Petroleum Resource Evaluation

Numerical Modeling Reservoir Simulation Theory

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Introduction

- \blacksquare The purpose of this section is to provide an orientation to the fundamentals of reservoir simulation so that one can recognize both the strong points and the potential trouble spots in the usage of reservoir simulation techniques.
- \blacksquare The use of a reservoir simulation model in an engineering study requires that the user have a fundamental understanding of the principles upon which the model is based. Specifically, the user should appreciate the types of errors that are inherent in a reservoir model and how these errors might effect the results.

Introduction

General Conservation Equation

- **Almost all reservoir simulation applications are based upon** the conservation of mass or heat.
- P A conventional black oil model conserves the mass of oil (as stb), the mass of gas (as Mscf) both rather complex mixtures, and the mass of water (as stb). For example, a material balance around a representative volume, a cube in this case can be expressed simply as:

General Conservation Equation

The conserved quantity entering the cube is given as the flux, F_x times the cross-sectional area to flow, A, multiplied by the time period, Δt , over which the flow occurs. The amount leaving the cube from the opposite face is expressed in a similar manner. The sink term represents production from a well.

General Conservation Equation

In – Out = Gain $[(F_x) A \Delta t] - [(F_{x + \Delta x}) A \Delta t + S \Delta t] = [(C_{t + \Delta t} - C_t) A \Delta x]$ & $F_{x + \Delta x}$ – F_{x})*x*& *S V*' $\bm{C_t}_{t + \Delta t}$ – $\bm{C_t}$) *t* & $\partial \bm{F}_{\mathbf{x}}$ $\frac{\partial}{\partial x}$ - q_v = $\partial \bm{\mathcal{C}}_t$ M *t*

where:

 $x = length$

 $t = time$

 F_x = flux (quantity conserved/unit time - unit cross-sectional area)

 $C =$ concentration (quantity conserved/unit volume)

 q_v = specific sink (quantity conserved/unit time -unit volume)

Constitutive and Transport Equations

To use the equation derived above, it is necessary to define the quantity we wish to conserve. It is in this step that a simulation model is first tailored to solve specific problems.

For example, let us conserve the mass (Ibs-mass) of a slightly compressible fluid in a horizontal reservoir. In this case we express the flux as:

$$
F_x = \rho u_x
$$

where : $\rho =$ fluid density (lbs-mass/ft²) u_x = volumetric (ft³/ft²-day)

Constitutive and Transport Equations

P The concentration is a function of both the fluid density and the porosity of the reservoir, i.e. :

$$
C = \phi \rho
$$

$$
\blacksquare \text{ where.}
$$

 $\rho =$ *fluid density (lbs mass/ft³)* $\dot{\phi}$ = reservoir porosity (fraction) - note fluid saturation is 1.0

■ The density and porosity may be expressed in terms of pressure through *constitutive* relationships.

$$
c_{f} = \frac{1}{\rho} \frac{d\rho}{dp}
$$
\nwhere:

\n
$$
c_{f} = \text{fluid compressibility } (psi^{-1})
$$
\n
$$
c_{r} = rock \text{ compressibility } (psi^{-1})
$$
\n
$$
\rho = \text{fluid density } (\text{lbs-mass}/\text{ft}^{2})
$$
\n
$$
\phi = \text{formation porosity (fraction)}
$$
\nJanuary 30, 2005

\nD. Baxendale

Constitutive and Transport Equations

■ The volumetric velocity may, in turn, be related to the pressure distribution in the reservoir by Darcy's law or a transport equation as :

$$
u_x = -\frac{k_x}{\mu} \frac{dp}{dx}
$$

■ *where:*
$$
\mu
$$
 = fluid viscosity (cp)
\n x = distance (feet)
\n k = permeability (.00633 md)
\n p = pressure (psia)
\n u_x = superficial velocity (ft³/ft²-day)

If we were considering a thermal problem the transport equation would be Fourier's law. Fick's law would be used if we were simulating a diffusion process. These transport laws are quite analogous. Also, these laws are often combined (e.g., a process where both convection and diffusion occur).

Diffusivity Equation

• Combining the constitutive and transport equations with the general conservation equation leads to the familiar single phase diffusivity equation i.e. :

$$
\frac{\partial}{\partial x}\left(\frac{k_x}{\mu} \frac{\partial p}{\partial x}\right) + \frac{\partial}{\partial y}\left(\frac{k_y}{\mu} \frac{\partial p}{\partial y}\right) + \frac{q_y}{\rho} = (c_r + c_f) \phi \frac{\partial p}{\partial t}
$$

P If the permeabilities and viscosity of the fluid do not vary across the reservoir, the standard form of the diffusivity equation as a linear differential equation in pressure is as follows :

$$
\frac{\partial^2 p}{\partial x^2} + \frac{\partial^2 p}{\partial y^2} - \frac{\mu}{k\rho} q_v = \frac{c_T \Phi \mu}{k} \frac{\partial p}{\partial t}
$$

Finite Difference Approximations

- \blacksquare The purpose of finite difference approximations is to express a differential equation as a algebraic equation approximating the original equation at a specific point.
- \blacksquare For instance, if the value of pressure, p, is represented graphically as a function of distance, x then the derivative of p with respect to x at x_i may be approximated in several ways using the values of the pressure p at known points in the immediate vicinity of i, that is

Finite Difference Approximations

Backward difference

Forward difference

$$
\frac{\partial p}{\partial x} = \frac{P_i - P_{i-1}}{\Delta x}
$$

Central difference

Each of the above three approximations to the first derivative are equally valid.

Finite Difference Approximations

 ∂

 ∂x 2

 $\frac{2p}{p}$ =

The second derivative of pressure with respect to distance can be determined in a similar manner but in this instanceadjacent values of the first derivative are used as the function of distance.

If the approximation to the first derivatives are usedrather than the exact valuesof these derivatives, we obtain an approximation to the second derivative ofpressure with respect to distance in terms of threepressure values i.e.

$$
\frac{\partial^2 p}{\partial x^2} = \frac{\left(\frac{p_{i+1} - p_i}{\Delta x}\right) - \left(\frac{p_i - p_{i-1}}{\Delta x}\right)}{\Delta x}
$$

$$
= \frac{\left(p_{i+1} - 2p_i - p_{i-1}\right)}{(\Delta x)^2}
$$

 ∂p

 ∂x) i +1/2

 $\frac{\partial p}{\partial p}$

 Δ *x* ∂x) $_{i}$ $_{-\nu_{2}}$

Finite Difference Approximations

The errors associated with these derivative approximations are referred to as truncation errors and can be quantified through the use of Taylor's series. For example the Taylor's Series Approximation of p_{i+1} is:

$$
p_{i+1} = p_i + \Delta x \left(\frac{\partial p}{\partial x}\right)_i + \frac{(\Delta x)^2}{2!} \left(\frac{\partial^2 p}{\partial x^2}\right)_i + \frac{(\Delta x)^3}{3!} \left(\frac{\partial^3 p}{\partial x^3}\right)_i + \dots
$$

Difference Approximation to First Derivative

$$
\left(\frac{\partial p}{\partial x}\right)_i = \frac{p_i - p_{i+1}}{\Delta x} + \Delta x \left(\frac{\partial p}{\partial x}\right)_i + \frac{(\Delta x)^2}{2!} \left(\frac{\partial^2 p}{\partial x^2}\right)_i + \frac{(\Delta x)^3}{3!} \left(\frac{\partial^3 p}{\partial x^3}\right)_i + \dots
$$

Finite Difference Approximations

The terms containing derivatives that remain in the series are referred to as the truncation error as they are dropped or truncated from the approximation. The truncation error is referred to as of order Δx or order $(\Delta x)^2$ depending on the form of the first term in truncated portion of the series.

