

Flux Optimization in Reverse Osmosis via the Solution-Diffusion Model

Hisham A. Maddah

Abstract—This paper suggests a new method of predicting flux values at reverse osmosis (RO) desalination plants. The study is initiated by using the solution-diffusion model that is applied to the groundwater source at Abqaiq plant (500 RO plant) at Saudi Aramco, Dhahran (Saudi Arabia) in order to calculate the osmotic pressure of the treated water for Shedgum/Abqaiq groundwater. For modelling purposes, the same technique is used to determine the osmotic pressure drops at the same plant configuration and operating conditions when using seawater sources such that of the Arabian Gulf and the Red Sea waters. High rejection brackish water RO (BWRO) element Toray TM720D-400 with 8" is the RO membrane type used at Abqaiq plant. The calculated osmotic pressures of the three water sources, assuming that they are all treated at Abqaiq plant, are utilized to determine the appropriate flux values as well as membrane resistances of different BWRO Toray membranes. Values of numerous parameters such as water permeability constant, applied pressure, gas constant, water temperature, water molar volume, membrane thickness, and water salinity/TDS are taken into account to develop our calculations through the solution-diffusion model. A comparison between low-pressure, standard and high-pressure BWRO Toray membranes performance have been established to select the ideal membrane type for the treatment of water from various sources at Abqaiq plant. The model results confirm an inverse relationship between the membrane thickness and the water flux rate. Also, a proportional linear relation between the overall water flux and the applied pressure across the membrane is identified. Higher flux rates and lower salinity indicate lower membrane resistance which yields to the higher water production. Modelled data predict that BWRO Toray TM720D-440 with 8" membrane is the optimal choice for treating waters from the three water sources at Abqaiq plant.

Index Terms—Reverse Osmosis, Flux, Water Treatment, Desalination, Modelling, Solution-Diffusion.

I. INTRODUCTION

The solution-diffusion model is a popular expression used to explain the transport in dialysis, reverse osmosis, gas permeation and pervaporation. Previous experimental data and modelling results verified that the flux rate is proportional to a gradient in the chemical potential [1].

There are two different models to describe and control the permeation in membranes for better separation. The first model is the solution-diffusion model where permeants dissolve (sorption) in the membrane material at the upstream interface in the presence of a concentration gradient that allows permeants to diffuse through the membrane and desorbed on the downstream interface side. The separation

between different permeants occurs because each material has a different diffusion rate in the membrane. The solution-diffusion model has been used since 1940 to explain the transport of gases across polymeric membranes. A second model called the pore-flow model, which depends on the presence of a pressure gradient for a convection flow of permeants through the membrane's tiny pores, is more limited compared to the first model. Exclusion or filtration of larger permeant's pores is the separation technique explained via the pore-flow model [1, 2].

There is a major difference between the solution-diffusion model and the pore-flow model in expressing the chemical potential. In the solution-diffusion model, the pressure within a membrane is uniform and that the chemical potential gradient is expressed only as a concentration gradient. Solution-diffusion membranes transmit pressure in the same way as liquids that is the reason for expressing the pressure difference across the membrane as a concentration gradient only. On the other hand, the chemical potential gradient in the pore-flow model is expressed only as a pressure gradient since the concentrations of both solvent and solute within a membrane are uniform. Fig. 1 shows a comparison between both models for a one-component solution in a pressure-driven permeation system [1, 2].

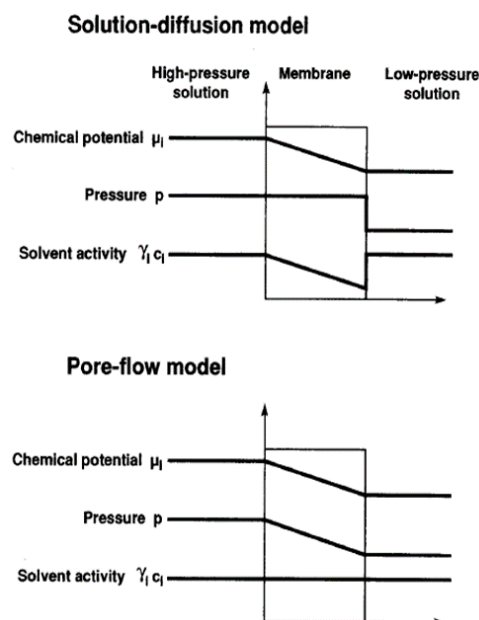


Fig. 1. Pressure-driven permeation of a one-component solution across a membrane according to the solution-diffusion and the pore-flow models; Adapted from [1, 2].

