

ACADEMIC REPORT

About IWM

Indian Women and Mathematics (IWM) is a collective of Indian mathematicians that has been in existence since 2009. Our objective is to encourage more women to pursue higher education in mathematics, and to organize events and networking opportunities that will enable them to take up careers in mathematics.

The IWM Annual Conferences aim to bring together women students, college and university teachers and early-career researchers with mathematicians, especially women mathematicians **not just from India but internationally,** working at the frontiers of mathematics, to exchange mathematical ideas and share their experiences.

A major goal of these events is to enable junior women mathematicians to interact with their senior colleagues, both individually and in small groups, as well as to present their own work. To this end, in addition to the invited talks, there are sessions featuring contributed talks, and a poster session. Advanced Ph.D. students and early-career researchers are encouraged to give a contributed talk or present a poster. Participation is *not* restricted to women only. Others are welcome to apply, especially those in the early stages of their careers.

For more information on IWM please visit the website <u>https://sites.google.com/site/iwmmath</u>.

The 2018 Annual Conference

The 2018 Annual Conference was held at Shiv Nadar University, in the National Capital Region, during June 21-23. It was sponsored by the National Board for Higher Mathematics. Significant financial support was also received from the Committee for Women in Mathematics (CWM) of the International Mathematical Union. The CWM support enabled us to reach out to neighbouring countries and, for the first time, the conference had a delegation of 6 women mathematicians from **Nepal**. The total number of registered participants in the conference was 85. These came from all parts of India.

The program of the conference featured 4 **plenary talks**, 4 **invited talks**, 4 **talks by young mathematicians**, 12 **contributed talks**, a **poster session**, and a **mini-course on knot theory**. There was also a **panel discussion** on "*Indian Women and Mathematics-looking behind and the road ahead*".

The **Scientific Committee** of the conference consisted of Gautam Bharali (Indian Institute of Science), Priyanka Grover (Shiv Nadar University), Amber Habib (Shiv Nadar University), Riddhi Shah (Jawaharlal Nehru University), Sachi Srivastava (University of Delhi), and Geetha Venkataraman (Ambedkar University Delhi).

The members of the **Organizing Committee** were Neha Gupta, Amber Habib, Sneh Lata, Satyanarayana Reddy, Charu Sharma (all from Shiv Nadar University) and Geetha Venkataraman (Ambedkar University Delhi).

Invited Contributions

Plenary Talks:

Speaker	Affiliation	Title
Neela Nataraj	IIT Bombay	Finite element methods: Research in India
		over last decade
Madhu Raka	Panjab University	Recent Developments on Conjectures of
		Woods and Minkowski
R. Parimala	Emory University	Quadratic forms and Clifford algebras
Vijaylaxmi Trivedi	Tata Institute of	Hilbert-Kunz Invariants, with Applications
	Fundamental Research	to Semistability, Tiling and F-thresholds

Mini-Course:

A mini-course of 3 lectures on **Knot Theory and Quantum Groups** was delivered by Dr Rama Mishra, IISER Pune.

Invited Talks:

Nikita Agarwal	IISER Bhopal	Stability of Switched Dynamical Systems
Sujata Ghosh	ISI Chennai	Formal studies of strategic reasoning
Jyotshana Prajapat	University of Mumbai	Some problems in potential theory and free
		boundaries
Anuradha Sharma	IIIT Delhi	On the structure and distances of repeated-
		root constacyclic codes of prime power
		lengths over finite commutative chain rings

Talks by Young Mathematicians:

Ananya Lahiri	Chennai Mathematical	Asymptotic properties of the volatility
	Institute	estimator from high-frequency data modelled
		by mixed fractional Brownian motion
Purvi Gupta	Rutgers University	Polynomial density on compact real
		manifolds
Shreedevi Masuti	Chennai Mathematical	On the Waring problem for binary forms
	Institute	
Vandana Rajpal	Shivaji College,	λ -theory of operator spaces
	University of Delhi	

Panel Discussion on "Indian Women and Mathematics-looking behind and the road ahead":

The panellists were: Riddhi Shah (Jawaharlal Nehru University), Gautam Bharali (Indian Institute of Science), Priyanka Grover (Shiv Nadar University), Purvi Gupta (Rutgers University), Amber Habib (Shiv Nadar University). The panel initiated a discussion on the outcomes so far of the IWM project, the need to continue, obstacles faced in the journey, and possibilities for the future.