By combining the Taylor's series approximations to the $i + 1$ and $i - 1$ points, we obtain an approximation to the second derivative and determine that the truncation error is of order $(\Delta x)^2$.

Finite Difference Approximations

Taylor's Series Approximation of pi - 1

$$
\left(\frac{\partial^2 p}{\partial x^2}\right)_i = \frac{p_{i+1} - 2p_i + p_{i-1}}{(\Delta x)^2} - \frac{(\Delta x)^2}{12} \left(\frac{\partial^4 p}{\partial x^4}\right)_i + \dots
$$

Combining the p_{i+1} and p_{i-1} formulations we obtain

$$
p_{i-1} = p_i - \Delta x \left(\frac{\partial p}{\partial x} \right)_i + \frac{(\Delta x)^2}{2!} \left(\frac{\partial^2 p}{\partial x^2} \right)_i - \frac{(\Delta x)^3}{3!} \left(\frac{\partial^3 p}{\partial x^3} \right)_i + \dots
$$

Finite Difference Approximations

By successive use of Taylor's series we are able to develop higher order approximations, for example:

$$
\left.\frac{\partial^2 p}{\partial x^2}\right)_i = \frac{-p_{i+2} + 16p_{i+1} - 30p_i + 16p_{i-1} - p_{i-2}}{12\Delta x^2} + (O(\Delta x)^4 \dots)
$$

Finite Difference Approximations

Using the finite difference approximations just discussed, we may rewrite the single phase diffusivity equation in approximate form as :

$$
\left|\frac{p_{i+1,j} - 2p_{i,j} + p_{i-1,j}}{(\Delta x)^2} + \frac{p_{i,j+1} - 2p_{i,j} + p_{i,j-1}}{(\Delta y)^2} - \left(\frac{\mu}{kh}q_{v}\right)_{i,j}\right|_{n \text{ or } n+1} = \frac{c_{t} \Phi \mu}{kh} \left(\frac{p_{n+1} - p_{n}}{\Delta t}\right)_{i,j}
$$

The figure shows an example of ^a calculation mesh, or grid, which is used to locate those discrete points in the reservoir, for which the difference equation can be written.

Finite Difference Approximations

Note that we have an option when writing the spatial derivatives of expressing the time level at the 'current' time level, n, or at the next time level $n + 1$. If we chose the n time level, we have an explicit expression while a choice of time level $n + 1$ is called implicit. For this equation, time level $n + 1$ is virtually always chosen to assure that the resulting computations are stable.

Writing the algebraic difference equations for each grid block results in an interdependent set of equations that can be expressed in the form of a matrix

:

Finite Difference Formulation

Linear Systems of Equations

Finite Difference Formulation

M atrix Formulation

Diffusivity Equation in Finite Difference Form

Usually, the more general form of the diffusivity equation would be used in a simulation model as shown below.

$$
\frac{\partial}{\partial x}\left(\frac{k_x h}{\mu} \frac{\partial p}{\partial x}\right) + \frac{\partial}{\partial y}\left(\frac{k_y h}{\mu} \frac{\partial p}{\partial y}\right) + \frac{q_y h}{\rho} = (c_r + c_f) \Phi h \frac{\partial p}{\partial t}
$$

Diffusivity Equation in Finite Difference Form

Using the difference representation at discrete points across the reservoir, allows us to vary the permeability and porosity across the grid.

$$
\frac{1}{(\Delta x)^2} \left[\left(\frac{k_x h}{\mu} \right)_{i+j_2, j} (p_{i+1, j} - p_{i, j}) - \left(\frac{k_x h}{\mu} \right)_{i-j_2, j} (p_{i, j} - p_{i-1, j}) \right]_{n+1}
$$

+
$$
\frac{1}{(\Delta y)^2} \left[\left(\frac{k_y h}{\mu} \right)_{i, j+j_2} (p_{i, j+1} - p_{i, j}) - \left(\frac{k_y h}{\mu} \right)_{i, j-j_2} (p_{i, j} - p_{i, j-1}) \right]_{n+1}
$$

-
$$
\left(\frac{q_y h}{\rho} \right)_{i, j} = (c_r + c_\rho) \Phi h \left(\frac{p_{n+1} - p_n}{\Delta t} \right)_{i, j}
$$

Diffusivity Equation in Finite Difference Form

$$
\mathbf{or}, \qquad \qquad \mathbf{or}, \qquad \qquad \mathbf{or}, \qquad \qquad \mathbf{or}, \qquad \qquad (P_{i+1,j} - p_{i,j}) - \left(\frac{k_x h(\Delta y)}{\mu(\Delta x)}\right)_{i \to i, j} (p_{i,j} - p_{i-1,j})\Big|_{n+1} + \left[\left(\frac{k_y h(\Delta x)}{\mu(\Delta y)}\right)_{i,j \to i} (p_{i,j+1} - p_{i,j}) - \left(\frac{k_y h(\Delta x)}{\mu(\Delta y)}\right)_{i,j \to i} (p_{i,j} - p_{i,j-1})\right]_{n+1} - \left(\frac{q_y h(\Delta x \Delta y)}{\rho}\right)_{i,j} = (c_r + c_j) \Phi h(\Delta x \Delta y) \left(\frac{p_{n+1} - p_n}{\Delta t}\right)_{i,j}
$$

This flexibility is one of the main advantages to using numerical techniques in the analysis of reservoir engineering problems.

Diffusivity Equation in Finite Difference Form

Transmissibility and pore volume which are common terms in the reservoir simulation vernacular. Pore volume is self-explanatory i.e.:

The transmissibility definition is nothing more than the Darcy's law coefficient for flow between two adjacent grid blocks.

 $T_{_{X_{i+1/2,j}}}$ $k_x h(\Delta y)$ $\mu\left(\Delta x\right)\;\int_{\,i\,^{+1}\!\!2}$ *j*

 $V_p = (\phi \Delta x \Delta y h)_{i,j}$

The production term now is expressed as a volumetric flow rate, that is

$$
Q = \left(\frac{q_v \Delta x \Delta y h}{\rho}\right)_{i,j}
$$

Diffusivity Equation in Finite Difference Form

And the resulting form of the diffusivity equation is :

$$
\left[T_{i+1/2,j}(p_{i+1,j} - p_{i,j}) - T_{i-1/2,j}(p_{i,j} - p_{i-1,j})\right]_{n+1}
$$
\n
$$
+ \left[T_{i,j+1/2}(p_{i,j+1} - p_{i,j}) - T_{i,j-1/2}(p_{i,j} - p_{i,j-1})\right]_{n+1}
$$
\n
$$
- Q = (c_r + c_j) V_p \left(\frac{p_{n+1} - p_n}{\Delta t}\right)_{i,j}
$$

Black Oil Model

The Black Oil Model assumes that three components exist in the system; oil, gas, and water. Gas may dissolve in oil, but oil does not vaporize into the gas phase. The other basic assumption of the mode l is that Darcy's law as modified by relative permeability to account fo r multiphase flow adequately describes the mass-transport phenomena, i.e.

$$
u_{xo} = \frac{k_x K_{ro}}{\mu_o} \left(\frac{\partial p_o}{\partial x} - \gamma_o \frac{\partial D}{\partial x} \right)
$$

