

## ABOUT THIS PACKET

This packet is designed based on the GED formula sheet. It contains explanations, examples and problems to work out. The point is to train to take the GED test and be familiar with the formulas used in the test.

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GED

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## Appreciation to the following

www.ged.com for the formula sheet they provide.
www.math-drills.com for work sheets
www.mathisfun.com for ideas regarding graphics and methods for presenting concepts www.virtualnerd.com for video links.
www.kutasoftware.com

## Introduction

Inside this packet are many tools you'll need to pass the math GED test. These tools are formulas.

You do not need to memorize each formula, just how to read them and use them.

The first thing you need to do is change your mindset from, "I cannot do this," to, "I can do this." Secondly do not fear formulas. Rather, learn to understand and read them.

First things first. Let us look at a few formulas:
Letters used in math are variables. A better way to look at variables is as place holders for an unknown number.
$A=\pi r^{2}$
$c=\Pi d$
$P=2 L+2 W$

In these formulas we are looking for the values of $\mathrm{A}, \mathrm{C}$ and P . We are looking for value of A, the lone letter on one side of the equal sign.

The other parts are $\pi$, or pi, 3.14 , and d which means diameter, $\mathrm{L}=$ Length, and $\mathrm{W}=$ width. P means perimeter.

In math you will be using these formulas, and you will be given the diameter, the length and width. We plug the numbers into the variable, the term used is substitution, that is to put the numbers in place of the letters they represent.

Note: The math used in these three formulas is, multiplication and addition. Most formulas use basic math, adding, subtracting, multiplying and dividing, and an occasional square root.

Take a breath, relax, take an attitude of, "I am going to learn this no matter how long it takes. I am sticking to it, keeping a positive attitude of, 'I can.'"

The next step is learning how to use a calculator. You cannot take your cellphone into the testing room; therefore, it is better that you use a calculator while in class. The calculator GED testing service uses for its virtual calculator is the TI 30sx. It is what we will use in class. Master the functions and life will become much easier.

Other helpful tips:
$>$ Ask for help.
$>$ Use a tutor if available.
$>$ Do your homework! Do more if necessary.

## Mathematics Formula Sheet, 2014 GED:

## Taken from GED testing Service.

Area of a:

| square | $\mathrm{A}=s^{2}$ |
| :--- | :--- |
| rectangle | $\mathrm{A}=l w$ |
| parallelogram | $\mathrm{A}=b h$ |
| triangle | $\mathrm{A}=\frac{1}{2} b h$ |
| trapezoid | $\mathrm{A}=\frac{1}{2} h\left(b_{1}+b_{2}\right)$ |
| circle | $\mathrm{A}=\pi r^{2}$ |
| Perimeter of a: | $\mathrm{P}=4 s$ |
| square | $\mathrm{P}=2 l+2 w$ |
| rectangle | $\mathrm{P}=s_{1}+s_{2}+s_{3}$ |
| triangle | $\mathrm{C}=2 \pi r \mathrm{OR} \mathrm{C}=\pi d ; \pi \approx 3.14$ |
| Circumference of a circle <br> Surface area and volume of a: | $\mathrm{SA}=p h+2 B$ |
| rectangular/right prism | $\mathrm{SA}=2 \pi r h+2 \pi r^{2}$ |
| cylinder | $\mathrm{SA}=\frac{1}{2} p s+B$ |
| pyramid | $\mathrm{SA}=\pi r s+\pi r^{2}$ |
| cone | $\mathrm{SA}=4 \pi r^{2}$ |
| sphere | $\mathrm{V}=B h$ |

( $p=$ perimeter of base with area $B ; \pi \approx 3.14$ )

## Data

| mean | mean is equal to the total of the values of a data set, <br> divided by the number of elements in the data set |
| :--- | :--- |
| median | median is the middle value in an odd number of ordered <br> values of a data set, or the mean of the two middle <br> values in an even number of ordered values in a data set |

## Algebra

| slope of a line | $m=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}$ |
| :--- | :--- |
| slope-intercept form of the equation of a line | $y=m x+b$ |
| point-slope form of the equation of a line | $y-y_{1}=m\left(x-x_{1}\right)$ |
| standard form of a quadratic equation | $y=a x^{2}+b x+c$ |
| quadratic formula | $x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$ |
|  | $a^{2}+b^{2}=c^{2}$ <br> Pythagorean Theorem <br> simple interest <br>  <br> distance formula <br> total cost |

[^0]
## Order of operations

There is a set pattern of doing math that must be followed. This allows various people, doing the same problem, to come up with the same answer. In school, many teachers called it PEMDAS.

```
P = Parentheses ()[]{}
E = Exponents 4 4
M = Multiplication
D = Division
A = Addition
S = Subtraction
```

The basic concept is, you have to do each one of these mathematical operations first before moving on to the next, 1) clear parentheses, 2) solve exponents, 3) Do any multiplication, 4) solve any division, 5) do any addition, and 6) do any subtraction. This is true but there are times when we will do some of these steps out of order.

When solving problems, read the problem LEFT to RIGHT. Always do the math LEFT TO RIGHT. However, the exceptions to this is clearing parentheses and exponents. Those almost always must be done first.

Example 1:

$$
9^{2} \div+14 \times(11-2)-15
$$

| $\begin{gathered} \text { 1: Parenthesis } 9^{2} \div 3+14 \times(11-2)-15 \\ \mathbf{9}^{2} \div 3+14 \times 9-15 \\ \hline \end{gathered}$ | $\text { 2) Exponents } \begin{aligned} \mathbf{9}^{2} \div \mathbf{3}+\mathbf{1 4} \times \mathbf{9 - 1 5} \\ \mathbf{8 1} \div \mathbf{3}+\mathbf{1 4} \times \mathbf{9 - 1 5} \\ \hline \end{aligned}$ |
| :---: | :---: |
| 3) Multiplication or Division, whichever comes first. $81 \div 3+14 \times \mathbf{9 - 1 5}$ $27+14 \times 9-15$ | 4) Now we can do the multiplication, it comes $2^{\text {nd }}$. $\begin{gathered} 27+14 \times 9-15 \\ 27+126-15 \\ \hline \end{gathered}$ |
| 5) Addition or Subtraction, whichever comes first. $\begin{gathered} 27+126-15 \\ 153-15 \end{gathered}$ | Addition or subtraction, whichever comes first. $\begin{gathered} 153-15 \\ 153-15=138 \end{gathered}$ |

Notice: Multiplication or Division, whichever comes first. Same for Addition and Subtraction, reading left to right. We see, reading left to right that division came first, then multiplication. For addition and subtraction, addition came first.

Sometimes, there will be exponents within parenthesis, or parentheses within parentheses.
$9^{2} \div 3 \times\left(11-2^{2}\right)-15$ We first must do the $2^{2}$ before we can clear the parentheses.
$9^{2} \div 3 \times\left(2+\left(11-2^{2}\right)\right)-15$. In this example, we'd have to do the exponent in the () first, then (11-4), once that is done, then we'd have to add the 2 , to clear the outer set of ( ) .
$9^{2} \div 3 \times(2+(11-4))-15$, First do the exponent inside the 2 nd set of ( )
$9^{2} \div 3 \times(2+7)-15$, Next, the subtraction inside the 2 nd set of ()
$9^{2} \div 3 \times 9-15$, Now, do the first exponent.
$81 \div 3 \times 9-15$, Multiplication or division whichever comes first then subtraction.

$$
\text { Answer = } 228
$$

## Order of Operations

## Solve each expression using the correct order of operations

$10-3^{2} \div 9$
$7^{2} \div(4+3)$
$\left(6+2^{2}\right) \times 10$
$\left(4^{3}-10\right) \div 6$
$9^{2} \div(4+5)$
$10+8-6^{2} \div\left(3^{2} x 4\right)$
$12-3+5 \times\left(6^{2} \div 2\right)$
$8 \div(10-9)^{3} \times 7+4^{2}$
$\left(8+5^{2}\right) x\left((9-7)^{2} \div 2\right)$
$(10 \times(6+4)) \div\left(2^{3}-7\right)^{2}$

## One and Two Step Equations

Vocabulary:
Terms: are the smallest pieces of an equation, a number like 2 , or $3 x$, are both terms.
Expression: And expression is only a piece like $x+5$ or $3 x-2 y$. There is no equal sign.
Equation: An equation is different from an expression simply because it has an = equal sigh and can be solved.

Solution: The answer after you have solved the equation.
Variables: Variables are letters used in place of an unknown number.
Inverse operations: Inverse means the opposite; the opposite of multiplication is division.
the opposite of division is multiplication and so on.
Example 1: Solve one step equation: $r+12=25$
The task here is to find out what the value of $r$ is. The $r$ represents an unknown number. Make sure you pay attention to the following steps.


## One Step:

The goal is to isolate the $r$ by itself on one side of the equal sign.
To do so, we need to get rid of the +12 . We use the inverse of +12 which is -12 . A negative 12 erases a positive 12 and we are left with nothing.

