths in the spray region (C > 0.7). Typical results are presented in Figure 5-8 which shows some examples of normalised chord size distributions. For each graph, the caption and legend provide the local air-water flow properties (C, F) and probe details. The histogram columns represent each the probability of chord size in a 0.5 mm chord interval. For example, the probability of bubble chords between 1 and 1.5 mm is represented by the column labelled 1 mm. Chord sizes larger than 15 mm are regrouped in the last column (> 15).

In the bubbly flow region (C < 0.3), the probability distribution functions showed a broad spectrum of bubble chords at each location. The range of bubble chord extended from less than 0.3 mm to more than 15 mm (Fig. 5-8). The bubble chord size distributions were skewed with a preponderance of small bubbles relative to the mean. In Figure 5-8, the mode of the probability distribution function was observed for chords between 0.5 and 1.5 mm. The probability distribution functions of bubble chord tended to follow a log–normal distribution at all locations and for all discharges. The result is consistent with the earlier data of CHANSON and TOOMBES (2002a) and GONZALEZ et al. (2005) in skimming flows.

In the spray region, the probability distribution functions of drop sizes showed also a wide range of droplet chords at each location. While the droplet chord size distributions were skewed with a preponderance of small droplets, the probability density function was flatter than that of the bubble chords (Fig. 5-8). In the upper spray region (C > 0.95), the probability distribution functions did not follow a log-normal distribution.

Fig. 5-8 - Probability distribution functions of chord sizes in skimming flows (A) $d_c/h = 1.15$, Step 10, double-tip probe ($\emptyset = 0.25 \text{ mm}$, $\Delta x = 7.0 \text{ mm}$) (A1) Bubble chord size data (C < 0.3)



(A2) Droplet chord size data (C > 0.7)





(B) $d_c/h = 1.45$, Step 10, double-tip probe ($\emptyset = 0.25 \text{ mm}$, $\Delta x = 7.0 \text{ mm}$)





6. INTEGRAL TURBULENT TIME AND LENGTH SCALES IN AIR-WATER SKIMMING FLOWS

6.1 Presentation

The correlation analyses were applied to some experiments during which two identical sensors separated by a distance Y were recorded simultaneously (Table 6-1). For some experiments, the probe sensors were located at the same vertical and streamwise distances y and x respectively, but they were separated in the transverse direction by a known distance Δz . For the experiments using the dual-tip probe, both sensors were located at the same vertical distance y, but they were separated in the streamwise direction by a known distance Δz .

Auto- and cross-correlation analyses were performed on the raw probe output signals (paragraph 3.4). Basic results included the maximum cross-correlation coefficient $(R_{xy})_{max}$, and the correlation time scales T_{xx} and T_{xy} where :

$$\mathbf{T}_{\mathbf{X}\mathbf{X}} = \int_{\tau=0}^{\tau=\tau \, (\mathbf{R}_{\mathbf{X}\mathbf{X}}=0)} \int_{\tau=0}^{\mathbf{R}_{\mathbf{X}\mathbf{X}}(\tau) * d\tau}$$
(6-1)

$$T_{XY} = \int_{\tau=\tau (R_{XY}=0)}^{\tau=\tau (R_{XY}=0)} R_{XY}(\tau) * d\tau$$
(6-2)

where R_{XX} is the normalised auto-correlation function, τ is the time lag, R_{XY} is the normalised crosscorrelation function between probe output signals, and $(R_{XY})_{max}$ the maximum cross-correlation coefficient (paragraph 3.4). Further relevant experimental results included the integral turbulent length scale L_{XY} , the integral turbulent time scale **T** and the advection length scale L_{XX} that are defined as :

$$L_{xy} = \int_{Y=0}^{Y=Y((R_{xy})_{max}=0)} \int_{Y=0}^{Y=Y((R_{xy})_{max}=0)} e^{A(R_{xy})_{max}} e^{A(R_{xy}$$

$$\mathbf{T} = \frac{\frac{Y = Y((R_{xy})_{max} = 0)}{\int (R_{xy})_{max} * T_{xy} * dY}}{L_{xy}}$$
(6-4)

$$L_{XX} = V * T_{XX}$$
(6-5)

where Y is the separation distance between probe sensors and V is the interfacial velocity.

Present experimental flow conditions are summarised in Table 6-1. All correlation analysis results are reported in Appendices D and E.

q_W	d _c	Re	Instrumentation	Δx	Δz	Step	Comments
	h					edge	
$m^{2/s}$				mm	mm		
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
0.116	1.15	4.6 E+5	2 single-tip probes	0	8.45	7	Run 060410a.
				0	8.45	8	Run 060410b.
				0	8.45	9	Run 060410c.
				0	3.6	10	Run 0604508b.
				0	6.3	10	Run 060412c.
				0	8.45	10	Run 060411a.
				0	10.75	10	Run 060411b.
				0	13.7	10	Run 060411c.
				0	16.7	10	Run 060412a.
				0	21.7	10	Run 060412b.
				0	29.5	10	Run 060413a.
				0	40.3	10	Run 060508a.
0.161	1.45	6.4 E+5	2 single-tip probes	0	8.45	8	Run 060512a.
				0	8.45	9	Run 060512b.
				0	3.6	10	Run 060509a.
				0	8.45	10	Run 060511b.
				0	13.7	10	Run 060509b.
				0	21.7	10	Run 060510a.
				0	40.3	10	Run 060510b.
				0	55.7	10	Run 060511a.
0.116	1.15	4.6 E+5	1 dual-tip probe	7.0	1.4	10	Run 060530a.
				9.6	1.4	10	Run 060613a.
0.143	1.33	5.7 E+5	1 dual-tip probe	7.0	1.4	7	Run 060614a.
				7.0	1.4	8	Run 060614b.
				7.0	1.4	9	Run 060615a.
				7.0	1.4	10	Run 060615b.
0.161	1.45	6.4 E+5	1 dual-tip probe	7.0	1.4	10	Run 060530b.
				9.6	1.4	10	Run 060613b.

Table 6-1 - Experimental measurements in skimming flows with identical probe sensors (Present study)

Notes : d_c : critical flow depth; Re : Reynolds number defined in terms of the hydraulic diameter; W : channel width.

Correlation functions

The correlation functions exhibited similar patterns for all investigated flow conditions with either a transverse or longitudinal separation (Table 6-1). Typical auto- and cross-correlation functions are presented in Figures 6-1 and 6-2.

The auto-correlation functions did not follow a Gaussian error function. Overall the auto-correlation functions R_{XX} were best fitted by :

$$R_{XX} = \frac{1}{1 + \left(\frac{\tau}{T_{0.5}}\right)^{1.3}}$$
(6-6)

where τ is the time lag and T_{0.5} is the time lag for which R_{XX} = 0.5. Figure 6-1 presents some comparison between Equation (6-6) and experimental data.

The experimental results showed that the cross-correlation functions exhibited clearly a marked maximum $(R_{xy})_{max}$ and followed a symmetrical "Gaussian" shape (Fig. 6-2). The maximum cross-correlation $(R_{xy})_{max}$ was a function of the sensor separation distance Y. Typically $(R_{xy})_{max}$ decreased with increasing sensor separation Y as illustrated in Figure 6-3. Within the range of investigations (Table 6-1), the transverse cross-correlation maxima dropped sharply for $\Delta z > 0.040$ m. The cross-correlation functions R_{xy} followed closely a Gaussian error function :

$$\frac{R_{xy}}{(R_{xy})_{max}} = \exp\left(-\frac{1}{1443} * \frac{(\tau - T)^2}{\tau_{0.5}}\right) \qquad \qquad \frac{\tau - T}{\tau_{0.5}} < 2 \quad (6-7)$$

where $(R_{XY})_{max}$ is the maximum normalised cross-correlation value observed for the time lag $\tau = T$, and $\tau_{0.5}$ is the time lag for which $R_{XY} = 0.5^*(R_{XY})_{max}$ (Fig. 3-3). The finding (Eq. (6-7)) was observed systematically for all cross-correlation functions with both transverse and streamwise sensor separations. Figure 6-2 presents a comparison between Equation (6-7) and experimental results. Figure 6-2A shows some data for $0.1 < y/Y_{90} < 1.1$ with one transverse spacing, and Figure 6-2B presents some data obtained with several transverse spacings Δz . Experimental details are given in the figure captions and legends. The results indicated that the data fitted Equation (6-7) reasonably well for $(\tau-T)/\tau_{0.5} < 2$.

Some earlier studies reported streamwise cross-correlation function data that followed relatively closely a Gaussian error function (e.g. CHANSON 2002, CHANSON and TOOMBES 2002a). Note that the radius of curvature of the cross-correlation function at $\tau = T$ is $\lambda_r = 0.8493 * \tau_{0.5}$.

Fig. 6-1 - Examples of auto-correlation functions - Flow conditions: $d_c/h = 1.15$, Re = 4.6 E+5, single-tip probe ($\emptyset = 0.35$ mm), Step edge 10 - Comparison with Equation (6-6)



Fig. 6-2 - Examples of cross-correlation functions for two probe sensors separated by a transverse distance Δz - Flow conditions: $d_c/h = 1.15$, Re = 4.6 E+5, single-tip probe ($\emptyset = 0.35$ mm) - Comparison with Equation (6-7)

(A) Step edge 10, $\Delta z = 8.45$ mm



(B) Step edge 10, $y/Y_{90} = 0.44$, C = 0.11, F = 123 Hz



Fig. 6-3 - Dimensionless distributions of maximum cross-correlation coefficients between two probe sensors separated by a transverse distance Δz - Flow conditions: $d_c/h = 1.45$, Re = 6.4 E+5, single-tip probe (\emptyset = 0.35 mm), Step edge 10



Cross-correlation function : discussion

In a developing boundary layer, FAVRE et al. (1957-58) observed that the transverse correlation coefficient of streamwise velocity dropped down to 0.2 at a transverse distance of about 0.1 to 0.15 times the boundary layer thickness δ . Their experiments were conducted in a 0.8 m wide smooth flat plate with hot-wire probes. The free-stream velocity was 12.2 m/s and the boundary layer thickness was about 33 mm.

In the present study, the transverse correlation coefficient between phase-detection probe signals dropped for a dimensionless transverse distance of about $\Delta z/h > 0.4$ and $\Delta z/Y_{90} > 2/3$. The results are of the same order of magnitude as the monophase flow results of FAVRE et al. (1957-58), and the differences may be a combination of differences in flow conditions, measurement and metrology.

6.2 Transverse integral time and length scales

Some typical distributions of correlation time scales T_{XX} and T_{XY} are presented in Figure 6-4. A definition sketch of typical skimming flow results is presented in Figure 6-4A. Figure 6-4B shows the vertical distributions of correlation time scales for several transverse spacings for the same flow conditions and at the same cross-section as the data shown in Figure 6-2. Note that the correlation time scales are presented in a dimensional form (units: seconds). Figure 6-4C presents a typical relationship between void fraction and correlation time scales at a given flow cross-section.

The results showed consistently that the auto-correlation time scales T_{XX} were larger than the transverse cross-correlation time scales T_{XY} . T_{XX} represents an integral time scale of the longitudinal bubbly flow

structures (Fig. 6-4). It is a characteristic time of the eddies advecting the air-water interfaces in the streamwise direction. T_{XY} is a characteristic time scale of the vortices with a transverse length scale Δz advecting the air-water flow structures. The cross-correlation time scale T_{XY} was nearly independent of the transverse separation Δz for $3 \le \Delta z \le 20$ mm, but it decreased with increasing transverse spacings for larger separation distances. This is illustrated in Figure 6-5. The present result suggested that some transverse length scale of the bubbly shear flow must be smaller than about 0.025 m or 0.25*h where h is the step height.

The relationship between the cross-correlation time scale T_{xy} and the void fraction followed closely a parabolic law :

$$\frac{T_{xy}}{(T_{xy})_{max}} = 4 * C * (1 - C)$$
(6-8)

where $(T_{xy})_{max}$ is the maximum cross-correlation time scale T_{xy} in the cross-section for a given separation distance Δz . Equation (6-8) is compared with experimental data in Figure 6-4C. Experimental observations of maximum time scale $(T_{xy})_{max}$ are reported in Table 6-2.

Both the distributions of auto- and cross-correlation time scales T_{XX} and T_{Xy} presented a similar parabolic shape for $0 \le C \le 0.95$ at all step edges and for all investigated flow rates (Fig. 6-4). However a marked change of shape for the auto-correlation time scale T_{XX} distribution was systematically observed in the upper spray region (C > 0.95). This change in profile is sketched in Figure 6-4A and highlighted in Figures 6-4B and 6-4C with an arrow. It is suggested that the pattern may indicate a change in the spray structure with the upper spray region . For C > 0.95, the spray consisted primarily of ejected droplets that do not interact with the rest of the flow.

Fig. 6-4 - Distributions of auto- and cross-correlation time scales T_{XX} and T_{XY} in skimming flows for several transverse distances Δz





(B) Normal distributions for $d_c/h = 1.15$, Re = 4.6 E+5, single-tip probe ($\emptyset = 0.35$ mm), Step edge 10 - Comparison with the measured void fraction distribution



(C) Relationship between auto- and cross-correlation time scales and void fraction in a cross-section - Flow conditions: $d_c/h = 1.15$, Re = 4.6 E+5, single-tip probe ($\emptyset = 0.35$ mm), Step edge 10 - Comparison with Equation (6-8)





Fig. 6-5 - Effect of the transverse separation Δz on the cross-correlation time scale T_{xy} in skimming flows -Flow conditions: $d_c/h = 1.15$, Re = 4.6 E+5, single-tip probe ($\emptyset = 0.35$ mm), Step edge 10

Table 6-2 - Experimental observations of maxima of transverse cross-correlation time scale T_{xy} and of maximum cross-correlation $(R_{xy})_{max}$ in a cross-section as a function of the transverse separation distance (Present study)

q_{W}	d _c	Re	Instrumentation	Step	Δz	Maximum	$(T_{XY})_{max}$	Comments
	h			edge		$(R_{xy})_{max}$	<i>y</i>	
$m^{2/s}$					mm	•	S	
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
0.116	1.15	4.6 E+5	2 single-tip probes	10	0	1 (+)	0.0053 (+)	
					3.6	0.6339	0.005	Run 060508b.
					6.3	0.4504	0.0037	Run 060412c.
					8.45	0.4293	0.0039	Run 060411a.
					10.75	0.3914	0.0038	Run 060411b.
					13.7	0.3172	0.0041	Run 060411c.
					16.7	0.3215	0.0039	Run 060412a.
					21.7	0.2391	0.0027	Run 060412b.
					29.5	0.182	0.0023	Run 060413a.
					40.3	0.1516	0.0023	Run 060508a.
0.161	1.45	6.4 E+5	2 single-tip probes	10	0	1 (+)	0.0055 (+)	
					3.6	0.6493	0.0048	Run 060509a.
					8.45	0.468	0.0041	Run 060511b.
					13.7	0.37	0.0044	Run 060509b.
					21.7	0.2845	0.0040	Run 060510a.
					40.3	0.1417	0.0020	Run 060510b.
					55.7	0.1166	0.0019	Run 060511a.

Notes : d_c : critical flow depth; Re : Reynolds number defined in terms of the hydraulic diameter; W : channel width; (⁺) : auto-correlation results.

Transverse integral turbulent length and time scales L_{XV} and T

Some experiments were repeated with several transverse separation distances $Y = \Delta z$. The transverse turbulent length and time scales, L_{XY} and **T** respectively, were calculated. All the results are given in Appendix E. Typical results in terms of dimensionless turbulent length scale L_{XY}/Y_{90} , integral turbulent time scale $\mathbf{T}^*\sqrt{g/Y_{90}}$ and advection length scale L_{XX}/Y_{90} are presented in Figure 6-6. The measured void fraction data are also shown in Figure 6-6. The data showed that the turbulent and advection length scales L_{XY} and L_{XX} were of the same order of magnitude although $L_{XY} \leq L_{XX}$.

The turbulent length scale L_{XY} represents a measure of the transverse size of the large vortical structures advecting the air bubbles and air-water packets. The turbulence time scale **T** characterises the integral turbulent time scale of these large eddies. The advection length scale L_{XX} is a characteristic longitudinal size of the large advecting eddies. Within Taylor's hypothesis of separate and additive advection and diffusion processes, the advection and turbulent length scales should be equal : $L_{XY} \approx L_{XX}$.

The present results highlighted that the relationships between the integral length scales L_{xy} and L_{xx} and integral time scale **T**, and the void fraction had a "skewed parabolic shape" with a maxima occurring for void fractions between 0.6 and 0.7 (Fig. 6-7). The dimensionless distributions of transverse turbulent length scale L_{xy}/Y_{90} , transverse integral turbulent time scale $\mathbf{T}^*\sqrt{g/Y_{90}}$ and advection length scale L_{xx}/Y_{90} were best correlated by :

$$\frac{L_{xy}}{(L_{xy})_{max}} = 1.75 * C^{0.57} * (1 - C)^{0.324} \qquad 0 \le C \le 1 (6-9)$$

$$\frac{\mathbf{T}}{\mathbf{T}_{\text{max}}} = 1.97 * \text{C}^{0.59} * (1 - \text{C})^{0.5} \qquad 0 \le \text{C} < 0.97 \quad (6-10)$$

$$\frac{L_{XX}}{(L_{XX})_{max}} = 1.6 * C^{0.55} * (1 - C)^{0.3} \qquad 0 \le C < 0.97 \quad (6-11)$$

where $(L_{xy})_{max}$, \mathbf{T}_{max} , and $(L_{xx})_{max}$ are the characteristic maxima in the cross-section (Table 6-3). Equation (6-9) to (6-11) are compared with data in Figure 6-7. Note that Equations (6-10) and (6-11) are not valid in the upper spray region (C > 0.95 to 0.97).

The transverse air-water turbulent length scales were closely related to the characteristic air-water depth Y_{90} : i.e., $L_{xy}/Y_{90} \approx 0.05$ to 0.2 (Fig. 6-7, Table 6-3). This result was irrespective of the dimensionless flow rate d_c/h and Reynolds numbers within the range of the experiments.

Fig. 6-6 - Dimensionless distributions of air-water transverse turbulent length scales L_{XY}/Y_{90} , transverse integral turbulent time scale $\mathbf{T}^*\sqrt{g/Y_{90}}$ and advection length scale L_{XX}/Y_{90} - Single-tip probe ($\emptyset = 0.35$ mm)



Fig. 6-7 - Dimensionless relationship between transverse turbulent length scale L_{xy}/Y_{90} , transverse integral time scale $\mathbf{T}^*\sqrt{g/Y_{90}}$ and advection length scale L_{xx}/Y_{90} , and void fraction at Step 10- Single-tip probe (\emptyset = 0.35 mm) - Comparison with Equation (6-9) to (6-11) (A) d_c/h = 1.15, Re = 4.6 E+5, Step edge 10



(B) $d_c/h = 1.45$, Re = 6.4 E+5, Step edge 10



Parameter	$\frac{d_c}{1.15}$	$\frac{d_c}{d_c}$ 1.45	Remarks
	h = 1.15	h = 1.45	
(1)	(2)	(3)	(4)
Transverse scales ($Y = \Delta z$)			Single-tip probe data ($\emptyset = 0.35$ mm).
$(L_{xy})_{max}/Y_{90}$	0.223	0.231	
T _{max} * $\sqrt{g/Y_{90}}$	0.0473	0.0408	$0 \leq C < 0.97$
$(L_{xx})_{max}/Y_{90}$	0.263	0.265	$0 \leq C < 0.97$
Streamwise scales $(Y = \Delta x)$			Double-tip probe data ($\emptyset = 0.25$ mm).
$(L_{xy})_{max}/Y_{90}$	0.1865	0.151	
T _{max} * $\sqrt{g/Y_{90}}$	0.0472	0.041	$0 \leq C < 0.97$
$(L_{xx})_{max}/Y_{90}$	0.231	0.132	$0 \leq C < 0.97$

Table 6-3 - Characteristic integral turbulent length and time scales, and advection length scales in skimming flows on a stepped chute (transverse and streamwise integral turbulent scales)

6.3 Streamwise integral time and length scales

Experimental results in terms of longitudinal integral turbulent length and time scales showed some trends similar to those observed with the transverse integral turbulent scales. Figures 6-8 and 6-9 present the streamwise integral scales obtained for the same flow conditions as the transverse integral scale data shown in Figures 6-6 and 6-7.

Herein the integral turbulent length scale L_{XY} represented a measure of the longitudinal scale of large vortices which advected the air bubbles and air-water packets. The present data showed that the streamwise and advection length scales were about the same although $L_{XY} \leq L_{XX}$. Both the transverse and streamwise turbulent length scales were close and the results yielded $L_{XY}/Y_{90} \approx 0.1$ to 0.2. The integral turbulent length scales were maximum for about C = 0.6 to 0.7 (Fig. 6-7 and 6-9, Table 6-3). Table 6-3 summarises the characteristic turbulent length and time scales for the present study.

The integral turbulent time scale **T** characterises the time scale of the large eddies advecting the air bubbles. The streamwise and transverse integral turbulent time scales were close and the data yielded $0.01 \le \mathbf{T}^* \sqrt{g/Y_{90}} \le 0.06$ (Fig. 6-6 and 6-8, Table 6-3). Fig. 6-8 - Distributions of auto- and cross-correlation time scales T_{XX} and T_{XY} in skimming flows for several streamwise separation distances Δx - Double-tip conductivity probe ($\emptyset = 0.25$ mm) - Comparison with the measured void fraction distribution











(A) $d_c/h = 1.15$, Re = 4.6 E+5, Step edge 10



6.4 Discussion

Some researchers studied fundamental processes affecting free-surface deformations and air-water freesurfaces: e.g., SARPKAYA (1996), CHANSON (1997a), BROCCHINI and PEREGRINE (2001), MOUAZE et al. (2005). However, few results were reported on turbulent length scales in bubbly shear flows but one study in hydraulic jumps (CHANSON 2006a). It is believed that the present data sets are unique.

What is the physical significance of the air-water integral turbulent length scale L_{XY} ? In bubbly flows, the turbulent length scales are closely linked with the characteristic sizes of the large-size eddies and their interactions with entrained air bubbles. This was evidenced by high-speed photographs demonstrated air bubble trapping in the large eddies of developing mixing layers (e.g. HOYT and SELLIN 1989, CHANSON 1997a). Herein the integral turbulent length scale L_{XY} represents a measure of the size of large vortical structures advecting air bubbles in the skimming flows. Present results emphasise that both streamwise and transverse turbulent length scales were nearly equal and they were closely related to the characteristic air-water depth Y_{90} : i.e., $L_{XY}/Y_{90} \approx 0.1$ to 0.2. The result was irrespective of the Reynolds numbers within the range of the experiments.

The advection length scale equals $L_{XX} = V * T_{XX}$. If the turbulent advection and diffusion of the bubbles are two separate additive processes, the advection length scale is about the integral turbulent length scale L_{XY} defined in terms of a streamwise separation distance Y. Present results showed close results for 0 < C < 0.95(Fig. 6-9). Some substantial difference was however observed in the upper spray region (C . 0.95 to 0.97) implying that the assumption of independent advection and diffusion processes and the hypothesis of "frozen turbulence" were not valid in this upper spray region.

7. DISCUSSION

7.1 Self-similarity in air-water flow properties

In the field of fluid mechanics, many flow types present some self-similarity. A self-similar process is one whose spatial distribution of properties at various times can be obtained from one another by a similarity transformation (BARENBLATT 1994,1996). Self-similarity is a powerful tool in turbulence flow research, and skimming flows on a stepped chute are one type of turbulent flows involving a wide spectrum of spatial and temporal scales. The non-linear interactions among vortices and particles at different scales lead usually to a complex flow structure. Thus relationships among flows at different scales are of crucial significance in understanding and controlling these flows. They play also a major role in comparing analytical, experimental and numerical results as these results are for different scales, and most stepped spillway applications are for prototype flow conditions with flow Reynolds number between 1 E+6 and more than 1 E+9 that cannot be modelled numerically nor physically.