Black Oil Model

The quantities being conserved are stock tank measures of oil, gas and water. The fluxes are as follows :

$$
Oil \tF_{xo} = \frac{u_{xo}}{B_o} \t (stb/ft^2 - day)
$$

Water
$$
F_{xw} = \frac{u_{xw}}{B_w}
$$
 (stb/ft²-day)

$$
Gas \tF_{xg} = \frac{u_{xg}}{B_g} + \frac{R_s u_{xo}}{B_o} \t(Msc/ft^2 - day)
$$

Black Oil Model

Concentrations :

$$
Oil \quad C_o = \frac{\Phi S_o}{B_o} \quad (stb/ft^3)
$$

Water
$$
C_w = \frac{\Phi S_w}{B_w}
$$
 (stb/ft³-day)

Gas
$$
C_g = \Phi \left(\frac{S_g}{B_g} + \frac{R_s S_o}{B_o} \right)
$$
 (*Mscf/ft*³)

Black Oil Model

Combining the conservation equations and the Darcy's law expressions result in:

 $B_{\!\scriptscriptstyle W}^{} \mu_{\scriptscriptstyle W}^{}$

$$
\nabla \left[\frac{k k_{ro}}{B_{o} \mu_{o}} (\nabla p_{o} - \gamma_{o} \nabla D) \right] - q_{vo} = \frac{\partial}{\partial t} \left(\Phi \frac{S_{o}}{B_{o}} \right)
$$

$$
\nabla \left[\frac{k k_{rw}}{B_{w} \mu_{w}} (\nabla p_{w} - \gamma_{w} \nabla D) \right] - q_{vw} = \frac{\partial}{\partial t} \left(\Phi \frac{S_{w}}{B_{w}} \right)
$$

$$
\nabla \left[\frac{k k_{r_g}}{B_g \mu_g} (\nabla p_g - \gamma_g \nabla D) + \frac{R_s k k_{r_o}}{B_o \mu_0} (\nabla p_o - \gamma_o \nabla D) \right] - q_{vg} = \frac{\partial}{\partial t} \Phi \left(\frac{S_g}{B_g} + R_{s} \frac{S_o}{B_o} \right)
$$

Black Oil Model

P These are supplemented by the two capillary pressure equations that relate phase pressures, and the saturation identity.

$$
p_o = p_w + p_{cwo}
$$
\n
$$
p_g = p_o + p_{cgo}
$$
\n
$$
S_o + S_w + S_g = 1.0
$$

• The dependent variables to be solved for in this system of six equations are the three phase pressures and the three phase saturations.

Black Oil Model

These equations are expressed in finite difference form, and then solved by techniques of linear algebra.

There are several different approaches to solving this set of equations. The technique selected depends to a large part on the conditions of the problem. A very straight forward iteration procedure called IMPES (implicit pressure -explicit saturation) will solve many problems in a cost effective manner.

However, there are situations (for instance, single well coning problems) in which it is necessary to use the more powerful Full Implicit procedure to achieve an answer.

Many simulators incorporate several of these procedures. January 30, 2005 D. Baxendale

Black Oil Model

Examination of the Black Oil Equations also reveals that there are several parameters (relative permeabilities, fluid densities, etc.) that are themselves functions of the pressure and saturation variables.

These non-linearities and how they are treated in the simulator have a profound influence on the computed results and model efficiency. If these non-linearities are treated as implicit, that is, at the next time step, $n + 1$, larger time steps can be used. However, the computational cost is higher.

Again, many simulators allow the user to select the degree of implicitness that is used in the computations during each portion of a simulation run.

Petroleum Resource Evaluation

Numerical Modeling Reservoir Simulation Application - BOAST

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Reservoir Simulation Application

Boast - Black Oil Applied Simulation Tool

BOAST is a Black Oil Applied Simulation Tool used routinely for performing evaluation and design work in modern petroleum reservoir engineering. In 1982 the U.S. Department of Energy released the original black oil model called BOAST. BOAST II was released in 1987, and BOAST III in 1995. The current version BOAST 98 (BOAST IV Beta) was first released in 1998. It is basically BOAST III in terms of functionality, updated with a graphical user interface and an Editor called EdBoast designed to provide more flexibility and to overcome some of the limitations of the original BOAST. Many features were added to improve the versatility of the model.

BOAST simulates isothermal, darcy flow in three dimensions. It assumes that reservoir fluids can be described by three fluid phases (oil, gas, and water) of constant composition with physical properties that depend on pressure only. It can simulate both oil and/or gas recovery by fluid expansion, displacement, gravity drainage, and capillary imbibition mechanisms. Some of the typical field production problems that can be handled by BOAST include but are not limited to:

- **Primary depletion studies;**
- **P** Pressure maintenance by water and/or gas injection; and
- **Exaluation of water flooding, operations.**
Boast - Black Oil Applied Simulation Tool

User-Friendly Enhancements:

- P Free format data entry on most data cards
- **Restructured recurrent data input to allow separate specification of time step size and output frequency**
- Restart capability
- One-line time step summary
- **Summary table of program output**
- Output pressure map corrected to user-specified datum
- **Gas PVT default option**
- \Box Reservoir Engineering Features:
	- Optional three-phase relative permeability algorithm
	- **Multiple rock regions allowed**
	- Multiple PVT regions allowed
	- **Bubble point pressure can vary with depth and PVT region**
	- **Several different analytic aquifer models**
	- **Direct input of noncontiguous layers**
	- Net and gross thicknesses allowed

Boast - Black Oil Applied Simulation Tool

- \blacksquare Well Model Features:
	- Individual well gas/oil ratio (GOR) and water/oil ratio (WOR) constraints
	- P Minimum oil production and maximum liquid withdrawal well constraints
	- Multiple wells per grid block
	- Gas well model using a laminar-inertial-turbulent analysis
	- Maximum water/gas injection rates

Numerical Features:

 \blacksquare

- **Two new iterative matrix solution methods:** y and z direction line successive over-relaxation (LSOR) methods
- Zero pore volume (inactive) grid blocks allowed
- Optional two-point upstream weighting for reducing numerical dispersion

Boast - Black Oil Applied Simulation Tool **Requirements**

The data editing application, *EDBOAST.EXE* limits the grid size of the reservoir being edited to the physical memory and/or the virtual memory size. The simulator application *BOAST98.EXE* also allows unlimited reservoir grid size. All the applications require Window 95, Windows NT, or Windows XP. Recommended physical memory size is 32 MB or higher for *BOAST98*, and also 32 MB or higher for *EDBOAST*. Recommended disk space varies according to print options selected for output files and also on the size of the reservoir grid. A range of from 40 MB to 100 MB of disk space use could be anticipated.

Limitations

The major limitations exist mainly in the application, Boast98.exe. The Boast98 limitations are:

- P A large grid size of x-direction blocks, y-direction blocks, and z-direction blocks or layers will force the use of virtual memory and drastically slow down the array iteration processes.
- Maximum well blocks of 200.
- Maximum time steps of 8000.
- Maximum data sets of 200.
- \blacksquare Maximum wells of 150.
- Maximum nodes per well of 10.
- P Maximum modifications to permeability, porosity, and transmissibility of 55 each (EdBoast only).
- Maximum rock regions and PVT regions of 5.
- Maximum table entries for relative permeability curves and for capillary pressure curves of 25.

The grid size for *BOAST98.EXE* and *EDBOAST* is unlimited since memory is allocated to fit grid demand.

