

Pascal Triangle Interesting Patterns

Putting it all together

Expand $(2x+3)^4$

$a = 2x$ $b = 3$

1. Number of terms? **5**
2. Which row to use of Pascal's Triangle? **5th row**
3. Ascending and descending orders of "a" and "b"
4. Plug in "a" and "b"
5. Simplify

$1(a)^4(b)^0 + 4(a)^3(b)^1 + 6(a)^2(b)^2 + 4(a)^1(b)^3 + 1(a)^0(b)^4$
 $1(2x)^4(3)^0 + 4(2x)^3(3)^1 + 6(2x)^2(3)^2 + 4(2x)^1(3)^3 + 1(2x)^0(3)^4$
 $16x^4 + 96x^3 + 216x^2 + 216x + 81$

Expand $(3x + y)^5$

- Number of terms? 6
- Which row to use of Pascal's Triangle? $6^{\text{th}} \text{ Row}$
- Ascending and descending orders of "a" and "b"
- Plug in "a" and "b"
- Simplify

$a = 3x$
 $b = y$

$$1(a)^5(b)^0 + 5(a)^4(b)^1 + 10(a)^3(b)^2 + 10(a)^2(b)^3 + 5(a)^1(b)^4 + 1(a)^0(b)^5$$

$$1(3x)^5(y)^0 + 5(3x)^4(y)^1 + 10(3x)^3(y)^2 + 10(3x)^2(y)^3 + 5(3x)^1(y)^4 + 1(3x)^0(y)^5$$

$$243x^5 + 405x^4y + 270x^3y^2 + 90x^2y^3 + 15xy^4 + y^5$$

Pascal's Triangle:

1							
1	1						
1	2	1					
1	3	3	1				
1	4	6	4	1			
1	5	10	10	5	1		
1	6	15	20	15	6	1	
1	7	21	35	35	21	7	1

Expand $(x-4y)^3$

$a=x$ $b=-4y$

1. Number of terms? **4**
2. Which row to use of Pascal's Triangle? **4th row**
3. Ascending and descending orders of "a" and "b" }
4. Plug in "a" and "b"
5. Simplify

1
1 1
1 2 1
1 3 3 1
1 4 6 4 1
1 5 10 10 5 1
1 6 15 20 15 6 1
1 7 21 35 35 21 7 1

$$1(a)^3(b)^0 + 3(a)^2(b)^1 + 3(a)^1(b)^2 + 1(a)^0(b)^3$$

$$1(x)^3(-4y)^0 + 3(x)^2(-4y)^1 + 3(x)^1(-4y)^2 + 1(x)^0(-4y)^3$$

$$x^3 - 12x^2y + 48xy^2 + 64y^3$$

Expand $(2x^2 - y)^4$

- Number of terms? **5**
- Which row to use of Pascal's Triangle? **5th row**
- Ascending and descending orders of "a" and "b"
- Plug in "a" and "b"
- Simplify

$a = 2x$ $b = -y$

$$1(a)^4(b)^0 + 4(a)^3(b)^1 + 6(a)^2(b)^2 + 4(a)^1(b)^3 + 1(a)^0(b)^4$$

$$1(2x)^4(-y)^0 + 4(2x)^3(-y)^1 + 6(2x)^2(-y)^2 + 4(2x)^1(-y)^3 + 1(2x)^0(-y)^4$$

$$16x^4 - 32x^3y + 24x^2y^2 - 8xy^3 + y^4$$

Pascal's Triangle:

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      1
     1 1
    1 2 1
   1 3 3 1
  1 4 6 4 1
 1 5 10 10 5 1
1 6 15 20 15 6 1
1 7 21 35 35 21 7 1
    
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