Participants from Nepal

The IWM project has started to network with mathematicians from neighbouring countries such as Bangladesh and Nepal, and we have participated in activities in Nepal. The 2018 Annual Conference featured a delegation of mathematicians from Nepal, who also gave talks and presented posters:

Dhana Kumari Thapa	Tribhuvan University	Contributed Talk
Saraswati Acharya	Kathmandu University	Contributed Talk
Anjana Pokharel	Tribhuvan University	Poster
Sharmila Shreshtha	Kathmandu University	Poster
Sarala Luitel	Tribhuvan University	
Tara Paudel	Tribhuvan University	
Prakriti Dhakal		

Images



Plenary Lecture by Neela Nataraj



Plenary Lecture by Vijaylaxmi Trivedi



Plenary Lecture by R Parimala



Mini-course by Rama Mishra

				IWM 2018-SCHE	DULE OF	<u>TALKS</u>			
				DAY 1-June 21, 2018					
9:00-9:30 9:30-10:00	10:00-11:00	11:00-11:30	11:30-12:30	12:30-13:05	13:05-14:30	14:30-15:15	15:15-15:55	15:55-16:25	16:25-17:40
Registration Inauguration	Plenary talk- Neela Nataraj	Tea	Mini course- Rama Mishra	Young mathematician- Purvi Gupta	Lunch	Invited talk- Anuradha Sharma	Contributed taiks (3 sessions, 2 taiks each) Parallel Session I- Preetl, Sheela Verma Parallel session II-Jyoti Singh, Dishari Chaudhuri Parallel Session III-Charu Sharma, A. Karthika	Tea & Poster	Panel discussion
				DAY 2-June 22, 2018					
9:00-10:00	10:00-10:45	10:45-11:15	11:15-12:30	12:30-13:05	13:05-14:30	14:30-15:30	15:30-16:15	16:15-17:15	
Plenary talk-Madhu Raka	Invited talk- Jyotshana Prajapat	Tea	Mini course- Rama Mishra	Young mathematician- Ananya Lahiri	tunch	Plenary talk- Vijaylaxmi Trivedi	Poster Session & Tea (Tea starts at 15:45)	Contributed talks (3 sessions, 3 talks each) Parallel Session I-Isha Garg, Anchal Aggarwal , Monimala Nej Parallel Session II-Lachit Bora, Neha Agarwal, Pinkimani Goswami Parallel session III-, Parbati Sahoo, Saraswati Acharya, Shivangi	
				DAY 3-June 23, 2018					
9:00-10:00	10:00-10:45	10:45-11:15	11:15-12:30	12:30-13:05	13:05-14:30	14:30-15:15	15:15-15:50	15:50-16:20	16:20
Plenary talk-R. Parimala	Invited talk- Nikita Agarwal	Tea	Mini course- Rama Mishra	Young mathematician- Vandana Rajpal	Lunch	Invited talk-Sujata Ghosh	Young mathematician-Shreedevi Masuti	Valedictory function	Farewell Tea

Abstracts

PLENARY TALKS

Speaker: Neela Nataraj (IIT Bombay)

Title: Finite element methods: Research in India over last decade

Abstract: In this talk, some major contributions of Indian mathematicians to the mathematical aspects of the finite element method in the last one decade will be outlined. A brief description of the method itself is provided so that the talk is accessible to anybody with a background in partial differential equations and numerical techniques for solving it. We will then focus on some of our recent contributions to the area that include FEM for nonlinear plate bending problems and distributed optimal control problems governed by plate bending problems.

Speaker: Madhu Raka (Punjab University)

Title: Recent developments on Conjectures of Woods and Minkowski

Abstract: In Geometry of Numbers, there is a longstanding classical conjecture of Minkowski on the product of n non-homogeneous linear forms. In this talk I will deliberate upon the history of the conjecture, different approaches tried to solve it including the approach via Woods Conjecture. I will also discuss some developments on these conjectures during the last decade. The conjectures are settled for n < = 9 only.