In the present study self-similarity was observed in terms of the distributions of air-water flow properties. Table 7-1 summarises some basic self-similarity equations that were observed during the present work. Self-similarity is illustrated for example in Figures 7-1, 5-6, 5-7, 6-2, and 6-7. These self-similar relationships were observed at both macroscopic and microscopic levels. For example, the distributions of void fraction and interfacial velocity at a macroscopic level, and the cross-correlation function and probability distribution functions of particle chords at a microscopic level (Table 7-1).

Self-similarity is closely linked with dynamic similarity (Section 2). In paragraph 2.2, it was argued that it is nearly impossible to achieve a true dynamic similarity in stepped spillway models because of number of relevant dimensionless parameters. Yet the experimental results showed a number of self-similar relationships (Table 7-1) that remain invariant under changes of scale : i.e., they have scaling symmetry which led in turn to remarkable application at prototype scales. Clearly the present results are most significant because they demonstrate a number of self-similar relationships characterising the air-water flow properties in skimming flow above stepped chutes. They provide a picture general enough to be used, as a first approximation, to characterise the air-water flow field in similar stepped spillway structures irrespective of the physical scale.

7.2 Flow resistance and residual energy

On a stepped chute, the skimming flows are characterised by significant form losses. The water skims over the step edges with formation of recirculating vortices between the main stream and the step corners. Form drag is predominant. Downstream of the inception point of free-surface aeration, the flow was gradually-varied flow during the present study. The average shear stress between the skimming flow and the cavity recirculation was deduced from the measured friction slope S_f :

$$f_{e} = \frac{8 * \tau_{o}}{\rho_{w} * U_{w}^{2}} = \frac{8 * g * \left(\int_{y=0}^{y=Y_{90}} (1 - C) * dy\right) * S_{f}}{U_{w}^{2}}$$
Gradually-varied flow (7-1)

where f_e is the equivalent Darcy-Weisbach friction factor, C is the local void fraction, y is measured normal to the pseudo-invert formed by the step edges, Y_{90} is the distance normal to the pseudo-bottom where C =

90%, U_W is the water flow velocity : $U_W = q_W/d$, q_W is the water discharge per unit discharge and d is the equivalent clear-water depth. The friction slope ($S_f = -\partial H/\partial x$) is the slope of the total head line, where H is the mean total head (HENDERSON 1966, CHANSON 1999a,2004a). Free-surface aeration is always substantial in prototype and laboratory skimming flows, and its effects must be accounted for using Equation (7-1).

Flow property (1)	Self-similarity (2)	Remarks (3)		
Void fraction distribution	$C = 1 - \tanh^2(\chi)$	$\chi = K' - \frac{y'}{2*D_0} + \frac{\left(y' - \frac{1}{3}\right)^3}{3*D_0}$		
		$0 \le y' \le 1$ Equation (5-3).		
Bubble count rate distribution	$\frac{F}{F_{max}} = 4 * C * (1 - C)$	$0 \le C \le 1$ Equation (5-7).		
Interfacial velocity distribution	$\frac{v}{v_{90}} = y'^{1/N}$	$\begin{array}{l} 0 \leq y' \leq 1 \\ \text{Equation (5-10).} \end{array}$		
	$\frac{\mathbf{V}}{\mathbf{V}_{90}} = 1$	$1 \le y' \le 2.5$ Equation (5-11).		
Turbulence level distribution	$Tu = 0.25 + a * \left(\frac{F * d_c}{V_c}\right)^b$	$0 \le C \le 1$ Equation (5-12).		
Probability distribution functions of bubble chords	Log-normal distribution	$0 \le C \le 0.3$		
Probability distribution functions of droplet chords	Log-normal distribution	$0.7 \leq C \leq 0.95$		
Cross-correlation function	$\mathbf{R}_{\mathbf{X}\mathbf{X}} = \frac{1}{1 + \left(\frac{\tau}{T_{0.5}}\right)^{1.3}}$	$0 \le y' \le 1$ Equation (6-6).		
Cross-correlation function (between two probe sensors separated by a distance Y)	$\frac{R_{xy}}{(R_{xy})_{max}} = \exp\left(-\frac{1}{1443} * \frac{(\tau - T)^2}{\tau_{0.5}}\right)$	$0 \le y' \le 1$ Equation (6-7). Both transverse and streamwise probe sensor		
Cross-correlation time scale distribution (between two probe sensors separated by a distance Y)	$\frac{T_{xy}}{(T_{xy})_{max}} = 4 * C * (1 - C)$	$0 \le C \le 1$ Equation (6-8). Both transverse and streamwise probe sensor separations.		
Distribution of transverse integral turbulent length scale	$\frac{L_{xy}}{(L_{xy})_{max}} = 1.75 * C^{0.57} * (1-C)^{0.324}$	$0 \le C \le 1$ Equation (6-9).		
Distribution of transverse integral turbulent time scale	$\frac{\mathbf{T}}{\mathbf{T}_{\text{max}}} = 1.97 * \text{C}^{0.59} * (1 - \text{C})^{0.5}$	$0 \le C \le 0.97$ Equation (6-10).		
Distribution of advection turbulent length scale	$\frac{L_{XX}}{(L_{XX})_{max}} = 1.6 * C^{0.55} * (1 - C)^{0.3}$	$0 \le C \le 0.97$ Equation (6-11).		

Table 7-1 - Self-similarity of the air-water flow properties in skimming flow above stepped chutes

Note : $y' = y/Y_{90}$.

Fig. 7-1 - Self-similarity in air-water skimming flows on a stepped chute

(A) Dimensionless void fraction distributions : $C = 1 - \tanh^2(\chi)$ with $\chi = K' - y'/(2*D_0) + (y'-1/3)^3/(3*D_0)$ Xeta



(B) Dimensionless bubble count rate distributions : $F/F_{max} = 4 * C * (1 - C)$



Flow resistance results are presented Figure 7-2 where the friction factor in skimming flows is plotted as a function of the dimensionless step roughness height $h*\cos\theta/D_H$, where h is the step height, θ is the angle between the pseudo-bottom formed by the step edges and the horizontal, and D_H is the hydraulic diameter. All the data are reported in Appendix C. In average, in the present study, the equivalent Darcy friction factor was $f_e \approx 0.14$ downstream of the inception point of free-surface aeration. The results are close to earlier results obtained in the same facility. Note that Equation (7-1) represents the equivalent Darcy friction factor in the aerated flow region only. In the developing boundary layer region, AMADOR et al. (2006) derived the flow resistance by applying an integral momentum method to PIV measurements and their results yielded f = 0.125 for $d_c/h = 2.1$ and Re = 4.4 E+5.

In Figure 7-2, the present flow resistance results are further compared with a comprehensive re-analysis of flow resistance data in skimming flows (CHANSON et al. 2002, CHANSON 2006b). The details of the experimental technique are summarised in the figure caption (Fig. 7-2). Overall, the equivalent Darcy friction factor was typically between 0.1 and 0.35 with no obvious correlation with the relative step roughness height, Reynolds, Froude nor Weber numbers, and the present data were comparable to previous studies. The friction factor data compared favourably with a simplified analytical model of the pseudo-boundary shear stress which may be expressed, in dimensionless form, as :

$$f_{d} = \frac{2}{\sqrt{\pi}} * \frac{1}{K}$$
(7-2)

where f_d is an equivalent Darcy friction factor estimate of the form drag, and 1/K is the dimensionless expansion rate of the shear layer. Equation (7-2) predicts $f_d \approx 0.2$ for K = 6 that is close to the observed friction factors (Fig. 7-2).

Residual energy

For the present investigations, the rate of energy dissipation $\Delta H/H_{max}$ and the dimensional residual energy H_{res}/d_c were estimated at the downstream end of the chute (Step 10), and the results are summarised in Table 7-2. The residual head H_{res} is the total head at the downstream end of the chute, and it equals :

$$H_{res} = d * \cos\theta + \frac{U_W^2}{2 * g}$$
(7-3)

where d is the equivalent clear-water depth and U_W is the flow velocity ($U_W = q_W/d$). The present results showed a decreasing rate of energy dissipation on the stepped chute with increasing discharge. For design engineers, however, it is more relevant to consider the dimensionless residual head H_{res}/d_c . Present results implied that the dimensionless residual head was about $2.4 \le H_{res}/d_c \le 3.3$, increasing slightly with increasing flow rate.

Note that the present results were obtained with a fully-developed, aerated flow at the chute downstream end. For larger discharges, the flow might not be fully-developed at the downstream end, and that the residual energy could be considerably larger (CHANSON 2001, MEIRELES et al. 2006).

Fig. 7-2 - Equivalent Darcy-Weisbach friction factor in air-water skimming flows - Comparison between present data and earlier studies (ANDRE et al. 2003, BaCara 1991, BOES 2000a, CHAMANI and RAJARATNAM 1999, CHANSON and TOOMBES 2001,2002a, GONZALEZ and CHANSON 2004, MATOS 2000, SHVAJNSHTEIN 1999, YASUDA and OHTSU 1999) for large size model data (Re > 1 E+5



Table 7-2 - Rate of energy dissipation and dimensional residual energy at the downstream end of the stepped chute (Step 10)

$\frac{d_c}{h}$	$\frac{\Delta H}{H_{max}}$	$\frac{H_{res}}{d_c}$	Remarks
(1)	(2)	(3)	(4)
1.0	0.58	2.96	Measured at Step edge 10.
1.15	0.54	2.85	
1.33	0.52	2.48	
1.45	0.51	2.35	
1.57	0.40	3.32	

7.3 Spray structure : the upper spray region

In the present study, detailed air-water flow measurements were conducted in the spray region. That region of the flow is characterised by water droplets surrounded by air and it is defined herein as C > 0.7. Herein, the air-water properties were recorded for void fractions C up to 0.999 corresponding to y/Y_{90} up to 2.5. The
experimental data showed some distinctive features in the upper spray region defined as C > 0.95 to 0.97, especially in terms of droplet chord size distributions and advection integral length scale distributions.

In the lower spray region (0.7 < C < 0.9 to 0.95), the probability distribution functions of water chord were skewed with a preponderance of small droplets relative to the mean and they followed closely a log-normal distribution (paragraph 5.3). The distributions of advection length scale L_{XX} showed a decrease in dimensionless length scales L_{XX}/Y_{90} with increasing distance y/Y90 and decreasing liquid fraction (1-C).

Some different results were observed in the upper spray region (C > 0.95 to 0.97). The probability distribution functions of droplet chords were relatively flat and did not follow a log-normal distribution. The PDF maxima were about 0.1 to 0.15 and most droplet chords were between 0.5 and 8 mm. For C > 0.95 to 0.97, the distributions of advection integral length scale showed increasing length scale with decreasing liquid fraction (1-C) (paragraphs 6.2 & 6.3). The result might suggest the existence of longitudinal "streaks" of water drops.

It is believed that the contrasting features of the upper spray region reflected a change in the microscopic flow structure. That is, the upper spray region consisted primarily of ejected water droplets that did not interact with the main flow nor with the surrounding air. These droplets tended to follow some ballistic trajectory (Fig. 7-3) and their "history" was dominated by the initial ejection process and possibly by droplet collisions.

Fig. 7-3 - High-speed photographs of water droplets in ballistic trajectory, viewed from upstream - Skimming flows, h = 0.1 m, $\theta = 21.8^{\circ}$

(A) $d_c/h = 1.45$, Re = 6.9 E+5 (shutter speed 1/125 s) - Note probe support in background



(B) $d_c/h = 1.35$, Re = 6.2 E+5 (shutter speed 1/200 s)- Note the double-tip probe in background



8. CONCLUSION

New air-water flow measurements were performed in skimming flows on a large stepped spillway model (Fig. 8-1). The channel slope was 21.8°, the step height was 0.1 m and the flow Reynolds numbers ranged from 3.8 E+5 to 7.1 E+5. Two types of phase-detection intrusive probes were used : single-tip conductivity probes ($\emptyset = 0.35$ mm) and double-tip conductivity probes ($\emptyset = 0.25$ mm). Measurements were conducted in the air-water flow region downstream of the inception point of free-surface aeration. For some experiments, two probe sensors were separated by a known transverse or longitudinal distance and sampled simultaneously at 20 kHz for 45 seconds. An advanced signal processing technique with new signal correlation analyses was developed. It was applied systematically to the present data sets.

The air water flow properties presented some basic characteristics that were qualitatively and quantitatively similar to previous studies in skimming flows. These included the distributions of void fraction, bubble count rate and interfacial velocity, the distributions of air and water chord sizes, and the flow resistance estimates. Further some self-similar relationships were observed systematically at both macroscopic and microscopic levels (Table 7-1). These included the distributions of void fraction, bubble count rate, interfacial velocity and turbulence level at a macroscopic scale, and the bubble chord distributions and auto- and cross-correlation functions at the microscopic level. Self-similarity is closely linked with dynamic similarity (Section 2). Although it is nearly impossible to achieve a true dynamic similarity in stepped spillway models because of the number of relevant dimensionless parameters, the experimental results showed a number of self-similar relationships that remained invariant under changes of scale. This result leads in turn to remarkable applications at prototype scales. The present findings are significant because they provides a picture general enough to be used to characterise the air-water flow field in prototype stepped spillways.

Correlation analyses yielded a characterisation of the large eddies advecting the bubbles. Basic results included the transverse and streamwise integral turbulent length scales, the transverse and longitudinal integral time scales, and the advection length scale. In air-water shear flows, the turbulent length scales were closely linked with the characteristics of the large-size eddies and their interactions with entrained air bubbles. Herein the turbulent length scales characterised a measure of the size of large vortical structures advecting air bubbles in the skimming flows. Both streamwise and transverse integral turbulent length scales were closely related to the characteristic air-water depth Y_{90} : i.e., $L_{xy}/Y_{90} \approx 0.05$ to 0.2. The integral turbulent time scales were within $0.01 \leq \mathbf{T}^* \sqrt{g/Y_{90}} \leq 0.06$. The results were irrespective of the Reynolds numbers within the range of the experiments.

Experimental measurements were conducted thoroughly in the spray region for y/Y_{90} up to 2.5 and C up to 0.999. The results highlighted the existence of an upper spray region for C > 0.95 to 0.97 (Fig. 8-1B). In the upper spray region, the distributions of droplet chord sizes and the distributions of integral advection scales (T_{XX}, L_{XX}) presented some marked difference with the rest of the flow. It is suggested that these patterns highlighted a change in spray structure, whereby the upper spray region consisted primarily of ejected droplets. The ejected droplets followed some ballistic trajectory, and they interacted little with the surrounding air nor with the rest of the flow until they re-attached.

Fig. 8-1 - Photographs of the experimental test section

(A) Side view, $d_c/h = 1.0$, Re = 3.8 E+5, Shutter speed: 1/80 s



(B) Looking downstream at some ejected droplets in the upper spray region for $d_c/h = 1.33$, Re = 5.7 E+5, Shutter speed: 1/320 s - The distance y between the pseudo-bottom formed by the step edges and the lower trolley support is shown



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APPENDIX A - AIR/WATER CHORD MEASUREMENTS WITH A SINGLE-TIP CONDUCTIVITY PROBE

A.1 Presentation

New experiments were performed in the Gordon McKAY Hydraulics Laboratory at the University of Queensland in the experimental channel which was previously used by CHANSON and TOOMBES (2001,2002a,2003) and GONZALEZ (2005) with smooth step faces, and by GONZALEZ et al. (2005) (Table A-1). The test section consisted of a broad-crested weir followed by ten identical steps (h = 0.1 m, l = 0.25 m). Air-water flow properties were measured with phase-detection intrusive probes : namely single-tip conductivity probes and double-tip conductivity probes (Table A-1).

Herein, we focus on some basic air-water chord measurements performed with the single-tip conductivity probes (needle probe design). The probe consisted of a sharpened rod (platinum wire $\emptyset = 0.35$ mm) coated with non-conductive epoxy and set into a stainless steel surgical needle ($\emptyset = 1.42$ mm) acting as the second electrode as sketched in Figure A-1. The probe was excited by an electronic system (Ref. UQ82.518) designed with a response time less than 10 µs and the probe signal output was scanned at 20 kHz for 45 s.

Reference	θ	Step	Flow conditions	Instrumentation	Remarks
		geometry			
	deg.				
(1)	(2)	(3)	(4)	(5)	(6)
GONZALEZ et	21.8	h = 0.1 m	$q_{\rm W} = 0.01$ to 0.219 m ² /s,	Double-tip conductivity	Experiments
al. (2005)		l = 0.25 m	Re = 4 E + 4 to 9 E + 5.	probe ($\emptyset = 0.025 \text{ mm}$).	CMH_05.
					W = 1 m.
Configuration S		Smooth		scanned at: 20 kHz for	
(smooth steps)		horizontal		20 s	
		steps			
Present study	21.8	h = 0.1 m			Experiments
		l = 0.25 m			GH_06.
					W = 1 m.
Series 1			$q_{\rm W} = 0.095$ to 0.18 m ² /s,	Single-tip conductivity	
			Re = 3.8 E+5 to 7.1 E+5	probe ($\emptyset = 0.35 \text{ mm}$)	
				scanned at: 20 kHz for	
			_	45 s	
Series 2			$q_{\rm W} = 0.12$ to 0.16 m ² /s,	Double-tip conductivity	
			Re = 4.6 E+5 to 6.4 E+5	probe ($\emptyset = 0.25 \text{ mm}$)	
				scanned at: 20 kHz for	
				45 s	

Table A-1 - Experimental investigations of stepped chute flows on flat slopes ($\theta < 30^\circ$)

Notes : h : step height; l : step length; q_W : discharge per unit width; Re : flow Reynolds number defined in terms of hydraulic diameter.



Fig. A-1 - Sketch of a single-tip conductivity probe

Signal processing

The measurement principle of a conductivity probe is based upon the difference in electrical resistivity between air and water. The resistance of water is one thousand times lower than the resistance of air bubbles. When the probe tip is in contact with water, current will flow between the tip and the supporting metal; when it is in contact with air no current will flow. A sketch of the single-tip conductivity probe is presented in Figure A-1.

In the present study, the air-water flow properties were calculated using a single threshold technique and the threshold was set at about 45 to 55% of the air-water voltage range. The basic outputs are the void fraction, bubble count rate and air/water chord times. The void fraction C is the proportion of time that the probe tip is in the air. The bubble count rate F is the number of bubbles impacting the probe tip per second. The air/water chord time is defined as the time spent by the air/water phase on the probe sensor. Bubble chord times were calculated from the raw probe signal. Statistical analyses of chord time distributions yield the median chord time, standard deviation, skewness and kurtosis of both air and water chord times, as well as the probability distribution functions of air and water chord times at each sampling location.

A.2 Pseudo-chord sizes

Herein the chord time results are presented in terms of pseudo-bubble/droplet chord size ch defined as : $ch = U_W * t_{ch}$ (A-1) where t_{ch} is the air/water chord time, U_W is the mean flow velocity defined as : $U_W = q_W/d$, q_W is the flow rate per unit width and d is the equivalent clear-water depth. The pseudo chord size ch is not equal to the air/water chord length because the mean flow velocity U_W may differ from the interfacial velocity.

The writers re-analysed some chord size data by GONZALEZ et al. (2005) obtained in the same chute with an identical step geometry. Their data were recorded with a 0.025 mm sensor scanned at 20 kHz for 20 s (Table A-1). With the double-tip probe, the signal processing yielded the true air/water chord sizes. Note that the chord size measurement is not a bubble/droplet diameter, but a characteristic streamwise size of the air/water particle as sketched in Figure A-1.

Measurements of true chord sizes and pseudo-chord sizes (Eq. A-1) were compared in terms of their probability distribution functions. Figure A-2 shows some typical normalised chord length probability distribution functions where each data point represents the probability of a bubble/droplet chord in 0.5 mm intervals : e.g., the probability of a chord length from 1.0 to 1.5 mm is represented by the data point labelled 1.25. The probability of bubble chord lengths greater than 15 mm is not shown for clarity. In Figure A-2, the measured bubble chord length distribution is the thick solid line and the thin dashed line is the pseudo-chord size distribution calculated using Equation (A-1). For the same flow conditions, Table A-2 presents some relative errors between true chord size and pseudo-chord size estimates for one cross-section. The data showed that the probability distribution functions were skewed with a preponderance of small particles relative the mean size. The distributions functions, the data did not follow a log-normal shape, but the number of particles might be insufficient for the results to be statistically meaningful.

The comparative analysis showed that Equation (A-1) overestimated the air/water chord sizes by 2% in average for $0 \le C \le 0.97$. This was indeed a very small difference. For C > 0.97, the error was larger but the droplet populations were small and not statistically representative. In this report, air/water chord time data will be presented in terms of pseudo-chord sizes because the results are easier to comprehend and to compare with dual-tip probe data, visual observations, high-speed photographs and movies. The approximation is supported by the very small differences between true and pseudo-chord sizes.

A.3 Effect of probe sensor size on chord data

The effects of the probe sensor size on chord size data were tested for one flow rate. For $d_c/h = 1.15$, the present pseudo-chord data (0.35 mm probe sensor) were compared with pseudo-chord size data obtained by GONZALEZ et al. (2005) for $d_c/h = 1.18$ with a 0.025 mm probe sensor. CHANSON and TOOMBES (2002c) tested the performances of two probe sensors sizes (0.025 and 0.35 mm) in skimming flows. Their data indicated consistently larger measured count rates with the 0.025 mm sensor probe.

Fig. A-2 - Chord size distributions in skimming flows : comparison between measured chord lengths and Equation (A-1) - Experimental data by GONZALEZ et al. (2005), $d_c/h = 1.18$, Re = 5 E+5, Step 10, Sensor size : 0.025 mm



(A) $y/Y_{90} = 0.29$, C = 0.107, F = 177.5 Hz, V = 3.1 m/s, 3550 bubbles

(B) $y/Y_{90} = 0.87$, C = 0.82, F = 170 Hz, V = 3.52 m/s, 3397 droplets



Ref.	Void Fraction	Nb of bubbles/droplets	Relative error (%)
(1)	(2)	(3)	(4)
05	0.107	3550	2.0
10	0.218	4980	-3.7
12	0.327	5601	-3.5
17	0.817	3397	0.82
19	0.893	2059	1.4
20	0.922	1476	-4.4
21	0.943	1119	8.7
22	0.961	785	4.9
24	0.973	518	11.6
25	0.98	409	14.6
27	0.987	274	9.9
28	0.99	198	-28.6
30	0.996	82	-15.4

Table A-2 - Relative error between chord sizes and pseudo-chord size for $d_c/h = 1.18$, step 10

Notes : Data : GONZALEZ et al. (2005); Errors calculated for bubble chord for C < 0.3 and droplet chords for C > 0.7.

A typical comparison is shown in Figure A-3. The figure caption and legend list the air-water flow conditions including local void fraction, count rates and the total number of bubbles/particles. Note that, for both experiments, the probes were scanned at 20 kHz per sensor, but the scan duration was 20 s for the data set of GONZALEZ et al. (2005) (0.025 mm sensor probe) versus 45 s for the present data set (0.35 mm sensor probe). Figure A-3 shows some pseudo-chord size probability distribution functions where each data point represents the probability of a chord length in 0.5 mm intervals. In Figure A-3, the pseudo-chord data with the 0.025 mm probe sensor are drawn with the thick solid line while the thin dashed line shows the data obtained with the 0.35 mm and 0.35 mm sensors in terms of pseudo-chord sizes for one cross-section. The relative error was calculated for bubble chords (C < 0.3) and droplet chords (C > 0.7).

The present comparison tested systematically the effects of the probe sensor size in terms of the pseudochord size probability distribution functions. The comparative results showed consistently larger measured count rates and a broader range of bubble/droplet sizes with the 0.025 mm probe sensor (Table A-3, columns 3 and 6). The pseudo chord sizes measured with 0.35 mm sensor were typically 18 to 50% larger (average 28%) than the pseudo-chord lengths measured with the 0.025 mm probe sensor. This suggested the existence of a significant proportion of small bubbles/droplets with sizes ranging from 0.025 to 0.35 mm. In the upper spray/splashing region (i.e. C > 0.97) however, the pseudo-droplet chord data were close implying that most water droplets were larger than 0.35 mm.