Boast - EdBoast

Menu Items

A simulation run can be started from either theEDBOAST or the BOAST98 application. However, beginning with the EDBOAST program, the user will be able to review the input data file first and locate any mistakes that apply to the BOAST98 application. To begin EDBOAST, double-click the icon representing the application with the mouse. At the top of the opened window, from left to right, are 7 horizontal menu items. These items are "FileName", " Directory", " Extension", " Options", " Help", " Quit", and "About". A brief description of each horizontal item is shown in the second line below the menu. The horizontaland vertical arrow keys permit moving from item to item. This method of describing the highlighted item generally applies to the vertical sub-items as well. If the arrow keys should fail to respond, re-entering the program will correct the problem.

Boast - EdBoast

File Name

The first item, "File Name", allows the selection of a pre-existing data input file. Select File Name by clicking once on the item. Then select the input file from the scrollable list of names. To scroll, use the up and down arrows on your keyboard. If the file is in another directory follow the next step.

Directory

A list of scrollable of subdirectories is found under the second item, "Directory", with the current directory shown in the top title. To find the parent directory, click on the double dots ".". Repeat the process of clicking the double dots to back farther up the directory hierarchy.

Extension

The "Extension" item allows the user to filter out the different types of files. The bottom line on the list shows which are input and which are output files and what their extensions are.

The file extensions included in the list are (1) input data files with the extension of .SIM for Boast98 simulations, (2) Boast98 input data files with an alternate extension of .NEW, (3) output results of Boast98 simulations in a table form with extensions of .TAB, (4) input help files with the extension of .HLP, (5) the main output results of Boast98 simulations with extensions of .OUT, (6) picture files with the extension of .PCX, (7) bit map files with extensions of .BMP resulting from captures of the screen during graphic displays using the F5 key or the "Capture" command, and (8) all files extensions are available (these files must be text file in an ASCII format).

Boast - EdBoast

The fourth item, "Options", has a variety of procedures on its vertical sub-item list. These sub-items are "New", "Preview", "Edit", "Boast98", and "Transfer".

- **E New:** Permits the user to create a new input data file for future simulation.
- **Preview:** will allow a read-only look at the contents of the file selected under File Name.
- **Edit:** brings the contents of the file into a series of dialogs for inputting or modifying reservoir data., and will bring up the "EdBoast Home Page" which has a series of 14 buttons for selecting which dialog group to access. A description of each highlighted button is shown on the second line below the title. The vertical arrow keys or the tab key are used to move to different highlighted buttons. Use the Abort button to leave the "EdBoast Home Page" buttons and before calling Boast98 under Options.
- **Boast98:** sub-item immediately begins simulation action on the current file selected. Calling "Boast98" under "Options" will place two running applications into memory, Boast98 and EdBoast. Each will still run independently, however, a file can no longer be edited while still engaged in simulation under Boast98.
- **Transfer:** will allow the user to run any application existing in the currently selected directory. Nothing will show in the list if there are no program applications available. Change directory to browse, then reselect "Transfer".

Boast - EdBoast

99 E

EdBoast Home Page

Selecting "Edit" under the "Options" item of the main menu brings up this EdBoast Home Page dialog window. The EdBoast Home Page consists of 14 home page buttons. These 14 buttons are "BEGIN", "GRID", "PORPERM", "TRANSM", "TABLE", "INITIAL", "CODES", "AQUI", "WELLS", "RECURR", "DEFAULT", "NEXT", "ACCEPT", and "ABORT".

Many of the button selections bring up dialog boxes with an integer of 0 or 1 and sometimes a minus 1. Whereonly a 0 or a 1 is used, the 0 means, NO or turn off, and the 1 means, YES or turn on. Please consult the Boast3manual for the meanings of each integer as a switch.

Boast - EdBoast

BEGIN:

Th**is first button introduces the Helma** frame, which contains 5 lines of reservoir description called frame, which contains 5 lines of reservoir Header". Will be the title card. The other 4 lines are runIIIFdehthFation records. IThEnext 2 b6xes in the
The ante et main 25 mee entrepentification tches for recosdst inlihdinaixtn2oboxesrinuthanidamother for wraiing a preserra tables This informations may be ϵ 6 ϵ found the parameter of page 11 ϵ of the Boast ϵ an0therator writing a post-run table. This <mark>infAlthouigh the ass the found ratnette</mark>rs are stated to b<mark>e</mark> $\frac{1}{2}$ still under construction $\frac{1}{2}$ the switches and input data appear to work at this time. For IREOPT = 1 , full restart editing of the saved restart file is not available. When $IREOPT = -1$, the no restart option is invoked. The restart option is initialized with $IREOPT = 0$. description called "Header". The first line of the "Header" will be the title card. comain 2 aptegers reples This igfswitches for PUSEAL INITIALIZATION PASSLATION IN RIN beginning of coast up to the Boasts manual.

#

E Button 2.GRID

 \blacksquare The GRID button brings up 5 or more dialogs or spreadsheets for entering reservoir model grid dimensions (II, JJ, $\&$ KK) and geometry data

Boast - EdBoast

GRID

The GRID button brings up 5 or more dialogs or spreadsheets for entering reservoir model grid dimensions (H, JJ, & KK) and geometry data (KDX, KDY, KDZ, & KDZNET) as found in pages 14-15 of the Boast3 manual. The values of the codes for KDX, etc. determine the type of dialog window that follows. Entering a frimus ¹¹ (⁻¹1), indicates a constant values for all grid blocks. Special spre**ad stitles cardowshe outhers, blines nates run**al array results from a value of 0 oridentil Kid *X* tiens records. The next 2 boxes in the **BSENDICT RUGHER CHILIDES the dialog frame, which** contains 5 lines of reservoir description called Header". The first line of the "Header" will be

Beft&tath pitialization or restart run and a pagther if a fructions is shown whi**erritises besone-mun talelc**omhainds of prantio**n** and peuts which can be use**d ounchant he the simaid shea**t p**age thil guilthe right onsus**e will also present the mennant these commands . These menu selections or key commands are Import, Export, Type, Graph, Cancel, Next, Group, and Home. frame contain 2 integers representing switches for \blacksquare Although the restart run parameters are stated to be

Also, a special dialog struction", the switches and input jed for grid dim**éata appear to x, or tritibri, numedZ, or UREOR, l**'& I**d**CODE). This dial**full restart editing of a the saved fre start file is enot**on value followed by a left_{VRi}pstbJd) a**vdhesht-REOP4) solumn number, and an** upper-most (J1) and a lower-most (J2) row number, along with a layer range (K1_d K2) for the grid region affested by the grid dimension value in the box. This same style of setting region values applies to several other modifications of reservoir prameters, such as porosity, permeability, and transmissibility. ttvailstb1e.) avv1hen IREOPT) solum nheumbere sturf option is invoked. The restart option is initialized With **IREOPT** = 0.

T Button 2.GRID
The next dialogs box requests the KEL code for inputting depth values and dip allgTEh(seG]RHD 15\uttonst3ringgsudp 5Aoprexore KEalloggslexrof -2 and 2 (noncontiguoud sheets for entering reservoir model grid dimensions (II, JJ, $\&$ KK) and geometry data

REGINE SIMULATION Application

(KDX, KDY, KDZ, & KDZNET) as found in P

Boast - EdBoast

TRANSM

The TRANSM button presents transmissibility modifications shown near the bottom of page 22 in the Boast3 manual. The dialog format is similar to the other modification dialogs.

Boast - EdBoast

TABLE

A description of the sequence of requested information for Rock and PVT regions and their respective relative permeability and capillary pressure tables is given beginning on page 24 of the Boast3 manual.

The first dialog from this button, allows entry for the number of distinct rock regions is to be changed and the number of regions where the PVT default region value of 1 is to be changed. The rock region is a saturation dependent data set for relative permeability. The PVT region is a pressure dependent data set, including oil, water, and gas PVT tables. At least one rock region and one saturation region is required.