Balance: What you do to one side of the equal sign, you must do to the other side. You must now us the same - 12 and subtract it from 25 .

Doing so, we have $r$ alone and 13 on the other side of the equal sign.
Example 2: Solve $5+x=3$


Notice that the variable x is in a different place. Doesn't matter. We still need to isolate the x on one side of the equation.

Using the opposite of a positive 5 , we use a -5 . They destroy each other and we are left with;

$$
x--2
$$

Example 3: Solve the following

$$
\frac{x}{5}=5 \quad \begin{aligned}
& \text { Very different looking? What does the x over } 5 \text { mean? } \\
& \begin{array}{l}
\text { Division, right? What's the opposite of multiplication? } \\
\text { Division! Recall, (3)5 means } 3 \times 5 \text {. () next to a letter or a } \\
\text { number indicates multiplication }
\end{array}
\end{aligned}
$$

## Our answer $\mathbf{x}=\mathbf{2 5}$

Infinite Algebra 1

## One-Step Equations

## Solve each equation.

1) $26=8+v$
2) $15+b=23$
3) $-15+n=-9$
4) $m+4=-12$
5) $x-7=13$
6) $m-9=-13$
7) $p-6=-5$
8) $v-15=-27$
9) $n+16=9$
10) $-104=8 x$
11) $14 b=-56$
12) $-6=\frac{b}{18}$
13) $10 n=40$

## Two Step Equations:

Now that you a basic understanding of one step equations, let's look at two step equations
Example 1: Solve $8 \mathrm{~b}+5=29$
The first step is the same as a one-step equation.


Example 2: Solve, two different types of equations.


Notice: both have 2 steps.
In the first problem we use a-2 and subtract from both sides. Then we divide the 3 off from the x .

In the second problem we have to remove the -2 by using $\mathrm{a}+2$, again on both sides. Then we use multiplication on both sides, and we are left with the x on one side and 28 on the other as the
solution.
Example 3: Solve $5+\frac{x}{6}=13$

## Step 1

Subtract 5 from both sides of the equation

Step 2
Then multiply both sides by 6

## Step 3

Simplify

$$
5+\frac{x}{6}=13
$$



$$
6\left(\frac{x}{6}\right)=(8) 6
$$

$$
x=48
$$

Recall, we did this with the one step equation on the previous page.

Algebra 1

## Two-Step Equations Practice

Solve each equation.

1) $3+5 r=-47$
2) $-5+\frac{n}{3}=-8$
3) $-53=3-8 n$
4) $\frac{b}{2}-2=0$
5) $-10 x+6=-74$
6) $\frac{m}{9}-7=-8$
7) $3-5 v=-22$
8) $9+\frac{r}{6}=7$
9) $-8=-3+\frac{m}{3}$
10) $7=\frac{x}{9}+8$

## Combining Like Terms

## Vocabulary:

Polynomial: A polynomial simply means, many numbers.
Terms: Recall, the word term can mean a number, 2, 7, 9. It can mean a number attached to a variable, such as 3 x or 8 y .

Like terms are terms that are similar. 2,7 and 9 are all numbers. $3 \mathrm{x}, 4 \mathrm{x}$ both have numbers and the same variable, as does $6 y$ and 9 y . These are like terms.

To solve some algebraic equations or simplify expressions, we must be able to combine like terms.

Example 1: simplify this expression. $3 x+5+7 y+2+9 x-4 y$

## We can use a chart to help us figure this out

Left to right, place the terms into the chart.
Numbers with $x$, numbers with $y$ and then numbers that are alone.

| $\# \mathbf{X}$ | \#Y | Numbers along |
| :---: | :---: | :---: |
| 3 x | 7 y | 5 |
| 9 x | -4 y | 2 |
| 12 x | 3 y | 7 |

Our simplified expression is $12 x+3 y+7$
You must pay attention to negative and positive numbers (integers) and recall the rules. The minus and plus signs attach to the terms now. $3 \mathrm{x}-2$, the 2 is listed as -2 .

Example 2: simplify $7 m+14 m-6 n-5 n+2 m$

| $\mathbf{\# m}$ | $\mathbf{\# m}$ | Numbers along |
| :---: | :---: | :---: |
| 7 m | -6 n |  |
| 14 m | -5 n |  |
| 2 m |  |  |
| 23 m | -11 n |  |

Our simplified expression is $23 m-11 n$

Example 3: Simplify $5 x+8 x+10 x^{2}-7 x^{2}-4 x$
We can use a chart to help us figure this out
Left to right, place the terms into the chart.

| $\# \mathbf{X}$ | $\# \boldsymbol{x}^{\mathbf{2}}$ | Numbers along |
| :---: | :---: | :---: |
| 5 x | $10 x^{2}$ |  |
| 8 x | $-7 x^{2}$ |  |
| -4 x |  |  |
| 9 x | $3 x^{2}$ |  |

Our simplified expression is $3 x^{2}-9 x$
Example 4: Simplify $4 x^{3}+3 x^{2}-7-x^{2}+2$

## We can use a chart to help us figure this out

Left to right, place the terms into the chart.

| $\# \boldsymbol{X}^{\mathbf{3}}$ | $\boldsymbol{\#} \boldsymbol{x}^{\mathbf{2}}$ | Numbers along |
| :---: | :---: | :---: |
| $4 x^{3}$ | $3 x^{2}$ | -7 |
|  | $x^{2}$ | 2 |
| $4 x^{3}$ | $2 x^{2}$ | 5 |

Our simplified expression is $4 x^{3}+2 x^{2}+5$
Use this charting method to sort out the terms. Don't forget integers. Add or subtract, combine as necessary and there you go, you have your simplified expression.
Example 5: Distributive property states $3(4+5 x)$ that you can multiply the 3 into the items within the parenthesis.

$$
3(4+5 x) \text { multiply the } 3 \text { and } 4 \text {, and the } 3 \text { and } 5 x=12+15 X
$$

Simplify: $-2(-3 x+4)-7$
Distribute the -2 into the parenthesis, $-2(-3 x+4)-7$
Combine like terms: $6 x-8-7$.
Simplified equation is now $6 x-15$

## CLASSWORK - Combining Like Terms \& Distributive Property

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## Combine like terms to simplify each expression.

1) $-4 x+5 x$
2) $1+5 v+v-6$
3) $4 n+4+1+3 n$
4) $11 a+11 a$
5) $-2 x-8-7 x+2$
6) $7 v+6 v$
7) $-8 x-10 x$
8) $6-7 n-2 n-8$
9) $2 k-k$
10) $-p-11+3$
11) $9 n+3 n$
12) $12 x+11-4$

## Use Distributive Property.

13) $3(-7-8 n)$
14) $-8(1+5 m)$
15) $8(r+1)$
16) $8(7 x+8)$
17) $2(6 n-8)$
18) $-3(8-b)$
19) $-5(8 v-2)$
20) $-2(x-5)$
21) $-(3 a-3)$
22) $-2(7-2 n)$
23) $-8(5-3 v)$
24) $-7(6 x-3)$

First, use Distributive Property, then Combine Llike Terms to simplify each expression.
25) $-n+4(n+1)$
26) $-3(1-3 x)+2 x$
27) $-2(-3 k+4)-7$
28) $-3 p-(-8+4 p)$
29) $-4+6(-4 x+3)$
30) $3 n+3(1+8 n)$
31) $-2+5(4+3 r)$
32) $-1+3(m+4)$
33) $-(-n+2)-2 n$
34) $-3(5+2 x)-7$

## Finding the circumference and area of a circle

The circumference, c , of a circle is the measure around the outside of the circle.

Diameter, $\mathbf{d}$, is the measurement across the center of the circle.

Radius, $\mathbf{r}$, is a measurement from the center of the circle to anywhere on the outside line of the circle.

You will need to know what the $d$, is in order


Area of a circle $=\pi \times$ radius $^{2}$

Circumference of a circle $=\pi \times$ diameter
remember that the diameter $=2 \times$ radius to find the circumference.

You will need to know what the $r$, is in order to find the area.

Formulas:

## Circumference

$c=\pi d$
Area
$A=\pi r^{2}$

Let us do this problem. What is the circumference and area of this circle?

Recall, when letters or symbols are right next to each other, that indicates multiplication
$\qquad$
$C=3.14 \times$

$$
C=
$$

$\qquad$

$$
A=3.14 \times ـ^{2}
$$

$A=$ $\qquad$

## Circumference and Area of Circles (A)

Find the circumference and area of each circle to one decimal place.


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## Finding the perimeter, area and missing side of a right triangle



Perimeter, $p$, in any triangle $p=a+b+c$, add up the three sides.

Area, $a=\frac{1}{2} b h$
b = base
h = height
a is usually the vertical side, 3 cm which is also the height.

The base $b$ is always the horizontal or bottom side.
Let's do this triangle
$p=3+4+5=12 \mathrm{~cm}$
In your calculator you enter, $0.5 \times 4 \times 3=6 \mathrm{sqcm}$ (note, must answer in square units sqft, sqin, sqcm.