A.3 Discussion

The notion of pseudo-chord size was used in earlier studies. For example, CHANSON et al. (2002,2006) in plunging jet flows. Generally the concept of pseudo-chord sizes is easier to comprehend and to compare with visual observations, high-speed photographs and movies than the bubble/droplet chord time data. However it is essential to validate Equation (A-1) in any complex air-water flows before using it.

The effects of probe sensor size on the air-water flow properties were seldom tested but in a few studies (CHANSON and TOOMBES 2002c). It is acknowledged that the probe sensor size may affect the results when the sensor size is large than the smallest bubbles. The true accuracy of the data is however a combination of both probe sensor size and scan rate, while the scan duration must be long enough to ensure a statistically meaningful sample.

Fig. A-3 - Normalised probability distribution functions of bubble/droplet chord sizes : comparison between 0.025 mm and 0.35 mm sensor probe sensor sizes

(A) Bubbly flow region

Probe sensor	d _c /h	Step	С	F (Hz)	Reference	Run
size (mm)	-	number				
0.025	1.18	10	0.107	177.5	GONZALEZ et al. (2005)	Sm13S10_05
0.35	1.15	10	0.106	118.1	Present study	060411S10_04



(B) Spray region



Table A-3 - Effect of the probe sensor size on the relative error in terms of pseudo-chords for $d_c/h = 1.15$, step 10

	GONZALEZ	et al.(2005)		Present	Study	Relative
Ref.	С	F	Ref.	С	F	error
		(Hz)			(Hz)	(%)
(1)	(2)	(3)	(4)	(5)	(6)	(7)
05	0.107	177.5	08	0.106	118.0	46.8
10	0.218	249.1	09	0.182	159.0	18.7
12	0.327	183.6	10	0.327	177.0	20.1
17	0.817	169	13	0.798	120.0	44.2
19	0.893	102.0	14	0.974	82.0	49.7
20	0.922	73.0	15	0.91	57.0	38.7
21	0.943	55.9	16	0.933	43.6	13.5
22	0.961	39.2	18	0.961	27.8	15.5
24	0.973	25.8	20	0.973	19.4	5.5
25	0.98	20.4	21	0.981	15.5	8.2
27	0.987	13.6	22	0.987	10.5	-4.1
28	0.99	9.8	24	0.993	7.1	
29	0.994	7.05	27	0.995	4.0	
30	0.996	4.05	28	0.996	4.4	-12.9

Notes : Errors calculated for bubble chord for C < 0.3 and droplet chords for C > 0.7.

APPENDIX B - SUMMARY OF AIR-WATER FLOW PROPERTIES

Notation

С	void fraction defined as the volume of air per unit volume of air and water;
C _{mean}	depth-average vid fraction defined in terms of Y_{90} : $C_{mean} = 1 - d/Y_{90}$;
d	equivalent clear water flow depth defined as: $d = \int_{C=0}^{C=0.90} (1 - C) * dy$;
d _c	critical flow depth (m);
F _{max}	maximum bubble count rate (Hz) at a given cross-section;
f	equivalent Darcy-Weisbach friction factor in air-water skimming flows;
g	gravity constant: $g = 9.80 \text{ m/s}^2$ in Brisbane, Australia;
Q _w	water discharge (m ³ /s);
W	channel width (m);
X	distance along the channel bottom (m);
Y90	characteristic depth (m) where the void fraction is 90%.

Results

Run	Q_W	Probe	Step edge	d	Y90	F _{max}	V ₉₀	C _{mean}
	m ³ /s		-	m	m	Hz	m/s	
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
060323a	0.0948	1-tip probe	6	0.0331	0.0790	150.4		0.580
			7	0.0388	0.0645	148.8		0.399
			8	0.0401	0.0645	166.4		0.379
			9	0.0380	0.0805	144.9		0.528
			10	0.0333	0.0585	173.1		0.431
060410a	0.1164	1-tip probe	7	0.0390	0.0748	161.9		0.479
			8	0.0458	0.0645	177.8		0.290
			9	0.0335	0.0635	177.8		0.472
			10	0.0389	0.0610	194.9		0.363
060614a	0.1431	2-tip probe	7	0.0428	0.0668	118.4	3.27	0.393
			8	0.0407	0.0620	168.9	3.27	0.343
			9	0.0440	0.0703	169.1	3.42	0.410
			10	0.0409	0.0633	199.7	3.42	0.390
060512a	0.1612	1-tip probe	8	0.0497	0.0745	129.4		0.333
			9	0.0476	0.0783	142.7		0.392
			10	0.0520	0.0735	154.1		0.293
060404a	0.1798	1-tip probe	8	0.0574	0.0795	99.0		0.278
			9	0.0562	0.0865	113.9		0.350
			10	0.0575	0.0845	135.2		0.319

APPENDIX C - FLOW RESISTANCE IN SKIMMING FLOWS

C.1 Presentation

On smooth chutes, the flow resistance is primarily skin friction. Skimming flows over a stepped spillway are characterised by significant form losses. The water skims over the step edges with formation of recirculating vortices between the main stream and the step corners. Form drag is predominant and, as KAZEMIPOUR and APELT (1983) stressed out, the form losses cannot be modelled satisfactorily by a Gauckler-Manning or Darcy-Weisbach formula. Nevertheless this study presents the flow resistance data in terms of an equivalent Darcy friction factor f because it is a dimensionless shear stress that derives from the momentum equation. (¹).

In *uniform equilibrium flows*, the momentum principle states that the boundary friction force equals exactly the gravity force component in the flow direction (HENDERSON 1966, CHANSON 2001a,2004a). That is, the weight of water component acting parallel to the pseudo-bottom formed by the step edges. It yields:

$$\tau_0 * P_W = \rho_W * g * A_W * \sin\theta$$
 Uniform equilibrium (C-1)

where τ_0 is the average shear stress between the skimming flow and recirculating fluid underneath, P_W is the wetted perimeter, ρ_W is the water density, g is the gravity constant, A_W is the water flow cross-section area and θ is the mean bed inclination angle. In dimensionless terms, and for a wide channel, Equation (C-1) becomes :

$$f_{e} = \frac{8 * \tau_{o}}{\rho_{w} * U_{w}^{2}} = \frac{8 * g * \left(\int_{y=0}^{y=Y_{90}} (1 - C) * dy\right) * \sin\theta}{U_{w}^{2}}$$
 Uniform equilibrium (C-2)

where f_e is the Darcy friction factor for air-water flow, C is the local void fraction, y is measured normal to the pseudo-invert formed by the step edges, Y₉₀ is the distance normal to the pseudo-bottom where C = 90% and U_w is the water flow velocity : U_w = q_w/d, q_w is the water discharge per unit discharge and d is the equivalent clear-water depth. The dimensionless shear stress is analogous to the Darcy friction factor (²) but it characterises the form drag loss.

In gradually-varied flows, the average shear stress between the skimming flow and the cavity recirculation are deduced from the friction slope $S_{f_i}(^3)$. For a wide channel the energy equation yields :

$$f_{e} = \frac{8 * \tau_{o}}{\rho_{w} * U_{w}^{2}} = \frac{8 * g * \left(\int_{y=0}^{y=190} (1 - C) * dy\right) * S_{f}}{U_{w}^{2}}$$
Gradually-varied flow (C-3)

where the friction slope equals $S_f = -\partial H/\partial x$, H is the mean total head and x is the curvilinear coordinate along the flow direction. Free-surface aeration is always substantial in prototype and laboratory skimming flows, and its effects must be accounted for using Equations (C-2) to (C-3).

²For a smooth invert chute, the boundary shear stress is defined as : $\tau_0 = f_e * \rho_W * U_W^2 / 8$ (e.g. CHANSON 1999a, p. 74).

¹This approach facilitates further a comparison between smooth and stepped chute data.

¹⁹⁹⁹a, p. 74).

³The friction slope is the slope of the total head line (HENDERSON 1966, CHANSON 1999a,2004a).

In the present study, the air-water flow measurements were performed systematically at step edges downstream of the inception point of free-surface aeration. Uniform equilibrium flow conditions were not achieved at the downstream end of the chute and the flow resistance was calculated using Equation (C-3). Importantly Equation (C-3) gives the equivalent Darcy friction factor in the aerated flow region only. It does not characterise the flow resistance in the clear-water flow region upstream of the inception point (⁴).

C.2 Experimental results

Flow resistance results are given in Table C-1 and Figure C-1. In Figure C-1, the present data are compared with a comprehensive re-analysis of flow resistance in skimming flows for large-size model data (h > 0.020 m, Re > 1E + 5), where Re is the flow Reynolds number defined in terms of the hydraulic diameter D_H (CHANSON et al. 2002, CHANSON 2006b). The flow resistance data are presented in Figure C-1 in terms of the equivalent Darcy friction factor as a function of the dimensionless step roughness height h*cosθ/D_H. Details of experimental technique are given in the caption.

Present flow resistance data are close to past study results in the same facility. In average for five flow rates, the equivalent Darcy friction factor in the present study was $f_e \approx 0.14$ downstream of the inception point of free-surface aeration. Overall, the equivalent Darcy friction factor in skimming flows ranged typically between 0.1 and 0.35 with no obvious correlation with the relative step roughness height, Reynolds, Froude nor Weber numbers (CHANSON et al. 2002, CHANSON 2004c). Experimental data with pressurised intakes tended to exhibit lower flow resistance (CHANSON 2006b).

The friction factor data compared however favourably with a simplified analytical model of the pseudoboundary shear stress which may be expressed in dimensionless form as :

$$f_{d} = \frac{2}{\sqrt{\pi}} * \frac{1}{K}$$
(C-4)

where f_d is an equivalent Darcy friction factor estimate of the form drag, and 1/K is the dimensionless expansion rate of the shear layer. The coefficient 1/K is assumed to be constant in a Prandtl mixing length model (RAJARATNAM 1976, SCHLICHTING 1979). Equation (C-4) predicts $f_d \approx 0.2$ for K = 6 that is close to observed friction factors (Fig. C-1).

⁴AMADOR et al. (2006) derived the flow resistance in the developing boundary layer flow over a stepped chute based upon an integral momentum method. Using PIV measurements, their results yielded f = 0.125 in average for θ = 51.3°, h = 0.05 m, d_c/h = 2.1 and Re = 4.4 E+5.

Table C-1 - Flow resistance in skimming flow (Present study)

Ref.	Qw	d _c /h	Re	f _e	Remarks
	$m^{3/s}$				
(1)	(2)	(3)	(4)	(5)	(6)
060323a	0.0948	1	3.8E+05	0.159	Step edges 6 to 10.
060410a	0.1164	1.15	4.6E+05	0.126	Step edges 7 to 10.
060614a	0.1431	1.33	5.7E+05	0.087	Step edges 7 to 10.
060512a	0.1612	1.45	6.4E+05	0.168	Step edges 8 to 10.
060404a	0.1798	1.57	7.1E+05	0.169	Step edges 8 to 10.

Fig. C-1 - Equivalent Darcy-Weisbach friction factor in air-water skimming flow - Comparison between present data, earlier studies (ANDRE et al. 2003, BaCara 1991, BOES 2000a, CHAMANI and RAJARATNAM 1999, CHANSON and TOOMBES 2001,2002a, GONZALEZ and CHANSON 2004, MATOS 2000, SHVAJNSHTEIN 1999, YASUDA and OHTSU 1999) for large size model data (Re > 1 E+5 and h > 0.02 m), and Equation (C-4)

f	equivalent Darcy friction factor deduced	BaCara (1991), SHVAJNSHTEIN (1999), YASUDA
	from clear-water flow readings	and OHTSU (1999)
fe	equivalent Darcy friction factor in air-	ANDRE et al. (2003), BOES (2000a), CHAMANI and
	water flow deduced from detailed void	RAJARATNAM 1999, CHANSON and TOOMBES
	fraction measurements	(2001,2002a), GONZALEZ and CHANSON (2004),
		MATOS (2000)



APPENDIX D - AIR-WATER FLOW TIME SCALES IN SKIMMING FLOWS ON A STEPPED CHUTE

D.1 Presentation

Air-water flow measurements were performed for a range of experiments. For some runs, two identical phase-detection sensors were recorded simultaneously. In some experiments, the probe sensors were located at the same vertical and streamwise distances y and x respectively, but they were separated in the transverse direction by a known distance Δz . Each single-tip conductivity probe consisted of a sharpened rod (platinum wire $\emptyset = 0.35$ mm) which was insulated except for its tip and set into a metal supporting tube (stainless steel surgical needle $\emptyset = 1.42$ mm) acting as the second electrode. The reference probe was located on the channel centreline. The second probe sensor was separated in the transverse direction by a known spacing Δz .

For other series of experiments, the two sensors were located at the same vertical distance y, but they were separated in the longitudinal direction by a known distance Δx . These experiments were conducted with some dual-tip probe. Each sensor consisted of a sharpened rod (platinum wire $\emptyset = 0.25$ mm) which was insulated except for its tip and set into a metal supporting tube (stainless steel surgical needle $\emptyset = 0.5$ mm (internal) and 0.8 mm (external)). The stainless steel tube acted as the second electrode and it was separated from the inner wire by some insulating epoxy. The longitudinal spacing between probe sensors Δx was measured with a microscope.

The probes were excited by an electronics (UQ82.518) designed with a response time less than 10 ms and calibrated with a square wave generator. Each sensor was scanned at 20 kHz for 45 seconds. Table D-1 summarises the range of investigations. Section D.2 presents the correlation analysis technique. All data sets are regrouped in Sections D3 and D4.

Notation

С	void fraction defined as the volume of air per unit volume of air and water;					
F	air bubble count rate (Hz) defined as the number of detected air bubbles per unit time;					
g	gravity acceleration (m/s ²) : $g = 9.80 \text{ m/s}^2$ in Brisbane (Australia);					
q_W	water discharge per unit width (m ² /s);					
Re	Reynolds number defined in terms of the hydraulic diameter;					
R _{XX}	normalised auto-correlation function (reference probe);					
R _{xy}	normalised cross-correlation function between two probe output signals;					
(R _{xy)max}	maximum cross-correlation between two probe output signals;					
T _{XX}	auto-correlation integral time scale : $\tau = \tau (B_{rmr} = 0)$					
	$T_{XX} = \int_{\tau=0}^{\tau=0} R_{XX}(\tau) * d\tau$					
T _{xy}	cross-correlation integral time scale : $\tau = \tau (R_{xy}=0)$					
	$T_{XY} = \int R_{XY}(\tau) * d\tau$ $\tau = \tau \left(R_{XY} = (R_{XY}) m_{TX} \right)$					
T _{0.5}	characteristic time lag τ for which $R_{XX} = 0.5$;					

V	interfacial velocity (m/s);
W	channel width (m);
У	distance (m) measured normal to the flow direction;
Δx	streamwise separation distance (m) between probe sensors;
Δz	transverse separation distance (m) between probe sensors;
μ	dynamic viscosity (Pa.s);
ρ	density (kg/m ³);
τ	time lag (s);
τ _{0.5}	characteristic time lag τ for which $R_{xy} = 0.5 * (R_{xy})_{max}$;
Ø	diameter (m);

Subscript

XX	auto-correlation of reference probe signal;
xy	cross-correlation;

Table D 1 Ennemine and al	man a a a su a su a da in al sina main a	flame milth identical	mucha anna ana (1	Our a contractor dev)
Table D-L - Experimental	measurements in skimming	tiows with identical	prope sensors ()	Present smay
	measurements in skinning	110 wb whill fuelitieur		1000m bluey
1	Ŭ		•	

q_W	$\frac{d_c}{d_c}$	Re	Instrumentation	Δx	Δz	Step	Comments
2.	h					euge	
m^2/s				mm	mm		
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
0.116	1.15	4.6 E+5	Two single-tip				W = 1.0 m, h = 0.10 m,
			probes				1 = 0.25 m.
				0	8.45	7	Run 060410a.
				0	8.45	8	Run 060410b.
				0	8.45	9	Run 060410c.
				0	3.6	10	Run 060508b.
				0	6.3	10	Run 060412c.
				0	8.45	10	Run 060411a.
				0	10.75	10	Run 060411b.
				0	13.7	10	Run 060411c.
				0	16.7	10	Run 060412a.
				0	21.7	10	Run 060412b.
				0	29.5	10	Run 060413a.
				0	40.3	10	Run 060508a.
0.161	1.45	6.4 E+5	Two single-tip				W = 1.0 m, h = 0.10 m,
			probes				1 = 0.25 m.
				0	8.45	8	Run 060512a.
				0	8.45	9	Run 060512b.
				0	3.6	10	Run 060509a.
				0	8.45	10	Run 060511b.
				0	13.7	10	Run 060509b.
				0	21.7	10	Run 060510a.
				0	40.3	10	Run 060510b.
				0	55.7	10	Run 060511a.
0.116	1.15	4.6 E+5	One dual-tip probe				W = 1.0 m, h = 0.10 m,
							1 = 0.25 m.
				7.0	1.4	10	Run 060530a.

				9.6	1.4	10	Run 060613a.
0.143	1.33	5.7 E+5	One dual-tip probe				
				7.0	1.4	7	Run 060614a.
				7.0	1.4	8	Run 060614b.
				7.0	1.4	9	Run 060615a.
				7.0	1.4	10	Run 060615b.
0.161	1.45	6.4 E+5	One dual-tip probe				W = 1.0 m, h = 0.10 m,
							l = 0.25 m.
				7.0	1.4	10	Run 060530b.
				9.6	1.4	10	Run 060613b.

Notes : d_c : critical flow depth; h : step height; l : step length; Re : Reynolds number defined in terms of the hydraulic diameter; W = channel width.

D.2 Correlation analyses

The probe signals were analysed in terms of the auto-correlation and cross-correlation functions calculated from the raw probe output signals. (Any analysis based upon the thresholded signals, or square-wave signals, tends to ignore the contributions of the smallest air-water particles.) The original signal data of 900,000 samples per sensor were segmented because the periodogram resolution is inversely proportional to the number of samples and it could be biased with large data sets (HAYES 1996, GONZALEZ 2005). All data signals were sub-divided into fifteen non-overlapping segments of 60,000 samples.

Basic results included the maximum cross-correlation coefficient $(R_{xy})_{max}$, and the correlation time scales T_{xx} and T_{xy} where :

$$T_{XX} = \int_{\tau=0}^{\tau=\tau (R_{XX}=0)} R_{XX}(\tau) * d\tau$$
(D-1)

$$T_{XY} = \int_{\tau=\tau (R_{XY}=0)}^{\tau=\tau (R_{XY}=0)} R_{XY}(\tau) * d\tau$$
(D-2)

where R_{XX} is the normalised auto-correlation function, τ is the time lag, and R_{XY} is the normalised crosscorrelation function between the two probe output signals (Fig. D-1). All auto-correlation results are presented for the reference probe sensor : that is, the reference probe on the channel centreline (z = 0) or the leading tip.

Discussion

Auto- and cross-correlation calculations were most successful for $0.05 \le C \le 0.95$. In the upper spray region $(C \ge 0.90 \text{ to } 0.95)$ and at some other locations, the calculations were unsuccessful for a number of reasons. These included flat cross-correlation functions without a distinctive peak, non-crossing of the correlation function(s) with the zero line, correlation functions with several peaks, meaningless correlation trends ... Such data points are indicated with (--) in the following tables of results.

While most correlation calculations can be automated, it must be stressed that human intervention are essential to validate each calculation step. Herein all calculations were performed by hand and all meaningless results were rejected.

Fig. D-1 - Auto- and cross-correlation functions for two identical phase-detection probes separated by a known distance Y - Definition sketches



D.3 Experimental results in terms of transverse separation Δz

D.3.1 Experimental results for $d_c/h = 1.15$

Location :	The University of Queensland (Australia)
Date :	April-June 2006
Experiments by :	G. CAROSI
Data processing by:	G. CAROSI and H. CHANSON
Data analysis by :	H. CHANSON and G. CAROSI
Experiment	Channel: width: 1.0 m, slope: 21.8°, h = 0.10 m, l = 0.25 m, 10 identical
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood
	staircase invert.
	$Q_w = 0.1164 \text{ m}^3/\text{s}, d_c = 0.115 \text{ m}, \text{Re} = 4.6 \text{ E}+5$
Instrumentation :	Two single-tip conductivity probe ($\emptyset = 0.35$ mm). Transverse separation
	distance Δz .
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.

Comments :	Inflow conditions : broad-crested weir.
	Inception of free-surface aeration: between step edges 6 and 7.
	Correlation analyses performed on fifteen segments of 60,000 samples.