The objective of this work is to estimate the osmotic pressure drop value of the high rejection brackish water RO membrane (Toray TM720D-400 with 8") by using the solution-diffusion model that is applied to Abqaiq plant (500

RO plant) for Shedgum/Abqaiq groundwater at Saudi Aramco, Dhahran, Saudi Arabia. Osmotic pressure drops have been calculated for the groundwater, the Arabian Gulf and the Red Sea waters at the same plant configuration and operating conditions of Abqaiq plant in Aramco.

The calculated osmotic pressures are utilized to determine the applied pressure drop across the membrane and the applicability of using different BWRO Toray membrane types for the treatment of seawaters. The maximum achievable water flux values are determined for the various suggested BWRO membranes for the three water sources. Also, the membrane resistance values have been investigated for comparison purposes. The ideal membrane for the treatment of various water sources at a RO plant with the same configuration of Abqaiq plant has been selected.

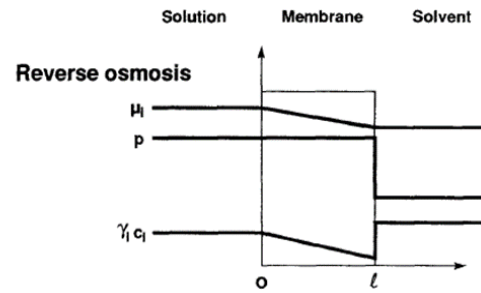
The feasibility of using BWRO membranes in desalination of Red Sea water in Jeddah, Saudi Arabia is studied at the same flux rate of the Arabian Gulf water source and same plant conditions of Abqaiq plant. The osmotic pressure drop, applied pressure drop, flux rates, and membrane resistance values for the Red Sea water source are compared with those of Shedgum/Abqaiq groundwater and Arabian Gulf water.

II. REVERSE OSMOSIS

In reverse osmosis, water flows from the salt solution to the pure waterside by applying pressure (Δp) that is greater than the osmotic pressure ($\Delta \pi$) [1]. Generally, in reverse osmosis, we must satisfy this condition ($\Delta p > \Delta \pi$) all the time to allow water to pass through the membrane and reach the permeate side [1, 2]. Reverse osmosis membranes are preferred over Ultrafiltration and Nanofiltration since they are capable of removing 90 to 99% of TDS in water [3].

Osmotic pressure ($\Delta \pi$) is defined as the pressure difference ($p_o - p_e$) across the membrane. If a pressure higher than the osmotic pressure is applied to the feed side (left side in Fig. 2) of the membrane, the process is called reverse osmosis. Fig. 2 shows the driving forces in a reverse osmosis membrane according to the solution-diffusion and the pore-flow models. μ_i and γ_i are the chemical potential and activity coefficient, respectively, of component i [1].

Dense solution-diffusion membrane



Porous, pore-flow membrane

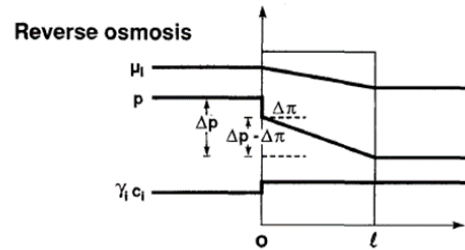


Fig. 2. Chemical potential, pressure, and solvent activity profiles in a reverse osmosis membrane according to the solution-diffusion and the pore-flow models; Adapted from [1].

III. METHODOLOGY AND DATA

Collected Abqaiq 500 RO plant data (Table I) have been used to determine osmotic pressure drop values for the RO membrane (Toray TM720D-400 with 8") from Equations (1) and (2). However, in order to calculate the osmotic pressure for seawater sources, we applied the same information of Shedgum/Abqaiq groundwater at Abqaiq 500 RO plant, except for the flux and salinity values, for the treatment of either the Arabian Gulf or the Red Sea waters as listed in Table I [1, 4].