## Pythagorean Theorem

$$
a^{2}+b^{2}=c^{2}
$$


$a$ is the vertical leg/side and $b$ is the horizontal or bottom side, $a=3 \mathrm{~cm}, \mathrm{~b}=4 \mathrm{~cm}$.

The longer or sloped side is c the hypotenuse.
Now enter them into the formula.
$3^{2}+4^{2}=c^{2}$
$9+16=c^{2}$
$25=c^{2}$ Not done yet, we have to unsquared $c$
$\sqrt{25}=c$ find the square root of 25.
5 = c, so five is the measurement of the side c

Now try one on your own


Calculate the perimeter and area for each triangle.
1.

$\mathrm{P}=? \mathrm{~mm}$
$\mathrm{A}=$ ? $\mathrm{mm}^{2}$
3.


$$
\begin{aligned}
& \mathrm{P}=? \mathrm{ft} \\
& \mathrm{~A}=? \mathrm{ft}^{2}
\end{aligned}
$$

5. 



$$
\begin{aligned}
& \mathrm{P}=? \text { in } \\
& \mathrm{A}=? \mathrm{in}^{2}
\end{aligned}
$$

4. 



$$
\begin{aligned}
& \mathrm{P}=? \mathrm{mi} \\
& \mathrm{~A}=? \mathrm{mi}^{2}
\end{aligned}
$$

2. 


$\mathrm{P}=? \mathrm{AU}$
$\mathrm{A}=? \mathrm{AU}^{2}$
6.

$\mathrm{P}=$ ? AU
$\mathrm{A}=? \mathrm{AU}^{2}$

## Pythagorean Theorem (A)

Name: $\qquad$ Date: $\qquad$
Calculate the missing side measurement using $a^{2}+b^{2}=c^{2}$.
1.

2.

3.

4.

5.

6.


[^1]

This is what is meant by surface area. This is the view if we unroll the cylinder, and add the top and bottom of the cylinder

## Formula: surface area

We must find the area of the top and bottom parts of the cylinder and the side of the cylinder itself.

Area of the top is $\pi r^{2}$
Area of the bottom is $\pi r^{2}$
Area of the side is $2 \pi r h$
Put together into one formula: $s a=2 \pi r^{2}+2 \pi r h$


$$
\pi=3.14, r=\text { radius and } h=\text { height }
$$

Let's try a problem.


$$
s a=2 \pi r^{2}+2 \pi r h
$$

Fill in the blanks and enter into calculator $\mathrm{Sa}=2 \times 3.14 \times$ $\qquad$ $+2 \times$ $\qquad$ $\times$ $\qquad$ $\times$ $\qquad$
$\mathrm{Sa}=$ $\qquad$

Volume is how much room is inside the cylinder. The formula is $v=\pi r^{2} \mathrm{~h}$.
Fill in the blanks and enter into the calculator.
$v=3.14 \times$ $\qquad$ $\times$ $\qquad$ $v=$ $\qquad$

Calculate the surface area and volume for each cylinder.
Surface Area $=\left(\pi r^{2} \times 2\right)+(\pi d \times h) \quad$ Volume $=\pi r^{2} \times h \quad d=2 r$
1.

$r=1.2 \mathrm{~km} \quad h=3.6 \mathrm{~km}$
Surface Area $=$
Volume $=$
2.

$d=12.6 \mathrm{~cm} \quad h=7.5 \mathrm{~cm}$
Surface Area $=$
Volume $=$
4.

$d=12 \mathrm{~m} \quad h=18.6 \mathrm{~m}$
Surface Area $=$
Volume $=$
$r=18 \mathrm{ft} \quad h=27.2 \mathrm{ft}$
Surface Area $=$
Volume $=$

## Finding the surface area and volume of a rectangle



## Surface area of a rectangle.

If we unfold a box, we notice that there are six sides that need to be taken into consideration.

And of course, we have a special formula for it.

Surface area formula: $s a=p h+2 b$
Break it down
$p=$ perimeter of the bottom flat side. Recall $p=21+2 w \quad$ The perimeter is $2 \times 10+2 \times 5, p=30 \mathrm{~cm}$
$b=$ the area of the flat bottom, $a=l w$
The base is $10 \times 5, a=50$
$\mathrm{h}=$ the height of the box.
Height of the box is 6 cm
Now use these numbers to fill in the formula, enter into calculator

## Let's try a problem



Perimeter, $2\left(\_\_\right)+2\left(\_\_\right)=$ $\qquad$
The base is $\qquad$ $\times$ $\qquad$ $+$ $\qquad$
Height = $\qquad$
Fill in the blanks
sa = $\qquad$ $\times$ $\qquad$ $+2 \times$ $\qquad$ , sa = $\qquad$

Volume formula $v=b h$
$\mathrm{v}=$ $\qquad$ $\times$ $\qquad$ , $\mathrm{v}=$ $\qquad$

## Volume and Surface Area of Rectangular Prisms (A)

Instructions: Find the volume and surface area for each rectangular prism.
1)

2)

3)

4)

5)

6)



Note: in the formula the variable $\mathbf{S}$, = the slope of the cone. The easiest formula to use to find the value of $\mathbf{S}$ is: $\mathbf{S}=\sqrt{ }(\mathbf{r} 2+\mathbf{h 2})$, which means, the square root of the radius squared plus the height squared. Simply input into calculator as is stated.

Don't forget to find the volume of the cone.
Let's do a problem.
Fill in the blanks with the right numbers


To find $s$, enter $\sqrt{ـ_{\_}{ }^{2}+\__{2}}{ }^{2}$ into your calculator Use the answer for s in the surface area equation.

$$
s a=3.14 \times \ldots \times \ldots+3.14 \times \ldots{ }_{2}{ }^{2}
$$

Your answer should be 296.73


#### Abstract

Surface Area and Volume of Cones (A)


Calculate the surface area and volume for each cone.

$$
\text { Surface Area }=\pi r\left(r+\sqrt{h^{2}+r^{2}}\right) \quad \text { Volume }=\pi r^{2} \frac{h}{3}
$$

1. 


2.

3.

4.


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## Finding the surface area and volume of a Sphere



| $\mathrm{SA}=4 \pi \mathrm{r}^{2}$ |
| :---: |
| $4^{*} \pi^{\star} 9^{2}$ |
| 4* $\pi^{*} 81$ |
| $321 \pi$ |
| SA $=1017.9 \mathrm{in}^{2}$ |
| $\mathrm{V}=(4 / 3) \pi \mathrm{r}^{\wedge} 3$ |
| (4/3) $\pi^{*} 9^{\wedge} 3$ |
| (4/3) $\pi^{*} 729$ |
| 972 |
| 3053. |

Finding the SA and Volume of a sphere looks daunting but if you know how to use the TI 30sx, it's no problem at all.

Notice, you only need one number, the radius for both formulas. The rest are constants, numbers that don't change.
$\pi=3.14$
$r=$ radius, note, SA radius squared but in volume it is cubed

4
$\frac{4}{3}$
$s a=4 \pi r^{2}$
$4 \times 3.14 \times$ $\qquad$ $\frac{4}{3} \times 3.14 x$ $\qquad$
 ${ }^{3}$

Understanding what numbers to input and how to input them into the calculator will make the difference.

## Surface Area and Volume of Spheres (A)

Calculate the surface area and volume for each sphere.

$$
\text { Surface Area }=4 \pi r^{2} \quad \text { Volume }=\frac{4}{3} \pi r^{3}
$$

1. 


2.

3.

4.


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| 1. A cosmetics company that makes <br> small cylindrical bars of soap wraps <br> the bars in plastic prior to shipping. <br> Find the surface area of a bar of soap <br> if the diameter is 5 cm and the height <br> is 2 cm . Use 3.14 for $\pi$. | 2. A company needs to buy boxes that <br> will hold their products. When stacked <br> up the products measure 15 inches <br> long, 8 inches wide, and 10 inches <br> high. What is the volume of the box <br> needed? |
| :--- | :--- |

## How to determine Mean and Median

What is Mean? This is just a fancy word for average. So, the next question is, how do you find the mean/average?

In order to find the mean or average, we must add up all the numbers in a set, i.e. $\{23,18,10$, $24,45,50$.$\} Add them together we get 170$. Not done yet. Now you must divide 170 by the number of items in the set. Items are the numbers in the set. There are 6 items in this set.
$170 \div 6=28.333$ is the mean or average.
You try: $\{110,35,88,45,90,125,79,66\}$
Add up the numbers = $\qquad$ . How many items are in the set? $\qquad$

Do the math, $\qquad$ $\div$ $\qquad$ $=$ $\qquad$ Mean =, $\qquad$

## Median:

To find the median, place the data set in order, smallest number to largest number (numerical order).
$\{10,18,23,24,45,50\}$, this data set has an even number of items, 6 . The median is the exact center of the set. If you notice that is between 23 and 24 . There is nothing there. In order to find the median of this set, add the 23 , and 24 together, $23+24=47$. Take this number, 47 and divide by 2 . The Median is 23.5 .