Speaker: Vijaylaxmi Trivedi (TIFR Mumbai)

Title: Hilbert-Kunz invariants, with applications to semistability, tiling and F-thresholds

Abstract: We give a brief survey of Hilbert-Kunz multiplicities and density functions. These are characteristic p singularity invariants for commutative Noetherian rings. The HK density function is a compactly supported continuous function and was introduced to study the numerical invariant e_{HK} (HK multiplicity).

This idea of replacing a number (e_{HK}) by a function (HK density) seems to be an effective technique to handle the notoriously difficult invariant e_{HK} .

On the other hand the HK multiplicity characterizes seemingly unrelated invariants like Frobenius semistablity of the vector bundles over curves, F-thresholds for curves and the tiling property of rational convex polytopes.

Speaker: R. Parimala (Emory University, USA)

Title: Quadratic forms and Clifford algebras

Abstract: Let k be a number field. Class field theory enables us to understand the Brauer group of k. The Clifford algebras of quadratic forms define classes in the Brauer group of k which are classes of quaternion algebras. Further Hasse--Minkowski theorem leads to the fact that every 5-dimensional indefinite quadratic form over k has a nontrivial zero. In this talk, we explain how over a general field of characteristic not 2, Clifford algebras play a central role in determining whether quadratic forms in large enough number of variables admit a nontrivial zero.

MINI-COURSE

Title: Knot Theory and Quantum groups

Speaker: Rama Mishra (IISER Pune)

Abstract: In this mini course I will provide exposure to research in knot theory and talk about the basic philosophy behind constructing knot invariants. It will be shown that in the process, certain quantum groups naturally arise. I will elaborate on Quantum groups in general and show how their representations lead to constructing knot invariants.

INVITED TALKS

Title: On the structure and distances of repeated-root constacyclic codes of prime power lengths over finite commutative chain rings **Speaker:** Anuradha Sharma (IIIT Delhi)

Abstract: Let p be a prime, s be a positive integer, and let \mathcal{R} be a finite commutative chain ring with the characteristic as a power of p. For a unit $\lambda \in \mathcal{R}, \lambda$ -constacyclic codes of length p^s over \mathcal{R} are ideals of the quotient ring $\mathcal{R}[x]/\langle x^{p^s} - \lambda \rangle$. We derive necessary and sufficient conditions under which the quotient ring is a chain. When $\mathcal{R}[x]/\langle x^{p^s} - \lambda \rangle$ is a chain ring, all λ -constacyclic codes of length p^s over \mathcal{R} are known. We establish algebraic structures of all λ -constacyclic codes of length p^s over \mathcal{R} when $\mathcal{R}[x]/\langle x^{p^s} - \lambda \rangle$ is a nonchain ring. We also determine the number of codewords in each of these codes. Using their algebraic structures, we obtain Hamming distances, b-symbol distances, Rosenbloom-Tsfasman (RT) distances, and Rosenbloom-Tsfasman (RT) weight distributions of all constacyclic codes of length p^s over \mathcal{R} ; where $2 \le b < p^s$. Apart from this, we derive necessary and sufficient conditions under which a constacyclic code of length p^s over \mathcal{R} is maximumdistance separable (MDS) with respect to the (i) Hamming metric, (ii) b-symbol metric, and (iii) Rosenbloom-Tsfasman (RT) metric. We also provide an algorithm to decode constacyclic codes of length \square^{\Box} over \Re .

This is a joint work with my PhD student, Ms. Tania Sidana.

Title: Some problems in potential theory and free boundaries

Speaker: Jyotshana Prajapat (University of Mumbai)

Abstract: I will introduce some problems, solved as well as open, in topics of potential theory and related to free boundary problems. Some symmetry results will also be discussed.