Water permeability is approximately determined to be $9.5 \times 10^{-7} \text{ cm}^2/\text{s}$ [8]. For water-salt solution, reverse osmosis permeation expression can be simplified as the following [1, 5]:

$$J_i = A(\Delta p - \Delta \pi) \quad (1)$$

$$A = \frac{P_i c_{io} v_i}{RT\ell} \quad (2)$$

Where;

J_i = Membrane flux of component i , water, gfd

Δp = Applied pressure drop across the membrane, psi

$\Delta \pi$ = Osmotic pressure drop across the membrane, psi

A = Water permeability constant, $\text{cm}^3/\text{atm s}$

P_i = Permeability of component i , water, cm^2/s

c_{io} = Initial mole concentration of water, ppm

v_i = Water molar volume, cm^3/mol

T = Water temperature, K

R = Gas constant, $\text{m}^3 \text{atm}/\text{mol K}$

ℓ = Membrane thickness which is assumed to be similar to spacer thickness, mil

Membrane resistance [8] constants for each BWRO Toray membrane has been calculated by using Equation (3).

$$J_i = \frac{\Delta p}{\kappa R_m} \quad (3)$$

Where;

J_i = Membrane flux of component i , water, gfd

Δp = Applied pressure across the membrane, psi

κ = Dynamic viscosity of water, $lb\ s/ft^2$

R_m = Membrane resistance, ft^{-1}

Van't Hoff [9] osmotic pressure (π) formula can estimate the osmotic pressure of an aqueous solution from its molar concentrations of dissolved species. The overall required osmotic pressure drop ($\Delta\pi$) in the water treatment plant has been investigated for the three various water sources from Equation (4).

$$\pi = \mathcal{M}RT \quad (4)$$

Where;

\mathcal{M} = Molar concentration of dissolved species, mol/L

R = Ideal gas constant, $(0.08206\ L\ atm/mol\ K)$

T = Water temperature, K

TABLE I: DATA OF RO MEMBRANE PROCESS AT ABQAIQ 500 RO PLANT (SHEDGUM/ABQAIQ GROUNDWATER) AND THE TWO SEAWATERS STUDIED SCENARIOS [1, 4, 6, 7]

Parameter	Shedgum/ Abqaiq Groundwater	Arabian Gulf Water	Red Sea Water
Membrane type	Toray TM720D-400 with 8"		
RO module	72 parallel membranes \times 8 units		
Membrane thickness (ℓ) [3]	Assumed to be similar to spacer thickness of 34 mil		
Membrane area (Area) [3]	400 ft^2		
Max pressure drop per vessel (Δp)	$\sim 60\ psi$		
Max pressure drop per membrane (Δp)	$\sim 20\ psi$		
Water salinity (c_{io})*	~ 2800 [4]	~ 41070 [6]	~ 42070 [7]
Membrane water flux (J_i)*	$\sim 18\ gfd$	$\sim 12\ gfd$	$\sim 12\ gfd$
Water temperature (T)	$\sim 25^\circ C$		
Water permeability constant (P_l)**	$9.5 \times 10^{-7}\ cm^2/s$		
Water molar volume (v_l)	$18\ cm^3/mol$		
Gas constant (R)	$8.2057 \times 10^{-5}\ m^3 atm/mol\ K$		

*Averaged values (unit is ppm for water salinity)

** Taken from Paul (2004), regardless of the temperature effect on permeability; can be calculated at different temperatures from Maddah (2016) [16]

Equation (5) defines the ability of a membrane to separate salt from the feed solution which is known as membrane removal percentage (χ) and it increases with the applied pressure. The feed TDS concentration is taken from the three studied various sources, as shown in Table I, while the outlet TDS concentration is determined by using Equation (5) at a similar removal percentage of Toray TM720D-400 with 8" membrane that is 99.8%, Table IV. The water molecular weight ($18\ g/mol$) should be used to convert our ppm values to molar concentrations of TDS.

$$\chi = \left(\frac{c_{jo} - c_{je}}{c_{jo}} \right) \times 100 \quad (5)$$

Where;