However, if the number set was $\{10,18,20,23,24,45,50\}$. This data set has an odd number of Items 7. To find the Median, count left to right and right to left and find the exact center.

$$
\{10,18,20,23, \underline{24,45,50}\}
$$

Notice, now there is a whole number, 23, dead center.

## Finding the Range:

if you subtract the smallest number from the largest number, in the case above, 125-35 = 88. This is the range of the data set.

## Finding the Mode:

If you look at the data set and notice there are two of the same numbers, ie: $\{110,35,88,45$, $90,125,90,79,66\}$, there are two 90 s. this is the mode, 90 . If there only single numbers there is no mode.

## Mean, Median, Mode, and Range (A)

Calculate the mean, median, mode, and range of each set of numbers.

1) $\{1,10,6,4,2,5,3,6,5,4\}$
2) $\{5,10,10,6,8,6,3,7,5,3\}$
3) $\{2,2,2,4,3,9,7,2,7,9\}$
4) $\{6,3,5,7,3,8,4,3,9,3\}$
5) $\{6,4,9,8,3,9,7,9,6,3\}$
6) $\{7,4,4,6,3,5,3,8,5,3\}$
7) $\{8,8,7,8,8,3,4,6,8,7\}$
8) $\{3,4,7,8,3,4,8,8,5,7\}$
1. The Blazers scored, $94,134,56,120$, 99,128 and 56 last week, what is the mean and median score for the week?

Mean
Median
3. Your environmental class project is to calculate the mean, median, mode and range of rain fall over a year's time. You have collected the following date in inches.
$\{36,10,28,8,38,28,30,17,20,35,44,37,29,36\}$
Mean $\qquad$ Median $\qquad$ Mode $\qquad$ Range $\qquad$
4. Quentin and Michael are on a bowling team. Below are their bowling scores.

Michael: 220, 240, 219, 199, 189
Quentin: 230, 204, 244, 200, 215
How much higher is Michael's median score than Quentin's median score?
2. You are looking to rent an apartment. You have looked at many apartments and want to find the mean and median to help you make a good decision. The rents are, \$1900, \$1300, \$1100, \$1800, \$950, \$1250, \$1700 and $\$ 2000$.
Mean
Median
$\qquad$
5. A bakery sells 30 cupcakes at $\$ 3.00$ each, 12 cakes at $\$ 20.00$ each, and 40 loaves of bread at $\$ 4.00$ each. What is the average price of an item sold?

## Coordinate Plan and Slope of a Line

To understand the slope of line, consider the following picture. You notice that $8 \%$ and the angle that represents downhill, this is slope.


Notice the downgrade sign on the coordinate plane, the angle of the line is the slope of the line.


## What do we need to know?

In order to use a graph and draw a line we have what is called ordered pairs. They are points on the graph represented by numbers. In the illustration below, we see to black dots on the blue arrow. To draw a line on a graph, there must be two points to connect. These two sets of numbers are called ordered pairs. For this graph they are $(-4,-2)$ and $(2,6)$.


Notice that the two black lines on the graph, one is horizontal and labeled X , the other is vertical and labeled Y .

These are called the $x$ and $y$ axis.
All ordered pairs represent an $X$ and $Y$ on the grid and are always expressed this way, $(X, Y) . X$ is always first.

Note: We always read a graph from left to right, so the first set of coordinates is, $(-4,-2)$, moving up to $(2,6)$.

Not to worry, let's try a few on the next page.

Put a dot on the graph for each set of ordered pairs.

1) $(6,2)$, let's do this together,

Find the $X$ first, in this case it is 6 , then trace it up the y axis up 2. Make a dot.

Notice, if you move to the left on the $X$ axis the numbers become negative, and if you move down on the $Y$ axis, the numbers also become

Negative. Give it a try!
2) $(-4,4)$
3) $(8,-4)$

4) $(2,6)$

Finding Slope when you have a graph and a line drawn on the graph.


Note where the dots are, "Coordinates." Always read left to right. The first dot is on the $y$ axis at $(0,1)$. There is no $x$ coordinate as the dot is on the $y$ axis. Moving left, we see the second dot is $(2,4)$

Starting at the dot on the $Y$ one, we can count up the $y$ axis to the four. We went up 3 spaces. Now count right two spaces for the 2 on the $X$.

This is called rise over run, $\frac{\text { Rise }}{\text { Run }}$. We went up 3 , and over 2.3 is the rise, 2 is the run and looks like this. $\frac{3}{2}$

Now it's your turn. Doing exactly what was done in the example of above, start with the lower left-hand dot, coordinate, and the do the second dot.

Don't forget to right it as $\frac{\text { Rise }}{\text { Run }}$

Finding the Slope of a Line Given a set of Ordered Pairs


Here we are, formula time.

$$
M=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}
$$

M stands for slope, the $\frac{Y_{2}-Y_{1}}{X_{2}-X_{1}}$ are simply empty place holders. They stand for two sets of ordered pairs. The $y_{2}$ and $X_{2}$ stand for the $x$ and $y$ coordinate in the second set of ordered pairs. Likewise the $Y_{1}$ and $X_{1}$ stands for the first set. Here is a set of ordered pairs. $(3,4)$ and $(5,1)$.

The first set is $(3,4)$ is your $X_{1}$ and $Y_{1}$
The second set $(5,1)$ is your $X_{2}$ and $Y_{2}$ Looking at it a different way

$$
\frac{\left(X_{1}, Y_{1}\right),\left(X_{2}, Y_{2}\right)}{(3,4),(5,1)}
$$

This always helps me keep track of $M=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}$ Taking this formula, fill in the $X$ and $Y s$ with the correct numbers and do the "Math!"
$M=\frac{1-4}{5-3}$ Here you are going to have to recall integer rules. $M=-\frac{3}{2}$ this is the slope of the line. Notice it is negative. the numbers and where they go.

Your Turn.

1) Determine the slope of a line given the following ordered pairs, ( $-2,-1$ ), (4, 3).
2) What is the slope of a line that has the following ordered pairs, $(2,1),(6,3)$ ?
3) What is the slope of a line that passes through $(-6,3)$ and $(4,-3)$ ?

Name:
Teacher :
$\qquad$ Score:

Date :

## Four Quadrant Ordered Pairs



Tell what point is located at each ordered pair.

1) $(+0,+0)$ $\qquad$ 3) $(-4,+0)$ $\qquad$ 5) $(-4,+4)$ $\qquad$ 7) $(+8,-1)$ $\qquad$
2) $(-4,-7)$ $\qquad$
3) $(+5,-6)$ $\qquad$
4) $(-5,-1)$ $\qquad$
5) $(-8,-1)$ $\qquad$

Write the ordered pair for each given point.
$\begin{array}{rll}\text { 9) } & \text { F } \\ \text { 10) } \\ \end{array}$
11) W $\qquad$
13) I
14) $R$ $\qquad$
15) A $\qquad$
$\qquad$
12) $N$ $\qquad$
16) $X$ $\qquad$

Plot the following points on the coordinate grid.
17) $\mathbf{Q}(+7,+1)$
19) $E(-7,-2)$
21) $G(-8,+8)$
23)
L ( $-5,-5$ )
18) $O(+4,-5)$
20) $T(-4,+2)$
22) $\mathrm{U}(+6,-7)$
24) $P(-1,-6)$
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Kuta Software - Infinite Algebra 1
Finding Slope From a Graph
Find the slope of each line.
1)

3)

5)

7)


Name $\qquad$ Date $\qquad$ Period
2)

4)

6)

8)


Name:
Score:
Teacher : $\qquad$ Date :

## Sketch Each Line

1) 



3)



6)

8)


## Y intercept Form

Simply put, the $Y$ intercept is where a line crosses the $Y$ axis.

If we look at the $y$ intercept as in the graph below, we see its ordered pair is $(0,4)$ Note: as the line crosses the $y$ axis on the graph, there is no $X$ value to consider.


Looking at the following graphs, what are the ordered pairs?



The formula $\mathrm{y}=\mathrm{mx}+\mathrm{b}$ is a standard form of the equation. We must understand what it means.
Defining the letters.
Recall that in an ordered pair you have an $x$ coordinate and a $y$ coordinate. Therefore, in the formula $y=m x+b$, we note, the $m$ is the slope of the line, and the $b$ is the $y$ intercept.
$\begin{aligned} y= & =\frac{4}{5} x+7 \\ & \downarrow \text {-intereept }(0,7) \\ & \downarrow \text { lope } m=-\frac{4}{5}\end{aligned}$
If $\mathrm{m}=\mathrm{a}$ whole number, $\mathrm{y}=3 \mathrm{x}+2$
The slope 3 is $\frac{\text { Rise of } 3}{\text { Run of } 1}$ or simply $\frac{3}{1} x$
If there is just an x , then it is a slope of 1

In this example, $-\frac{4}{5}$ is the slope, recall this means $\frac{\text { Rise }}{\text { Run }}$.
The 7 is the $y$ intercept. We can use this to plot the next point and draw a line.