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Help GRAPHS

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ACCEPT CANCEL

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Boast - EdBoast

INITIAL

This button introduces a set of more dialogs for each layer and containing the pressure and saturation as found beginning on page 31 manual.

*Edi

BEAIL of Cil Boget) ODELL CTN.

 $\ln x$

Boast - EdBoast

CODES

This button introduces debug and diagnostic controls options and solution method specifications as found beginning on page 32 of the Boast3 manual. The data can be entered in a series of 2 dialogs.

Edit of C:\Boast\ODEH.SIN \Box \times Debug, Diagnostic, and Run Control Parameters Codes for controlling diagnostic output and debugging They do not provide information for debugging the input Any one will generate a very large volume of output. SOR Parameter debug output control Solution matrix debug output control RC04 - 0 Density & saturation debug output RSRTP Sergen output step skip control Max. time steps allowed before termination (50) NMAX 3650 1.500000 **FACT** Time step decr. factor. fixed=1.8. often=0.5 = FACTS 0.250000 3650.000000 20.000000 500000.000000 **CORMA** Limiting minimum avg. Field pressure, psi 150.000000 Limiting maximum avg. field pressure, psi 10000.000000 ACCEPT CANCEL

Boast - EdBoast

AQUI

This button introduces the installation of theaquifer data as found beginning on page 35 of the Boast3 manual.

WELLS

This button introduces well data as foundbeginning on page 37 of the Boast3 manual. The total number of wells that will be used inthe entire simulations must be entered first. Then each well ID, the number of well nodes, and the well name for each well are entered. This is followed by X, Y, Z locations of each well node being entered. The well direction, IDIR, is entered to conform to the Boast3 format.

Boast - EdBoast

RECURR

This button introduces a set of 6 dialogs for each data set for entering recurrent data as found beginning on page 38 of the Boast3 manual. The total number of data sets entered (up to 200) is displayed in the first window(s) presented. Up to 21 data sets with associated information are allowed in the first page and 22 data sets on each succeeding page. This allows a preview of the number (IOMETH) of elapsed times (FTIO) in days and also a break down on the number of NEW and OLD (modified) wells are in each data set. This preview is repeated twice. Once for "Data set deletion" . The second for "Data set selection". The second preview is followed by 6 separate dialogs, if only YES is selected.

Data set deletion. By saying YES, the entire group of data sets is retained and data set selection is next. By saying NO, the last data set number is presented for deletion. To delete any other data set, enter a different number. This decision may be canceled immediately or later by the ABORT command in the Home Page. It is always wise to look over the data set to be deleted before a deletion is made. After a deletion has been made and accepted, the data set numbers following the deleted set are moved back by one. (Note: If the YES and NO button should every disappear use the Enter key to bring them back. This happens when another program window overlaps the preview or a resize event occurs.) Data set selection will be offered next.

Boast - EdBoast

RECURR

Every data set and associated dialog procedure can be identified in the title found at the top of each window.

Old and New well selection. Each dataset will include the number of old andnew wells. A new well is one that iffully defined with a PID and PWF value for each layer. An old well then is one that has been previously defined. The same IDWELL number is kept for the old WELLID as was used when it was anew well. For the old wells, the program remembers the PID and PWF values placed there as new wells. The PID and PWF values can be changed for a well by redefining the same IDWELL number as a new well. This is also truefor the values of ALIT and BLIT for adry gas reservoir. These values of ALIT and BLIT can be produced with the program GASDEL, mentioned in the Boast 3 manual.

Boast - EdBoast

DEFAULT

This button will initiate a set of pre-selected input data, which will allow the beginner a quick step forward. The selection of this button will warn a person that their data will be overwritten by the defaultinput data. Even if a YES is chosen for this warning, using the ABORT button will reject saving this overwritten file. One more chance is give to reject modified or defaulted information when the ACCEPT button is chosen by next choosing NO to the question "Open output file?".

NEXT

This button will advance to the next button in the line up. This is the same as the Tab plus the Enter key being hit. The Up and Down arrow keys will advance or reverse the highlighted button selections.

ACCEPT

This button will allow the saving of the edited input data under the same or a different file name. This button selection can be canceled by choosing NO instead of YES.

ABORT

Returns to the original main menu. The same file name is in the buffer and another command such as Preview or Boast98 can apply to file name previously selected.

Boast - EdBoast

Alternatively Use an Editor

Rather that use EdBoast one can always use and Editor like WinEdit or WordPad to change the *.sim file, which is the Boast input file that will be run.

This is the most efficient way to edit the simulation deck for knowledge users.

[ODEH553.SIM] TESTING RESTART OPTION IN BOAST3 6/05/95 ID2: INITIALIZATION RUN WITH IREOPT = 0 ID3: ONE RESTART RECORD WRITTEN AT 1825 DAYS ID4: NO INPUT RESTART FILE IS NEEDED; HENCE USING "DUMMY.RIN" ID5: OUTPUT RESTART FILE IS NAMED "ODEH553.ROT" RESTART AND POST-RUN CODES 0 0 <--- IREOPT, IPOSTP 1 0 0 0000.< --- IRNUM,IRSTRT, NN,TMAX (NN & TMAX used only for IREOPT=l) DUMMY.RIN <--- Input Restart File Name - used only for IREOPT=l ODEH553.ROT <-- Output Restart File Name -TO BE USED AS INPUT FOR RESTART RUN! 1825. <--- Times @ which Restart Records are written GRID DATA 5 5 3 GRID BLOCK LENGTHS -1 -1 0 0 2000. 2000. 20. 30. 50. 20. 30. 50. GRID BLOCK LENGTH MODIFICATIONS 5*0 CONSTANT DEPTH TO TOP OF LAYER ONE 0 0.0 <---KEL, ALPHA 8325. POROSITY AND PERMEABILITY DISTRIBUTIONS -1 0 0 0 .30 500. 50. 200. 500. 50. 200. 100 37.5 20.83 POROSITY & PERMEABILITY MODS: (IPCODE replaced by KPHIMP,KXMP,KYMP,KZMP) 0 0 0 0 1 1 1 1 TRANSMISSIBILITY MODIFICATIONS

BOAST98

In this primary menu display, the "Option" menu item has been selected. The opened menu item "Option" shows a list of sub-items with"Simulate" highlighted. The last line in the list, "Start selection" is a description of the highlighted sub-item. Use the up and down arrows to highlight different sub selections. A mouse click ona sub-item will invoke thedescribed procedure. In this case, an Enter key, or a mouse click on Simulate will begin the reservoir simulation of the selected file name, "ODEH.SIM", as seen in the second to the bottom line. This file name is often seenalso seen on the right side of the second line from the top.

BOAST98

The right mouse click during a simulation run will cause animmediate suspension of simulation after finishing one more time step. A secondary menu is displayed as shown in the figure above. The highlighted menu item "Explore" has its description shown on the second line. Inthis case, "Explore" would select from a large number variables and plot as 1, 2, and 3 dimensional graphic constructions. The runsimulation is resumed whenthe menu item "Resume" isselected.

BOAST98

The use of history matching is selected before simulation begins. The charts of the history matching are only viewed under the Explore menu selection during simulation suspension.

