

Supplementary Material: The Mathematical Basis of Refined Unified Matrix Node Theory (MNT)

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1 Introduction

This supplementary document details the mathematical foundation of the Refined Unified Matrix Node Theory (MNT). It includes derivations, expanded equations, and in-depth explanations for each aspect of the framework.

2 Core Equations

2.1 Main Governing Equation

The central equation of MNT is:

$$\Gamma_{\text{MNT}}(i, j, t) = \Lambda_{\text{nl}}(i, j, t) + \rho_q(r_{ij}) + F(i, j) + \theta_{\text{id}}(t, r_{ij}) + \Delta_{\text{chaos}}(t)$$

- $\Gamma_{\text{MNT}}(i, j, t)$: Total energy at time t for nodes i and j .
- $\Lambda_{\text{nl}}(i, j, t)$: Nonlinear feedback term.
- $\rho_q(r_{ij})$: Quantum energy density.
- $F(i, j)$: Resonance term capturing coherence and oscillatory adjustments.
- $\theta_{\text{id}}(t, r_{ij})$: Interdimensional corrections.
- $\Delta_{\text{chaos}}(t)$: Chaotic fluctuation corrections.

2.2 Energy Difference (ΔE)

The energy difference ΔE captures the dynamic evolution of energy states:

$$\Delta E(t) = N_c \cdot n^2 + \delta \sin(\theta'(t) \cdot n)$$

- $N_c = 10^{-6}$: Node interaction constant.
- $\delta = 10^{-8}$: Oscillation parameter.
- n : Quantum node number.
- $\theta'(t)$: Adjusted angular dependence.

3 Derivations

3.1 Vacuum Energy Density

The vacuum energy density $\rho_{\text{vac}}(t)$ is derived from the accumulated energy difference:

$$\rho_{\text{vac}}(t) = \int_0^t \frac{\Delta E(t')}{\frac{4}{3}\pi l_p^3 \cdot t_p} dt'$$

- $l_p = 1.616255 \times 10^{-35}$ m: Planck length.
- $t_p = 5.39 \times 10^{-44}$ s: Planck time.

Derivation^{*}: 1. Start with the energy difference $\Delta E(t')$. 2. Divide by the Planck volume $\frac{4}{3}\pi l_p^3$ and time scale t_p . 3. Integrate over time to account for accumulation.

3.2 Cosmological Constant

The cosmological constant $\Lambda(t)$ is derived from the vacuum energy density:

$$\Lambda(t) = \frac{8\pi G \rho_{\text{vac}}(t)}{c^4}$$

- $G = 6.67430 \times 10^{-11}$ m³kg⁻¹s⁻²: Gravitational constant.
- $c = 3 \times 10^8$ m/s: Speed of light.

4 Angular Corrections

4.1 Time-Dependent Angular Adjustment

The adjusted angular dependence $\theta'(t)$ accounts for time and relativistic corrections:

$$\theta'(t) = \theta \cdot \sqrt{1 - \frac{v^2}{c^2}} \cdot f(t)$$

- θ : Initial angle.
- v : Velocity of the node.
- $f(t)$: Scaling function:

$$f(t) = \frac{1}{1 + \frac{t}{T}}$$

where T is the characteristic timescale ($T = 10^{17}$ s).

5 Applications and Predictions

5.1 Gravitational Wave Predictions

The framework predicts quantum corrections in gravitational waveforms:

$$\Delta\psi_{\text{GW}} = \int \alpha \cos(\omega t) dt$$

- α : Scaling parameter for corrections.
- ω : Wave frequency.

5.2 Dark Matter Interactions

Predicted cross-section for dark matter interactions:

$$\sigma_{\text{DM}} = G_F^2 \frac{m_{\text{DM}}^2}{2\pi} + \Delta_{\text{MNT}}$$

- G_F : Fermi coupling constant.
- m_{DM} : Dark matter particle mass.
- Δ_{MNT} : Corrections from MNT.

5.3 Cosmic Evolution

Vacuum energy density contributes to cosmic acceleration:

$$R(t) \propto e^{\Lambda(t)}$$

6 Summary

This document provides a comprehensive breakdown of the mathematical basis of MNT. The equations, derivations, and predictions form the backbone of the framework, offering a robust foundation for further validation and exploration.