Your chance to try find the slope $m$ and the y intercept, y int.

$$
\begin{array}{ll}
Y=-2 x+6 & m=\_\quad y \text { int } \\
Y=\frac{3}{7} x+1 & m=\ldots \quad y \text { int }
\end{array}
$$

Coordinate planes, slope and y intercept application problems
\(\left.$$
\begin{array}{|l|l|l|}\hline \begin{array}{l}\text { 1. Find the slope of a line that passes } \\
\text { through the following points, }(-2,6), \\
\text { and }(6,-2) .\end{array} & \begin{array}{l}\text { The following equation is used to calculate } \\
\text { bike rental. Per hour rental fee, } \$ 3 \text {, onetime } \\
\text { fee of } \$ 10 .\end{array}
$$ <br>

Y=3 \mathrm{x}+10\end{array}\right\}\)\begin{tabular}{l}

2. | Graph a line for the following equation |
| :--- |
| $\mathrm{y}=3 \mathrm{x}+7$ | <br>

| 3. Write an equation that you can use to |
| :--- |
| calculate bike rental. You will charge a |
| flat fee of $\$ 5.00$ and an hourly rental rate |
| of $\$ 2.00$ per hour. | <br>

\hline 4. Using your equation from \#3, fill in the <br>
total cost based upon your equation.
\end{tabular}



Kuta Software - Infinite Algebra 1
Finding Slope From Two Points
Find the slope of the line through each pair of points.

1) $(19,-16),(-7,-15)$
2) $(1,-19),(-2,-7)$
3) $(-4,7),(-6,-4)$
4) $(20,8),(9,16)$
5) $(17,-13),(17,8)$
6) $(19,3),(20,3)$
7) $(3,0),(-11,-15)$
8) $(19,-2),(-11,10)$

Name:
Teacher :

## Sketch Each Line

1) 


2)

equation $y=-3 x-3$
3)

equation $y=\frac{1}{2} x+4$
4)

5)




## Point Slope Form

Point slope is another linear equation and is useful when we know the coordinates, ordered pair, of one point on the graph and the slope, $m$. With this information we can calculate the $y=m x+b$ and graph.

The formula
Or another way to see it.


Lets look at an example


Ordered pair, $x=-1$ and $y=-5$
Slope or $m=4$.
All you need to do is put the -1 into the $x_{1}$ and -5 into the $y_{1}$ and 4 into the $m$.

Then treat like other equations and isolate the $y$ on one side of the $=$ sign
$y-y_{1}=m\left(x-x_{1}\right)$
Input point and slope

$$
Y-(-5)=4(x-(-1))
$$

$Y+5=4(x+1) \quad$ Distribute the 4 , that is $4 * x$ and $4 * 1$ to

$$
Y+5=4 x+4 \quad \text { clear the parenthesis }
$$

$$
Y=4 x-1
$$

$$
\text { Subtract the } 5 \text { from both sides of the }
$$

Also, note the $y-(-5)$ and the ( $x-(-1)$ ) that the double negatives turn the -5 into a positive 5 and the -1 into a positive 1.

$$
y-y_{1}=m\left(x-x_{1}\right)
$$

Known point $\longrightarrow(-1,-5) \mathrm{m}=4 \longleftrightarrow$ Known Slope

Your turn

1) $m=3,(2,1)$
$y=$ $\qquad$
2) $m=8,(2,3)$
$y=$ $\qquad$

## Algebra 1

Name
5.5 Point-Slope Form

O 2014 Kuta Software LIC. All rights roserved.
Date $\qquad$ Period Write the point-slope form of the equation of the line through the given point with the given slope.

1) through: $(2,3)$, slope $=2$
2) through: $(-4,-5)$, slope $=\frac{5}{4}$
3) through: $(4,-3)$, slope $=\frac{1}{4}$
4) through: $(-2,0)$, slope $=-1$
5) through: $(-2,2)$, slope $=-\frac{3}{2}$
6) through: $(0,-5)$, slope $=-\frac{3}{2}$
7) through: $(1,4)$, slope $=7$
8) through: $(-3,5)$, slope $=-\frac{1}{3}$
9) through: $(-5,1)$, slope $=\frac{2}{5}$
10) through: $(-2,-5)$, slope $=4$
11) through: $(-2,-2)$, slope $=2$
12) through: $(2,-2)$, slope $=-3$
13) through: $(1,-1)$, slope $=-1$
14) through: $(-5,2)$, slope $=\frac{3}{5}$
15) through: $(-1,4)$, slope $=-9$
16) through: $(2,-2)$, slope $=-\frac{7}{2}$
17) through: $(-5,-4)$, slope $=\frac{2}{5}$
18) through: $(1,-1)$, slope $=-3$
19) through: $(4,2)$, slope $=0$
20) through: $(2,-1)$, slope $=-\frac{3}{2}$

## Inequalities

The term, inequality in math means a statement that uses the following symbols
Less then: <
Greater than: >
Less than or equal to: $\leq$,
Greater than or equal to: $\geq$,
Solving inequalities is no different than other equations. $X+2>12$, as we all equations we are trying to isolate the variable $x$ on one side of the sign, in this case, $>$.
$x+2-2>12-2$, subtract 2 from both sides of the equation.
$x>10$
Exception: When you divide or multiply in the final step with a negative number then the sign flips to the opposite sign.
$>-2 x+5 \geq 25$, subtracting 5 from both sides we are left with $-2 x \geq 20$. We must divide the 2 from the $x$ and 20, our answer will be $x \leq 10$. Note the sign flipped to less than or equal to.

## Another example:

Joan is planning her wedding. She has 200 guests coming. She rents a hall for $\$ 2000$. She only has $\$ 7500$ to spend for renting the hall and feeding her guests. She needs to know how much she can spend on each guest for lunch. Write an inequality to express this situation.

200 guests
$x$ is the unknown lunch cost per guest
\$2000, hall rental
We write it like this
$\$ 7500$ is maximum $\$ \$$ to spend.

$$
200 x+2000 \leq 7500
$$

We solve inequalities the way we solve all equations by isolating the variable. Using the example for Joan, we start by subtracting 2000 from both sides of the equation. Then we divide 200 from both sides and we are left with $x$ on onside and a remained on the other side of the equation.

```
200x+2000\leq7500
    -2000 -2000 1 1 st subtract from both sides
```

    \(\underline{200} x \leq \underline{5500} \quad 2^{\text {nd }}\) divide both sides by 200
    200200
    \(x \leq 27.5 \quad\) Cost per person \(x\) is \(\$ 27.50\) per person maximum.
    Kuta Software - Infinite Algebra 1
Two-Step Inequalities

Name $\qquad$
Date $\qquad$ Period $\qquad$
Solve each inequality and graph its solution.

1) $2 x+4 \geq 24$

2) $\frac{m}{3}-3 \leq-6$

3) $-4(-4+x)>56$
4) $-b-2>8$
5) $-4(3+n)>-32$
${ }_{1}{ }_{2}$
6) $4+\frac{n}{3}<6$
7) $-3(r-4) \geq 0$

8) $-7 x+7 \leq-56$
9) $-3(p-7) \geq 21$
$\rightarrow-5-4-2-1 \quad 0 \quad 12_{3}$

10) $\frac{-9+a}{15}>1$


## Inequalities word problems

Use the first problem as an example of how to write an inequality, see if you can do it.

1) At the beginning of summer, Keith has $\$ 500$ in a saving account. He wants to spend $\$ 50$ a week on food, clothing, movie tickets and popcorn over the summer. Keith wants to have $\$ 200$ left by the end of summer. Which inequality will tell him how many weeks over the summer he can spend $\$ 50$ and still have $\$ 200$ in his savings account?
a. $500 x-200 \leq 50$
b. $50 x+200 \geq 500$
c. $50 x-200 \leq 500$
d. $200 x-50 \geq 50$
2) Joe charges a flat rate of $\$ 3.00$ and an additional $\$ 1.50$ per mile to ride in his cab. If Joan has $\$ 10$ to spend on a taxi ride, how far can she go? Make an inequality that can be used to calculate this.
3) Alyson is trying to decide if she wants to join a gym. The membership has a flat fee of $\$ 125$ for pool and hot tub maintenance and charges $\$ 20$ a month for membership. She has only $\$ 400$ in her budget to pay for this. Write an equality that she can use to determine how many months she can afford.
4) You own a roofing company and you want to create an equation that you can use to price out jobs. You charge a straight labor fee of $\$ 3000$, and you charge 82 per square. Your customers generally do not want to pay more than $\$ 5000$. Which inequality represents this problem?
5) Its prom night and your son wants to rent a limo to take his girlfriend to the prom and then to dinner after words. The Limo costs $\$ 125$ per hour, and you will be renting the limo for five hours. The limo company charges $\$ 3.50$ a mile the limo is driven. Your son wants to drive his girlfriend to dinner and then around town. You only have $\$ 800$ for this. Create an inequality to find out how many miles they can drive around.