BOAST98

When the simulator is run and the following generic output files are created:

-
- 1. B.OUT Output listing 2. B.SCR Screen output

3. B.WEL Well production summary 4. B.TAB Field production summary
- 3. B.WEL Well production summary 4. B.TAB Field production summary
S. B.GWN Grid & wellblock data for B3PLOT2 6. B.BPD Binary production data for B3PLOT2
- S. B.GWN Grid & wellblock data for B3PLOT2 6. B.BPD Binary production data for I

7. B.CGD Grid & well data for COLORGRID 8. B.MAP Binary file of 3D arrays for 7. B.CGD Grid & well data for COLORGRID
-
- -
	- **COLORGRID**

BOAST98

* TOTAL RUN SUMMARY * *****************************

BOAST98

* TIME STEP SUMMARY * *****************************

MINIMUM AVERAGE RESERVOIR PRESSURE WAS NOT ACHIEVED ---SIMULATION IS BEING TERMINATED

BOAST98

Exercise 1

Run EdBoast and load the Boast input file *Depletion.sim*. View the input file and notice that the water injection wells have been switched off for this run. this was done by commenting out the desired lines with "*C*". Run this case and plot the results from the *Depletion.out* file.

- (1) What are the oil and gas recovery factors?
- (2) When does the reservoir drop below bubble point pressure?
- (3) What is wrong with this run?

Exercise 2

Copy Depletion.sim and name the copy Waterflood.sim. Edit Waterflood.sim and delete the comment character (the lines with *"C"*), to switch the water injection wells back on. Run this case and plot the reulsts frome the *Waterflood.out* file.

- (1) What are the oil and gas recovery factors?
- (2) When does the reservoir drop below bubble point pressure?
- (3) When does water breakthrough?
- (3) What is wrong with this run?

Petroleum Resource Evaluation

Numerical Modeling Reservoir Simulation Applied Modeling

David BaxendaleEquinox International Petroleum Consultants David.Baxendale@bigfoot.com

Introduction

 \blacksquare In general, the key steps of a reservoir study can be summarized as follows :

- Statement and Prioritization of Objectives
- **Reservoir Characterization**
- Model Selection
- Model Construction
- Validation
- Predictions
- Documentation

 \blacksquare Emphasis will be placed on the basic principles involved and the engineering and geologic control needed within each of the above steps. Depression of the above steps.

Introduction

Statement and Prioritization of Objectives

- \blacksquare A clear statement of objectives is the most important step in a study. When several goals are involved, a prioritization process is needed.
	- **Pressure and production forecasts**
	- Critical gas and water coning rates
	- **Timing and sizing of facilities (e.g., platforms)**
	- **I**n-fill drilling requirements
	- **Comparative benefits of gas vs. water injection**
	- Workover potential evaluation
	- **Lease-line migration**

Statement and Prioritization of Objectives

- **The modeling requirements of each objective are usually** incompatible with one another, and thus the need for prioritizing objectives arises because of cost time constraints.
- \blacksquare For example, the griding and layering of a model to study workover potential can be very different from that of a model directed at estimating lease-line migration

Reservoir Characterization

 \blacksquare Reservoir characterization (RC) can be described as three interdependent components :

I fluid characterization,

- **P** rock characterization, and
- **geologic modeling.**

 \blacksquare The purpose of RC is to capture geologic and petrophysical features which affect reservoir flow mechanisms. The roleengineering control and judgment plays in developing the reservoir model will be emphasized.

Reservoir Characterization

Reservoir Characterization

In essence this process has three objectives :

- **To identify the key reservoir features**
- **To identify the main drive mechanisms**
- To determine the reservoir volumetrics (STOIIP, GIIP, WIIP)
- RC forms the foundation for the other simulation steps; hence, any error in RC can be costly in terms of engineering results.
- \blacksquare Of the three components of RC, the geologic model is the most important and perhaps the most complex. This is where engineering control is especially needed. Since the primary issues in reservoir simulation involve in-situ flow, a geologic model must be able to capture features that directly affect in-situ flow.

Reservoir Characterization

- \blacksquare Specifically it must :
	- P Identify stratification and degree of vertical communication of the zones.
	- **Define what constitutes pay and reservoir.**
	- **E** Establish areal connectivity and the variation in reservoir quality.
	- **IDENTIFY** Contrasting lithologic zones (high versus low permeability streaks).
	- **I** Identify reservoir boundary conditions (e.g., sealing versus non-sealing faults, sand continuity toward neighboring areas, aquifer extent).
	- **Distinguish between localized versus regional geologic** features.

January 30, 2005 D. Baxendale

Reservoir Characterization

Reservoir Characterization

January 30, 2005

45

Reservoir Simulation Applied Modeling Phase II Simulation Grid YZ Cross Section

Reservoir Simulation Applied Modeling Phase II Simulation Grid XZ Cross Section

Reservoir Simulation Applied Modeling Phase II Porosity Distribution - YZ Cross Section

Reservoir Simulation Applied Modeling Phase II Porosity Distribution - XZ Cross Section

Reservoir Simulation Applied Modeling Phase II CO₂ Areal Distribution

Reservoir Characterization

- What is expected from a geologic model for reservoir simulation is a 3-D version of the same schematics.
- **The six features noted above directly affect reservoir** performance. To the degree that they are known, one may speak of a complete geologic model. Very often available data do not permit full resolution of items "1" through "6". If so, the task is to identify the areas where uncertainties exist and explore their impact on the study results through sensitivity analyses.
- P History-matching offers limited possibilities in enhancing RC. The non-unique aspect of the process excludes its use as a definitive criteria, although qualitative assessments can certainly be made.

Reservoir Characterization

- $\overline{}$ Often reservoirs are layered based on time stratigraphic markers. Geological properties (i.e., S_w , k) are then mapped within each stratigraphic layer. However, the non-reservoir portion of the rock is also important in determining the in-situ flow performance of reservoirs.
- The areal and vertical communication (within and between layers) can be deduced from these maps when used as adjuncts to other tools such as Repeat Formation Tests (RFT).

Reservoir Characterization

Example

The lithology in the reservoir is quite varied and consists of limestone, dolomite, sandy dolomite, sandstone and shale. The presence of large pressure differentials indicates a very stratified reservoir system.

Reservoir Characterization

A spinner survey on the same well also indicates significant amounts of crossflow, further supporting the vertical non-communication among geologic layers (in effect, zero vertical permeability).

This example shows the useful role engineering data, such as provided through RFTs and spinner surveys, can play in RC.

Reservoir Characterization

Reservoir Characterization

The second objective of RC is to identify the main encroachment mechanisms ofthe reservoir. This is important since it will affect the model selection process.

Three alternative encroachmentmechanisms are shown for a four-layer reservoir. A complete RC for this system should point to the right alternative which in turn will simplify the model selection. The point is that an understanding of the basic reservoir mechanisms must precede the numerical phase of the study.

Reservoir Characterization

The third objective of RC is reservoir volumetric determination. Two emerging techniques in RC appear promising.

\blacksquare Geostatistics

Kriging which provides a minimum error-variance estimate of any unsampled data; however, has the tendency to smooth out details and extreme values of the original data set. Has several general forms: Simple Kriging, Ordinary Kriging, Kriging with a Trend Model, Kriging with an External Drift, Factorial Kriging, etc.

Stochastic Simulation which builds alternative, equally probable, high resolution models of spatial data. The simulation is considered conditional if the resulting realizations honor the data values at their locations. Again numerous forms are available: Gaussian Simulation, Sequential Indicator, Boolean Simulation, Simulated Annealing etc.

\blacksquare Seismic methods

These diverse approaches hold the potential to significantly improve the quality and completeness of RC for reservoir simulation, particularly when used as adjuncts to (as opposed to substitutes for) other geologic and engineering data. January 30, 2005 D. Baxendale

Model Selection

- **P** "What simulation model is best suited to meet our objectives?"
- **The answer lies in a systematic model selection process,** which can be grouped under six main headings, each describing a facet of modeling:
	- \blacksquare Process
	- Functionality
	- \blacksquare Scope
	- **Dimensionality**
	- Approach
	- \blacksquare Grid Selection

Model Selection

Model Selection - Process

As shown a total in the next few slides there are 48 modeling possibilities available once the process (e.g., immiscible, miscible, thermal) is identified. Each choice has certain advantages and disadvantages.