χ = Membrane removal percentage, %

c_{jo} = Initial concentration of component j , salt, ppm

c_{je} = Final concentration of component j , salt, ppm

Table II shows the applied pressure drop per element (RO module) must be at 20 psi or below and must be 60 psi or below per vessel [4, 6]. The assumption of having equal pressure on membranes per vessel would simplify our calculations. Altaee's study showed that permeate flow, pressure and recovery rate are distributed almost equally to membranes per RO vessel [10]. A field study confirmed an improved performance by rearranging the elements in pressure vessels in order to reduce the pressure drop and permeate conductivity across the vessel [11]. Typical flux rates and maximum recovery values for the groundwater and the two studied water source scenarios (the Arabian Gulf and the Red Sea waters) at Abqaiq 500 RO plant are given in Table III.

TABLE II: OPERATING DESIGN LIMITS OF THE OVERALL RO MODULE AT ABQAIQ 500 RO PLANT FOR SHEDGUM/ABQAIQ GROUNDWATER [4, 12, 13]

Operating Limits	
Maximum Operating Pressure	600 psi (4.1 MPa)
Maximum Feed Water Temperature	113 °F (45 °C)
Maximum Feed Water SDI15	5
Feed Water Chlorine Concentration	Not Detectable
Feed Water pH Range, Continuous Operation	2-11
Feed Water pH Range, Chemical Cleaning	1-12
Maximum Pressure Drop per Element	20 psi (0.14 MPa)
Maximum Pressure Drop per Vessel	60 psi (0.4 MPa)

TABLE III: CHARACTERISTICS OF GROUNDWATER SOURCE AND THE STUDIED WATER SOURCES AT ABQAIQ 500 RO PLANT [4]

Water Source	Shedgum/Abqai q Groundwater	Arabian Gulf	Red Sea
Feed silt density index	$SDI < 3$	$SDI < 4$	$SDI < 4$
Typical target flux, gfd	18	12	12
Max. element recovery, %	19	14	14

The determined osmotic pressure values for the RO membrane (Toray TM720D-400 with 8") of the groundwater and the two studied water source scenarios are used again in Equation (1) to calculate the applied pressure drop and suggested flux values. The same osmotic pressure drop for each case is utilized to determine the results of different Toray BWRO membrane types at high, low and standard operating pressure as shown in Table IV. It is worth mentioning that our applied pressure drop must be higher than the calculated osmotic pressure in order to have a positive flux.

TABLE IV: VARIOUS TORAY BRACKISH WATER RO 8" DIAMETER MEMBRANES [13, 14]

Category	Type	Rejection (%)	Thickness (mil)*
Standard	TM720-370	99.7	31
	BWRO	99.7	28
High-pressure	TM720DA400	99.8	31
	TM720D-400	99.8	34
	TM720D-440	99.8	28
	TM720C-440	99.2	28
Low-pressure	TM720L-400	99.5	31
	TM720L-440	99.5	28

* Since enough data are not available, the membrane thickness is assumed to be the same as spacer thickness to ease our calculations

TS-diagrams [7] are used to determine the exact value of water densities at different feed sources from the average water temperature and water salinity, Table V. Exact water densities allow us to convert gas constant values from $m^3 atm/mol K$ to $kg atm/mol K$ to progress calculations.

Water Source	Temperature (°C)	Salinity (ppm)	Density (kg/m^3)
Shedgum/Abqaiq Groundwater	25	2800 [2]	999.19
Arabian Gulf	25	41070 [4]	1027.97
Red Sea	25	42070 [6]	1028.67

Water Source	A (cm/atm s)	J_i (cm/s)	J_i/A (atm)	$\Delta\pi$ (atm)	$\Delta\pi$ (psi)	$\Delta\pi$ per vessel < 60 (psi)
Shedgum/Abqaiq Groundwater	0.00808	0.00083	0.10288	0.441	6.48	51.84
Arabian Gulf	0.00755	0.00056	0.07417	0.470	6.90	55.21
Red Sea	0.00754	0.00056	0.07430	0.470	6.90	55.20

IV. RESULTS AND DISCUSSIONS

TM-720-370 and TM720-440 are standard BWRO membranes and TM720C-440, TM720L-400 and TM720L-440 are low-pressure BWRO membranes whereas TM720DA400, TM720D-400, and TM720D-440 are high-pressure BWRO membranes, Table IV.