## Quadratic Functions

So far, all the formulas you have done have been linear, that is, they make straight lines when graphed. This section focuses on quadratic functions. When graphed, they created a curved line. So, what the is a quadratic function?
$>$ The best way to describe a function is comparing it to a snack vending machine.
$>$ There are many different types of snacks, each costing a different amount.
$>$ You put in a certain amount and you get out a certain product.

This is basically what a function is, you put in certain known numbers, do the math and it returns a certain answer. Change the numbers you put in, and you get a different answer.


Lets look at it!


Coefficients are known numbers. The Constant is always the same.
The $f(x)$ means, the function of $x$. That is, the $x$ is the variable $x$ are numbers that change, the input, like the vending machine, the choice you make and the associated cost.

Example: $f(x)=x^{2}-6 x+5$

We can start by drawing a table For the $x$, we can input whatever numbers we want but keep is simple, start with zero.

This is called a table of values

| $\mathbf{X}$ | 0 | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{F}(\mathbf{x})$ |  |  |  |  |  |  |

We can now input the numbers for $x$ into the equation and do the calculations.

| $\mathbf{X}$ | 0 | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{F}(\mathbf{x})$ | 5 | 0 | -3 | -4 | -3 | 0 |

## Let's do the math: start with 0

$f(x)=(0)^{2}-6(0)+5$
We substitute a 0 in place of all the $x^{\prime} s$.
$f(x)=0-0+5$
Do the math, 2 times 0 squared $=0,6$ times zero $=0$
$f(x)=5$
Our final answer.

## Let's do the math: now do the 1

$f(x)=(1)^{2}-6(1)+5$
We substitute a 0 in place of all the $x^{\prime} s$.
$f(x)=1-6+5$
Do the math, 2 times 0 squared $=0,6$ times zero $=0$
$f(x)=0$
Our final answer.

Do this for all the numbers in the table.
Once you have the table filled out you can plot points on a graph.
The $x$ are $x$ coordinates and the $f(x)$ are $y$ coordinates in ordered pairs.

| $\mathbf{X}$ | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{F}(\mathbf{x})$ | 5 | 0 | -3 | -4 | -3 | 0 |
| Pairs | $(0,5)$ | $(1,0)$ | $(2,-3)$ | $(3,-4)$ | $(4,-3)$ | $(5,0)$ |



Notice, the line is not a straight line but curved.
Vocabulary: Palabra, this is what this type of line is called.

Note how the coordinates are placed on the graph and then the line is drawn through the points.

The very tip of the line is called the vertex

Quadratic Function practice problem
$f(x)=-x^{2}-6 x-1$

Table of Values

| $\mathbf{X}$ | -6 | -5 | -4 | -3 | -2 | -1 | 0 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{F}(\mathbf{x})$ |  |  |  |  |  |  |  |  |
| Pairs |  |  |  |  |  |  |  |  |

Input each number into the equation, do the math and complete the table for $f(x)$. Once done, graph your points and connect it with a line.


Name: $\qquad$ Score: $\qquad$

Printable Math Worksheets @ www.mathworksheets4kids.com

## Quadratic Equations

This is the standard form of a quadratic equation.

$$
a x^{2}+b x+c=0
$$

$a, b, c$ going to be known numbers, coefficients.

This is the quadratic formula used to solve quadratic equations. Try and read it!

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$

Let's see how this works.
Problem: $5 x^{2}+6 x+1=0$. Notice that this equation follows the standard from shown above.
Therefore, we have our $a, b$, and $c$. substitute the proper numbers for $a, b, c$.
$a=5$
$b=6$

$$
x=\frac{-6 \pm \sqrt{6^{2}-4(5)(1)}}{2(5)}
$$

$c=1$

$$
\begin{gathered}
x=\frac{-6 \pm \sqrt{36-20}}{10} \\
x=\frac{-6 \pm \sqrt{16}}{10} \\
x=\frac{-6 \pm 4}{10}
\end{gathered}
$$

Here we can split this into two problems because it is -6 plus or minus.

$$
\begin{array}{cc}
x=\frac{-6+4}{10} & x=\frac{-6-4}{10} \\
x=-\frac{1}{5} & x=-1
\end{array}
$$

Your Turn
$2 x^{2}+3 x-20=$
$\mathrm{a}=$
$b=$
$\mathrm{c}=$


Kuta Software - Infinite Algebra 1
Using the Quadratic Formula

Name $\qquad$
Date $\qquad$ Period $\qquad$
Solve each equation with the quadratic formula.

1) $m^{2}-5 m-14=0$
2) $b^{2}-4 b+4=0$
3) $2 m^{2}+2 m-12=0$
4) $2 x^{2}-3 x-5=0$
5) $x^{2}+4 x+3=0$
6) $2 x^{2}+3 x-20=0$
7) $4 b^{2}+8 b+7=4$
8) $2 m^{2}-7 m-13=-10$

## Quadradic Function word problems

Instructions: Use a table to determine the correct answers

1. A fire work rocket is launched off a hill above a lake. The rocket will fall into the lake after it has reached its maximum height. Given the following function, $f(x)=-16 x^{2}+64 x+80$,
a. $\quad 160 \mathrm{ft}$
b. 120 ft
c. 90
d. 144 ft
2. You are a world class fast ball pitcher. You will be tossing a ball straight up into the air. You are 6 feet tall so when you release the ball, it will be 9 feet off the ground. You will use -16 for the force of gravity acting on the ball and the speed of the ball will be 90 miles an hour. Given these numbers, and using a table, determine the maximum height the ball will reach in 4.4 seconds. Your function is $f(x)=-16 x^{2}+90 x+9$

## CONGRATUALTIONS: YOU HAVE FINISHED THE BOOK.

## Answer Sheets

## Order of Operations

## Solve each expression using the correct order of operations

$10-3^{2} \div 9$
$7^{2} \div(4+3)$
$\left(6+2^{2}\right) \times 10$
9
7
$9^{2} \div(4+5)$
$10+8-6^{2} \div\left(3^{2} x 4\right)$
9
9
17
$12-3+5 \times\left(6^{2} \div 2\right)$
$8 \div(10-9)^{3} \times 7+4^{2}$
99 72
$\left(8+5^{2}\right) x\left((9-7)^{2} \div 2\right)$
$(10 \times(6+4)) \div\left(2^{3}-7\right)^{2}$
66

## Infinite Algebra 1

## One-Step Equations

## Name

$\qquad$

Solve each equation.

1) $26=8+v$
\{18\}
2) $15+b=23$
\{8\}
3) $3+p=8$
\{5\}
4) $-15+n=-9$
\{6\}
5) $x-7=13$
\{20\}
6) $p-6=-5$
\{1\}
7) $n+16=9$
$\{-7\}$
8) $14 b=-56$
$\{-4\}$
9) $10 n=40$
\{4\}

## Algebra 1

## Two-Step Equations Practice

Solve each equation.

1) $3+5 r=-47$
2) $-5+\frac{n}{3}=-8$
$-10$
-9
3) $-53=3-8 n$
4) $\frac{b}{2}-2=0$

7

4
5) $-10 x+6=-74$

8
7) $3-5 v=-22$

5
9) $-8=-3+\frac{m}{3}$
$-15$
$-9$
8) $9+\frac{r}{6}=7$
$-12$
10) $7=\frac{x}{9}+8$
6) $\frac{m}{9}-7=-8$
$-9$

## CLASSWORK - Combining Like Terms \& Distributive Property

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## Combine like terms to simplify each expression.

1) $-4 x+5 x \quad x$
2) $1+5 v+v-6-5+6 v$
3) $4 n+4+1+3 n 7 n+5$
4) $11 a+11 a 22 a$
5) $-2 x-8-7 x+2-9 x-6$
6) $7 v+6 v 13 v$
7) $-8 x-10 x-18 x$
8) $6-7 n-2 n-8-2-9 n$
9) $2 k-k k$
10) $-p-11+3-p-8$
11) $9 n+3 n \quad 12 n$
12) $12 x+11-4 \quad 12 x+7$

## Use Distributive Property.

13) $3(-7-8 n)-21-24 n$
14) $-8(1+5 m)-8-40 m$
15) $8(r+1) 8 r+8$
16) $8(7 x+8) 56 x+64$
17) $2(6 n-8) 12 n-16$
18) $-3(8-b)-24+3 b$
19) $-5(8 v-2)-40 v+10$
20) $-2(x-5)-2 x+10$
21) $-(3 a-3)-3 a+3$
22) $-2(7-2 n)-14+4 n$
23) $-8(5-3 v)-40+24 v$
24) $-7(6 x-3)-42 x+21$

First, use Distributive Property, then Combine Llike Terms to simplify each expression.
25) $-n+4(n+1)$
$3 n+4$
27) $-2(-3 k+4)-7$
$6 k-15$
29) $-4+6(-4 x+3)$
$14-24 x$
31) $-2+5(4+3 r)$
$18+15 r$
33) $-(-n+2)-2 n$
$-n-2$

$$
\text { 26) } \begin{gathered}
-3(1-3 x)+2 x \\
-3+11 x
\end{gathered}
$$

28) $-3 p-(-8+4 p)$
$-7 p+8$
29) $3 n+3(1+8 n)$
$27 n+3$
30) $-1+3(m+4)$
$11+3 m$
31) $-3(5+2 x)-7$
$-22-6 x$

## Circumference and Area of Circles (A) Answers

Find the circumference and area of each circle to one decimal place.

