

# Covid-19 Model for the United States

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Worldometer (<https://www.worldometers.info/coronavirus/country/us/>) reported 1212 covid-19 deaths in the US yesterday, dropping to a weekly average of 986, consistent with the final re-calibration of the **CDE-k** model first released on April 19. This model had initially been prompted by two major developments: (1) the Wuhan data upon which the original March 23 model was based had since been disclosed to have been erroneous, with actual mortality about 50% higher than originally reported; and (2) as deaths declined in Italy, they strongly diverged away from the symmetrical model, which was based on the faulty Wuhan data. Still preferring a simple analytical solution to this modeling challenge, I borrowed from a paper I wrote back in my twenties,<sup>1</sup> when I could still solve partial differential equations! Although the topic of that paper was using novel solutions to the Convective Dispersion Equation (CDE) to better describe the movement of chemicals through soil, it turns out that completely analogous physical processes are apparently involved in the “diffusion” of covid-19 through human communities. As shown in **Figure 1**, such an equation gives a compelling fit to observed mortality data for Italy. Here is the equation (simplified from Equation 11 in the 1988 paper):

$$D_i = \frac{\delta \exp[-\{(t_m/t_i) - 1\}^2/2k]}{(t_i/t_m)}$$

where  $D_i$  is the number of deaths on day  $t_i$  (the number of days since first death);  $k$  is a fitted constant (0.25) proportional to the rate at which dispersion increases;  $t_m$  is a fitted constant (37 days) proportional to the time from first death to peak deaths:  $t_m = 2k t_{peak}/(\sqrt{1+4k}-1)$ ; and  $\delta$  is a fitted constant proportional to mortality.

The parameter  $k$  was initially fit to the observed Italian data using a transformation method given in the 1988 paper (see **Figure 2**). The fact that the data are linear when transformed in this manner (lower right of **Figure 2**) is strong evidence that this equation is giving a good fit to the data. I found that the data far before and far after the peak had to be removed to preserve linearity, and so when reconstructing the overall curve shown in **Figure 1**, the model was built by assuming Italy was infected by four waves offset by 5 days each. Based on the still slowing decline in Italy revealed in the weekly averages, the model was re-parameterized on April 25, resulting in a higher value for  $k$ : 0.25.

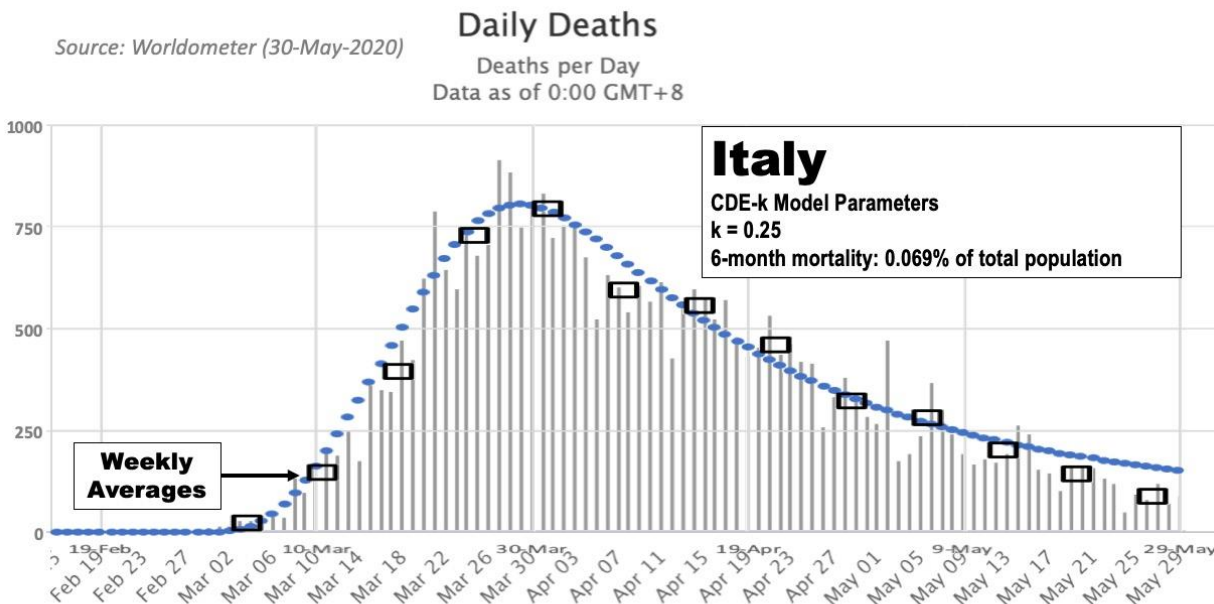
Based on the continuing slower decline seen in the US vs. Italy,  $k$  was increased to 0.5. The **CDE-k** model was applied to all individual cities in the US, with the imputed first death now assumed to have taken place 4 days before the reported date (see **Figure 3**). Reported dates of first death were used for the top 100 metro areas. The remaining one-third of the country was modeled using 1000 progressively smaller simulated cities, with their days to first death modeled stochastically using a regression among the largest cities, which showed a significant inverse trend between population size and date of first death.