P Most Reservoir Engineering problems fall into the third category, since engineering decisions require a knowledge of both energy and saturation with respect to time

Model Selection - Functionality

 \blacksquare The next and most important step after the process selection is to define the overall function of the model based on the objectives under consideration.

Energy Models

• Primarily aimed at computation of reservoir pressures.

\blacksquare Front-Tracking

■ *Used to track the phase distribution of reservoir fluids.*

Energy & Front-Tracking

^P *Are used to compute both reservoir pressures and fluid saturation distributions in time.*

 \blacksquare Most reservoir engineering problems fall in the third category, since engineering decisions require a knowledge of both energy and saturation with respect to time.

Model Selection - Functionality

However, there is a sizeable class of problems where only one of the two aspects is important. Some typical applications under each category are given below.

Model Selection - Scope

The next decision involves determining the model boundaries. Generally, there are two choices : Sector or Slice Models and Full-Field Models (FFM) .

Model Selection - Scope

B Slice Models (SM)

- SMs represent only a segment of the full reservoir and, therefore, require two very important assumptions :
	- *Fluxes across the SM boundaries are known or can be estimated.*
	- *Results from the SM can be accurately scaled up to the full field.*
- Full-Field Models (FFM).

FFMs allow representation of the reservoir in its entirety, including neighboring fields. No assumptions need to be made regarding model-boundary fluxes.

In general, for Energy models where the main question concerns material balance, FFMs are the more appropriate model while SMs are more suited for Front-Tracking models because of the finer grid necessary to define the frontal movement.

Model Selection - Dimensionality

Dimensionality can be 0-D, 1-D, 2-D, or 3-D depending on the objectives, and the reservoir mechanisms (e.g., coning, cusping) and flow attributes (e.g., stratification). Important questions to be answered are:

- P How many dimensions does the reservoir exhibit in regard to insitu flow performance (i.e., Are there areal as well as vertical effects?)
- Which dimensions are important to the objectives?

Functionality, dimensionality and model-grid size are so intricately related they cannot be determined independently, and hence the process is iterative.

Model Selection - Approach

■ Actual

■ Actual models represent the reservoir characteristics based on real data, and offer the possibility of validation of this data. Commensurate with increased data availability, the accuracy of simulation results can be improved. Most reservoir engineering problems are best suited for Actual models.

Conceptual

■ Conceptual models use a more idealized version of real data to achieve a simpler representation of the reservoir, and thus offer limited validation, and the accuracy of model results is often untested. Their main utility lies in simple process evaluations and/or reservoir parameter sensitivity studies where validation is not critical to the integrity of the results.
Model Selection - Grid

Functionality and dimensionality of the model and the well-spacing of the reservoir jointly define the resolution required (vertically or areally) for pressure and saturation computations.

The resolution dictates the number andcoarseness of the cells. Because computer resources are limited, the grid determination is an iterative process balancing available computing capabilities and modelling needs.

Model Selection - Grid

A general classification of models based on grid size is given below :

Model Selection - Grid

Note that consideration of Very-fine type models is possible only for moderately-sized fields (1000 acres or less). For instance, the grid requirements for a 10,000-acre, 100-ft-thick reservoir will be as follows :

Current PC computing capabilities limit black-oil models to roughly 1,000,000 active cells, with practical considerations reducing it further to 500,000 to 750,000 cells.

Model Selection - Grid

- \blacksquare We are thus faced with compromises in modeling options for large fields:
	- Changing the scope of the model from FFM to SM, thus reducing the modeled area.
	- Reducing the dimensionality from 3-D to 2-D or 1-D.
	- **Reducing the number of layers under consideration.**
- **These compromises are perfectly reasonable so long as** they are not contrary to the study objectives and the RC. This further emphasizes the need for completing the RC step before selecting the model.

Model Selection - Grid

Radial flow exists near the wellboreand linear or Cartesian flow existswithin the reservoir away from the wellbore.

For field-wide studies the growth or decay of reservoir volumes activated by unsteady-state flow is small and hence linear flow is modeled i.e., via linear grid

On the other hand, for converging flow near wells the growth or decay of reservoir volumes activated by unsteady-state flow is large and radial flow is modeled via radial grid. Therefore, radial flow is important in only very localised areas of the reservoir and linear flow is modeled in most reservoir studies.

Model Construction

The transformation of geologic and petrophysical data into a simulation model constitutes a potential source of errors, due to scale-dependencies.

Key reservoir parameters such as vertical and horizontalpermeabilities, relative permeability, porosity, capillarity and residual oil saturation depend on model cell dimensions. This scale dependency must be recognized in the model construction step.

Model Construction

- An equality between laboratory-measured, well test derived, and correct model values of permeabilities will be coincidental for most reservoirs. This is a consequence of several factors:
	- **Inherent in modeling is the presumption of direct connectivity (along a** straight path) between two adjoining blocks. Yet in-situ flow occurs along a path of least resistance which is anything but a straight path, particularly in heterogeneous environments.
	- The flow path can be through micro-fractures, super-permeability streaks, or in the case of near-wellbore flow via any other channel (e.g., behind pipe leaks). Because laboratory, well test and model flow occur in different scales, their corresponding flow capacities can only be the same when the dominant flow features noted above are scaleindependent.

Model Construction

P Vertical Permeability

- Lake and others have noted the problem associated with scale dependency in permeability assignments, i.e., that core-plug based k_{v} data bear little resemblance to model-cell scale values. Experience indicates that:
	- \blacksquare k_v is not a measurable quantity in the scale of the model grids.
	- *For most reservoirs, the available reservoir control (e.g., wells, logs, correlations) is and probably will always be insufficient to provide the reservoir description to compute* k_y *at the model cell scale.*
- **B** Because of the above there is an level of uncertainty in k_v assignments.

Model Construction

P Vertical Permeability

- **Thus the problem is reduced to arriving at a best guess for initializing the** model, and then relying on history-matching to refine the initial value. Haldorsen and others have published excellent methodologies for guesstimating initial vertical permeability distributions in reservoir models based on geostatistical and/or geologic interpretations.
- For reservoirs where adequate data exist (e.g., RFTs, production profiles), history-matching offers the most practical and effective way of determining model cell scale k_v (via the process of refinement couple with the noted techniques).
- For reservoirs where adequate data exist (e.g., RFTs, production profiles), history-matching offers the most practical and effective way of determining model cell scale k_v (via the process of refinement couple with $\overline{\text{January 30, 2005}}$ the noted techniques).

Model Construction

Horizontal Permeability

- Scale-dependency is also present for k_h ; however, this is not as severe since we are mainly dealing with arithmetic averages (harmonic averages used for k_v).
- When data with different scales (such as cores and well tests) are compared the values are different. The best approach in k_h assignments appears to be:
	- P *Initializing with a best-guess based on permeability transforms calibrated with in-situ data (i.e., well tests).*
	- P *Refining through history-matching.*
- **Implementation of best guess does not guarantee correct scale-up** to model cell conditions.

Validation

There are four ideas that are central to the discussion on validation:

- P History-matching is only a component of validation.
- **There are degrees of validation and history-matching, often when** the term "history-matched" is used, the reference is to a partiallyvalidated model.
- History-matching must not be achieved at the expense of parameter modifications that are physically and/or geologically wrong.
- Even when a model is full validated, simulation results are bound to be probabilistic and not definitive.