Title: Stability of Switched Dynamical Systems

Speaker: Nikita Agarwal (IISER Bhopal)

Abstract: A continuous-time switched system is a piecewise continuous dynamical system with finitely many subsystems, and a piecewise constant function, known as the switching signal, which determines the switching of the system between subsystems. A signal is represented by the admissible switching from one subsystem to another, and the times at which these switchings take place. In this talk, the switching between subsystems will be governed by an underlying digraph. That is, the system can switch from a subsystem to another if there is a directed edge between the corresponding vertices on the underlying graph.

Even when all the subsystems are stable, the switched system may be unstable for some switching signal. Moreover, one can construct a signal which can stabilize a switched system with all unstable subsystems. Thus, it is evident that the stability of a switched system not only depends on the properties of subsystems, but also on the switching signal. In this talk, we will discuss some sufficient conditions on the switching times under which the switched system will be stable. We will introduce a novel concept of simple loop dwell time and use it to derive these sufficient conditions for stability. This approach is an improvement over other notions such as dwell time and average dwell time which are popularly used to derive sufficient conditions for stability. Further this approach will give rise to a slow-fast switching mechanism which is effective and useful for application purposes.

Title: Formal studies of strategic reasoning

Speaker: Sujata Ghosh (ISI Chennai)

Abstract: In addition to 'real' games like chess and bridge, strategies play out in many different areas of life. As such, the study of strategic reasoning in games has become an integral part of many areas of science. After providing a brief overview of these relevant areas, the talk will focus on a particular kind of games, namely dynamic games, and discuss certain formal investigations of these games from the viewpoints of logic and game theory. The talk will not assume any prior knowledge of logic or game theory.

TALKS BY YOUNG MATHEMATICIANS

Title: Polynomial density on compact real manifolds

Speaker: Purvi Gupta (Rutgers University, USA)

Abstract: In this talk, we will discuss some questions regarding the minimum embedding (complex) dimension of abstract compact (real) manifolds conditional on certain approximation-theoretic considerations. The primary challenge comes from the so-called CR-singularities of an embedding. We will discuss why this is the case, and how they can be dealt with in certain dimensions.

This is a joint work with R. Shafikov (UWO, Canada).

Title: Asymptotic properties of the volatility estimator from high-frequency data modelled by mixed fractional Brownian motion

Speaker: Ananya Lahiri (CMI)

Abstract: Properties of mixed fractional Brownian motion (MFBM) has been discussed by Cheridito (2001) and Zili (2006). We have proposed an estimator of volatility parameter for a model driven by MFBM. Model is essentially geometric mixed fractional Brownian motion if we can name it so. The motivation for this model is from a paper by Sun L. (2013). We have considered

the estimator of the volatility parameter from high-frequency data. In our article, we have shown that this estimator of the volatility parameter has some desirable asymptotic properties, namely strong consistency, asymptotic normality. We have also calculated Barry Esseen bound and provided with some simulation studies to support our findings.

Title: λ -theory of operator spaces

Speaker: Vandana Rajpal (DU)

Abstract: We extend the λ -theory of operator spaces given in Defant and Wiesner (J. Funct. Anal. 266(9): 5493{5525, 2014), that generalizes the notion of the projective, Haagerup and Schur tensor norm for operator spaces to matrix ordered spaces and Banach *-algebras. The ideal structure of λ -tensor product of C* -algebras has also been discussed. This is a joint work with Ajay Kumar and Preeti Luthra.

Title: On the Waring problem for binary forms

Speaker: Shreedevi Masuti (CMI)

Abstract: It is well-known that every homogeneous polynomial with coefficients in the field of complex numbers can be written as a sum of powers of linear forms. Given a form F, the Waring problem asks for the minimal number of summands needed for such an expression of F. In this talk we will discuss the Waring problem for binary forms. This is my joint work with Laura Brustenga.

CONTRIBUTED TALKS

Title: A Note on Lindelöf Spaces

Speaker: A. Karthika (SriKrishna College of Eng. and Tech., Tamil Nadu)

Abstract: The aim of this paper is to obtain the characterizations of Lindelöf spaces with respect to grill. We also introduce the G-regular and G-normal spaces in grill topological spaces and exhibit the relationship among them.