D.3.1.1 Step edge 7

Δz	У	С	F	T _{XX}	(R _{xy}) _{max}	T _{xy}
mm	mm		Hz	sec.		sec.
8.45	1.5	0.023	41.2	0.001138	0.039598	0.000253
	6.5	0.039	54.2	0.001846	0.029276	0.000241
	11.5	0.045	55.9	0.001549	0.069302	0.000342
	12.5	0.046	57	0.001642	0.056696	0.000204
	13.5	0.047	58.7	0.001415	0.054021	0.000244
	16.5	0.058	63.2	0.001674	0.095058	0.000435
	19.5	0.078	75.2	0.001915	0.117507	0.000176
	21.5	0.086	82.3	0.001985	0.153981	0.000974
	26.5	0.173	118	0.003083	0.237158	0.001573
	31.5	0.286	147.9	0.003673	0.30839	0.002397
	36.5	0.427	161.9	0.004054	0.329295	0.002663
	41.5	0.573	150	0.003812	0.336687	0.002424
	46.5	0.687	130.8	0.003557	0.323703	0.002274
	51.5	0.759	106.8	0.003311	0.299907	0.001678
	56.5	0.791	90.4	0.003068	0.286926	0.00165
	61.5	0.833	75.4	0.003052	0.277592	0.001372
	66.5	0.866	62.9	0.003162	0.253003	0.001436
	71.5	0.886	55.8	0.00305	0.262698	0.001448
	76.5	0.907	47.5	0.002923	0.235481	0.001212
	81.5	0.926	38.2	0.003063	0.250306	0.001333
	86.5	0.932	35.4	0.00292	0.24193	0.001135
	91.5	0.94	32	0.003033	0.219811	0.001172
	96.5	0.96	23.1	0.002899	0.213702	0.000897
	101.5	0.966	19.7	0.002779	0.206452	0.001104
	106.5	0.971	16.4	0.003116	0.210604	0.00102
	111.5	0.98	11.8	0.002879	0.175065	0.000594
	116.5	0.986	8.7	0.003167	0.18069	0.001245
	121.5	0.986	8.6	0.003087	0.195403	0.001037
	126.5	0.987	7.5	0.003379	0.197714	0.001102
	131.5	0.991	5.3	0.003628	0.166628	0.001249
	131.5	0.993	4.2	0.004918	0.144221	0.000868
	136.5	0.994	3.9	0.005275	0.177924	0.000784
	141.5	0.995	3.3	0.00705	0.180191	0.001755
	146.5	0.995	3.1	0.007349	0.13411	0.000849

Notes : Blue italic : s	uspicious data;	Red Bold :	possibly incorrect	t data; () :	meaningless data.
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D.3.1.2 Step edge 8

Δz	У	С	F	T _{XX}	$(R_{xy})_{max}$	T _{xy}
mm	mm		Hz	sec.		sec.
8.45	1.5	0.01	28			
	6.5	0.022	43.8			
	9.5	0.031	53.7	0.000208	0.034112	0.000231

11.5	0.03	53.2	0.000649	0.023608	0.000157
13.5	0.033	56.8	0.000782	0.040429	0.000209
16.5	0.036	56.7	0.000659	0.043847	0.000201
19.5	0.039	59.3	0.000613	0.040833	0.000167
21.5	0.044	63.8	0.000701	0.070214	0.000354
26.5	0.069	82.5	0.001139	0.120278	0.000667
31.5	0.129	116.2	0.00222	0.208081	0.001601
36.5	0.226	151.1	0.002786	0.310492	0.002545
41.5	0.452	177.8	0.003388	0.368183	0.003352
46.5	0.574	173.2	0.003074	0.379823	0.003282
51.5	0.699	138.5	0.003456	0.386382	0.003325
56.5	0.815	99.1	0.002638	0.334799	0.002593
61.5	0.879	68.1	0.002269	0.301261	0.002009
66.5	0.915	49.9	0.001174	0.269959	0.001773
71.5	0.93	41	0.001883	0.242849	0.001522
76.5	0.95	29.7	0.00209	0.234915	0.001435
81.5	0.959	24.7	0.001704	0.218581	0.00113
86.5	0.965	20.7	0.001757	0.186307	0.001077
91.5	0.978	14.7	0.001775	0.199186	0.001085
96.5	0.98	13	0.000269	0.192624	0.000906
101.5	0.986	8.9	0.000403	0.190426	0.0007
106.5	0.989	7.3	0.001585	0.128367	0.000632
111.5	0.99	6.1	0.001759	0.146703	0.000656
116.5	0.992	5.6	0.001715	0.165646	0.000638
121.5	0.995	3.9	0.001724	0.118605	0.000283
126.5	0.996	3.1	0.001697	0.11617	0.000433
131.5	0.996	3.1	0.001986	0.179758	0.000566
131.5	0.997	2	0.002152	0.136295	0.000478
136.5	0.998	1.7	0.001923	0.117221	0.000476
141.5	0.998	1.8	0.002144	0.147577	0.000871
146.5	0.998	1.4	0.003138	0.073672	0.000159
151.5	0.999	0.7			

D.3.1.3 Step edge 9

Δz	У	С	F	T _{XX}	$(R_{xy})_{max}$	T _{xy}
mm	mm		Hz	sec.		sec.
8.45	1.5	0.032	57.6	0.00119	0.032832	0.000238
	6.5	0.037	62.4	0.001199	0.035902	0.00026
	9.5	0.044	64.8	0.001195	0.051598	0.000324
	11.5	0.049	70.5	0.001038	0.062925	0.000441
	16.5	0.056	74.2	0.000286	0.095865	0.00047
	19.5	0.069	83.9	0.001248	0.123403	0.000611
	20.5	0.072	82.5	0.001213	0.136883	0.000639
	21.5	0.081	90.4	0.001336	0.154601	0.001
	26.5	0.132	115	0.002067	0.233391	0.001449
	31.5	0.226	149.4	0.002878	0.330521	0.002659
	36.5	0.373	177.8	0.003327	0.381587	0.003342
	41.5	0.524	165.7	0.003248	0.416467	0.003498
	46.5	0.662	142.4	0.00266	0.363789	0.002655
	51.5	0.768	109.2	0.002191	0.331338	0.002129
	56.5	0.825	90.7	0.002037	0.330177	0.001862

56.5	0.867	71.2	0.002086	0.314084	0.001793
61.5	0.887	61.3	0.001857	0.29519	0.001563
66.5	0.917	48.3	0.001823	0.274568	0.001479
71.5	0.9487	33.2	0.002001	0.263716	0.001391
76.5	0.957	28.6	0.001852	0.273583	0.001529
81.5	0.968	21.5	0.002099	0.239386	0.001461
86.5	0.977	16.6	0.003849	0.237739	0.00106
91.5	0.976	16.6	0.001787	0.220008	0.001217
96.5	0.985	12	0.001936	0.21219	0.001134
101.5	0.986	11	0.001738	0.165755	0.000668
111.5	0.99	7.1	0.001826	0.17029	0.001009
116.5	0.993	5.6	0.001817	0.15927	0.000758
121.5	0.995	4.1	0.002268	0.196018	0.00052
126.5	0.996	3.5	0.00227	0.158337	0.000524
131.5	0.996	2.9	0.00245	0.140632	0.000692
131.5	0.997	2.4	0.002111	0.142107	0.000674
136.5	0.998	1.6	0.004578	0.149602	0.000383
141.5	0.999	1.4	0.003469	0.132007	0.000504
146.5	0.999	0.8	0.006519	0.154553	0.000953

D.3.1.4 Step edge 10

Δz	У	С	F	(R _{xy}) _{max}	T _{xy}
mm	mm		Hz	•	sec.
3.6	2	0.03	57.5	0.158185	0.000623
	7	0.031	55.7	0.169267	0.000544
	10	0.04	65.2	0.195803	0.000575
	12	0.035	56.8	0.192472	0.000535
	14	0.043	66.7	0.221972	0.000619
	17	0.057	77.8	0.28246	0.0009
	20	0.095	105.5	0.389683	0.001726
	22	0.114	117.2	0.41402	0.00203
	27	0.169	135.8	0.506588	0.003035
	32	0.34	184.1	0.592643	0.004291
	37	0.514	185.1	0.627345	0.005006
	42	0.68	152.9	0.633925	0.004395
	47	0.785	108.6	0.628892	0.003962
	52	0.847	84.3	0.611512	0.003464
	57	0.896	60.4	0.594158	0.003121
	62	0.927	47.3	0.577221	0.002622
	67	0.935	37.8	0.570193	0.002765
	72	0.953	30.4	0.554563	0.002443
	77	0.967	23.9	0.524584	0.002076
	82	0.973	18.8	0.534248	0.00209
	87	0.981	14.8	0.512693	0.002453
	92	0.984	12.4	0.520675	0.001963
	97	0.988	9.1	0.53526	0.002453
	102	0.993	4.6	0.469976	0.002065
	107	0.993	6.6	0.483538	0.001812
	112	0.995	5	0.470599	0.001946
	117	0.995	4.3	0.461753	0.00213
	122	0.997	2.5	0.470253	0.002171
	127	0.998	1.8	0.586978	0.002436
	132	0.999	1.3	0.448505	0.002174

132	0.999	0.7	0.292012	0.002121
137	0.999	0.9	0.318358	0.00211
142	0.999	0.9	0.41464	0.00213
147	0.999	1	0.28518	0.001851
152	1	0.5		

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

Δz	У	С	F	$(R_{xy})_{max}$	T _{xy}
mm	mm		Hz	•	sec.
6.2	2	0.043	79.8	0.033749	0.000212
	7	0.043	78.9	0.028173	8.18E-05
	10	0.051	86	0.039177	0.000162
	12	0.051	87.3	0.050949	0.000175
	14	0.051	85.5	0.048991	0.000149
	17	0.062	95.2	0.070501	0.0003
	20	0.069	102	0.085866	0.000257
	22	0.082	110.1	0.105475	0.000498
	27	0.109	130.7	0.186996	0.000932
	32	0.192	168	0.308611	0.002095
	37	0.403	177.8	0.412795	0.003394
	42	0.572	177.8	0.448469	0.003728
	47	0.709	159.9	0.450443	0.003289
	52	0.816	114.1	0.432183	0.003001
	57	0.867	86.9	0.351419	0.00212
	62	0.917	57.1	0.334977	0.001803
	67	0.94	43.5	0.299723	0.001511
	72	0.949	35.2	0.261851	0.001031
	77	0.966	26.3	0.267562	0.000938
	82	0.974	21	0.261579	0.001028
	87	0.976	17.7	0.270546	0.000816
	92	0.983	14	0.241304	0.0007
	97	0.987	11.1	0.222471	0.000446
	102	0.989	8.6	0.205582	0.000814
	107	0.992	6.6	0.221689	0.000576
	112	0.994	5.1	0.208606	0.000609
	117	0.996	3.4	0.16207	0.000261
	122	0.996	3.8	0.179831	0.000295
	127	0.997	2.4	0.216852	0.000415
	132	0.997	2.8	0.19021	0.000531
	137	0.998	1.6	0.184822	0.000587
	142	0.998	1.8	0.157231	0.000363
	147	0.999	1.4	0.111714	0.000624
	152	0.999	1.2	0.134326	0.000314
	157	0.999	0.9	0.086934	0.000406

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

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-	Δz	У	С	F	T _{XX}	$(R_{xy})_{max}$	T _{xy}
_	mm	mm		Hz	sec.		sec.
-	8.45	2	0.021	47.8			
		7	0.035	68.2			
		10	0.039	71	0.001195	0.039862	0.000229
		12	0.041	71.8	0.001118	0.030559	0.000187
		14	0.044	69.3	0.001152	0.058069	0.00027
		17	0.045	76.9	0.001026	0.059802	0.000193
		20	0.054	82.3	0.001288	0.082879	0.000485

22	0.069	94.9	0.001464	0.089351	0.000489
27	0.106	122.8	0.001941	0.181247	0.000905
37	0.327	194.9	0.004205	0.412343	0.003858
42	0.515	194	0.005275	0.429348	0.003828
47	0.636	171.6	0.004955	0.378996	0.002849
52	0.798	120.3	0.004118	0.38045	0.002845
57	0.874	79.4	0.004168	0.319106	0.001836
62	0.91	56.5	0.003405	0.289437	0.00151
67	0.933	44	0.003277	0.260788	0.001279
72	0.955	32.5	0.002721	0.255749	0.001394
77	0.961	28.2	0.002943	0.247855	0.001266
82	0.965	22.4	0.002852	0.227229	0.001105
87	0.973	20.5	0.002716	0.186716	0.000806
92	0.981	16.7	0.002562	0.171111	0.000898
97	0.987	11.2	0.002792	0.169898	0.000836
102	0.988	10.1	0.002695	0.145445	0.000876
107	0.993	4.8	0.002972	0.120924	0.000601
112	0.993	6.4	0.002814	0.159079	0.000688
117	0.996	3.7	0.002881	0.131298	0.000663
122	0.995	3.6	0.002801	0.147952	0.000579
127	0.997	2.9	0.003264	0.13718	0.000777
132	0.998	2.3	0.003805	0.116257	0.00063
132	0.999	1.4	0.005658		
137	0.998	1.2	0.006233	0.122243	0.00051
142	0.998	1.9	0.006948	0.15187	0.000741
147	0.999	1.4	0.006659	0.081157	0.000503
152	0.999	1.2	0.007154	0.099427	0.000182

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

Δz	У	С	F	$(R_{xy})_{max}$	T _{xy}
mm	mm		Hz	-	sec.
10.75	2	0.033	65.6		
	7	0.041	77.9		
	10	0.052	84.1	0.021898	5.35E-05
	12	0.052	85.3	0.025106	0.000138
	14	0.059	94.3	0.033983	0.000129
	17	0.064	95.6	0.057365	0.000226
	22	0.083	111.3	0.088022	0.000476
	27	0.14	142.4	0.211847	0.00157
	32	0.263	185.3	0.282966	0.002924
	37	0.435	209.1	0.360338	0.003583
	42	0.594	185.5	0.391415	0.003846
	47	0.733	152.8	0.346699	0.003111
	52	0.836	100.3	0.313994	0.002342
	57	0.881	74.6	0.277629	0.002027
	62	0.912	60.1	0.249525	0.001576
	67	0.939	44.9	0.221428	0.00147
	72	0.955	33.7	0.185232	0.001335
	77	0.965	26.2	0.146827	0.000896
	82	0.974	21.8	0.190872	0.000958
	87	0.977	17.5	0.163553	0.0009
	92	0.981	15.1	0.151483	0.000735
	97	0.984	12.7	0.133015	0.000828
	102	0.988	9.9	0.12937	0.000551
	107	0.991	7.3	0.115336	0.000354
	112	0.994	5.1	0.101391	0.000484
	117	0.995	4.3	0.11032	0.000685
	122	0.996	3.5	0.093171	0.000377

127 0.996 3.5 0.0933	375
132 0.997 2.5 0.1314	413 <i>0.000556</i>
137 0.998 1.7 0.0834	488 <i>0.000301</i>
142 0.998 1.8 0.0924	421 5.2E-05
147 0.998 1.4 0.0410	026 0.000172
152 0.999 1.3 0.0564	421 <i>0.000313</i>
157 0.999 1.1 0.0288	316 3.37E-05

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

Δz	У	С	F	$(R_{xy})_{max}$	T _{xy}
mm	mm		Hz		sec.
13.7	2	0.033	68.7		
	7	0.049	86.3		
	10	0.05	85.3		
	12	0.049	82.2	0.014551	4.74E-05
	14	0.067	102.3	0.033448	0.000217
	17	0.077	104.4	0.048978	0.000291
	20	0.085	112.6	0.040326	0.000268
	22	0.086	111.9	0.060137	0.000549
	27	0.145	146.1	0.135366	0.001174
	32	0.224	184	0.207485	0.001928
	37	0.458	210.4	0.317194	0.003819
	42	0.654	175.1	0.30809	0.004105
	47	0.762	134.7	0.293931	0.003181
	52	0.853	93.8	0.238829	0.002102
	57	0.897	67.8	0.215513	0.001966
	62	0.928	51	0.161563	0.001037
	67	0.937	42.7	0.151676	0.001166
	72	0.958	32.2	0.103897	0.000741
	77	0.964	28.1	0.109676	0.000772
	82	0.974	21.7	0.10755	0.000577
	87	0.981	15.2	0.095628	0.000766
	92	0.983	13.1	0.093721	0.000526
	97	0.988	9.6	0.057554	0.000485
	102	0.992	7.8	0.074179	0.000268
	107	0.99	7.3	0.058817	0.000477
	112	0.993	5.8	0.054683	0.000551
	117	0.993	5.3	0.073196	0.000419
	122	0.995	4.6	0.034342	0.000228
	127	0.998	2	0.077217	0.000956
	132	0.997	2.2	0.052943	0.000123
	137	0.998	1.9		
	142	0.999	1.3	0.045236	0.000613
	147	0.998	1.6	0.029252	3.14E-05
	152	0.999	1.2	0.034407	5.69E-05
	157	0.999	0.8	0.053532	0.000184

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

Δz	У	С	F	$(R_{xy})_{max}$	T _{xy}
mm	mm		Hz		sec.
16.7	2	0.02	38.5		
	7	0.023	43.1		
	10	0.025	42.7		
	12	0.028	46.6		
	14	0.033	52		

17	0.038	58.2		
20	0.053	69.6	0.041741	0.000291
22	0.059	72.7	0.046857	0.000272
27	0.12	112.8	0.138677	0.001544
32	0.245	154.7	0.256048	0.003016
37	0.396	172.7	0.316665	0.003796
42	0.58	163.4	0.321489	0.00377
47	0.732	123.4	0.304742	0.00391
52	0.817	92.4	0.262547	0.002709
57	0.863	71.6	0.218607	0.00235
62	0.898	56.1	0.179784	0.001455
67	0.928	42.1	0.16047	0.001586
72	0.942	34.3	0.15877	0.001728
77	0.959	27.7	0.120136	0.001317
82	0.966	22.4	0.112714	0.001541
87	0.977	15.4	0.10188	0.00136
92	0.979	14.7	0.078795	0.00097
97	0.982	12.5	0.078795	0.00097
102	0.986	10	0.086232	0.00087
107	0.991	7	0.072424	0.000554
112	0.993	5.6	0.046026	0.000509
117	0.994	4.4		
122	0.995	3.8	0.046218	0.000513
127	0.997	2.7		
132	0.997	2.9	0.062121	0.000424
137	0.998	1.5	0.048318	0.000533
142	0.998	1.8		8.6E-05
147	0.999	1.4		
152	0.999	0.9		
157	0.999	0.8		

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

Δz	У	С	F	$(R_{xy})_{max}$	T _{xy}
mm	mm		Hz		sec.
21.7	2	0.032	71		
	7	0.043	78		
	10	0.046	81.5		
	12	0.052	88.8		
	14	0.054	87.6		
	17	0.06	93.6		
	20	0.074	104.9		
	22	0.076	107.4	0.03327	0.000239
	27	0.125	140.9	0.069534	0.000691
	32	0.218	177.8	0.136396	0.001511
	37	0.47	177.8	0.212364	0.00268
	42	0.605	177.8	0.239136	0.00268
	47	0.707	159.5	0.217778	0.002469
	52	0.82	116.2	0.199857	0.002336
	57	0.887	79.1	0.151437	0.001636
	62	0.913	60.5	0.126211	0.00136
	67	0.934	47.5	0.085117	0.001017
	72	0.952	35.3	0.073861	0.000872
	77	0.963	28.6	0.083064	0.000703
	82	0.969	24.9	0.076541	0.000725
	87	0.974	20	0.064038	0.000474
	92	0.983	14	0.036482	0.000222
	97	0.987	11.2	0.049278	0.000587
	102	0.988	9.7	0.032742	0.00029

107	0.992	6.8	0.02762	0.000161
112	0.992	6.6	0.031273	0.000142
117	0.995	4.4	0.034354	0.000135
122	0.997	2.8		
127	0.997	2.5	0.03471	0.000193
132	0.997	2.4	0.033649	0.000191
137	0.998	2		
142	0.998	1.4		
147	0.999	1.1		
152	0.999	1.1		
157	0.999	0.7		

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

Δz	У	С	F	$(R_{xy})_{max}$	T _{xy}
mm	mm		Hz	-	sec.
29.5	2	0.023	0.2		
	7	0.034	66.2		
	10	0.043	76.2		
	12	0.039	72		
	14	0.045	75.4		
	17	0.052	83		
	20	0.06	89		
	22	0.067	96.5		
	27	0.114	127.9	0.053267	0.000534
	32	0.188	161.2	0.124866	0.001614
	37	0.387	177.8	0.154782	0.001892
	47	0.667	167.6	0.181993	0.002346
	52	0.796	118.3	0.156013	0.00183
	57	0.872	78.8	0.117262	0.001203
	62	0.908	59.5	0.075743	0.000959
	67	0.929	46.1	0.073171	0.000797
	72	0.949	35.8		
	77	0.963	26.3		
	82	0.967	24.6	0.043878	0.000461
	87	0.979	16.2		
	92	0.982	14.4		
	97	0.986	11.4		
	102	0.988	9.7		
	107	0.992	7.4		
	112	0.994	5.2		
	117	0.995	4.6		
	122	0.997	2.9		
	127	0.996	3.6		
	132	0.997	2.4		
	137		1.8		
	147	0.999	1.1		
	152	0.999	0.8		
-	157	0.999	0.8		

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

Δz	у	С	F	(R _{xy}) _{max}	T _{xy}
mm	mm		Hz		sec.
40.2	22				
40.3	22	0.071	91.6		
40.3	22 27	0.071 0.127	91.6 121	 0.051034	0.000391

37	0.351	177.8	0.142367	0.001731
42	0.515	177.8	0.122922	0.001418
47	0.664	154.3	0.151645	0.002296
52	0.8	104.2	0.081088	0.001323
57	0.861	79.4	0.076761	0.00112
62	0.897	60.5	0.048962	0.000267
67	0.926	44	0.048503	0.000506
72	0.949	33.6		
77	0.954	30.2	0.022588	0.000148
82	0.967	23.2		

D.3.2 Experimental results for $d_{C}/h = 1.45$

Location :	The University of Queensland (Australia)
Date :	April-June 2006
Experiments by :	G. CAROSI
Data processing by:	G. CAROSI and H. CHANSON
Data analysis by :	H. CHANSON and G. CAROSI
Experiment	Channel: width: 1.0 m, slope: 21.8° , h = 0.10 m, 1 = 0.25 m, 10 identical
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood
	staircase invert.
	$Q_w = 0.1612 \text{ m}^3/\text{s}, d_c = 0.145 \text{ m}, \text{Re} = 6.4 \text{ E}+5$
Instrumentation :	Two single-tip conductivity probe ($\emptyset = 0.35$ mm). Transverse separation
	distance Δz .
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.
Comments :	Inflow conditions : broad-crested weir.
	Inception of free-surface aeration: between step edges 7 and 8.
	Correlation analyses performed on fifteen segments of 60,000 samples.

D.3.2.1 Step edge 8

Δz	у	С	F	T _{XX}	(R _{xy}) _{max}	T _{xy}
mm	mm		Hz	sec.		sec.
8.45	1.5	0.001	3.2	0.000355		
	6.5	0.003	6.1	0.000449		
	9.5	0.004	7.5	0.000719		
	11.5	0.003	6.5	0.000394		
	13.5	0.006	10	0.001692		
	16.5	0.005	9	0.00053		
	19.5	0.007	11.8	0.00052	0.049273	0.000152
	21.5	0.009	13	0.000564	0.062959	0.000252
	26.5	0.013	16.7	0.000826	0.065619	0.000384
	31.5	0.027	27.4	0.001493	0.15587	0.000976
	36.5	0.068	48.6	0.002414	0.274678	0.002043
	41.5	0.171	84.6	0.003218	0.376068	0.003083
	46.5	0.345	121	0.003697	0.435922	0.003958
	51.5	0.512	129.4	0.003804	0.448027	0.004165
	56.5	0.669	119.1	0.003628	0.413605	0.003561
	61.5	0.799	86	0.00294	0.35245	0.002494
	66.5	0.852	70.4	0.002696	0.317522	0.002255
	71.5	0.889	56.5	0.002519	0.300835	0.002014
	76.5	0.907	46.9	0.002458	0.287712	0.00175

81.5	0.93	37.4	0.002679	0.263545	0.00178
86.5	0.949	28.1	0.002778	0.273884	0.001706
91.5	0.959	24.3	0.002606	0.233332	0.001625
96.5	0.956	25.3	0.00232	0.236056	0.001544
101.5	0.972	17.3	0.002129	0.201313	0.001205
106.5	0.976	14.3	0.002026	0.245969	0.00126
111.5	0.983	10.7	0.002387	0.216309	0.001179
116.5	0.985	10.2	0.001975	0.181623	0.000726
121.5	0.99	6.8	0.002135	0.148415	0.000785
126.5	0.992	6.4	0.002206	0.136806	0.001137
131.5	0.991	6.5	0.00209	0.169506	0.000807
131.5	0.994	4	0.002507	0.145739	0.000791
136.5	0.995	3.3	0.002394	0.128645	0.000581
141.5	0.997	2.7	0.002336	0.116997	0.000625
146.5	0.997	2.1	0.002589	0.093473	0.000716

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

D.3.2.2 Step edge 9

Δz	У	С	F	T _{XX}	$(R_{xy})_{max}$	T _{xy}
mm	mm		Hz	sec.	-	sec.
8.45	1.5	0.013	26.3	0.000739		
	6.5	0.025	38.4	0.001162	0.058648	0.000243
	9.5	0.027	37.8	0.00164	0.050659	0.000332
	11.5	0.031	39.9	0.00141	0.088398	0.000734
	13.5	0.031	39.5	0.00143	0.082299	0.000636
	16.5	0.038	44.5	0.001561	0.085998	0.000542
	19.5	0.037	43.8	0.001423	0.105406	0.000737
	21.5	0.042	45.8	0.001348	0.16899	0.001022
	26.5	0.059	55.6	0.001273	0.099872	0.000665
	31.5	0.091	72.7	0.001827	0.241151	0.00153
	36.5	0.159	100.5	0.00261	0.33251	0.002629
	41.5	0.276	131.6	0.003136	0.388097	0.003264
	46.5	0.411	142.7	0.003658	0.433142	0.003926
	51.5	0.562	135	0.00345	0.429691	0.003558
	56.5	0.666	117.8	0.002735	0.424157	0.003068
	61.5	0.753	100.5	0.002858	0.375266	0.002748
	66.5	0.811	82.9	0.00271	0.358838	0.002332
	71.5	0.858	67.2	0.002139	0.341548	0.001995
	76.5	0.886	54.3	0.002244	0.324843	0.001907
	81.5	0.917	45.8	0.002118	0.279371	0.001516
	86.5	0.929	38.1	0.002274	0.304788	0.001785
	91.5	0.943	31.7	0.002381	0.270212	0.001672
	96.5	0.963	23.6	0.002049	0.224755	0.00117
	101.5	0.97	19.4	0.002296	0.229541	0.001248
	106.5	0.98	14	0.002138	0.213727	0.001179
	111.5	0.98	13.6	0.002381	0.223751	0.001224
	116.5	0.983	11.8	0.001986	0.174763	0.000823
	121.5	0.988	8.3	0.002402	0.198373	0.001089
	126.5	0.99	7	0.002303	0.209296	0.001029
	131.5	0.991	6.2	0.002277	0.167164	0.000316
	131.5	0.994	4.2	0.002173	0.158214	0.000749
	136.5	0.996	2.6	0.002487	0.126307	0.000498
	141.5	0.997	3	0.002634	0.121011	0.000322
	146.5	0.997	2.2	0.002734	0.103776	0.000414