Equations (1) and (2) allowed us to calculate osmotic pressure drop ($\Delta\pi$) for each water source; calculations are reported in Table VI. It is shown that the osmotic pressure of the groundwater source is less than the Arabian Gulf and the Red Sea water sources which is related to the flux rates and water salinity. Flux rates for the Arabian Gulf and the Red Sea waters are approximately half of the groundwater source. However, water salinity of the groundwater source is much lower than the other sources. Therefore, the required applied pressure drop must be larger in the case of seawater sources due to the higher determined osmotic pressure values of these sources. Since the plant configuration has 8 elements per vessel, we should have a maximum osmotic pressure of 60 psi or less per vessel which is equivalent to a max pressure of 7.5 psi per membrane; assuming that the pressure is distributed equally on membranes per vessel. The selected applied pressure range for our study is 6.5 to 7.5 psi; maximum pressure values are assigned to the different membranes based on their category as illustrated in Table VII.

TABLE VII: ASSIGNED PRESSURE VALUES FOR TORAY BWRO MEMBRANES

Category	Type	Δp Range (psi)*
Standard BWRO	TM720-370	6.50 - 7.25
	TM720-440	6.50 - 7.25
High-pressure BWRO	TM720DA400	6.50 - 7.50
	TM720D-400	6.50 - 7.50
	TM720D-440	6.50 - 7.50
Low-pressure BWRO	TM720C-440	6.50 - 7.00
	TM720L-400	6.50 - 7.00
	TM720L-440	6.50 - 7.00

*High and low-pressure values are taken relative to the standard pressure

The relationship between the applied pressure drops and the overall water flux rates for the groundwater source are obtained in Figures 3, 4 and 5 for standard, high-pressure and low-pressure Toray BWRO membranes, respectively. Figure 3 shows that the maximum possible flux for the groundwater in the standard membranes is around 11 gfd for TM720-440 membrane, wherein Figures 4 and 5 the highest observed groundwater flux in the high-pressure and low-pressure membranes are 14.7 gfd for TM720D-440 and 7.5

gfd for TM720C-440 and TM720L-440, respectively (blue and green lines overlap in Figure 5). This observation is associated with the membrane thickness in which the least membrane thickness (28 mils) has been capable to achieve the highest flux. This confirms an inverse relationship between the membrane thickness and the water flux rate. Further, there is a linear relationship between the applied pressure drop and the overall water flux.

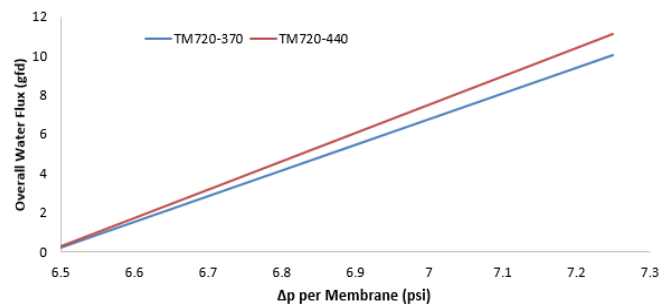


Fig. 3. Effect of different applied pressures on the groundwater flux for Toray standard BWRO membranes.

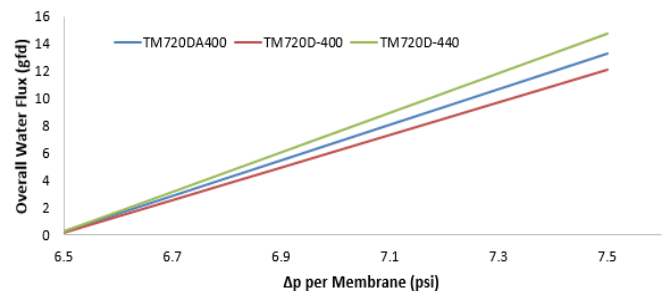


Fig. 4. Effect of different applied pressures on the groundwater flux for Toray high-pressure BWRO membranes.