Both the **CDE-k** model (dark blue dots) and the original Wuhan model proposed on March 23 (light blue dots) are shown in **Figure 3**. The **CDE-k** model predicts a US death toll of 106,000 through May 31, and a 6-month death toll of 159,400. IHME (<https://covid19.healthdata.org/projections>) drastically raised their projections on May 4 to mortality levels almost identical to the **CDE-k** model. As a resident of St. Louis, I've added the specific result for the St. Louis metro region (**Figure 4**). I've included the IHME results for the entire state of Missouri, because IHME does not report separate results for St. Louis. This may be partially responsible for the discrepancy between the two sets of predictions.

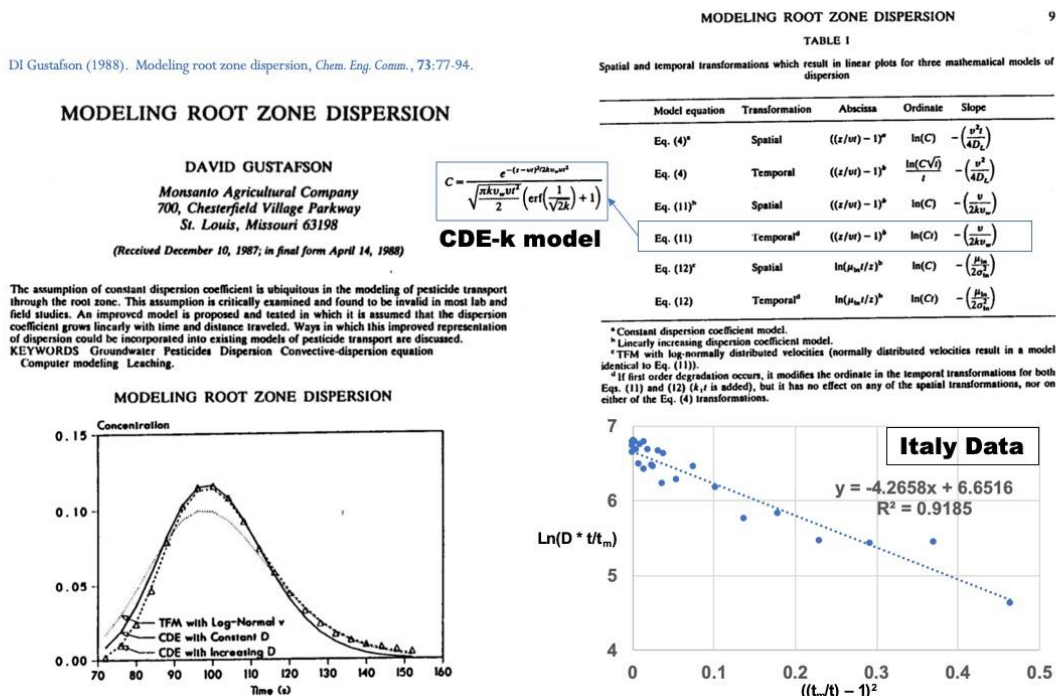
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<sup>1</sup> DI Gustafson (1988). Modeling root zone dispersion, *Chem. Eng. Comm.*, **73**:77-94.