D.3.2.3 Step edge 10

Δz	у	С	F	$(R_{xy})_{max}$	T _{xy}
mm	mm		Hz	•	sec.
3.6	2	0.022	39.9	0.099504	0.000453
	7	0.018	33.7	0.101896	0.000283
	10	0.022	35.6	0.15787	0.000452
	12	0.025	40.9	0.190176	0.00069
	14	0.027	41.5	0.188603	0.00039
	17	0.029	44	0.209376	0.000605
	20	0.03	43.7	0.262669	0.000692
	22	0.038	49.3	0.284375	0.001091
	27	0.061	63.3	0.373629	0.001835
	32	0.106	87.9	0.484859	0.002877
	37	0.192	120.2	0.567565	0.003831
	42	0.356	145.9	0.649016	0.004683
	47	0.521	154.8	0.649348	0.004816
	52	0.66	137.8	0.643395	0.004075
	57	0.748	114.4	0.6313	0.003712
	62	0.808	97.6	0.621748	0.003143
	67	0.859	75	0.595864	0.003134
	72	0.905	56.4	0.590193	0.002729
	77	0.932	42.4	0.573615	0.002295
	82	0.941	38.8	0.545173	0.00222
	87	0.958	28.5	0.531459	0.001821
	92	0.964	24.5	0.532311	0.002492
	97	0.976	17.7	0.523779	0.001686
	102	0.98	15.1	0.514571	0.00176
	107	0.986	11.3	0.483799	0.001588
	112	0.988	8.9	0.454517	0.001527
	117	0.991	6.7	0.498068	0.001631
	122	0.992	5.8	0.494381	0.001397
	127	0.996	3.2	0.450932	0.001078
	132	0.996	3	0.485283	0.001188
	132	0.997	2.8	0.411066	0.001293
	137	0.998	2.3	0.315081	0.000917
	142	0.998	1.7	0.375474	0.000967
	147	0.999	1.6	0.347041	0.000727
	152	0.999	1.2	0.372967	0.000773

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

Δz	У	С	F	T _{XX}	(R _{xy}) _{max}	T _{xy}
mm	mm		Hz	sec.		sec.
8.45	2	0.008	20.8	0.000853		
	7	0.012	27.9	0.00078		
	10	0.015	30.2	0.000973	0.025536	4.93E-05
	12	0.013	25.6	0.001131	0.023117	6.72E-05
	14	0.017	31.2	0.000982	0.043561	0.000248
	17	0.018	32.8	0.000969	0.032841	0.000206
	20	0.025	37.5	0.001233	0.065581	0.000239
	22	0.024	37.5	0.001184	0.093218	0.000368
	27	0.03	43.7	0.001351	0.081444	0.000332
	32	0.055	61.7	0.002243	0.183291	0.001153

37	0.092	81.6	0.002956	0.255018	0.001668
42	0.211	130.5	0.004463	0.390404	0.003162
47	0.306	147.4	0.005319	0.448788	0.004126
52	0.536	157.9	0.005057	0.455203	0.003983
57	0.655	137.6	0.005516	0.468004	0.004079
62	0.775	107.2	0.004919	0.436758	0.003763
67	0.858	76.4	0.004069	0.361126	0.002426
72	0.904	54.3	0.003816	0.345901	0.002217
77	0.927	43.1	0.00375	0.296393	0.001831
82	0.94	35.8	0.003863	0.292538	0.001744
87	0.962	24.7	0.003537	0.270508	0.001566
92	0.969	19.8	0.003358	0.25594	0.001295
97	0.977	16	0.003036	0.232306	0.001247
102	0.981	13.2	0.003242	0.217154	0.001137
107	0.987	9.8	0.002833	0.170989	0.0011
112	0.99	7.8	0.002983	0.210569	0.00094
117	0.992	6.2	0.003028	0.186865	0.000693
122	0.994	4.8	0.00328	0.18043	0.000513
127	0.996	3.4	0.00333	0.115671	0.00069
132	0.997	2.7	0.003568	0.106955	0.000575
132	0.997	2.2	0.003715	0.136502	0.000928
137	0.997	2.1	0.005863	0.147605	0.001263
142	0.998	1.8	0.003762	0.126155	0.000693
147	0.998	1.6	0.005294	0.099393	0.000331
152	0.999	1.1	0.005855	0.075653	0.000445

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

Δz	У	С	F	(R _{xy}) _{max}	T _{xy}
mm	mm		Hz		sec.
13.7	2	0.009	21.2		
	7	0.014	28.1		
	10	0.018	34.7		
	12	0.017	33.8		
	14	0.02	36.6		
	17	0.023	38.4		
	20	0.023	38.8		
	22	0.03	44.4		
	27	0.037	49.6		
	32	0.046	56.5	0.068875	0.000515
	37	0.119	98.2	0.184595	0.001805
	42	0.186	119.7	0.251277	0.002627
	47	0.358	159.3	0.341293	0.00427
	52	0.519	156.8	0.37	0.004411
	57	0.666	136.2	0.352815	0.003769
	62	0.774	107.9	0.285568	0.002928
	67	0.85	82.7	0.240592	0.002551
	72	0.876	67.5	0.206681	0.001853
	77	0.908	53.3	0.19846	0.001881
	82	0.935	39.4	0.171901	0.001548
	87	0.95	31	0.154642	0.001509
	92	0.961	26.3	0.112389	0.001005
	97	0.972	19.6	0.101666	0.000805
	102	0.978	15.7	0.091734	0.000554
	107	0.983	12.5	0.089973	0.000952
	112	0.985	10.8	0.083816	0.000816
	117	0.988	9.1	0.074718	0.000659
	122	0.992	6.3	0.069384	0.00049
	127	0.994	4.7	0.068335	0.000322

132	0.996	3.1	0.062823	0.00033
132	0.996	3.6	0.053583	0.000217
137	0.998	2		
142	0.997	2.1		
147	0.998	1.9	0.042303	4.25E-05
152	0.998	1.4		

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

Δz	У	С	F	(R _{xy}) _{max}	T _{xy}
mm	mm		Hz	-	sec.
21.7	2	0.004	11		
	7	0.01	22.3		
	10	0.013	25.8		
	12	0.012	24		
	14	0.012	24		
	17	0.014	28.1		
	20	0.015	27.8		
	22	0.016	29.7		
	27	0.023	35.1		
	32	0.033	42.1		
	37	0.06	62.2	0.083233	0.000908
	42	0.108	85.2	0.130063	0.001258
	47	0.222	127	0.208383	0.002712
	52	0.396	155.5	0.255555	0.003356
	57	0.532	147.2	0.284473	0.003956
	62	0.704	124.3	0.246368	0.003282
	67	0.795	95.2	0.245163	0.003001
	72	0.866	66.9	0.199363	0.002385
	77	0.916	47.6	0.143855	0.001732
	82	0.926	43.4	0.13481	0.001324
	87	0.947	31.7	0.109588	0.001149
	92	0.965	22.7	0.095288	0.001036
	97	0.969	20.3	0.077942	0.000743
	102	0.978	15.3		
	107	0.984	11.9	0.062037	0.000633
	112	0.989	8.2	0.051796	0.000525
	117	0.989	8.3		
	122	0.992	5.8	0.040173	0.000233
	127	0.993	5	0.045095	0.000442
	132	0.996	3.5	0.022657	0.000107
	132	0.996	3	0.040402	5.24E-05
	137	0.996	2.7		
	142	0.998	1.8	0.046693	0.000113
	147	0.998	1.6	0.020593	2.43E-05
	152	0.999	1.4	0.045742	8.29E-05

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

Δz	У	С	F	(R _{xy}) _{max}	T _{xy}
mm	mm		Hz		sec.
40.3	22	0.022	34		
	27	0.025	37.1		
	32	0.048	55.7	0.030402	0.000104
	37	0.096	79.9		
	42	0.156	104.5	0.087065	0.001302
	47	0.312	143.2	0.140587	0.001975

50	0 502	156.2	0 141711	0.001722
52	0.302	130.2	0.141/11	0.001/33
57	0.667	137.7	0.139181	0.001957
62	0.759	109.3	0.130445	0.001652
67	0.836	80.8	0.114481	0.001558
72	0.886	59.3	0.106652	0.001208
77	0.916	47.9	0.066078	0.000793
82	0.939	36.6	0.055418	0.000896
87	0.95	32.4		
92	0.964	23.1		
97	0.976	15.8	0.050844	0.000498
102	0.98	12.5		

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

Δz	у	С	F	(R _{xy}) _{max}	T _{xy}
mm	mm		Hz		sec.
54.7	22	0.022	36.2		
	27	0.027	35.8		
	32	0.049	53.3		
	37	0.077	72.6		
	42	0.173	113.2		
	47	0.336	151.5	0.069687	0.001218
	52	0.457	156.7	0.109424	0.001543
	57	0.638	137.4	0.116555	0.001896
	62	0.764	107	0.112778	0.00164
	67	0.856	76.4	0.050864	0.000513
	72	0.893	58.6		
	77	0.927	44.3	0.034142	0.000379
	82	0.949	31		
	87	0.961	24.6		

D.4 Experimental results in terms of streamwise separation Δx

D.4.1 Experimental results for $d_c/h = 1.15$

Location :	The University of Queensland (Australia)					
Date :	April-June 2006					
Experiments by :	G. CAROSI					
Data processing by:	G. CAROSI and H. CHANSON					
Data analysis by :	H. CHANSON and G. CAROSI					
Experiment	Channel: width: 1.0 m, slope: 21.8° , h = 0.10 m, 1 = 0.25 m, 10 identical					
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood					
	staircase invert.					
	$Q_{\rm W} = 0.1164 \text{ m}^3/\text{s}, d_{\rm C} = 0.115 \text{ m}, \text{Re} = 4.6 \text{ E}+5$					
Instrumentation :	Double-tip conductivity probe ($\emptyset = 0.35 \text{ mm}, \Delta x$). Streamwise/longitudinal					
	separation distance Δx .					
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.					
Comments :	Inflow conditions : broad-crested weir.					
	Inception of free-surface aeration: between step edges 6 and 7.					
	Correlation analyses performed on fifteen segments of 60,000 samples.					

Δx	у	С	F	T _{XX}	$(R_{xy})_{max}$	T _{xy}	Tu
mm	mm		Hz	sec.		sec.	
7.0	2	0.062	114.9	0.00119	0.264389	0.000754	
	7	0.061	108.8	0.00072	0.255737	0.000691	0.55763
	12	0.065	108.8	0.000793	0.31752	0.000907	0.649896
	14	0.061	104.7	0.00307	0.304801	0.001234	0.888
	17	0.062	103.2	0.000751	0.323598	0.000769	0.542867
	20	0.1	138.1	0.001225	0.42137	0.001108	0.295671
	22	0.104	139.4	0.000265	0.457885	0.001492	
	27	0.152	165.1	0.002016	0.536603	0.002271	0.864995
	32	0.373	207.1	0.00307	0.62678	0.003575	1.245963
	37	0.551	228.5	0.003559	0.681533	0.004459	1.619106
	42	0.64	208.5	0.002885	0.707943	0.004886	1.016596
	47	0.763	146.4	0.003835	0.71271	0.004813	1.529532
	52	0.855	100.2	0.003957	0.716521	0.004226	1.365287
	57	0.908	68.2	0.003107	0.714641	0.003718	0.92975
	62	0.925	55.3	0.003356	0.682112	0.002779	0.536476
	67	0.943	42	0.00261	0.715595	0.00306	0.639129
	72	0.954	34.5	0.003179	0.719335	0.003297	0.65151
	77	0.966	25.1	0.003087	0.703615	0.003114	0.665568
	82	0.973	22.4	0.003422	0.68642	0.003114	0.626625
	87	0.981	15.8	0.003724	0.669381	0.002835	0.476352
	92	0.985	12.4	0.004424	0.622795	0.002766	0.572504
	97	0.987	10.9	0.004932	0.643073	0.002994	0.562814
	102	0.991	8	0.006372	0.567063	0.002601	0.345584
	107	0.992	6.6	0.007313	0.60096	0.003118	0.550167
	112	0.994	5.7	0.00927	0.539257	0.003212	
	117	0.995	4.7	0.008757	0.545707	0.002699	
	122	0.996	3.6	0.009318	0.55074	0.00347	
	127	0.997	2.9	0.009796	0.520841	0.003164	
	132	0.997	2.6	0.00953	0.534634	0.003377	
	137	0.998	1.7		0.488095	0.004152	
	137	0.998	1.5		0.332272	0.001608	
	142	0.999	1.3		0.477699		
	147	0.999	1				
	152	0.999	1		0.434798		

D.4.1.1 Step edge 10, $\Delta x = 7.0 \text{ mm}$

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

D.4.1.2 Step edge 10, $\Delta x = 9.6 \text{ mm}$

Δx	У	С	F	(R _{xy}) _{max}	T _{xy}	Tu
mm	mm		Hz		sec.	
9.6	0	0.022	52.6	0.038459	0.000204	0.687788
	5	0.08	137.8	0.16166	0.000547	0.660602
	8	0.091	146	0.204673	0.000845	0.654595
	10	0.09	145.6	0.218867	0.000803	0.5319
	12	0.095	148.8	0.223153	0.000737	0.536114
	15	0.1	150.5	0.242839	0.000886	0.638843
	18	0.109	157.2	0.246755	0.000792	
	20	0.117	162	0.272943	0.000948	0.579795
	25	0.133	175.9	0.302928	0.001006	0.561041
	30	0.283	201.4	0.382121	0.001503	0.661304
	35	0.455	237.2	0.456723	0.002311	0.895614

40	0.585	257.5	0.529283	0.00328	1.13515
45	0.71	240	0.576331	0.003674	1.174311
50	0.763	166.9	0.577746	0.003626	1.106536
55	0.852	118.6	0.581312	0.003075	0.835481
60	0.906	77.7	0.584708	0.002538	0.658357
65	0.926	61.7	0.569659	0.002338	0.612871
70	0.947	46	0.571163	0.002124	0.548644
75	0.958	36.4	0.566752	0.002056	0.498758
80	0.966	30.9	0.556409	0.001745	0.461192
85	0.974	23.2	0.53619	0.001879	0.512495
90	0.98	19.1	0.537882	0.001717	0.481148
95	0.984	14.3	0.540713	0.001646	0.415056
100	0.987	12.6	0.50333	0.001447	0.456337
105	0.99	10.1	0.527014	0.001536	0.419261
110	0.992	7.4	0.52155	0.001587	
115	0.993	6.6	0.486483	0.001301	0.460031
120	0.994	5.9	0.509765	0.001398	0.399447
125	0.995	4.3	0.461084	0.001664	0.492853
130	0.997	2.9	0.363794	0.000382	0.366637
130	0.997	2.8	0.448422	0.00105	0.392292
135	0.998	2.1	0.432515	0.001003	0.395014
140	0.999	1.4	0.297799	0.000673	0.361881

D.4.2 Experimental results for $d_c/h = 1.33$

-					
Location :	The University of Queensland (Australia)				
Date :	April-June 2006				
Experiments by :	G. CAROSI				
Data processing by:	G. CAROSI and H. CHANSON				
Data analysis by :	H. CHANSON and G. CAROSI				
Experiment	Channel: width: 1.0 m, slope: 21.8° , h = 0.10 m, 1 = 0.25 m, 10 identical				
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood				
	staircase invert.				
	$Q_{\rm W} = 0.1431 \text{ m}^3/\text{s}, d_{\rm C} = 0.133 \text{ m}, \text{Re} = 5.7 \text{ E}+5$				
Instrumentation :	Double-tip conductivity probe ($\emptyset = 0.35$ mm, $\Delta x = 7.0$ mm).				
	Streamwise/longitudinal separation distance Δx .				
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.				
Comments :	Inflow conditions : broad-crested weir.				
Inception of free-surface aeration: between step edges 6 and 7.					
Correlation analyses performed on fifteen segments of 60,000 sampl					

D.4.2.1 Step edge 7, $\Delta x = 7.0 \text{ mm}$

Δx	У	С	F	T _{XX}	(R _{xy}) _{max}	T _{xy}	Tu
mm	mm		Hz	sec.		sec.	
7.0	1	0.039	54.3	0.001579	0.376365	0.001414	0.71526
	6	0.046	54.1	0.002087	0.444767	0.002119	0.866731
	9	0.058	60.7	0.002069	0.438511	0.002264	0.971498
	11	0.047	52.1	0.002085	0.476891	0.002241	0.87424
	13	0.049	54.6	0.001523	0.450022	0.001809	0.711428
	16	0.07	69.6	0.001444	0.509917	0.001918	0.744325
	19	0.067	61.2	0.000604	0.529508	0.002213	0.803926
21	0.055	50.3	0.001671	0.522856	0.002032	0.704383	
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26	0.078	55.6	0.002022	0.652343	0.00262	0.745315	
31	0.142	76.2	0.002714	0.695446	0.003246	0.875342	
36	0.243	95.7	0.003391	0.742968	0.004308		
41	0.449	118.4	0.003594	0.769282	0.004529	1.063733	
46	0.614	111.6	0.003959	0.777725	0.004721	1.121155	
51	0.737	93.4	0.003732	0.780794	0.004535	0.967145	
56	0.812	72.8	0.003124	0.784843	0.003874	0.757351	
61	0.892	47.8	0.003071	0.783501	0.003576	0.610889	
66	0.891	52.5	0.002616	0.772142	0.003041	0.497231	
71	0.949	28.2	0.002593	0.759315	0.002801	0.497107	
76	0.959	22.3	0.002507	0.773983	0.002833	0.412965	
81	0.948	27.4	0.002792	0.776286	0.002889	0.409203	
86	0.965	19.2	0.002483	0.774714	0.002692	0.371937	
91	0.976	14	0.002227	0.758431	0.002398	0.391721	
96	0.974	14.7	0.002742	0.776436	0.002941	0.390394	
101	0.983	10.6	0.002289	0.717564	0.002378	0.472662	
106	0.983	9.8	0.002891	0.734801	0.002748	0.370619	
111	0.989	6.8	0.00289	0.683911	0.002262	0.360383	
116	0.99	6.3	0.002983	0.706695	0.002603	0.38552	
121	0.993	4.5	0.003635	0.715755	0.003096	0.443416	
126	0.994	3.8	0.004314	0.698192	0.003104	0.524868	
131	0.995	3	0.003249	0.652472	0.002713	0.297568	
131	0.995	2.8	0.003885	0.684631	0.003288	0.38562	
136	0.997	2.1	0.005665	0.540334	0.002005	0.260521	
141	0.997	1.8					

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

Δx	у	С	F	T _{XX}	$(R_{xy})_{max}$	T _{xy}	Tu
mm	mm		Hz	sec.		sec.	
7.0	1	0.03	51.1	0.00068	0.160346	0.00051	0.541202
	6	0.795	107.7	0.000669	0.208917	0.00052	0.53025
	9	0.997	1.9	0.000658	0.237024	0.000588	0.48753
	11	0.027	50.4	0.000647	0.29398	0.000666	0.43253
	13	0.027	46.7	0.000674	0.322964	0.000699	0.50943
	16	0.026	43.9	0.000852	0.357039	0.000913	0.57821
	19	0.033	50.6	0.000756	0.365766	0.000853	0.54711
	21	0.036	53.1	0.001054	0.404832	0.001097	0.54652
	26	0.043	61	0.002156	0.537376	0.002235	0.82908
	31	0.047	63.8	0.003037	0.609727	0.003366	1.11745
	36	0.088	81.2	0.003918	0.679499	0.004421	-
	41	0.183	121.1	0.003962	0.710943	0.004544	1.35632
	46	0.34	154.6	0.003796	0.721029	0.004633	1.35465
	51	0.534	168.9	0.003666	0.733043	0.004155	0.99927
	56	0.679	143.2	0.002692	0.756494	0.003244	0.62862
	61	0.848	83.6	0.002772	0.748431	0.003144	0.59292
	66	0.895	61.9	0.00319	0.74609	0.003382	0.57125
	71	0.92	48.2	0.003151	0.766854	0.003265	0.47350
	76	0.931	42.4	0.002884	0.742764	0.003018	0.46839
	81	0.946	33.7	0.002984	0.764227	0.003143	0.53187
	86	0.947	32.4	0.003008	0.743085	0.00301	0.54955
	91	0.963	24.1	0.002716	0.724061	0.002812	0.55088
	96	0.97	19.6	0.002613	0.682411	0.002639	0.48111
	101	0.974	17.1	0.002877	0.74803	0.002941	0.45415
	106	0.983	12.1	0.003213	0.720062	0.002884	0.41177

D.4.2.2 Step edge 8, $\Delta x = 7.0 \text{ mm}$

111	0.983	11.4	0.002938	0.714971	0.002649	0.523605
116	0.986	9.8	0.003572	0.657664	0.002683	0.487904
121	0.992	5.7	0.00397	0.630698	0.00235	0.398042
126	0.993	5.3	0.003567	0.642847	0.002556	0.4718
131	0.994	4.4	0.005182	0.56598	0.002346	0.389208
131	0.995	3.8	0.00481	0.648881	0.00314	0.471728
136	0.996	2.8	0.004692	0.613263	0.003198	0.517306
141	0.996	2.9				

D.4.2.3 Step edge 9, $\Delta x = 7.0 \text{ mm}$

Δx	У	С	F	T _{XX}	$(R_{xy})_{max}$	T _{xy}	Tu
mm	mm		Hz	sec.		sec.	
7.0	0.5	0.057	92.7	0.001603	0.347479	0.001487	0.830665
	5.5	0.048	74.8	0.001697	0.411164	0.001811	0.918665
	8.5	0.072	101.9	0.001347	0.408226	0.001599	0.835701
	10.5	0.062	85.3	0.001659	0.444109	0.001891	0.924776
	12.5	0.063	83.4	0.001925	0.441414	0.002107	0.870024
	15.5	0.07	87.5	0.001506	0.487285	0.001992	0.889707
	18.5	0.071	87.2	0.001568	0.444809	0.001776	0.778827
	20.5	0.08	91.5	0.001442	0.500249	0.00173	0.738502
	25.5	0.101	99.8	0.001847	0.564681	0.002309	0.864571
	30.5	0.149	120.3	0.002105	0.617373	0.002704	0.937386
	35.5	0.249	152.9	0.003083	0.681669	0.003834	
	40.5	0.377	169.1	0.003276	0.723366	0.004345	1.314698
	45.5	0.556	162.6	0.003856	0.75829	0.004994	1.472303
	50.5	0.664	143	0.003686	0.757416	0.004848	1.392821
	55.5	0.766	112.4	0.002983	0.764981	0.004133	1.028179
	60.5	0.829	92.5	0.002818	0.758787	0.003589	0.803548
	65.5	0.858	81.8	0.002789	0.759834	0.003418	0.940336
	70.5	0.902	60.8	0.002572	0.749763	0.003129	0.614661
	75.5	0.91	52.6	0.003296	0.768848	0.003668	0.706371
	80.5	0.933	43.7	0.002821	0.754711	0.003075	0.553842
	85.5	0.946	33.4	0.003197	0.754295	0.003268	0.583318
	90.5	0.961	26.1	0.002768	0.728013	0.00287	0.531449
	95.5	0.968	22.4	0.002807	0.709856	0.00264	0.440988
	100.5	0.975	18.4	0.003248	0.720647	0.003102	0.599684
	105.5	0.982	13.4	0.003573	0.717162	0.003215	0.627315
	110.5	0.986	10.1	0.003227	0.705085	0.002821	0.465233
	115.5	0.99	7.7	0.003582	0.700909	0.002943	0.500669
	120.5	0.991	6.7	0.004023	0.669627	0.002724	0.556434
	125.5	0.994	4.5	0.004305	0.615726	0.002683	0.388839
	130.5	0.996	3.5	0.005349	0.629856	0.003205	0.545155
	130.5	0.997	2.5	0.006603	0.515989	0.002566	0.418759
	135.5	0.997	1.9				
	140.5	0.998	1.6				

Notes : *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

D.4.2.4 Step edge 10, $\Delta x = 7.0 \text{ mm}$

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$\Delta \mathbf{x}$	У	С	F	T _{XX}	(R _{xy}) _{max}	T _{xy}	Tu
mm	mm		Hz	sec.		sec.	