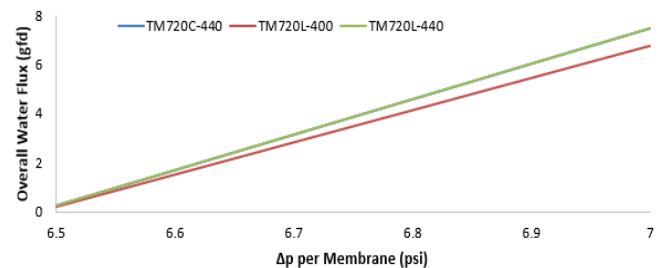


Fig. 5. Effect of different applied pressures on the groundwater flux for Toray low-pressure BWRO membranes.

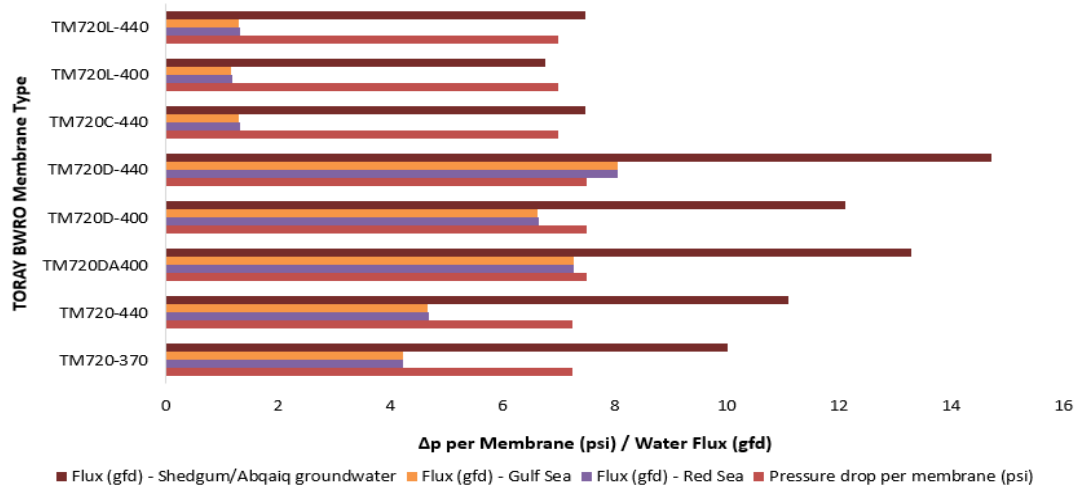


Fig. 6. Observed water flux for various water sources at different applied pressures using Toray BWRO membranes.

Fig. 6 identifies a proportional relationship between the water flux and the applied pressure across the membrane. The highest recorded flux is accounted for TM720D-440 for Shedgum/Abqaiq groundwater because water TDS is low for groundwater and TM720D-440 has the lowest thickness and the highest pressure range. The Arabian Gulf and the

Red Sea water sources almost have similar flux rates at the same applied pressures due to the similarities in their water salinity levels. TM720C-440, TM720L-400 and TM720L-440 membranes reserved the lowest flux values since they are categorized as low-pressure BWRO membranes.

TABLE VIII: VAN'T HOFF CALCULATIONS FOR THE REQUIRED OSMOTIC PRESSURES USING DIFFERENT WATER SOURCES

Water Source	Concentration (mol/L)		Membrane Removal (%)	Osmotic Pressure (atm)			$ \Delta\pi $ (psi)
	TDS _{in}	TDS _{out}		π_{in}	π_{out}	$ \Delta\pi $	
Shedgum/Abqaiq Groundwater	0.156	0.00031	99.8	3.81	0.01	3.80	55.80
Arabian Gulf	2.282	0.005	99.8	55.82	0.11	55.71	818.41
Red Sea	2.337	0.005	99.8	57.18	0.11	57.07	838.34

Fig. 7 demonstrates the membrane resistance for the three studied water sources. Seawater sources have higher membranes resistances than the groundwater source because

of their lower flux and higher TDS. TM720L-400 has the highest membrane resistance since it is in the low-pressure category and has the highest membrane thickness of 31 mils.