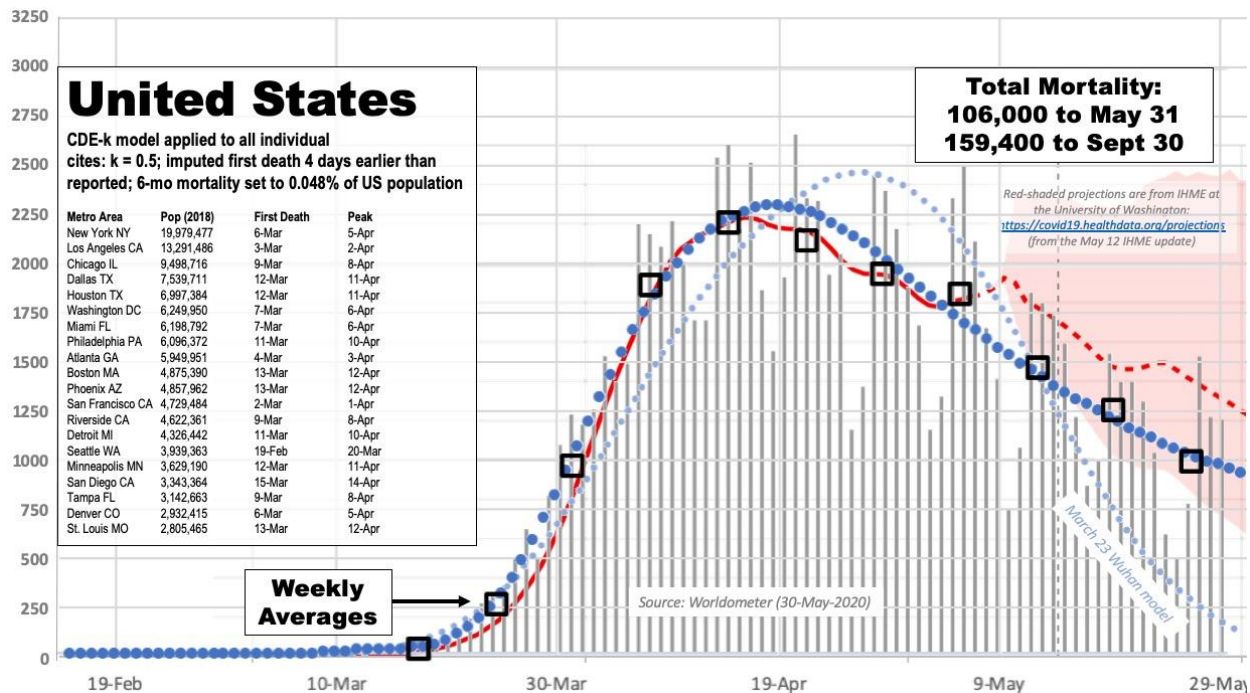
Disclaimer: This is only a model. As the saying goes: “All models are wrong - some are useful.” So we know this model is wrong, but we don’t know if it is useful. Nevertheless, perhaps it helps calibrate expectations for what is likely to come here in the US in the coming weeks.



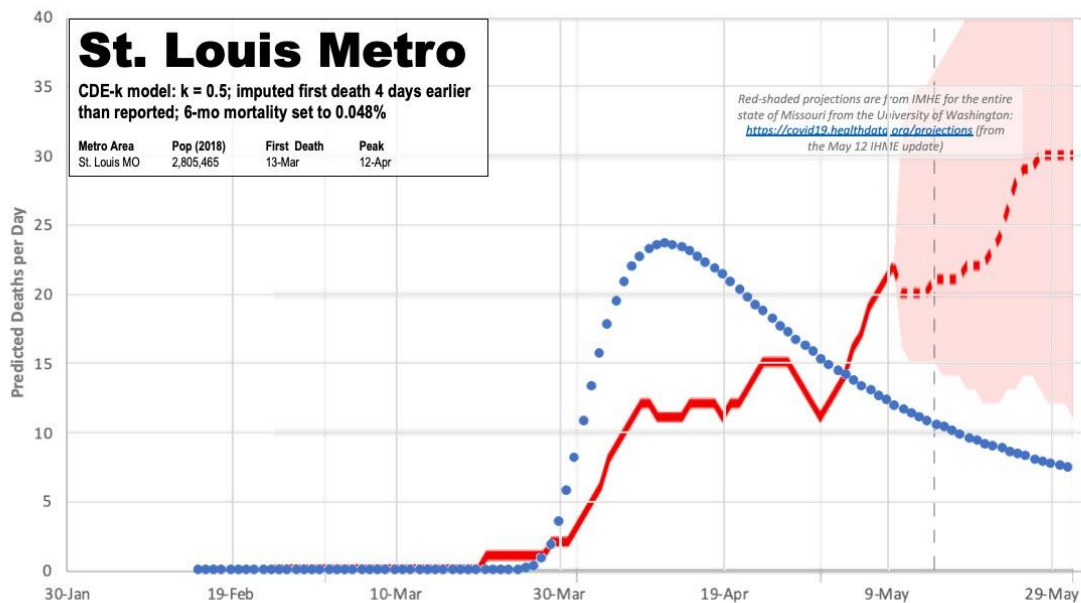
**Figure 1.** Application of the CDE-k model to observed mortality data in Italy.



**Figure 2.** Source document (Gustafson 1988) for the CDE-k model.



**Figure 3.** Application of the March 23 Wuhan model (light blue) and the CDE-k model (dark blue) to the US, overlaid by Worldometer data (gray bars, black boxes), as well as May 12 data (solid red line) and projections (red dashed line and shading) from IHME.



**Figure 4.** Application of the CDE-k model to St. Louis, with May 12 Missouri data (solid red line) and projections (red dashed line and shading) from IHME.