7.0	1.5	0.042	87.7	0.000629	0.209806	0.000541	
	6.5	0.053	98.4	0.000834	0.292804	0.000845	
	9.5	0.052	94.3	0.000872	0.300971	0.000916	0.687693
	11.5	0.048	88	0.000607	0.283516	0.000723	0.533877
	13.5	0.052	90	0.000683	0.311088	0.000817	0.572963
	16.5	0.055	89.8	0.000729	0.327854	0.00074	0.502104
	19.5	0.063	102	0.000694	0.358372	0.000862	
	26.5	0.081	110.8	0.001078	0.450549	0.001156	0.644338
	31.5	0.126	145.3	0.001966	0.53345	0.002136	0.747365
	36.5	0.187	166.8	0.002841	0.601759	0.003168	1.180327
	41.5	0.41	199.7	0.004049	0.683871	0.004688	1.774786
	46.5	0.571	199.2	0.004139	0.724431	0.005108	1.792577
	51.5	0.678	161.2	0.004345	0.746485	0.005525	1.943015
	56.5	0.814	112.5	0.003821	0.759131	0.004834	1.318069
	61.5	0.886	76.8	0.003912	0.748266	0.004497	1.073947
	66.5	0.924	51	0.003507	0.741208	0.003736	0.800066
	71.5	0.944	38.8	0.003359	0.750629	0.003534	0.710763
	76.5	0.955	31.8	0.003314	0.726486	0.003441	0.709057
	81.5	0.967	23.7	0.003387	0.726729	0.003429	0.680787
	86.5	0.974	20	0.00346	0.724215	0.003279	0.854175
	91.5	0.981	15.6	0.003112	0.686873	0.002754	0.478292
	96.5	0.985	12.3	0.003635	0.698636	0.003055	0.494324
	101.5	0.989	8.3	0.004056	0.671801	0.002936	0.512453
	106.5	0.991	7.1	0.004026	0.646803	0.002735	0.485592
	111.5	0.993	5.5	0.004081	0.647725	0.002824	0.608745
	116.5	0.995	4.4	0.004553	0.608084	0.00255	0.495045
	121.5	0.995	4	0.005173	0.600479	0.003014	0.454956
	126.5	0.997	2.8	0.007249	0.536074	0.002802	0.474336
	131.5	0.996	2.7	0.007113	0.629105	0.003668	0.173744
	136.5	0.998	1.6	0.009353	0.566952	0.004487	1.154547
	141.5	0.999	1.2	0.010264	0.427093	0.002625	
	146.5	0.999	1.4				
	151.5	0.999	1				

D.4.3 Experimental results for $d_C/h = 1.45$

Location :	The University of Queensland (Australia)					
Date :	April-June 2006					
Experiments by :	G. CAROSI					
Data processing by:	G. CAROSI and H. CHANSON					
Data analysis by :	H. CHANSON and G. CAROSI					
Experiment	Channel: width: 1.0 m, slope: 21.8° , h = 0.10 m, l = 0.25 m, 10 identical					
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood					
	staircase invert.					
	$Q_w = 0.1612 \text{ m}^3/\text{s}, d_c = 0.145 \text{ m}, \text{Re} = 6.4 \text{ E}+5$					
Instrumentation :	Double-tip conductivity probe ($\emptyset = 0.35 \text{ mm}, \Delta x$). Streamwise/longitudinal					
	separation distance Δx .					
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.					
Comments :	Inflow conditions : broad-crested weir.					
	Inception of free-surface aeration: between step edges 7 and 8.					
	Correlation analyses performed on fifteen segments of 60,000 samples.					

Δx	У	С	F	T _{XX}	$(R_{xy})_{max}$	T _{xy}	Tu
mm	mm		Hz	sec.		sec.	
7.0	2	0.007	17.5	0.000509	0.181468	0.000453	0.510077
	7	0.01	21.8	0.000594	0.273554	0.000698	0.56445
	10	0.011	23.5	0.000263	0.248417	0.000644	
	12	0.013	26.5	0.000609	0.259366	0.000555	0.4743
	14	0.017	29.6	0.000657	0.306884	0.000835	0.624014
	17	0.03	52.4	0.00076	0.366902	0.000893	0.60415
	20	0.027	48.2	0.000646	0.337786	0.000744	0.581754
	22	0.03	50	0.000718	0.369965	0.000784	0.599563
	27	0.041	58.9	0.00091	0.454099	0.001152	0.57449
	32	0.068	81.6	0.001553	0.500399	0.001802	0.729119
	37	0.124	107.1	0.002571	0.610495	0.002779	0.951531
	42	0.196	133.1	0.003545	0.673669	0.003951	1.344192
	47	0.348	165.9	0.004483	0.719679	0.005057	1.825543
	52	0.521	168.9	0.004187	0.748688	0.004992	1.5687
	57	0.715	136.8	0.003756	0.755693	0.00458	1.31569
	62	0.79	113.1	0.003565	0.751256	0.004235	1.142123
	67	0.858	83.6	0.003593	0.745092	0.003994	0.9175
	72	0.913	57	0.003117	0.748285	0.003344	0.680576
	77	0.935	44.2	0.00326	0.747248	0.003472	1.894483
	82	0.951	36.5	0.002795	0.733112	0.002746	0.55314
	87	0.965	27.7	0.002983	0.729626	0.002819	0.526467
	92	0.976	20.2	0.003376	0.707357	0.00276	0.474946
	97	0.98	16.5	0.003261	0.694297	0.002607	0.50282
	102	0.982	13.9	0.00372	0.723157	0.002771	0.470028
	107	0.989	9.9	0.00505	0.637117	0.002442	0.32658
	112	0.99	8.1	0.005512	0.619228	0.002393	0.414015
	117	0.992	6.9	0.00636	0.624409	0.002756	0.399977
	122	0.995	4.8	0.00778	0.583857	0.002458	0.105463
	127	0.995	4	0.008697	0.555392	0.002598	
	132	0.995	4.3	0.008995	0.567112	0.002934	
	132	0.997	2.9		0.544159		
	137	0.997	2.6		0.541278		
	142	0.998	1.8				
	147	0.998	1.7				
	152	0.999	1				

D.4.3.1 Step edge 10, $\Delta x = 7.0 \text{ mm}$

D.4.3.2 Step edge 10, $\Delta x = 9.6 \text{ mm}$

Δx	У	С	F	T _{XX}	$(R_{xy})_{max}$	T _{xy}	Tu
mm	mm		Hz	sec.		sec.	
9.6	0	0.053	5.8				
	5	0.012	29.5	0.049417	0.00019	0.403972	
	8	0.035	81.7	0.1093	0.000296	0.381092	
	10	0.039	84.8	0.121427	0.000382	0.366015	
	12	0.026	59.9	0.096115	0.000267	0.373153	
	15	0.047	94.3	0.180257	0.000421	0.388148	
	18	0.052	99	0.184676	0.000559		
	20	0.062	112.7	0.222364	0.000551	0.463487	
	25	0.071	117.9	0.292837	0.000835	0.499244	
	30	0.068	113.3	0.28901	0.000764	0.460181	

35	0.08	123	0.319277	0.000808	0.438083	
40	0.088	125	0.320664	0.000792	0.4053	
45	0.124	149.5	0.437437	0.001489	0.536502	
50	0.167	153.4	0.545563	0.002427	0.700627	
55	0.294	185.8	0.614334	0.003401	0.988448	
60	0.511	192.7	0.662247	0.004125	1.189168	
65	0.617	179.2	0.677186	0.004096	1.113039	
70	0.782	128.3	0.662946	0.003333	0.823126	
75	0.869	88.8	0.643304	0.002727	0.632891	
80	0.947	43.3	0.598996	0.002115	0.499834	
85	0.964	31.3	0.587268	0.001865	0.421467	
90	0.972	25	0.569822	0.001663	0.416834	
95	0.978	19	0.599323	0.001644	0.367183	
100	0.985	13.5	0.582659	0.001566	1.202521	
105	0.987	11.1	0.525884	0.001398	0.409692	
110	0.989	10	0.578211	0.001322	0.342654	
115	0.993	6.7	0.543289	0.001297	0.377245	
120	0.994	5.8	0.482436	0.001104	0.305683	
125	0.995	4.3	0.475139	0.001039	0.297412	
130	0.996	3.8	0.498344	0.001101	0.320875	
130	0.998	2.5	0.500669	0.001093	0.308174	
135	0.998	2.1	0.492897	0.001172	0.419171	
140	0.998	1.7	0.448952	0.000948	0.384834	

APPENDIX E - INTEGRAL AIR-WATER LENGTH AND TIME SCALES IN SKIMMING FLOWS ON A STEPPED CHUTE

E.1 Presentation

When two probe sensors are separated by a transverse or streamwise distance Y, their signals may be analysed in terms of the auto-correlation and cross-correlation functions R_{XX} and R_{XY} respectively (App. D). In the present study, the probe sensors were scanned at 20 kHz for 45 s. The data sets of 900,000 samples per sensor were segmented because the periodogram resolution is inversely proportional to the number of samples and it could be biased with large data sets (HAYES 1996, GONZALEZ 2005). The signals were sub-divided into fifteen non-overlapping segments of 60,000 samples. In addition, the correlation analyses were conducted on the raw probe output signals. With a single-threshold technique, any analysis based upon thresholded signals (or square-wave signals) tends to ignore the contributions of the smallest air-water particles.

Identical experiments were repeated with different separation distances Y (Y = Δz or Δx) and an integral turbulent length scale was calculated as :

$$L_{xy} = \int_{Y=0}^{Y=Y((R_{xy})_{max}=0)} \int_{Y=0}^{(R_{xy})_{max}} * dY$$
(E-1)

where R_{xy} is the normalised cross-correlation function between the two probe output signals, $(R_{xy})_{max}$ the maximum cross-correlation coefficient, and Y is the separation distance. The integral turbulent length scale L_{xy} is a function of the inflow conditions, streamwise position x/d_c and normal distance y/d_c . In the present study, the length scale L_{xy} represents a measure of the transverse/streamwise length scale of the large vortical structures advecting air bubbles and air-water packets.

An integral turbulent time scale is :

$$\mathbf{T} = \frac{\int (R_{xy})_{max} * T_{xy} * dY}{L_{xy}}$$
(E-2)

T represents the transverse/streamwise integral time scale of the large eddies advecting air bubbles.

Discussion

Auto- and cross-correlation calculations were most successful for $0.05 \le C \le 0.95$. In the upper spray region ($C \ge 0.90$ to 0.95) and at a few other locations, the calculations were unsuccessful for a number of reasons. These included flat cross-correlation functions without a distinctive peak, non-crossing of the correlation function(s) with the zero line, correlation functions with several peaks, meaningless correlation trends ... Such data points are indicated with (--) in the following tables of results. While most correlation calculations can be automated, it must be stressed that human intervention are essential to validate each calculation step. Herein all calculations were performed by hand and all meaningless results were rejected.

Note that another streamwise length scale is the advection length scale defined as :

$$L_{XX} = V * T_{XX}$$
(E-3)

where V is the advective velocity magnitude and T_{XX} is an auto-correlation time scale of the longitudinal bubbly flow structures :

$$T_{XX} = \int_{\tau=0}^{\tau=\tau (R_{XX}=0)} R_{XX}(\tau) * d\tau$$
(E-4)

 $L_{\rm XX}$ is a characteristic longitudinal size of the large eddies advecting air bubbles.

E.2 Experimental results. (1) Transverse integral length and time scales

E.2.1 Experimental results for $d_C/h = 1.15$

Location :	The University of Queensland (Australia)					
Date :	April-June 2006					
Experiments by :	G. CAROSI					
Data processing by:	G. CAROSI and H. CHANSON					
Data analysis by :	H. CHANSON and G. CAROSI					
Experiment	Channel: width: 1.0 m, slope: 21.8°, h = 0.10 m, 1 = 0.25 m, 10 identical					
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood					
	staircase invert.					
	$Q_w = 0.1164 \text{ m}^3/\text{s}, d_c = 0.115 \text{ m}, \text{Re} = 4.6 \text{ E}+5$					
Instrumentation :	Two single-tip conductivity probe ($\emptyset = 0.35$ mm). Transverse separation					
	distance Δz .					
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.					
Comments :	Inflow conditions : broad-crested weir.					
	Inception of free-surface aeration: between step edges 6 and 7.					
	Correlation analyses performed on fifteen segments of 60,000 samples.					

D.2.1.1 Step edge 10

C11	• •	•		CM	
('horoot	oriotio	011	wator	tlow	proportion
v naracu	CHNE	<u> </u>	walet	110.000	DIODELLES
Charact	or ibute	wiii	mater	110 11	properties

		Yç	90 (+)	d (+)	Cmean (+)	$U_{W}(^{+})$	$F_{max}(^+)$	
			m	m		m/s	Hz	
		0.	0598	0.041	0.4518	3.98	189.3	
_								
	у	С	F	L _{xy}	Т	L _{XX}	Remarks	
		(+)	(+)	Eq. (E-1)	Eq. (E-2)	Eq. (E-3)		
	mm		Hz	mm	millisec.	mm		
	(1)	(2)	(3)	(4)	(5)	(6)	(4)	
_	2	0.028	52.4	2.37	0.593		Transverse integration	
	7	0.038	70.9	2.39	0.513			
	10	0.043	74.7	2.65	0.772	3.563		
	12	0.044	75.7	2.70	0.711	3.332		
	14	0.050	79.5	2.93	0.735	3.435		
	17	0.055	85.5	3.28	0.797	3.060		
	20	0.064	91.8	3.85	1.203	3.840		
	22	0.074	100.0	4.35	1.321	4.364		
	27	0.121	130.8	6.82	1.748	5.786		
	32	0.237	175.1	10.18	2.904			
	37	0.424	189.3	12.85	3.440	12.537		
	42	0.594	177.9	11.78	3.691	15.725		
	47	0.718	148.7	13.36	3.189	14.773		
	52	0.826	104.4	11.83	2.690	12.276		
	57	0.881	74.3	10.47	2.303	12.426		

62	0.915	55.6	9.00	1.907	10.149	
67	0.937	42.9	8.35	1.893	9.769	
72	0.953	33.4	6.64	1.849	8.111	
77	0.963	26.7	6.68	1.649	8.775	
82	0.970	22.4	6.66	1.687	8.503	
87	0.977	17.4	6.00	1.755	8.098	
92	0.982	14.2	5.61	1.567	7.637	
97	0.986	11.2	5.54	1.786	8.324	
102	0.989	8.8	5.20	1.648	8.033	
107	0.992	6.7	5.06	1.611	8.860	
112	0.994	5.4	4.94	1.648	8.390	
117	0.995	4.2	4.65	1.746	8.588	
122	0.996	3.5	4.56	1.764	8.351	
127	0.997	2.7	5.15	2.008	9.731	
132	0.997	2.4	4.88	1.948	11.343	
137	0.998	1.6	3.93	2.846	18.580	
142	0.998	1.7	4.19	3.074	20.713	
147	0.999	1.4	3.33	3.198	19.852	
152	0.999	1.1	4.58	5.680	21.326	
157	0.999	0.9	4.29			

Notes :

(⁺) : data collected for 360 s at 20 kHz;

 L_{xy} , **T** : transverse integral scales;

Blue italic : suspicious data;

Red Bold : possibly incorrect data;

(--): meaningless data.

Fig. E-1 - Normal distributions of transverse integral length scale L_{xy} , (transverse) integral times scale \mathbf{T} , and streamwise Taylor length scale L_{xx} for $d_c/h = 1.15$, Step 10 - Comparison with the measured void fraction distribution



Location :	The University of Queensland (Australia)
Date :	April-June 2006
Experiments by :	G. CAROSI
Data processing by:	G. CAROSI and H. CHANSON
Data analysis by :	H. CHANSON and G. CAROSI
Experiment	Channel: width: 1.0 m, slope: 21.8° , h = 0.10 m, 1 = 0.25 m, 10 identical
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood
	staircase invert.
	$Q_w = 0.1612 \text{ m}^3/\text{s}, d_c = 0.145 \text{ m}, \text{Re} = 6.4 \text{ E}+5$
Instrumentation :	Two single-tip conductivity probe ($\emptyset = 0.35$ mm). Transverse separation
	distance Δz .
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.
Comments :	Inflow conditions : broad-crested weir.
	Inception of free-surface aeration: between step edges 7 and 8.
	Correlation analyses performed on fifteen segments of 60,000 samples.

E.2.2 Experimental results for $d_C/h = 1.45$

D.2.2.1 Step edge 10

Characteristic air wate<u>r flow properties</u> Y_{00} (⁺)

cristic un	Ye	$\frac{1}{90}(^{+})$	d (+)	C _{mean} (⁺)	U _W (⁺)	$F_{max}(^+)$	
		m	m		m/s	Hz	
	0.	0735	0.052	0.2929	3.33	154.1	
у	С	F	L _{XV}	Т	L _{XX}	Ren	narks
			Eq. (E-1)	Eq. (E-2)	Eq. (E-3)		
mm		Hz	m	S	m		
(1)	(2)	(3)	(4)	(5)	(6)	(*	4)
2	0.010	23.0	2.220	0.607	2.837	Transverse ir	ntegration.
7	0.013	27.3	2.231	0.488	2.594		0
10	0.016	30.3	2.596	0.616	3.236		
12	0.015	28.7	2.720	0.790	3.763		
14	0.018	32.0	2.817	0.590	3.264		
17	0.020	34.1	2.850	0.688	3.222		
20	0.023	35.9	3.241	0.795	4.099		
22	0.025	38.4	3.472	0.963	3.937		
27	0.033	44.0	3.790	1.364	4.492		
32	0.056	59.8	6.713	1.646	7.460		
37	0.104	85.2	7.816	2.414	9.831		
42	0.200	118.5	11.972	2.967	14.843		
47	0.337	147.2	15.197	3.532	17.689		
52	0.515	154.1	16.630	3.371	16.815		
57	0.652	135.4	16.979	3.432	18.345		
62	0.766	108.6	15.628	2.932	16.357		
67	0.845	80.4	13.640	2.572	13.530		
72	0.891	59.6	12.589	2.252	12.691		
77	0.922	46.0	10.460	1.983	12.472		
82	0.939	37.3	9.826	1.927	12.847		
87	0.956	28.2	7.894	1.823	11.764		
92	0.965	22.7	7.353	1.918	11.167		
97	0.975	17.6	8.101	1.448	10.097		
102	0.980	14.2	5.678	1.810	10.782		
107	0.986	10.8	6.129	1.535	9.423		
112	0.988	8.8	6.028	1.503	9.920		
117	0.991	7.1	5.642	1.608	10.070		

122	0.993	5.4	5.794	1.447	10.908	
127	0.995	4.0	5.342	1.400	11.073	
132	0.996	3.1	5.108	1.549	11.864	
132	0.997	2.8	5.118	1.598	12.353	
137	0.997	2.3	3.877	2.448	19.498	
142	0.998	1.8	5.162	1.432	12.512	
147	0.998	1.7	4.322	1.840	17.604	
152	0.999	1.3	4.748	1.912	19.471	

Notes :

(⁺): data collected for 315 s at 20 kHz;
L_{xy}, **T**: transverse integral scales; *Blue italic*: suspicious data;

Red Bold : possibly incorrect data;

(--): meaningless data.

Fig. E-2 - Normal distributions of transverse integral length scale L_{XY} , (transverse) integral times scale \mathbf{T} , and streamwise Taylor length scale L_{XX} for $d_c/h = 1.45$, Step 10 - Comparison with the measured void fraction distribution



E.3 Experimental results. (2) Longitudinal/streamwise integral length and time scales

The longitudinal integral scales were calculated based upon the auto- and cross-correlation function for some double-tip probes. Note that only two streamwise probe separation distances were used : $\Delta x = 7.0$ and 9.6 mm.

E.3.1 Experimental results for $d_c/h = 1.15$

Location :	The University of Queensland (Australia)
Date :	April-June 2006

Experiments by :	G. CAROSI				
Data processing by: G. CAROSI and H. CHANSON					
Data analysis by : H. CHANSON and G. CAROSI					
Experiment	Channel: width: 1.0 m, slope: 21.8° , h = 0.10 m, 1 = 0.25 m, 10 identical				
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood				
	staircase invert.				
	$Q_w = 0.1164 \text{ m}^3/\text{s}, d_c = 0.115 \text{ m}, \text{Re} = 4.6 \text{ E}+5$				
Instrumentation :	Double-tip conductivity probes ($\emptyset = 0.25$ mm). Transverse separation				
	distance Δx .				
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.				
Comments :	Inflow conditions : broad-crested weir.				
	Inception of free-surface aeration: between step edges 6 and 7.				
	Correlation analyses performed on fifteen segments of 60,000 samples.				

D.3.1.1 Step edge 10

Characteristic air water flow properties

		Ye	90 (+)	d (+)	C _{mean} (⁺)	$U_{W}(^{+})$	$F_{max}(^+)$	
			m	m		m/s	Hz	
		0.	0574	0.0364	0.365	3.35	233	
-	У	С	F	L _{xy}	Т	L _{XX}	Remark	s
		(+)	(+)	Eq. (E-1)	Eq. (E-2)	Eq. (E-3)		
	mm		Hz	mm	millisec.	mm		
	(1)	(2)	(3)	(4)	(5)	(6)	(4)	
	1	0.042	83.8	5.02	0.90	3.99	Streamwise integ	ration.
	6	0.071	123.3	5.78	0.63	2.41		
	8	0.074	146.0	6.85				
	11	0.078	127.2	6.45	0.77	2.66		
	13	0.078	126.8	6.41	1.70	10.28		
	16	0.081	126.9	6.63	0.71	2.52		
	19	0.105	147.7	7.13	1.00	4.11		
	21	0.111	150.7	7.47	0.84	0.89		
	26	0.143	170.5	8.04	1.75	6.75		
	31	0.328	204.3	8.99	2.64	10.28		
	36	0.503	232.9	9.74	3.22	11.93		
	41	0.613	233.0	10.34	3.32	9.67		
	46	0.737	193.2	10.67	3.61	12.85		
	51	0.809	133.6	10.69	3.43	13.26		
	56	0.880	93.4	10.71	2.88	10.41		
	61	0.916	66.5	10.57	2.49	11.24		
	66	0.935	51.9	10.64	2.35	8.74		
	71	0.951	40.3	10.67	2.55	10.65		
	76	0.962	30.8	10.56	2.44	10.34		
	81	0.970	26.7	10.41	2.47	11.46		
	86	0.978	19.5	10.20	2.50	12.48		
	91	0.983	15.8	9 99	2.62	14.82		
	96	0.986	12.6	10.10	2.82	16.52		
	101	0.989	10.3	9.49	3.09	21.35		
	101	0.901	8.4	9.81	3.54	24.50		
	111	0.003	6.6	9.01	2.37 2 12	24.50		
	116	0.993	57	0.70 0.70	7.12	20.34		
	121	0.994	J.7 18	9.26	<i>A</i> 22	27.54		
	121	0.795	7.0 3.6	9.40 9.00	7.22 1 10	37.22		
	120	0.990	2.8	8.43	4.41	31.02		
	1.51	0.727	2.0	0.40	7.71	51.95		

133.5	0.998	2.3	8.76	
136	0.998	1.8	7.91	
141	0.999	1.4	7.73	
147	0.999	1.0		
152	0.999	1.0	6.15	

Notes :

(⁺) : data collected for 90 s at 20 kHz;

 L_{xy} , **T** : transverse integral scales;

Blue italic : suspicious data;

Red Bold : possibly incorrect data;

(--) : meaningless data.