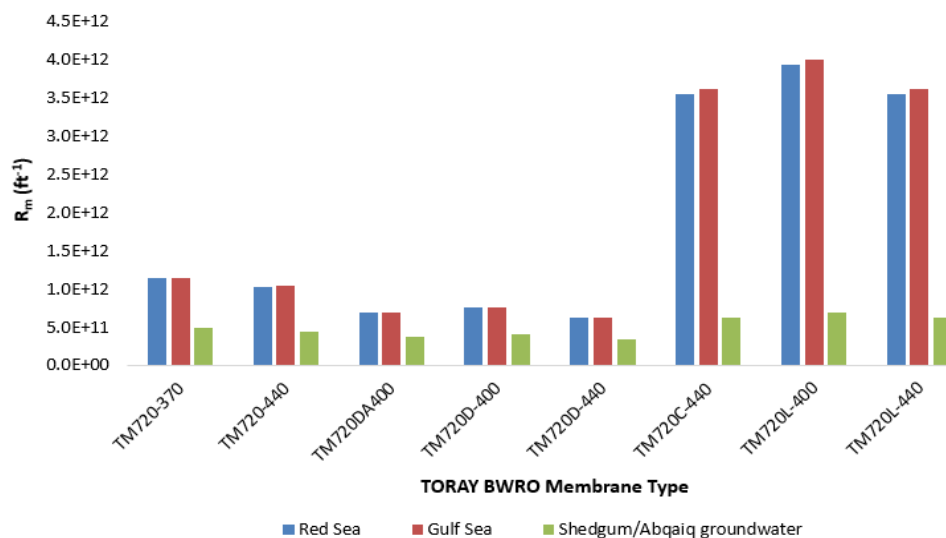


Fig. 7. Observed membranes resistance of various water sources in Toray BWRO membranes

Equation (4) calculations are shown in Table VIII. The study predictions estimated that the overall osmotic pressure drops required for seawater and groundwater treatment plants are approximately 55 psi and 830 psi, respectively. The higher the salinity difference between the fed and the produced water, the more the osmotic pressure drop we need to overcome in order to produce treated water (positive flux).

V. CONCLUSION

The application of the solution-diffusion model to Abqaiq plant (500 RO plant) is initiated by using various parameters to calculate the osmotic pressure of Toray TM720D-400 with 8" membrane for Shedgum/Abqaiq groundwater treatment. For the same membrane, the osmotic pressure values are determined for the Arabian Gulf and the Red Sea waters to predict flux rates in other membranes for seawater

situations. Low-pressure, standard and high-pressure BWRO Toray membranes performance has been compared to identify the optimal membrane for treating saline water from three the studied water sources at Abqaiq 500 RO plant.

The assumption of having a membrane thickness that is similar to its spacer thickness may not seem very accurate. However, it is true that we should have a proportional relation between both thicknesses which suggests that our results are still valid. A linear relationship has been observed between the water flux and the applied pressure drops. It is proved that membrane flux decreases with the increase in membrane thickness at constant pressure drop. Modelling results endorse that BWRO Toray TM720D-440 with 8" membrane is the optimum membrane choice for the water treatment from the three water sources at Abqaiq 500 RO plant since it has the lowest membrane resistance and the highest overall water flux.

ACKNOWLEDGMENT

The author would like to express his gratitude toward the Saudi Arabian Cultural Mission (SACM) and King Abdulaziz University (KAU) for their support and encouragement to accomplish this work. Also, the author would like to thank Saudi Aramco Company (Eng. Mohammed Almughawi) for sharing their valuable data of Abqaiq 500 RO plant.

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Hisham A. Maddah is a lecturer in the Chemical Engineering Department at King Abdulaziz University (KAU) in Rabigh, KSA; he is currently sponsored by KAU to complete the PhD studies at the University of Illinois at Chicago (UIC). Mr. Maddah has received his BS and MS degrees in chemical engineering from KAU in 2012 and the University of Southern California (USC) in 2017, respectively. He has worked in the oil/gas industry for two years with the Chemical Business Department in Saudi Aramco (2012–2014) before shifting to academia in 2014. Mr. Maddah has published more than 30 articles/conference papers related to chemical engineering and higher education in reputed international peer-reviewed journals. His research interests are (1) Desalination; (2) Photovoltaics; (3) Nanotechnology; (4) Low-dimensional materials and (5) Higher education administration.