$\mathrm{d}=7.9 \mathrm{~cm}$
$\mathrm{C}=24.8 \mathrm{~cm}$
$\mathrm{~A}=49$ sq. cm

$\mathrm{d}=6.3 \mathrm{~cm}$
$\mathrm{C}=19.8 \mathrm{~cm}$
$\mathrm{A}=31.2$ sq. cm

$\mathrm{r}=7.3 \mathrm{~cm}$
$\mathrm{C}=45.9 \mathrm{~cm}$
$\mathrm{~A}=167.4 \mathrm{sq} . \mathrm{cm}$

$\mathrm{d}=5.5 \mathrm{~cm}$
$\mathrm{C}=17.3 \mathrm{~cm}$
$\mathrm{A}=23.8$ sq. cm

$\mathrm{d}=9.5 \mathrm{~mm}$
$\mathrm{C}=29.8 \mathrm{~mm}$
$\mathrm{A}=70.9$ sq. mm

$\mathrm{r}=1 \mathrm{yd}$
$\mathrm{C}=6.3 \mathrm{yd}$
$\mathrm{A}=3.1$ sq. yd

$\mathrm{r}=9.7 \mathrm{~m}$
$\mathrm{C}=60.9 \mathrm{~m}$
$\mathrm{A}=295.6$ sq. m

$\mathrm{d}=7 \mathrm{~m}$
$\mathrm{C}=22 \mathrm{~m}$
$\mathrm{A}=38.5$ sq. m

$\mathrm{r}=0.5 \mathrm{~m}$
$\mathrm{C}=3.1 \mathrm{~m}$
$\mathrm{A}=0.8$ sq. m

$\mathrm{r}=2.4 \mathrm{~cm}$
$\mathrm{C}=15.1 \mathrm{~cm}$
$\mathrm{A}=18.1$ sq. cm

$\mathrm{d}=0.9 \mathrm{mi}$
$\mathrm{C}=2.8 \mathrm{mi}$
$\mathrm{A}=0.6$ sq. mi

$\mathrm{r}=8$ in
$\mathrm{C}=50.3$ in
$\mathrm{A}=201.1$ sq. in

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## Perimeter and Area of Triangles (A) Answers

Calculate the perimeter and area for each triangle.
1.

$\mathrm{P}=62.9 \mathrm{~mm}$
$\mathrm{A}=168.3 \mathrm{~mm}^{2}$
3.

$\mathrm{P}=23.8 \mathrm{ft}$
$\mathrm{A}=24 \mathrm{ft}^{2}$
4.

$\mathrm{P}=29.8 \mathrm{mi}$
$\mathrm{A}=37.525 \mathrm{mi}^{2}$
5.

$\mathrm{P}=41.3 \mathrm{in}$
$\mathrm{A}=73.08 \mathrm{in}^{2}$
6.

$\mathrm{P}=64 \mathrm{AU}$
$\mathrm{A}=175.78 \mathrm{AU}^{2}$

## Area and Volume of Cylinders (A) Answers

Calculate the surface area and volume for each cylinder.

$$
\text { Surface Area }=\left(\pi r^{2} \times 2\right)+(\pi d \times h) \quad \text { Volume }=\pi r^{2} \times h \quad d=2 r
$$

1. 


$r=1.2 \mathrm{~km} \quad h=3.6 \mathrm{~km}$
Surface Area $=36.19 \mathrm{~km}^{2}$
Volume $=16.29 \mathrm{~km}^{3}$
2.

$d=12.6 \mathrm{~cm} \quad h=7.5 \mathrm{~cm}$
Surface Area $=546.26 \mathrm{~cm}^{2}$
Volume $=935.17 \mathrm{~cm}^{3}$
3.

$r=18 \mathrm{ft} \quad h=27.2 \mathrm{ft}$
Surface Area $=5112 \mathrm{ft}^{2}$
Volume $=27,686.23 \mathrm{ft}^{3}$
4.


$$
d=12 \mathrm{~m} \quad h=18.6 \mathrm{~m}
$$

$$
\text { Surface Area }=927.4 \mathrm{~m}^{2}
$$

Volume $=2103.61 \mathrm{~m}^{3}$

## Pythagorean Theorem (A) Answers

## Name:

$\qquad$ Date: $\qquad$
Calculate the missing side measurement using $a^{2}+b^{2}=c^{2}$.
1.

2.


$$
\begin{array}{r}
12.8^{2}+16^{2}-c^{2} \\
c-\sqrt{163.84+256} \\
c=20.49 \mathrm{in}
\end{array}
$$

3. 


4.

$8.7^{2}+10.2^{2}-c^{2}$ $c=\sqrt{75.69+104.04}$
$c=13.41 \mathrm{ml}$
5.

6.


$$
\begin{array}{r}
6^{2}+8^{2}-c^{2} \\
c-\sqrt{36+64} \\
c=10 \mathrm{ft}
\end{array}
$$

[^2]
## Volume and Surface Area of Rectangular Prisms Answer (A)

Instructions: Find the volume and surface area for each rectangular prism.
Formula: Volume (V) $=\boldsymbol{l} w h$, Surface Area $(A)=2(l w+w h+l h)$
1)


$$
\begin{aligned}
& \mathrm{V}=7.9 \times 4.5 \times 4.0=142.2 \mathrm{~cm}^{3} \\
& \mathrm{~A}=2 \mathrm{x}((7.9 \times 4.5)+(4.5 \times 4.0)+(7.9 \times 4.0))=170.3 \mathrm{~cm}^{2}
\end{aligned}
$$

3) 



$$
\begin{aligned}
& \mathrm{V}=6.6 \times 2.0 \times 3.3=43.6 \mathrm{~km}^{3} \\
& \mathrm{~A}=2 \mathrm{x}((6.6 \times 2.0)+(2.0 \times 3.3)+(6.6 \times 3.3))=83.2 \mathrm{~km}^{2}
\end{aligned}
$$

5) 



```
V=6.3\times1.8x1.9 = 21.5 m
A=2x((6.3x1.8)+(1.8x1.9)+(6.3xl.9))}=53.5\mp@subsup{\textrm{m}}{}{2
```

2) 



$$
\begin{aligned}
& \mathrm{V}=8.0 \times 2.2 \times 5.0=88.0 \mathrm{mi}^{3} \\
& \mathrm{~A}=2 \mathrm{x}((8.0 \times 2.2)+(2.2 \times 5.0)+(8.0 \times 5.0))=137.2 \mathrm{mi}^{2}
\end{aligned}
$$

4) 


$\mathrm{V}=7.1 \times 6.6 \mathrm{x} 7.8=365.5 \mathrm{yd}^{3}$ $\mathrm{A}=2 \mathrm{x}((7.1 \times 6.6)+(6.6 \times 7.8)+(7.1 \times 7.8))=307.4 \mathrm{yd}^{2}$
6)

$\mathrm{V}=6.8 \times 6.4 \times 5.9=256.8 \mathrm{in}^{3}$ $\mathrm{A}=2 \mathrm{x}((6.8 \times 6.4)+(6.4 \times 5.9)+(6.8 \times 5.9))=242.8 \mathrm{in}^{2}$

## Surface Area and Volume of Cones (A) Answers

Calculate the surface area and volume for each cone.

$$
\text { Surface Area }=\pi r\left(r+\sqrt{h^{2}+r^{2}}\right) \quad \text { Volume }=\pi r^{2} \frac{h}{3}
$$



Surface Area: $2720 \mathrm{~km}^{2}$ Volume: $9203 \mathrm{~km}^{3}$
2.


Surface Area: $30,159 \mathrm{~cm}^{2}$ Volume: $301,593 \mathrm{~cm}^{3}$
4.


Surface Area: $2603 \mathrm{ft}^{2}$ Volume: $8579 \mathrm{ft}^{3}$

## Surface Area and Volume of Spheres (A) Answers

Calculate the surface area and volume for each sphere.

$$
\text { Surface Area }=4 \pi r^{2} \quad \text { Volume }=\frac{4}{3} \pi r^{3}
$$

1. 



Surface Area: $4071.5 \mathrm{~nm}^{2}$ Volume: $24,429.0 \mathrm{~nm}^{3}$
2.


Surface Area: $7980.1 \mathrm{~km}^{2}$ Volume: $67,033.2 \mathrm{~km}^{3}$
3.


Surface Area: $6705.5 \mathrm{~km}^{2}$
Volume: $51,632.7 \mathrm{~km}^{3}$
4.