Title: Contractive maps on operator ideals and norm inequalities III

Speaker: Anchal Aggarwal (Sant Longowal Inst. of Eng. and Tech.)

Abstract: Let (I, |||.||) be a norm ideal of operators equipped with a unitarily invariant norm |||.||. We discuss some generalized Lyapunov type norm inequalities for operators, which are motivated by the work of Bhatia and Drissi, Hiai and Kosaki and JociÄ. We exploit integral representations and series expansions of certain functions to prove that certain ratios of linear operators acting on operators in I are contractive. This leads to several new and old norm inequalities for operators which were earlier in the matrix settings.

Title: Uncovering the network amongst the stocks returns by studying the non-linear interactions in high frequency data of the Indian Stock Market

Speaker: Charu Sharma (SNU)

Abstract: We explore the detection of clusters of stocks that have similar properties and tend to move together in the Indian Stock Market. We have based our study on high frequency data for the year 2014. This was a year when general elections happened in India, and thus we have verified that the "stronger network connections" remained unaffected by the elections. We have used functional and nonlinear variants of principal component analysis, FPCA and KPCA. The nonlinear methods resulted in establishing stronger networks in comparison to linear methods. Of the two prominent clusters that showed up in our analysis, one corresponded to the banking sector and another to the IT sector. The cluster corresponding to banking sector emerged as an isolated, standalone cluster, which remain unaffected even during the election periods. The other smaller clusters found are from the automobile industry and the energy sector. Inter cluster interactions were also observed. The learning gained from these interactions is substantial as one can exploit this insight in developing trading strategies for intraday traders.

Title: Some Aspects in Complex Dynamics **Speaker:** Dhana Kumari Thapa (Tribhuvan University, Nepal)

Abstract: Complex Dynamics is considered as an interesting subject of theory and application. My presentation aims reviewing some aspects in complex dynamics.

Title: (σ, τ) -Derivations of Integral Group rings

Speaker: Dishari Chaudhuri (IISER Mohali)

Abstract: A result due to E. Spiegel (Comm. Algebra, Vol. 22, pg. 2955-2959, 1994) says that every derivation of an integral group ring of a finite group is inner. An extension of this result to (σ, τ) -derivation of an integral group ring of a finite group will be presented. The work has been communicated. Details can be found in <u>https://arxiv.org/pdf/1803.09418.pdf</u>.

Title: Positivity properties of some non-negative matrices

Speaker: Isha Garg (NIT Jalandhar)

Abstract: In the present talk, we will discuss positivity properties of matrices $[f(p_i + p_j)]$ and $[f(p_i - p_j)]$ where f is a non-negative operator concave or operator convex function on $[0, \infty)$ and p_1, p_2, \cdots, p_n are distinct positive real numbers. The results for these matrices for power function t^r on $[0, \infty)$ for r > 0 are proved by Bhatia and Jain in 2015 and Dyn, Goodman and Michelli in 1986. Our results generalize these results and lead to many known and new results.

Title: Derived functors of Graded local cohomology modules

Speaker: Jyoti Singh (Visvesvaraya National Institute of Technology, Nagpur)

Abstract: Let $R = [X1 \dots, Xn]$, where K is a field of characteristic zero and R is standard graded. Let $m = (X1, \dots, Xn)$ and let E be the *injective hull of R/m. Let A(K) be the nth Weyl algebra over K. If T is graded Lyubeznik functor on * Mo(R), then we show that T(R) is generalized Eulerian An(K) module. As an application, we show that $H_m^i T(R) \cong E(n)^{a_i}$ for some $a_i \ge 0$.

(This is the joint work with Prof. Tony J. Puthenpurakal, IIT Bombay).

Title: On Selmer group of certain admissible extensions

Speaker: Lachit Bora (JNU)

Abstract: Selmer group of an elliptic curve has been object of study for a long time. We investigate the dual Selmer group for a certain admissible extension namely the compositum of the so-called GL_2-extension and the anticyclotomic extension of an imaginary quadratic number field over the Iwasawa algebra of the Galois group of this extension. This is a part of our thesis in preparation.

