

Everything $\ln(x)$ and e^x

Special properties of logarithms

$$\ln(1) = 0$$

$$\ln(e) = 1$$

$$e^{\ln x} = x$$

A common log has a base of 10.
A natural log has a base of e

Definition of \ln

$$y = \ln(x) \leftrightarrow e^y = x$$



One-to-one property of logarithms
If $\ln(A) = \ln(B)$, then $A = B$

You can't take the log of a negative number!

Product Rule of Logarithms
 $\ln(xy) \leftrightarrow \ln(x) + \ln(y)$
Quotient Rule of Logarithms
 $\ln\left(\frac{x}{y}\right) \leftrightarrow \ln(x) - \ln(y)$
Power Rule of Logarithms
 $\ln(x^y) \leftrightarrow y \ln(x)$

Expand the Following

$$\ln(4\sqrt{x})$$

$$\ln\left(\frac{e^3}{x}\right)$$

$$\ln\left(\frac{9}{x^4 y^7}\right)$$

$$\ln(x-9)$$

vs.

$$\ln(x^2-9)$$

Condense the Following

$$\ln(x) - \ln(7) + 3\ln(y)$$

$$2\ln(x) - [\ln(7) + \ln(y)]$$

$$\ln(6x^2 + 7x - 5) - \ln(3x + 5)$$

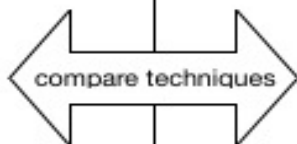
$$\frac{\ln(9)}{\ln(2)}$$

$$\ln\left(\frac{9}{2}\right)$$

Using ln to solve exponential equations

solve WITHOUT using ln. $2^{2x-5} = \frac{1}{16}$

solve using ln $2^{2x-5} = \frac{1}{16}$



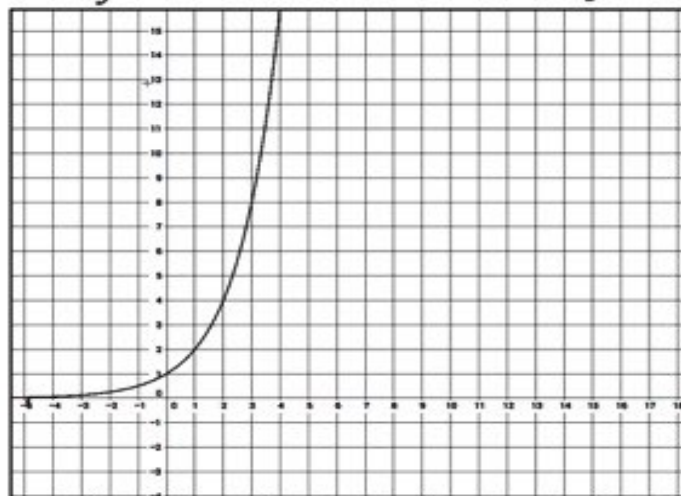
solve using ln $e^{-x+4} - 10 = 2$

solve using ln $-2e^{3x+4} + 8 = 6$

Graphing Logs in relation to their exponential inverses.

$y = 2^x$ given below

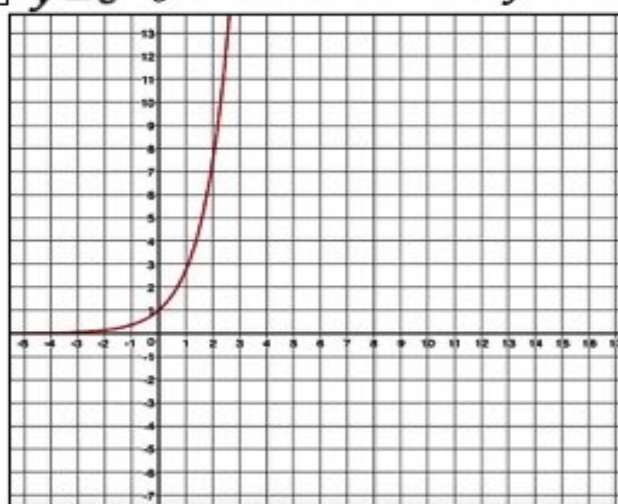
$y = \log_2 x$



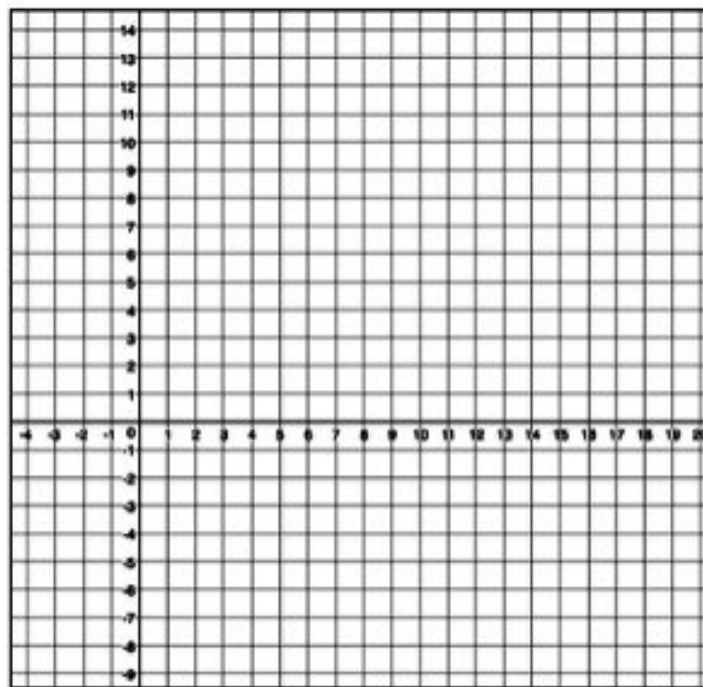
x	$y = 2^x$	$y = \log_2 x$
-2		
-1		
0		
1		
2		
3		
4		

$y = e^x$ given below

$y = \ln x$



x	$y = e^x$	$y = \ln x$
-2		
-1		
0		
1		
2		
3		
4		



Graph the function below and supply all the work asked for.

$$y = 3\ln(x+2) + 1$$

Parent: _____

Multiplier: _____

Shift: _____

X - int: _____

Y - int: _____

Asymptote: _____

Solving using the one-to-one property

$$\ln(x) + \ln\left(\frac{x}{2}\right) = \ln(8)$$

$$3\ln(x) = \ln(8) - \ln(27)$$

Various examples of solving \ln equations

$$4\ln(x) + 3 = 10.25$$

$$\ln(\sqrt{x+2}) = 2$$

check your answers!

check your answers!

$$\ln(x-2) + \ln(2x-3) = 2\ln(x)$$

$$e^{\ln(3x-7)} = 2$$

check your answers!

check your answers!