Surface Area: $6763.7 \mathrm{AU}^{2}$ Volume: $52,306.1 \mathrm{AU}^{3}$

## Mean, Median, Mode, and Range (A) Answers

## Calculate the mean, median, mode, and range of each set of numbers.

1) $\{1,10,6,4,2,5,3,6,5,4\}$

Mean: 4.6
Median: 4.5
2) $\{5,10,10,6,8,6,3,7,5,3\}$

Mean: 6.3
Median: 6
3) $\{2,2,2,4,3,9,7,2,7,9\}$

Mean: 4.7
Median: 3.5
4) $\{6,3,5,7,3,8,4,3,9,3\}$

Mean: 5.1
Median: 4.5
5) $\{6,4,9,8,3,9,7,9,6,3\}$

Mean: 6.4
Median: 6.5
6) $\{7,4,4,6,3,5,3,8,5,3\}$

Mean: 4.8
Median: 4.5
7) $\{8,8,7,8,8,3,4,6,8,7\}$

Mean: 6.7
Median: 7.5
8) $\{3,4,7,8,3,4,8,8,5,7\}$

Mean: 5.7
Median: 6

Modes: 4, 5, 6
Range: 9

Modes: 3, 5, 6, 10 Range: 7

Mode: 2
Range: 7

Mode: 3
Range: 6

Mode: 9
Range: 6

Mode: 3
Range: 5

Mode: 8
Range: 5

Mode: 8
Range: 5

Name :
Teacher :
$\qquad$ Score:

Date :

## Four Quadrant Ordered Pairs



Tell what point is located at each ordered pair.

1) $(+0,+0) \xrightarrow{K}$
2) $(-4,+0) \quad D$
3) $(-4,+4) \quad \mathrm{V}$
4) ( $+8,-1$ ) $\qquad$
5) $(-4,-7) \quad \mathrm{S}$
6) $(+5,-6)$ Z
7) $(-5,-1) \quad \mathrm{C}$
8) $(-8,-1) \quad \mathrm{B}$

Write the ordered pair for each given point.
9) $\quad \mathrm{F} \quad(+0,+7)$
11) W $(+1,+1)$
13) $1 \quad(-9,-5)$
15) $\mathrm{A} \quad(-2,+1)$
10) J $(-4,+7)$
12) $\mathrm{N}(+4,+0)$
14) $\quad$ R $(+9,+8)$
16) $X \quad(-7,+9)$

Plot the following points on the coordinate grid.
17) $Q(+7,+1)$
19) $\mathrm{E}(-7,-2)$
21) $G(-8,+8)$
23)
L ( $-5,-5$ )
18) $O(+4,-5)$
20) $\mathrm{T}(-4,+2)$
22) $\mathbf{U}(+6,-7)$
24) $P(-1,-6)$
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## Kuta Software - Infinite Algebra 1

Finding Slope From a Graph
Name $\qquad$

Find the slope of each line.
1)

2)

3)

5)


0
7)

$-2$
4)

6)


4
8)


Name:
Teacher :

Score :
Date :

## Sketch Each Line

1) 



3)

4)

5)



8)


Kuta Software - Infinite Algebra 1
Finding Slope From Two Points
Name $\qquad$

Find the slope of the line through each pair of points.

1) $(19,-16),(-7,-15)$ $-\frac{1}{26}$
2) $(1,-19),(-2,-7)$
-4

Date $\qquad$ Period $\qquad$ -
3) $(-4,7),(-6,-4)$
$\frac{11}{2}$
4) $(20,8),(9,16)$
$-\frac{8}{11}$
5) $(17,-13),(17,8)$
6) $(19,3),(20,3)$
Undefined
0
7) $(3,0),(-11,-15)$
8) $(19,-2),(-11,10)$
$\frac{15}{14}$
$-\frac{2}{5}$

Name:

Score :
Date :

## Sketch Each Line


2)

equation $y=-3 x-3$
2)
3)

4)

5)



8)


Answers to 5.5 Point-Slope Form (ID: 1)

1) $y-3=2(x-2)$
2) $y+2=2(x+2)$
3) $y+5=\frac{5}{4}(x+4)$
4) $y+2=-3(x-2)$
5) $y+3=\frac{1}{4}(x-4)$
-) $y+1=-(x-1)$
6) $y=-(x+2)$
7) $y-2=\frac{3}{5}(x+5)$
8) $y-2=-\frac{3}{2}(x+2)$
9) $y-4=-9(x+1)$
10) $y+5=-\frac{3}{2} x$
11) $y+2=-\frac{7}{2}(x-2)$
12) $y-4=7(x-1)$
13) $y+4=\frac{2}{5}(x+5)$
14) $y-5=-\frac{1}{3}(x+3)$
15) $y+1=-3(x-1)$
16) $y-1=\frac{2}{5}(x+5)$
17) $y-2=0$
18) $y+5=4(x+2)$
19) $y+1=-\frac{3}{2}(x-2)$

Kuta Software - Infinite Algebra 1
Two-Step Inequalities

Name $\qquad$
Date $\qquad$ Period $\qquad$
Solve each inequality and graph its solution.

1) $2 x+4 \geq 24$

2) $\frac{m}{3}-3 \leq-6$

3) $-3(p+1) \leq-18$
4) $-4(-4+x)>56$
5) $-b-2>8$

6) $4+\frac{n}{3}<6$

7) $-7 x+7 \leq-56$

8) $-3(r-4) \geq 0$

9) $-4(3+n)>-32$
4
$n<5$


10) $-3(p-7) \geq 21$

11) $-11 x-4>-15$

12) $\frac{-9+a}{15}>1$

$a>24$
Name $\qquad$

Answer key
Function Table

Score: $\qquad$
Complete the function table and sketch the graph.

1) $f(x)=x^{2}-6 x+11$

| $x$ | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 6 | 3 | 2 | 3 | 6 |

2) $f(x)=-(x+1)^{2}+3$

| $x$ | -3 | -2 | -1 | 0 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | -1 | 2 | 3 | 2 | -1 |

3) $f(x)=x^{2}+4 x+1$

| $x$ | -4 | -3 | -2 | -1 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 1 | -2 | -3 | -2 | 1 |




4) $f(x)=x^{2}-2$

| $x$ | -2 | -1 | 0 | 1 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 2 | -1 | -2 | -1 | 2 |


7) $f(x)=-x(x-4)$

| $x$ | 0 | 1 | 2 | 3 | 4 |
| :---: | :--- | :--- | :--- | :--- | :--- |
| $f(x)$ | 0 | 3 | 4 | 3 | 0 |


5) $f(x)=(x-1)^{2}+1$

| $x$ | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 5 | 2 | 1 | 2 | 5 |


8) $f(x)=-x^{2}-4 x-2$

| $x$ | -4 | -3 | -2 | -1 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | -2 | 1 | 2 | 1 | -2 |


6) $f(x)=x^{2}-8 x+16$

| $x$ | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 4 | 1 | 0 | 1 | 4 |


9) $f(x)=3 x^{2}$

| $x$ | -2 | -1 | 0 | 1 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 12 | 3 | 0 | 3 | 12 |



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Kuta Software - Infinite Algebra 1
Using the Quadratic Formula

Name $\qquad$
Date $\qquad$ Period $\qquad$
Solve each equation with the quadratic formula.

1) $m^{2}-5 m-14=0$
$\{7,-2\}$
2) $b^{2}-4 b+4=0$
\{2\}
3) $2 m^{2}+2 m-12=0$

$$
\{2,-3\}
$$

4) $2 x^{2}-3 x-5=0$ $\left\{\frac{5}{2},-1\right\}$
5) $x^{2}+4 x+3=0$
$\{-1,-3\}$
6) $2 x^{2}+3 x-20=0$

$$
\left\{\frac{5}{2},-4\right\}
$$

7) $4 b^{2}+8 b+7=4$
$\left\{-\frac{1}{2},-\frac{3}{2}\right\}$
8) $2 m^{2}-7 m-13=-10$
$\left\{\frac{7+\sqrt{73}}{4}, \frac{7-\sqrt{73}}{4}\right\}$

## Answers for word problems

Surface Area Volume Applications Page 25 Mean, mode, median and range page 28

1) $70.65 \mathrm{~cm}^{2}$
2) $200 \mathrm{in}^{3}$
3) $700 \mathrm{in}^{2}$
4) 28.26
5) 72 and 538.82 lbs
6) 25.12 ft squared
7) 26.62 cubed and 165 ft squared
8) 2.355
9) Mean 98.14 , median 99
10) Mean 1500 , median 1500
11) Mean 28.28 , median 29.5 , mode 36 , range 28
12) 4 pts
13) $\$ 5.97$

Coordinate plain page 37

1) -1 ,
2) Graph
3) $Y=2 x+5$
4) Ordered pairs $(1,7)(2,9)(3,11)$
$(4,14)$

Quadratic Function Page 51


1) $D 144 \mathrm{ft}$
2) 95.24 ft .

[^0]:    Provided by GED ${ }^{\oplus}$ Testing Service.

[^1]:    Math-Drills.com

[^2]:    Math-Drills.com