Title: Exponents of primitive symmetric companion matrices

Speaker: Monimala Nej (SNU)

Abstract: In this paper, we found:

(i) total number of primitive and imprimitive symmetric companion matrices.

(ii) the exponent set for the class of primitive symmetric companion matrices. More generally we found exponent of every primitive symmetric companion matrix.

(iii) the number of primitive symmetric companion matrices with a given exponent for certain cases.

Title: Synchronization of a new asymmetric fractional order hyper chaotic system using adaptive control.

Speaker: NEHA AGRAWAL (DU)

Abstract: In this paper we have introduced a new fractional order hyperchaotic system and investigated its chaos synchronization using adaptive control technique.

Title: Wormholes in R^2-gravity within the f(R, T) formalism

Speaker: Parbati Sahoo (BITS Pilani, Hyderabad)

Abstract: We propose, as a novelty in the literature, the modelling of wormholes within the particular case of the f(R,T) gravity, namely $f(R,T)=R+\arc{2}+\arc{$

Title: A new example of Pseudo-free group

Speaker: Pinkimani Goswami (USTM)

Abstract: Most of the existing public key cryptosystems are based on the intractability of certain mathematical problems such as integer factorization problem, discrete logarithm problem etc. Many of those problems involve computations in a group and have the common property that they can become completely unsolved if the corresponding group is replace with a free group. So, instead of making assumption that such-and-such problem is difficult to solve in a group, one can say once and for all that the given group is difficult to distinguish from a free group. Such a group is called pseudo-free group. The RSA group Z_N. where N is the product of two safe primes is the only known example of pseudo-free group and it is an interesting problem to find another example of pseudo-free group. In this article, we have given a new example of pseudo-free groups.

Title: Operator system tensor products and C*-envelopes

Speaker: Preeti (Delhi University)

Abstract: The relationship between an operator system and its C*-envelope is a mysterious one. We discuss the topic of tensor product of operator systems and characterization of some structural properties of operator systems via canonically associated C*-envelopes. This talk is based on my doctoral thesis.

Title: The Effects of Sex and Menstrual Cycle Phases on Human Temperature Distribution

Speaker: Saraswati Acharya (Kathmandu University, Nepal)

Abstract: The paper deals implication of Pennes bio-heat equation by considering the suitable physical and physiological parameters of human body relying on dermal thickness of males and females for temperature distribution on the layers of dermal part. The mathematical model involving bio-heat equation has been solved using finite element method and Crank-Nicolson technique to numerically investigate two dimensional temperature distributions. Initially, human dermal region under consideration is divided into six parts: stratum corneum,

stratum germinativum, papillary region, reticular region, fatty layer and muscle part of subcutaneous tissue.

The results delineate tissue temperature distribution during follicular and luteal phases of females. The study is further carried out for the temperature distribution results of these phases as compared to males temperature distribution. The analysis presents that during the luteal phase of females, the tissue temperature is lower as compared to males when atmospheric temperature T falls below body core temperature. Likewise, females luteal phase temperature is slightly higher as compared to males when T exceeds body core temperature. But females follicular phase temperature is lower as compared to females luteal phase and males body temperature either T is greater or less body core. The above differences of females compared to males under same atmospheric conditions may be the causes of females hormonal variation during the menstrual cycle phases.

Title: On Eigenvalue problem related to the Laplacian in a class of doubly connected domains

Speaker: Sheela Verma (IIK Kanpur)

Abstract: In this work, we consider two eigenvalue problems on some specific doubly connected domain.

First we consider the Steklov-Dirichlet eigenvalue problem on punctured domain (a smaller ball is take out from a bigger ball) and prove that the first eigenvalue of this problem attains its maximum only if balls are concentric.

Next we study Neumann eigenvalue problem on a punctured geodesically symmetric domain and prove that the first non-zero Neumann eigenvalue attains its maximum for annular domain.

This work is being sent for publication.

Title: METHODS TO SOLVE DIOPHANTINE EQUATIONS

Speaker: SHIVANGI ASTHANA (NORTH EASTERN HILL UNIVERSITY)

Abstract: In this paper our main aim is to highlight the different methods used to solve

Diophantine Equations.