Validation

■ Validation can be broken into a sequence of steps : **Initialization**

■ *Process of reviewing the model to be sure that all data have been properly input.*

Equilibration

■ *Bringing the model to equilibrium with respect to internal and external boundary conditions.*

■ History-Matching

■ *Process of modifying the model parameters to achieve a match between model and measured field performance over a period of time at known rates.*

Calibration

P *Adjusting parameters to match field performance with known back*

January 30, 2005 *pressures.* D. Baxendale

Validation - History Matching

 \blacksquare The general format of the manual history-matching process:

P Formulate a Plan

• Review the reservoir-production data to determine which data should be fixed (e.g., rates, pore volumes), what parameters should be adjusted, and what level of control criteria should be used to obtain a match.

\blacksquare Adjust the Data

■ This step is needed mainly to a) allocate production data areally and vertically to the pertinent areas and zones, b) correct field production data to separator conditions consistent with model conditions and c) correct reported pressures for simulation use.

Validation - History Matching

Full Field Matching of Rates, Pressures, Well Matching of Rates, and Flood FrontsPressures, and Flood Fronts **Oil Rate Pressure0.0 0.1 0.2 0.3 0.4** 0.4 **400034007100Field3200Field**Oil Rate (kSTBD) **3000 Model3000 Model280026002000Measured Depth (ft) 72002400 1000220020000 1945 1955 1965 1975 19851800 73001975 1980 1985 1990Time (Years) Time (Years) Water Cut** *Cut Water Rate* **7400100050Model at 1966**Water Cut (Percent) Rate (KSTBD) **FieldFieldModel at 199880040 ModelModelLog at 9/21/98 30600750020400Vater 20010 0 0 1975 1980 1985 19901975 1980 1985 1990**

One hydrocarbon phase is a target, and the simulator predicts the other phase. In the above example oil is the target phase, and hence the perfect match for oil, the quality of the match is from the other phases and pressures.

Time (Years)

January 30, 2005 D. Baxendale

Time (Years)

Validation - History Matching

E Match Pressures

- The process is iterative and involves global changes (affecting all cells in the model) before making local changes (affecting only some cells).
- **Spatial pressure gradients can be more** rapidly matched by changing conductance and/or total mobility than by changing total compressibility and/or pore volume.
- **Temporal pressure gradients can be more** rapidly matched by changing compressibility and/or pore volume than by changing conductance and/or total mobility.

Validation - History Matching

P **Match Saturations**

- Changes in a well's producing GOR and/or water-cut performance can be caused by nearwellbore (coning, cusping) or field wide (gascap shrinkage) effects.
- Near wellbore behavior can be matched by modifying well relative permeability curves, while field-wide behavior can be matched by changes to inter-block curves.
- Changes to inter-block curves should be a last resort. The most effective approach is to initialize models with correctly scaled-up relative permeability curves. Any changes to permeability curves must be explained in terms of geologic and reservoir flow features.

Validation - History Matching

Levels and Criteria of Control

The history-matching process can range from being superficial to thorough depending on data availability. The purpose of a history-matched model is to duplicate:

- **P** Pressure and saturation distributions existing in the field both areally and vertically and
- Observed water cuts and GORs both on a field and well basis.
- **Often, achievement of the latter is accepted as a sufficient** condition for history-matching, when in reality both purposes have to be fulfilled for a full match.

Validation - History Matching

Levels and Criteria of Control

The following figure shows the model pressures versus the observed vertical pressures from the Dunlin field RFT data, as reported by Barbe.

Validation - History Matching

■ Levels and Criteria of Control

- \blacksquare There are two levels of control : field level and well level. At the field level, the intent is to ensure that a given model represents the main drive mechanisms of the reservoir.
- While at the well level, matching of well production rates and RFTs is the objective.
- No quantitative measures of history-matching are given due to the diversity of reservoir problems. For instance for a reservoir which has declined by 1000 psi over a given period, a pressure match with a mean error of 50 psi could be considered acceptable. Yet for a reservoir which has declined only 200 psi over a comparable period, a 50 psi error would be unacceptable.

Validation - Calibration

History-matching uses specified production rates and is directed toward matching pressures and phase distributions. Predictions runs require that production rates be computed.

An uncalibrated model can result in amismatch between historical and predictive well performance. Hence the purpose of this step is to eliminate this mismatch and allow a smooth transition between the historicaland predictive model phases.

Validation - Calibration

 \blacksquare Calibration is achieved by running the model at the back pressures held against the wells. This could be at one or several time-steps. The well PIs and/or wellbore flow parameters are adjusted to duplicate field-observed rates. Although the calibration step is usually done after the history-matching step, there are times when it must be done beforehand (e.g., when modeling multi-layer flow into a well). This is because in stratified reservoirs the correct allocation of rates among layers is dependent on the absolute value of the well's PI (and not solely on the ratios of PIs of various layers).

History Matching - Arun Field Example

Development History

The field was discovered in 1971 by Arun A1.

The initial field development begun in 1975 with the cluster concept (clusters III and II), followed in 1977 with the first liquid production with gas re-cycling, and in 1978 with the first LNG shipment.

In 1982 two additional clusters (I and IV) were developed, for a total of four, and the LNG Plant was expanded in 1984, with NGL Plant & LPG Sales starting 1988.

Eleven bigbore wells (9 5/8 tubing) were drilled from 1992 through to 1995. As of January, 2001 a total of 111 wells have been drilled in the field, including 29 sidetracks.

The Dehydration project was initiated in 1992, followed in 1995 by the Booster Compressors project. In 1999 gas injection was halted, and the gas injectors were converted to producers. Finally, in 2000 the Arun-I contract expired, and the LPG sales were terminated. January 30, 2005 D. Baxendale

History Matching - Arun Field Example

Field Surveillance: Numerical Simulation Model

History Matching - Arun Field Example

Global grid is 14 x 30 x 9 (x,y,z) for a total of 3,780 of which 1,901 are active.

Local Grid Refinement 1(LGR1) is 14 x 42 x 9 resulting in a total of 5,292 grid blocks.

LGR2 is 16 x 70 x 9 for atotal of 10,080 grid blocks.

History Matching - Arun Field Example

History Matching Variables

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History Matching - Arun Field Example

History Matching - Arun Field Example

Predictions

- **This is the phase where most study objectives are met. To avoid the** common errors noted earlier, prediction cases must be carried out while recognizing the limitations of the particular model being used:
	- Lack of validation (e.g., reservoirs with sparse geologic or engineering data).
	- Modeling/mathematical constraints due to compromises in model selection.
	- Inherent uncertainties in RC and/or scale-up of RC to model dimensions.
- **The recognition of these factors and in turn, the realization of the** probabilistic nature of simulation is critical to its use in a rational manner.

Predictions

- **The key point here is that despite the limitations noted above,** most study objectives can still be met by conducting sensitivity runs using "bracketing."
	- **IDENT** Identify the main limitations of the model.
	- **I** Identify the key parameters (reservoir, model, etc.) causing the limitations.
	- **Conduct parameter sensitivity cases to evaluate the effects on** model results.

 These parameters may include geologic attributes such as sand continuity or aquifer size

Documentation

- **The last step requires little elaboration, but no project can** be considered complete without it. The main function of the documentation is to outline the :
	- Objectives, data, and methodology.
	- **Results and conclusions.**
	- **Example 1** Limitations of results and the methodology.
- \blacksquare In particular, the last point is important for any engineering decision that will be based on the study.