Fig. E-3 - Normal distributions of streamwise integral length scale L_{xy} , (streamwise) integral times scale **T**, and streamwise Taylor length scale L_{xx} for $d_c/h = 1.15$, Step 10 - Comparison with the measured void fraction distribution



E.3.2 Experimental results for $d_c/h = 1.45$

Location :	The University of Queensland (Australia)
Date :	April-June 2006
Experiments by :	G. CAROSI
Data processing by:	G. CAROSI and H. CHANSON
Data analysis by :	H. CHANSON and G. CAROSI
Experiment	Channel: width: 1.0 m, slope: 21.8° , $h = 0.10$ m, $1 = 0.25$ m, 10 identical
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood
	staircase invert.
	$Q_{\rm w} = 0.1612 \text{ m}^3/\text{s}, d_{\rm c} = 0.145 \text{ m}, \text{Re} = 6.4 \text{ E}+5$

Instrumentation :	Double-tip conductivity probes ($\emptyset = 0.25$ mm). Transverse separation
	distance Δx .
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.
Comments :	Inflow conditions : broad-crested weir.
	Inception of free-surface aeration: between step edges 6 and 7.
	Correlation analyses performed on fifteen segments of 60,000 samples.

D.3.3.2 Step edge 10

	Characteristic	air	water	flow	properties
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	Y	90 (⁺)	d (+)	C _{mean} (⁺)	$U_{W}(^{+})$	$F_{max}(^+)$	
		m	m		m/s	Hz	
	0.	0758	0.0546	0.280	2.24	161.3	
у	С	F	L _{xy}	Т	L _{XX}	Remarks	
	(+)	(+)	Eq. (E-1)	Eq. (E-2)	Eq. (E-3)		
mm		Hz	mm	millisec.	mm		
(1)	(2)	(3)	(4)	(5)	(6)	(4)	
1	0.030	11.7	4.61	0.48	1.14	Streamwise integration.	
6	0.011	25.7	5.13	0.60	1.33	-	
9	0.023	52.6	5.40	0.42	0.59		
11	0.026	55.7	5.53	0.53	1.36		
13	0.022	44.8	5.60	0.67	1.47		
16	0.039	73.4	6.43	0.72	1.70		
19	0.040	73.6	6.32	0.63	1.44		
21	0.046	81.4	6.72	0.66	1.60		
26	0.056	88.4	7.58	0.90	2.03		
31	0.068	97.5	7.78	1.38	3.47		
36	0.102	115.1	8.51	2.11	5.75		
41	0.142	129.1	8.82	2.91	7.93		
46	0.236	157.7	9.80	3.61	10.02		
51	0.344	161.2	10.64	3.55	9.36		
56	0.505	161.3	11.12	3.43	8.40		
61	0.651	152.9	11.41	3.39	7.97		
66	0.738	131.4	11.48	3.30	8.03		
71	0.848	92.7	11.40	2.77	6.97		
76	0.902	66.5	11.27	2.73	7.29		
81	0.949	39.9	10.91	2.23	6.25		
86	0.965	29.5	10.82	2.26	6.67		
91	0.974	22.6	10.60	2.31	7.55		
96	0.979	17.8	10.73	2.19	7.29		
101	0.984	13.7	10.76	2.38	8.32		
106	0.988	10.5	9.98	2.63	11.29		
111	0.990	9.1	10.23	2.67	12.32		
116	0.993	6.8	10.03	3.07	14.22		
121	0.995	5.3	9.44	3.41	17.40		
126	0.995	4.2	9.25	3.72	19.45		
131	0.996	4.1	9.46	3.90	20.11		
131	0.998	2.7	9.37				
136	0.998	2.4	9.30				
141	0.998	1.8	9.29				
147	0.998	1.7					
152	0.999	1.0					

Notes :

 $(^+)$: data collected for 90 s at 20 kHz;

L_{xy}, **T** : transverse integral scales; *Blue italic* : suspicious data; **Red Bold** : possibly incorrect data; (--) : meaningless data.

Fig. E-4 - Normal distributions of streamwise integral length scale L_{XY} , (streamwise) integral times scale \mathbf{T} , and streamwise Taylor length scale L_{XX} for $d_c/h = 1.45$, Step 10 - Comparison with the measured void fraction distribution



APPENDIX F - EXPERIMENTAL MEASUREMENTS OF VOID FRACTION, BUBBLE COUNT RATE, INTERFACIAL VELOCITY AND TURBULENCE INTENSITY IN SKIMMING FLOWS ON A STEPPED CHUTE

Notation

С	void fraction defined as the volume of air per unit volume of air and water;								
F	bubble count rate (Hz) defined as the number of bubbles pierced by the probe sensor per								
	second;								
h	step height (m);								
1	step length (m);								
Tu	turbulence intensity u'/V calculated by correlation analyses;								
u'	root mean square of longitudinal component of turbulent velocity (m/s);								
V	time-averaged interfacial velocity (m/s);								

<u>F.1 Experimental data for $d_C/h = 1.0$ </u>

Location :	The University of Queensland (Australia)
Date :	April-June 2006
Experiments by :	G. CAROSI
Data processing by:	G. CAROSI and H. CHANSON
Data analysis by :	H. CHANSON and G. CAROSI
Experiment	Channel: width: 1.0 m, slope: 21.8° , h = 0.10 m, 1 = 0.25 m, 10 identical
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood
	staircase invert.
	$Q_w = 0.0948 \text{ m}^3/\text{s}, d_c = 0.10 \text{ m}, \text{Re} = 3.85 \text{ E}+5$
Instrumentation :	Single-tip conductivity probe ($\emptyset = 0.35 \text{ mm}$).
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.
Comments :	Inflow conditions : broad-crested weir.
	Inception of free-surface aeration: step edge 5.

Run	Step	У	С	F	Run	Step	у	С	F
	euge			IJ.,		euge			IJ.,
		IIIII		ΠZ			ШШ		ΠZ
060322a	6	1.0	0.004	9.7	060327a	7	13.0	0.047	49.7
		1.5	0.006	12.5			16.0	0.052	50.9
		2.0	0.007	15.8			19.0	0.060	55.5
		3.0	0.015	27.4			21.0	0.074	65.0
		5.0	0.028	42.4			23.0	0.065	60.7
		6.0	0.043	57.2			26.0	0.099	76.2
		7.0	0.042	56.8			28.0	0.127	92.4
		8.0	0.047	59.3			31.0	0.168	104.1
		9.0	0.051	62.3			34.0	0.264	133.8
		10.0	0.052	62.7			36.0	0.349	148.8
		11.0	0.065	71.8			41.0	0.533	140.6
		11.5	0.071	75.4			46.0	0.636	126.1
		12.0	0.074	78.1			51.0	0.801	86.8
		13.0	0.065	71.7			56.0	0.844	65.4

16.0	0.093	86.0	61.0	0.883	51.0
21.0	0.197	127.3	66.0	0.909	40.1
26.0	0.291	145.8	71.0	0.926	31.7
31.0	0.414	150.4	76.0	0.948	22.6
41.0	0.737	112.5	81.0	0.971	13.5
46.0	0.815	82.0	86.0	0.968	15.2
51.0	0.859	62.5	91.0	0.979	10.0
56.0	0.905	43.1	96.0	0.985	7.6
61.0	0.843	62.2	101.0	0.981	9.2
66.0	0.849	60.0	106.0	0.997	1.6
71.0	0.868	55.8	111.0	0.998	1.4
76.0	0.896	45.7	116.0	0.998	1.3
81.0	0.918	38.3	121.0	0.994	3.2
86.0	0.915	37.2	126.0	0.994	2.9
91.0	0.929	31.4	131.0	0.996	2.4
96.0	0.931	29.6	141.0	0.998	1.4
106.0	0.953	22.5	146.0	0.998	1.3
111.0	0.962	17.8	1.0	0.000	0.9
116.0	0.967	14.7	136.0	0.997	1.6
121.0	0.974	12.4			
126.0	0.979	9.7			
131.0	0.984	7.8			
136.0	0.987	6.5			
141.0	0.991	4.4			
146.0	0.992	4.0			
156.0	0.996	2.2			

Run	Step	У	С	F	Run	Step	У	С	F
	eage			Цa		edge			\mathbf{U}_{7}
0.602071	0	11111	0.015	ПZ 20. Г	0.60220	0	1.0	0.010	<u>п</u> 2
0603276	8	6.0	0.015	29.5	060328a	9	1.0	0.018	25.9
		11.0	0.023	40.2			1.5	0.021	28.6
		16.0	0.029	42.3			4.0	0.032	40.1
		21.0	0.050	57.3			8.0	0.041	46.4
		26.0	0.084	78.5			9.0	0.046	51.0
		31.0	0.166	114.2			6.0	0.039	42.8
		36.0	0.291	147.6			11.0	0.056	57.1
		41.0	0.490	158.8			13.0	0.056	54.0
		46.0	0.637	133.4			18.0	0.084	74.0
		51.0	0.761	99.4			19.0	0.092	77.4
		56.0	0.840	72.3			21.0	0.129	98.0
		61.0	0.885	52.7			23.0	0.115	93.3
		66.0	0.922	36.6			26.0	0.237	131.2
		71.0	0.929	31.8			31.0	0.392	144.9
		76.0	0.948	24.9			36.0	0.506	135.9
		81.0	0.958	20.6			41.0	0.614	120.7
		86.0	0.964	16.8			46.0	0.694	101.8
		91.0	0.975	12.5			51.0	0.753	85.6
		96.0	0.979	10.9			56.0	0.782	78.5
		101.0	0.981	9.7			61.0	0.818	68.9
		106.0	0.985	7.2			66.0	0.841	62.6
		111.0	0.986	6.9			71.0	0.865	55.5
		116.0	0.991	5.2			76.0	0.881	49.8
		121.0	0.993	3.7			81.0	0.907	42.2
		126.0	0.994	3.6			86.0	0.916	37.0
		131.0	0.995	3.3			91.0	0.928	33.6

136.0	0.997	1.9	96.0	0.942	28.3
49.0	0.725	113.3	101.0	0.956	22.6
54.0	0.824	78.5	106.0	0.962	20.4
59.0	0.881	55.2	111.0	0.972	14.8
64.0	0.904	43.4	116.0	0.979	11.8
69.0	0.931	32.0	121.0	0.984	9.0
34.0	0.254	147.6	126.0	0.985	8.5
39.0	0.414	166.4	131.0	0.990	6.1
44.0	0.576	153.8	136.0	0.991	5.6
			141.0	0.993	4.5

Run	Step	У	C	F
	edge			
		mm		Hz
060328b	10	1.0	0.007	17.4
		2.0	0.009	21.2
		4.0	0.013	29.4
		6.0	0.019	36.9
		9.0	0.022	39.9
		11.0	0.024	42.4
		13.0	0.028	44.8
		16.0	0.030	46.9
		19.0	0.043	56.8
		21.0	0.051	63.5
		23.0	0.064	73.6
		26.0	0.101	94.0
		31.0	0.202	141.2
		36.0	0.349	173.1
		41.0	0.528	163.3
		46.0	0.684	134.5
		51.0	0.801	95.2
		56.0	0.883	60.6
		61.0	0.927	38.4
		66.0	0.947	29.0
		71.0	0.961	21.1
		76.0	0.968	18.6
		81.0	0.976	14.1
		86.0	0.982	11.3
		91.0	0.984	9.7
		96.0	0.988	7.6
		101.0	0.988	7.8
		106.0	0.991	6.0
		111.0	0.994	4.5
		116.0	0.994	4.2
		121.0	0.995	3.3
		131.0	0.996	2.7
		126.0	0.995	3.2
		136.0	0.997	1.9
		141.0	0.998	1.6

<u>F.2 Experimental data for $d_{\underline{C}}/h = 1.15$ </u>

Location :	The University of Queensland (Australia)
Date :	April-June 2006

Experiments by :	G. CAROSI
Data processing by:	G. CAROSI and H. CHANSON
Data analysis by :	H. CHANSON and G. CAROSI
Experiment	Channel: width: 1.0 m, slope: 21.8° , h = 0.10 m, 1 = 0.25 m, 10 identical
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood
	staircase invert.
	$Q_w = 0.1164 \text{ m}^3/\text{s}, d_c = 0.115 \text{ m}, \text{Re} = 4.6 \text{ E}+5$
Instrumentation :	Single-tip conductivity probe ($\emptyset = 0.35$ mm).
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.
Comments :	Inflow conditions : broad-crested weir.
	Inception of free-surface aeration: between step edges 6 to 7.

Run	Step	у	С	F	Run	Step	У	С	F
	euge	mm		Hz		euge	mm		Hz
060410a	7	1.5	0.023	41.2	060410b	8	1.5	0.010	28.0
		6.5	0.039	54.2			6.5	0.022	43.8
		11.5	0.045	55.9			9.5	0.031	53.7
		12.5	0.046	57.0			11.5	0.030	53.2
		13.5	0.047	58.7			13.5	0.033	56.8
		16.5	0.058	63.2			16.5	0.036	56.7
		19.5	0.078	75.2			19.5	0.039	59.3
		21.5	0.086	82.3			21.5	0.044	63.8
		26.5	0.173	118.0			26.5	0.069	82.5
		31.5	0.286	147.9			31.5	0.129	116.2
		36.5	0.427	161.9			36.5	0.226	151.1
		41.5	0.573	150.0			41.5	0.452	177.8
		46.5	0.687	130.8			46.5	0.574	173.2
		51.5	0.759	106.8			51.5	0.699	138.5
		56.5	0.791	90.4			56.5	0.815	99.1
		61.5	0.833	75.4			61.5	0.879	68.1
		66.5	0.866	62.9			66.5	0.915	49.9
		71.5	0.886	55.8			71.5	0.930	41.0
		76.5	0.907	47.5			76.5	0.950	29.7
		81.5	0.926	38.2			81.5	0.959	24.7
		86.5	0.932	35.4			86.5	0.965	20.7
		91.5	0.940	32.0			91.5	0.978	14.7
		96.5	0.960	23.1			96.5	0.980	13.0
		101.5	0.966	19.7			101.5	0.986	8.9
		106.5	0.971	16.4			106.5	0.989	7.3
		111.5	0.980	11.8			111.5	0.990	6.1
		116.5	0.986	8.7			116.5	0.992	5.6
		121.5	0.986	8.6			121.5	0.995	3.9
		126.5	0.987	7.5			126.5	0.996	3.1
		131.5	0.991	5.3			131.5	0.996	3.1
		131.5	0.993	4.2			131.5	0.997	2.0
		136.5	0.994	3.9			136.5	0.998	1.7
		141.5	0.995	3.3			141.5	0.998	1.8
		146.5	0.995	3.1			146.5	0.998	1.4
		151.5	0.996	2.8			151.5	0.999	0.7
Run	Step edge	у	С	F	Run	Step edge	У	С	F

Hz

mm

Hz

mm

060410c	9	1.5	0.032	57.6	060411a	10	2.0	0.021	47.8
		6.5	0.037	62.4			7.0	0.035	68.2
		9.5	0.044	64.8			10.0	0.039	71.0
		11.5	0.049	70.5			12.0	0.041	71.8
		16.5	0.056	74.2			14.0	0.044	69.3
		19.5	0.069	83.9			17.0	0.045	76.9
		20.5	0.072	82.5			20.0	0.054	82.3
		21.5	0.081	90.4			22.0	0.069	94.9
		26.5	0.132	115.0			27.0	0.106	122.8
		31.5	0.226	149.4			32.0	0.182	156.9
		36.5	0.373	177.8			37.0	0.327	194.9
		41.5	0.524	165.7			42.0	0.515	194.0
		46.5	0.662	142.4			47.0	0.636	171.6
		51.5	0.768	109.2			52.0	0.798	120.3
		56.5	0.825	90.7			57.0	0.874	79.4
		56.5	0.867	71.2			62.0	0.910	56.5
		61.5	0.887	61.3			67.0	0.933	44.0
		66.5	0.917	48.3			72.0	0.955	32.5
		71.5	0.949	33.2			77.0	0.961	28.2
		76.5	0.957	28.6			82.0	0.965	22.4
		81.5	0.968	21.5			87.0	0.973	20.5
		86.5	0.977	16.6			92.0	0.981	16.7
		91.5	0.976	16.6			97.0	0.987	11.2
		96.5	0.985	12.0			102.0	0.988	10.1
		101.5	0.986	11.0			107.0	0.993	4.8
		111.5	0.990	7.1			112.0	0.993	6.4
		116.5	0.993	5.6			117.0	0.996	3.7
		121.5	0.995	4.1			122.0	0.995	3.6
		126.5	0.996	3.5			127.0	0.997	2.9
		131.5	0.996	2.9			132.0	0.998	2.3
		131.5	0.997	2.4			132.0	0.999	1.4
		136.5	0.998	1.6			137.0	0.998	1.2
		141.5	0.999	1.4			142.0	0.998	1.9
		146.5	0.999	0.8			147.0	0.999	1.4
							152.0	0.999	1.2

Location :	The University of Queensland (Australia)
Date :	April-June 2006
Experiments by :	G. CAROSI
Data processing by:	G. CAROSI and H. CHANSON
Data analysis by :	H. CHANSON and G. CAROSI
Experiment	Channel: width: 1.0 m, slope: 21.8° , h = 0.10 m, 1 = 0.25 m, 10 identical
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood
	staircase invert.
	$Q_w = 0.1164 \text{ m}^3/\text{s}, d_c = 0.115 \text{ m}, \text{Re} = 4.6 \text{ E}+5$
Instrumentation :	Double-tip conductivity probe ($\emptyset = 0.25 \text{ mm}, \Delta x = 7.0 \text{ mm}$).
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.
Comments :	Inflow conditions : broad-crested weir.
	Inception of free-surface aeration: between step edges 6 to 7.

Run	Step edge	У	V	С	F	Tu u'/V
	-	mm	m/s		Hz	
060530a	10	2.0	2.75	0.062	114.9	

7.0	2.80	0.061	108.8	0.56
12.0	2.92	0.065	108.8	0.65
14.0	2.92	0.061	104.7	0.89
17.0	3.04	0.062	103.2	0.54
20.0	3.11	0.100	138.1	0.30
22.0	3.18	0.104	139.4	
27.0	3.18	0.152	165.1	0.86
32.0	3.18	0.373	177.8	1.25
37.0	3.18	0.551	177.8	1.62
42.0	3.18	0.640	177.8	1.02
47.0	3.11	0.763	146.4	1.53
52.0	3.11	0.855	100.2	1.37
57.0	3.18	0.908	68.2	0.93
62.0	3.26	0.925	55.3	0.54
67.0	3.26	0.943	42.0	0.64
72.0	3.26	0.954	34.5	0.65
77.0	3.18	0.966	25.1	0.67
82.0	3.18	0.973	22.4	0.63
87.0	3.26	0.981	15.8	0.48
92.0	3.18	0.985	12.4	0.57
97.0	3.11	0.987	10.9	0.56
102.0	3.33	0.991	8.0	0.35
107.0	3.26	0.992	6.6	0.55
112.0	3.18	0.994	5.7	
117.0	3.11	0.995	4.7	
122.0	3.11	0.996	3.6	
127.0	2.98	0.997	2.9	
132.0	3.26	0.997	2.6	
137.0	3.33	0.998	1.7	
137.0	3.33	0.998	1.5	
142.0	3.33	0.999	1.3	
147.0	3.26	0.999	1.0	
152.0	4.00	0.999	1.0	

<u>F.3 Experimental data for $d_{\underline{c}}/h = 1.33$ </u>

Location :	The University of Queensland (Australia)
Date :	April-June 2006
Experiments by :	G. CAROSI
Data processing by:	G. CAROSI and H. CHANSON
Data analysis by :	H. CHANSON and G. CAROSI
Experiment	Channel: width: 1.0 m, slope: 21.8°, h = 0.10 m, l = 0.25 m, 10 identical
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood
	staircase invert.
	$Q_w = 0.1431 \text{ m}^3/\text{s}, d_c = 0.133 \text{ m}, \text{Re} = 5.7 \text{ E}+5$
Instrumentation :	Double-tip conductivity probe ($\emptyset = 0.25 \text{ mm}, \Delta x = 7.0 \text{ mm}$).
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.
Comments :	Inflow conditions : broad-crested weir.
	Inception of free-surface aeration: between step edges 6 to 7.

Run	Step edge	У	V	С	F	Tu u'/V
		mm	m/s		Hz	
060614a	7	1.0	2.50	0.039	54.3	0.72

		6.0	2.55	0.046	54.1	0.87	
		9.0	2.64	0.058	60.7	0.97	
		11.0	2.75	0.047	52.1	0.87	
		13.0	2.80	0.049	54.6	0.71	
		16.0	2.86	0.070	69.6	0.74	
		19.0	2.80	0.067	61.2	0.80	
		21.0	2.00	0.007	50.3	0.00	
		21.0	2.92	0.033	55.6	0.70	
		20.0	5.11	0.078	33.0	0.75	
		31.0	3.26	0.142	/6.2	0.88	
		36.0	3.26	0.243	95.7		
		41.0	3.33	0.449	118.4	1.06	
		46.0	3.33	0.614	111.6	1.12	
		51.0	3.33	0.737	93.4	0.97	
		56.0	3.26	0.812	72.8	0.76	
		61.0	3.33	0.892	47.8	0.61	
		66.0	3.26	0.891	52.5	0.50	
		71.0	3.33	0.949	28.2	0.50	
		76.0	3.33	0.959	22.3	0.41	
		81.0	3 33	0 948	27.4	0.41	
		86.0	3.42	0.965	19.2	0.37	
		91 O	3 33	0.976	1/.2	0.39	
		06.0	3.33	0.970	14.0	0.39	
		90.0 101.0	2.55	0.974	14.7	0.39	
		101.0	5.20 2.10	0.965	10.0	0.47	
		106.0	3.18	0.983	9.8	0.37	
		111.0	3.42	0.989	6.8	0.36	
		116.0	3.18	0.990	6.3	0.39	
		121.0	3.26	0.993	4.5	0.44	
		126.0	3.26	0.994	3.8	0.52	
		131.0	3.18	0.995	3.0	0.30	
		131.0	3.18	0.995	2.8	0.39	
		136.0	3.18	0.997	2.1	0.26	
		141.0	3.26	0.997	1.8		
060614b	8	1.0	2.92	0.027	50.4	0.54	
		6.0	2.92	0.030	51.1	0.53	
		9.0	2.98	0.027	46.7	0.49	
		11.0	2.86	0.026	43.9	0.43	
		13.0	3.11	0.033	50.6	0.51	
		16.0	2.10			0.50	
			I X	0.036	531	0.58	
		19.0	3.18 3.11	0.036	53.1 61.0	0.58	
		19.0 21.0	3.18 3.11 3.11	0.036 0.043 0.047	53.1 61.0 63.8	0.58 0.55 0.55	
		19.0 21.0 26.0	3.18 3.11 3.11 3.18	0.036 0.043 0.047	53.1 61.0 63.8	0.58 0.55 0.55	
		19.0 21.0 26.0	3.18 3.11 3.11 3.18 2.26	0.036 0.043 0.047 0.088 0.183	53.1 61.0 63.8 81.2	0.58 0.55 0.55 0.83	
		19.0 19.0 21.0 26.0 31.0	3.18 3.11 3.11 3.18 3.26	0.036 0.043 0.047 0.088 0.183	53.1 61.0 63.8 81.2 121.1	0.58 0.55 0.55 0.83 1.12	
		19.0 19.0 21.0 26.0 31.0 36.0	3.18 3.11 3.11 3.18 3.26 3.26	0.036 0.043 0.047 0.088 0.183 0.340	53.1 61.0 63.8 81.2 121.1 154.6	0.58 0.55 0.55 0.83 1.12	
		19.0 19.0 21.0 26.0 31.0 36.0 41.0	3.18 3.11 3.11 3.18 3.26 3.26 3.26	0.036 0.043 0.047 0.088 0.183 0.340 0.534	53.1 61.0 63.8 81.2 121.1 154.6 168.9	0.58 0.55 0.55 0.83 1.12 1.36	
		19.0 19.0 21.0 26.0 31.0 36.0 41.0 46.0	3.18 3.11 3.11 3.18 3.26 3.26 3.26 3.26 3.26	0.036 0.043 0.047 0.088 0.183 0.340 0.534 0.679	53.1 61.0 63.8 81.2 121.1 154.6 168.9 143.2	0.58 0.55 0.55 0.83 1.12 1.36 1.35	
		$ \begin{array}{r} 19.0 \\ 19.0 \\ 21.0 \\ 26.0 \\ 31.0 \\ 36.0 \\ 41.0 \\ 46.0 \\ 51.0 \\ \end{array} $	3.18 3.11 3.11 3.18 3.26 3.26 3.26 3.26 3.26 3.26	0.036 0.043 0.047 0.088 0.183 0.340 0.534 0.679 0.795	53.1 61.0 63.8 81.2 121.1 154.6 168.9 143.2 107.7	0.58 0.55 0.55 0.83 1.12 1.36 1.35 1.00	
		$ \begin{array}{r} 19.0 \\ 19.0 \\ 21.0 \\ 26.0 \\ 31.0 \\ 36.0 \\ 41.0 \\ 46.0 \\ 51.0 \\ 56.0 \\ \end{array} $	3.18 3.11 3.11 3.18 3.26 3.26 3.26 3.26 3.26 3.26 3.26 3.26	$\begin{array}{c} 0.036\\ 0.043\\ 0.047\\ 0.088\\ 0.183\\ 0.340\\ 0.534\\ 0.679\\ 0.795\\ 0.848\\ \end{array}$	53.1 61.0 63.8 81.2 121.1 154.6 168.9 143.2 107.7 83.6	0.58 0.55 0.55 0.83 1.12 1.36 1.35 1.00 0.63	
		$ 19.0 \\ 19.0 \\ 21.0 \\ 26.0 \\ 31.0 \\ 36.0 \\ 41.0 \\ 46.0 \\ 51.0 \\ 56.0 \\ 61.0 \\ $	3.18 3.11 3.11 3.18 3.26 3.26 3.26 3.26 3.26 3.26 3.33 3.26	$\begin{array}{c} 0.036\\ 0.043\\ 0.047\\ 0.088\\ 0.183\\ 0.340\\ 0.534\\ 0.679\\ 0.795\\ 0.848\\ 0.895 \end{array}$	53.1 61.0 63.8 81.2 121.1 154.6 168.9 143.2 107.7 83.6 61.9	0.58 0.55 0.55 0.83 1.12 1.36 1.35 1.00 0.63 0.59	
		$ 19.0 \\ 19.0 \\ 21.0 \\ 26.0 \\ 31.0 \\ 36.0 \\ 41.0 \\ 46.0 \\ 51.0 \\ 56.0 \\ 61.0 \\ 66.0 \\ $	3.18 3.11 3.11 3.18 3.26 3.26 3.26 3.26 3.26 3.26 3.26 3.26	$\begin{array}{c} 0.036\\ 0.043\\ 0.047\\ 0.088\\ 0.183\\ 0.340\\ 0.534\\ 0.679\\ 0.795\\ 0.848\\ 0.895\\ 0.920\\ \end{array}$	53.1 61.0 63.8 81.2 121.1 154.6 168.9 143.2 107.7 83.6 61.9 48.2	0.58 0.55 0.55 0.83 1.12 1.36 1.35 1.00 0.63 0.59 0.57	
		$ \begin{array}{r} 19.0 \\ 19.0 \\ 21.0 \\ 26.0 \\ 31.0 \\ 36.0 \\ 41.0 \\ 46.0 \\ 51.0 \\ 56.0 \\ 61.0 \\ 66.0 \\ 71.0 \\ \end{array} $	3.18 3.11 3.11 3.18 3.26 3.26 3.26 3.26 3.26 3.26 3.26 3.26	0.036 0.043 0.047 0.088 0.183 0.340 0.534 0.679 0.795 0.848 0.895 0.920 0.931	53.1 61.0 63.8 81.2 121.1 154.6 168.9 143.2 107.7 83.6 61.9 48.2 42.4	$\begin{array}{c} 0.58\\ 0.55\\ 0.55\\ 0.83\\ 1.12\\\\ 1.36\\ 1.35\\ 1.00\\ 0.63\\ 0.59\\ 0.57\\ 0.47\\ \end{array}$	
		$ \begin{array}{r} 19.0 \\ 19.0 \\ 21.0 \\ 26.0 \\ 31.0 \\ 36.0 \\ 41.0 \\ 46.0 \\ 51.0 \\ 56.0 \\ 61.0 \\ 66.0 \\ 71.0 \\ 76.0 \\ \end{array} $	3.18 3.11 3.11 3.18 3.26 3.33 3.26 3.33 3.42 3.42 3.42	0.036 0.043 0.047 0.088 0.183 0.340 0.534 0.679 0.795 0.848 0.895 0.920 0.931 0.946	53.1 61.0 63.8 81.2 121.1 154.6 168.9 143.2 107.7 83.6 61.9 48.2 42.4 33.7	$\begin{array}{c} 0.58\\ 0.55\\ 0.55\\ 0.83\\ 1.12\\\\ 1.36\\ 1.35\\ 1.00\\ 0.63\\ 0.59\\ 0.57\\ 0.47\\ 0.47\\ 0.47\\ \end{array}$	
		$ \begin{array}{r} 19.0 \\ 19.0 \\ 21.0 \\ 26.0 \\ 31.0 \\ 36.0 \\ 41.0 \\ 46.0 \\ 51.0 \\ 56.0 \\ 61.0 \\ 66.0 \\ 71.0 \\ 76.0 \\ 81.0 \\ \end{array} $	3.18 3.11 3.11 3.18 3.26 3.33 3.42 3.42 3.42 3.42 3.42	0.036 0.043 0.047 0.088 0.183 0.340 0.534 0.679 0.795 0.848 0.895 0.920 0.931 0.946 0.947	53.1 61.0 63.8 81.2 121.1 154.6 168.9 143.2 107.7 83.6 61.9 48.2 42.4 33.7 32.4	$\begin{array}{c} 0.58\\ 0.55\\ 0.55\\ 0.83\\ 1.12\\\\ 1.36\\ 1.35\\ 1.00\\ 0.63\\ 0.59\\ 0.57\\ 0.47\\ 0.47\\ 0.53\\ \end{array}$	
		$ 19.0 \\ 19.0 \\ 21.0 \\ 26.0 \\ 31.0 \\ 36.0 \\ 41.0 \\ 46.0 \\ 51.0 \\ 56.0 \\ 61.0 \\ 66.0 \\ 71.0 \\ 76.0 \\ 81.0 \\ 86.0 \\ $	3.18 3.11 3.11 3.18 3.26 3.33 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.33	0.036 0.043 0.047 0.088 0.183 0.340 0.534 0.679 0.795 0.848 0.895 0.920 0.920 0.931 0.946 0.947 0.963	53.1 61.0 63.8 81.2 121.1 154.6 168.9 143.2 107.7 83.6 61.9 48.2 42.4 33.7 32.4 24.1	$\begin{array}{c} 0.58\\ 0.55\\ 0.55\\ 0.83\\ 1.12\\\\ 1.36\\ 1.35\\ 1.00\\ 0.63\\ 0.59\\ 0.57\\ 0.47\\ 0.47\\ 0.47\\ 0.53\\ 0.55\\ \end{array}$	
		19.0 19.0 21.0 26.0 31.0 36.0 41.0 46.0 51.0 56.0 61.0 66.0 71.0 76.0 81.0 86.0 91.0	3.18 3.11 3.11 3.18 3.26 3.33 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.33 3.42 3.33 3.42 3.33 3.33 3.42 3.33 3.33 3.33	0.036 0.043 0.047 0.088 0.183 0.340 0.534 0.679 0.795 0.848 0.895 0.920 0.931 0.946 0.947 0.963 0.970	53.1 61.0 63.8 81.2 121.1 154.6 168.9 143.2 107.7 83.6 61.9 48.2 42.4 33.7 32.4 24.1 19.6	$\begin{array}{c} 0.58\\ 0.55\\ 0.55\\ 0.83\\ 1.12\\\\ 1.36\\ 1.35\\ 1.00\\ 0.63\\ 0.59\\ 0.57\\ 0.47\\ 0.47\\ 0.47\\ 0.53\\ 0.55\\ 0.55\\ 0.55\\ \end{array}$	
		19.0 19.0 21.0 26.0 31.0 36.0 41.0 46.0 51.0 56.0 61.0 66.0 71.0 76.0 81.0 86.0 91.0 96.0	3.18 3.11 3.11 3.18 3.26 3.33 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.42 3.33 3.33 3.33 3.33 3.33 3.33 3.33	0.036 0.043 0.047 0.088 0.183 0.340 0.534 0.679 0.795 0.848 0.895 0.920 0.931 0.946 0.947 0.963 0.974	53.1 61.0 63.8 81.2 121.1 154.6 168.9 143.2 107.7 83.6 61.9 48.2 42.4 33.7 32.4 24.1 19.6 17.1	$\begin{array}{c} 0.58\\ 0.55\\ 0.55\\ 0.83\\ 1.12\\\\ 1.36\\ 1.35\\ 1.00\\ 0.63\\ 0.59\\ 0.57\\ 0.47\\ 0.47\\ 0.53\\ 0.55\\ 0.55\\ 0.48\\ \end{array}$	

		106.0	3.42	0.983	11.4	0.41
		111.0	3.33	0.986	9.8	0.52
		116.0	3.33	0.992	5.7	0.49
		121.0	3.33	0.993	5.3	0.40
		126.0	3.33	0.994	4.4	0.47
		131.0	3 33	0.995	3.8	0.39
		131.0	3.26	0.996	2.8	0.37
		136.0	3.20	0.996	2.0	0.52
		141.0	3.33	0.990	2.7	0.52
0606150	0	0.5	2.55	0.997	02.7	0.82
000015a	9	0.5	2.09	0.037	92.1	0.03
		5.5 9.5	2.92	0.048	/4.8	0.92
		8.5	2.80	0.072	101.9	0.84
		10.5	2.98	0.062	85.3	0.92
		12.5	2.98	0.063	83.4	0.87
		15.5	2.98	0.070	87.5	0.89
		18.5	2.98	0.071	87.2	0.78
		20.5	3.11	0.080	91.5	0.74
		25.5	3.11	0.101	99.8	0.86
		30.5	3.18	0.149	120.3	0.94
		35.5	3.33	0.249	152.9	
		40.5	3.33	0.377	169.1	1.31
		45.5	3.33	0.556	162.6	1.47
		50.5	3.18	0.664	143.0	1.39
		55.5	3.26	0.766	112.4	1.03
		60.5	3.42	0.829	92.5	0.80
		65.5	3.42	0.858	81.8	0.94
		70.5	3.42	0.902	60.8	0.61
		75.5	3.33	0.910	52.6	0.71
		80.5	3.42	0.933	43.7	0.55
		85.5	3.42	0.946	33.4	0.58
		90.5	3.42	0.961	26.1	0.53
		95.5	3.50	0.968	22.4	0.44
		100.5	3.33	0.975	18.4	0.60
		105.5	3.33	0.982	13.4	0.63
		110.5	3.42	0.986	10.1	0.47
		115.5	3.33	0.990	7.7	0.50
		120.5	3.50	0.991	6.7	0.56
		125.5	3.42	0 994	4 5	0.39
		130.5	3.42	0.996	3 5	0.55
		130.5	3.50	0.997	2.5	0.33
		135.5	3 59	0.997	19	
		140.5	3.78	0.998	1.5	
060615b	10	140.5	2 75	0.042	87.7	
0000150	10	6.5	2.75	0.042	07.7	
		0.5	2.00	0.055	04.2	0.60
		9.J	2.09	0.032	94.3 99.0	0.09
		11.5	2.90	0.040	00.0	0.55
		15.5	2.90	0.052	90.0	0.57
		10.5	3.11 2.26	0.035	07.8 102.0	0.50
		19.5	5.20 2.26	0.003	102.0	
		20.5	3.26	0.081	110.8	0.64
		31.5	3.26	0.126	145.3	0.75
		36.5	3.42	0.187	166.8	1.18
		41.5	3.42	0.410	199.7	1.77
		46.5	3.33	0.571	199.2	1.79
		51.5	3.33	0.678	161.2	1.94
		56.5	3.42	0.814	112.5	1.32

61.5	3.42	0.886	76.8	1.07
66.5	3.42	0.924	51.0	0.80
71.5	3.50	0.944	38.8	0.71
76.5	3.50	0.955	31.8	0.71
81.5	3.59	0.967	23.7	0.68
86.5	3.50	0.974	20.0	0.85
91.5	3.42	0.981	15.6	0.48
96.5	3.50	0.985	12.3	0.49
101.5	3.50	0.989	8.3	0.51
106.5	3.50	0.991	7.1	0.49
111.5	3.50	0.993	5.5	0.61
116.5	3.50	0.995	4.4	0.50
121.5	3.59	0.995	4.0	0.45
126.5	3.59	0.997	2.8	0.47
131.5	3.59	0.996	2.7	0.17
136.5	3.42	0.998	1.6	1.15
141.5	3.59	0.999	1.2	
146.5	3.78	0.999	1.4	
151.5	3.42	0.999	1.0	

<u>F.4 Experimental data for $d_{\underline{C}}/h = 1.45$ </u>

Location :	The University of Queensland (Australia)
Date :	April-June 2006
Experiments by :	G. CAROSI
Data processing by:	G. CAROSI and H. CHANSON
Data analysis by :	H. CHANSON and G. CAROSI
Experiment	Channel: width: 1.0 m, slope: 21.8° , h = 0.10 m, 1 = 0.25 m, 10 identical
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood
	staircase invert.
	$Q_w = 0.1612 \text{ m}^3/\text{s}, d_c = 0.145 \text{ m}, \text{Re} = 6.4 \text{ E}+5$
Instrumentation :	Single-tip conductivity probe ($\emptyset = 0.35 \text{ mm}$).
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.
Comments :	Inflow conditions : broad-crested weir.
	Inception of free-surface aeration: between step edges 7 to 8.

Run	Step	У	С	F	Run	Step	У	С	F
	edge			TT		edge			
		mm		HZ			mm		HZ
060512a	8	1.5	0.001	3.2	060512b	9	1.5	0.013	26.3
		6.5	0.003	6.1			6.5	0.025	38.4
		9.5	0.004	7.5			9.5	0.027	37.8
		11.5	0.003	6.5			11.5	0.031	39.9
		13.5	0.006	10.0			13.5	0.031	39.5
		16.5	0.005	9.0			16.5	0.038	44.5
		19.5	0.007	11.8			19.5	0.037	43.8
		21.5	0.009	13.0			21.5	0.042	45.8
		26.5	0.013	16.7			26.5	0.059	55.6
		31.5	0.027	27.4			31.5	0.091	72.7
		36.5	0.068	48.6			36.5	0.159	100.5
		41.5	0.171	84.6			41.5	0.276	131.6
		46.5	0.345	121.0			46.5	0.411	142.7
		51.5	0.512	129.4			51.5	0.562	135.0
		56.5	0.669	119.1			56.5	0.666	117.8

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96.50.95625.396.50.96323.6101.50.97217.3101.50.97019.4106.50.97614.3106.50.98014.0111.50.98310.7111.50.98013.6116.50.98510.2116.50.98311.8121.50.9906.8121.50.9888.3126.50.9926.4126.50.9907.0	
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111.50.98310.7111.50.98013.6116.50.98510.2116.50.98311.8121.50.9906.8121.50.9888.3126.50.9926.4126.50.9907.0	
116.50.98510.2116.50.98311.8121.50.9906.8121.50.9888.3126.50.9926.4126.50.9907.0	
121.50.9906.8121.50.9888.3126.50.9926.4126.50.9907.0	
126.5 0.992 6.4 126.5 0.990 7.0	
131.5 0.991 6.5 131.5 0.991 6.2	
131.5 0.994 4.0 131.5 0.994 4.2	
136.5 0.995 3.3 136.5 0.996 2.6	
141.5 0.997 2.7 141.5 0.997 3.0	
146.5 0.997 2.1 146.5 0.997 2.2	
151.5 0.998 1.8	

Run	Sten	V	С	F
IXull	edge	У	C	I
	cuge	mm		Hz
060511b	10	2.0	0.008	20.8
		7.0	0.012	27.9
		10.0	0.015	30.2
		12.0	0.013	25.6
		14.0	0.017	31.2
		17.0	0.018	32.8
		20.0	0.025	37.5
		22.0	0.024	37.5
		27.0	0.030	43.7
		32.0	0.055	61.7
		37.0	0.092	81.6
		42.0	0.211	130.5
		47.0	0.306	147.4
		52.0	0.536	157.9
		57.0	0.655	137.6
		62.0	0.775	107.2
		67.0	0.858	76.4
		72.0	0.904	54.3
		77.0	0.927	43.1
		82.0	0.940	35.8
		87.0	0.962	24.7
		92.0	0.969	19.8
		97.0	0.977	16.0
		102.0	0.981	13.2
		107.0	0.987	9.8
		112.0	0.990	7.8
		117.0	0.992	6.2
		122.0	0.994	4.8
		127.0	0.996	3.4
		132.0	0.997	2.7
		132.0	0.997	2.2
		137.0	0.997	2.1

$\begin{array}{cccccccccccccccccccccccccccccccccccc$	142.0	0.998	1.8
152.0 0.999 1.1	147.0	0.998	1.6
10210 01777 111	152.0	0.999	1.1

Location :	The University of Queensland (Australia)
Date :	April-June 2006
Experiments by :	G. CAROSI
Data processing by:	G. CAROSI and H. CHANSON
Data analysis by :	H. CHANSON and G. CAROSI
Experiment	Channel: width: 1.0 m, slope: 21.8° , h = 0.10 m, 1 = 0.25 m, 10 identical
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood
	staircase invert.
	$Q_{\rm W} = 0.1612 \text{ m}^3/\text{s}, d_{\rm C} = 0.145 \text{ m}, \text{Re} = 6.4 \text{ E}+5$
Instrumentation :	Double-tip conductivity probe ($\emptyset = 0.25 \text{ mm}, \Delta x = 7.0 \text{ mm}$).
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.
Comments :	Inflow conditions : broad-crested weir.
	Inception of free-surface aeration: between step edges 7 to 8.

Run	Step	у	V	С	F	Tu
	edge					u'/V
	-	mm	m/s		Hz	
060530b	10	2.0	3.42	0.007	17.5	0.51
		7.0	3.18	0.010	21.8	0.56
		10.0	3.42	0.011	23.5	
		12.0	3.42	0.013	26.5	0.47
		14.0	3.50	0.017	29.6	0.62
		17.0	3.50	0.030	52.4	0.60
		20.0	3.42	0.027	48.2	0.58
		22.0	3.50	0.030	50.0	0.60
		27.0	3.50	0.041	58.9	0.57
		32.0	3.68	0.068	81.6	0.73
		37.0	3.68	0.124	107.1	0.95
		42.0	3.68	0.196	133.1	1.34
		47.0	3.68	0.348	165.9	1.83
		52.0	3.68	0.521	168.9	1.57
		57.0	3.68	0.715	136.8	1.32
		62.0	3.68	0.790	113.1	1.14
		67.0	3.59	0.858	83.6	0.92
		72.0	3.59	0.913	57.0	0.68
		77.0	3.59	0.935	44.2	1.89
		82.0	3.59	0.951	36.5	0.55
		87.0	3.59	0.965	27.7	0.53
		92.0	3.59	0.976	20.2	0.47
		97.0	3.59	0.980	16.5	0.50
		102.0	3.59	0.982	13.9	0.47
		107.0	3.68	0.989	9.9	0.33
		112.0	3.68	0.990	8.1	0.41
		117.0	3.59	0.992	6.9	0.40
		122.0	3.59	0.995	4.8	0.11
		127.0	3.68	0.995	4.0	
		132.0	3.59	0.995	4.3	
		132.0	3.68	0.997	2.9	
		137.0	3.78	0.997	2.6	
		142.0	3.59	0.998	1.8	
		147.0	3.78	0.998	1.7	

Location :	The University of Queensland (Australia)				
Date :	April-June 2006				
Experiments by :	G. CAROSI				
Data processing by:	G. CAROSI and H. CHANSON				
Data analysis by :	H. CHANSON and G. CAROSI				
Experiment	Channel: width: 1.0 m, slope: 21.8° , h = 0.10 m, 1 = 0.25 m, 10 identical				
characteristics :	steps. Open channel with perspex sidewalls and smooth marine plywood				
	staircase invert.				
	$Q_w = 0.1798 \text{ m}^3/\text{s}, d_c = 0.157 \text{ m}, \text{Re} = 7.1 \text{ E}+5$				
Instrumentation :	Single-tip conductivity probe ($\emptyset = 0.35 \text{ mm}$).				
	Scan rate: 20 kHz per probe sensor, Sampling duration: 45 sec.				
Comments :	Inflow conditions : broad-crested weir.				
	Inception of free-surface aeration: between step edges 7 and 8.				

<u>F.5 Experimental data for $d_{\underline{c}}/h = 1.57$ </u>

Run	Step	У	С	F	Run	Step	У	С	F
	edge	mm		H_7		edge	mm		H_7
060404a	8	1.0	0.004	3.8	060404b	9	1.0	0.003	8.0
000 4 0 4 0	0	1.0 6.0	0.004	1.0	0004040	,	6.0	0.003	19.2
		9.0	0.000	1.0			9.0	0.012	20.7
		11.0	0.001	1.6			11.0	0.014	19.6
		13.0	0.003	3.5			13.0	0.010	15.0
		16.0	0.005	4.7			16.0	0.013	17.6
		19.0	0.002	2.8			19.0	0.011	14.5
		21.0	0.001	2.5			21.0	0.009	12.9
		26.0	0.002	3.6			26.0	0.014	15.6
		31.0	0.004	4.5			31.0	0.023	23.9
		36.0	0.011	9.7			36.0	0.046	37.0
		41.0	0.024	18.6			41.0	0.102	61.6
		46.0	0.080	39.1			46.0	0.178	82.2
		51.0	0.193	69.0			51.0	0.344	109.1
		56.0	0.411	98.6			56.0	0.457	113.9
		61.0	0.556	99.0			61.0	0.618	110.4
		66.0	0.748	84.7			66.0	0.720	96.9
		71.0	0.812	68.2			71.0	0.796	79.6
		76.0	0.874	53.1			76.0	0.840	66.7
		81.0	0.913	42.3			81.0	0.873	56.1
		86.0	0.932	34.3			86.0	0.897	49.8
		91.0	0.930	32.8			91.0	0.926	37.2
		96.0	0.954	24.5			96.0	0.955	25.1
		101.0	0.962	20.3			101.0	0.956	24.6
		106.0	0.969	17.3			106.0	0.974	15.7
		111.0	0.978	14.8			111.0	0.979	13.7
		116.0	0.983	10.8			116.0	0.983	11.4
		121.0	0.984	9.3			121.0	0.990	7.4
		126.0	0.988	8.1			126.0	0.991	6.2
		131.0	0.988	7.0			131.0	0.993	5.2
		131.0	0.992	5.0			131.0	0.994	4.2
		136.0	0.996	3.3			136.0	0.996	2.9
		141.0	0.996	2.9			141.0	0.997	2.4

151.0 0.998 1.9 151.0 0.998	1.4

Run	Step	У	C	F
	eage	mm		Hz
060404c	10	1.0	0.002	7.3
		6.0	0.006	13.5
		9.0	0.007	15.1
		11.0	0.007	13.8
		13.0	0.007	14.9
		16.0	0.009	17.6
		19.0	0.010	18.6
		21.0	0.013	21.7
		26.0	0.013	20.4
		31.0	0.020	27.2
		36.0	0.044	43.6
		41.0	0.077	61.0
		46.0	0.121	82.5
		51.0	0.222	108.9
		56.0	0.417	135.2
		61.0	0.564	131.7
		66.0	0.687	116.1
		71.0	0.773	96.7
		76.0	0.840	74.4
		81.0	0.880	61.0
		86.0	0.907	49.0
		91.0	0.925	44.2
		96.0	0.950	30.1
		101.0	0.958	27.1
		106.0	0.972	20.1
		111.0	0.979	14.5
		116.0	0.980	13.8
		121.0	0.986	10.1
		126.0	0.988	8.1
		131.0	0.992	6.2
		131.0	0.994	4.6
		136.0	0.995	4.0
		141.0	0.995	3.8
		146.0	0.996	2.6
		151.0	0.997	2.3

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