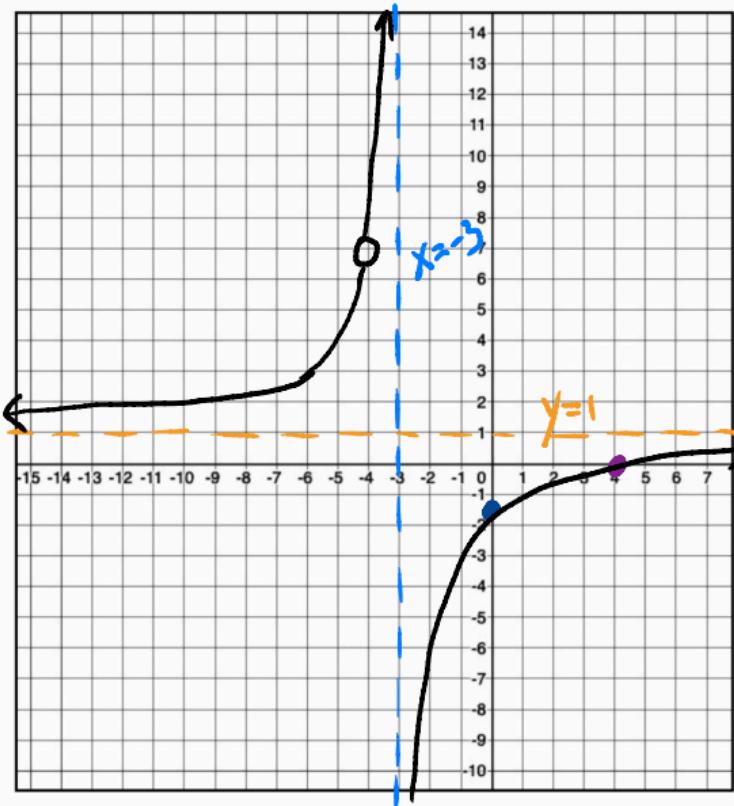


MORE Graphing Rational Functions Part 2 - Non-Transformational



$$f(x) = \frac{x^2 - 16}{x^2 + 7x + 12} \rightarrow \frac{(x+4)(x-4)}{(x+4)(x+3)}$$

| | |
|------------------------|---|
| x-intercepts: | $(4, 0)$ |
| Vertical Asymptotes: | $x = -3$ |
| Horizontal Asymptotes: | $y = 1$ |
| Holes: | $\text{at } x = -4$ |
| y-Intercept(s): | $(0, -\frac{4}{3})$ |
| Domain: | $(-\infty, -4) \cup (-4, -3) \cup (-3, \infty)$ |
| Range | $y \neq 1$ |

X-int

$$x-4=0$$

$$x=4$$

holes

$$x+4=0$$

$$x=-4$$

vertical asymptote

$$x+3=0$$

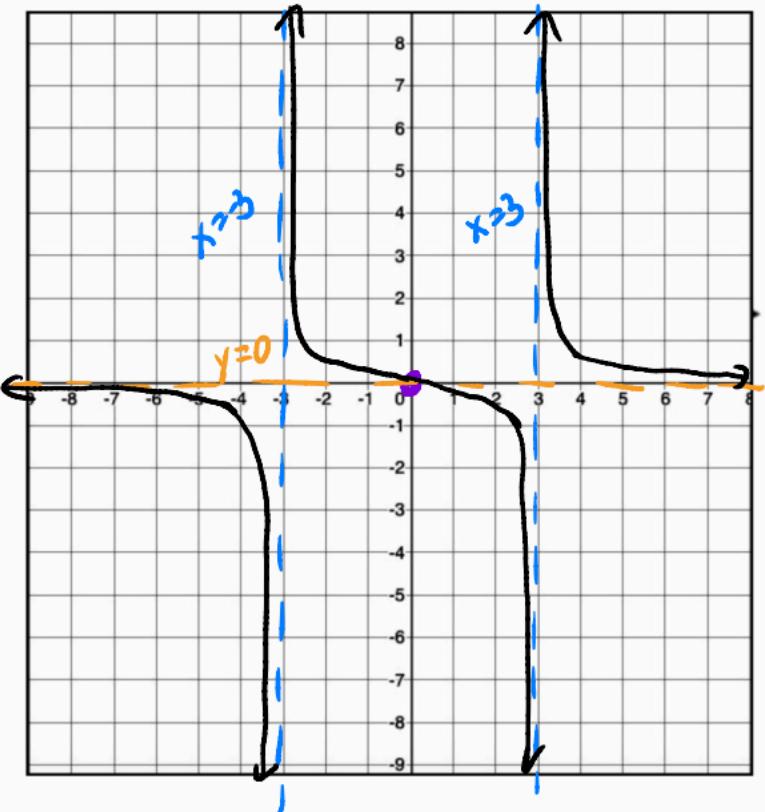
$$x=-3$$

y-intercept

$$f(0) = \frac{(0)^2 - 16}{(0)^2 + 7(0) + 12} = -\frac{4}{3}$$

horizontal asymptote

$$y=1$$



$$f(x) = \frac{x}{x^2 - 9} \rightarrow \frac{x}{(x-3)(x+3)}$$

| | |
|------------------------|---|
| x -intercepts: | $(0, 0)$ |
| Vertical Asymptotes: | $x=3 \quad x=-3$ |
| Horizontal Asymptotes: | $y=0$ |
| Holes: | none |
| y -Intercept(s): | $(0, 0)$ |
| Domain: | $(-\infty, -3) \cup (-3, 3) \cup (3, \infty)$ |
| Range: | |

x -int vertical asymptote horizontal asymptote

$$x=0 \quad (x-3)(x+3)=0 \quad y=0$$

$$x-3=0 \quad x+3=0$$

$$x=3 \quad x=-3$$

x -int

$$f(0) = \frac{0}{0^2 - 9} = 0$$

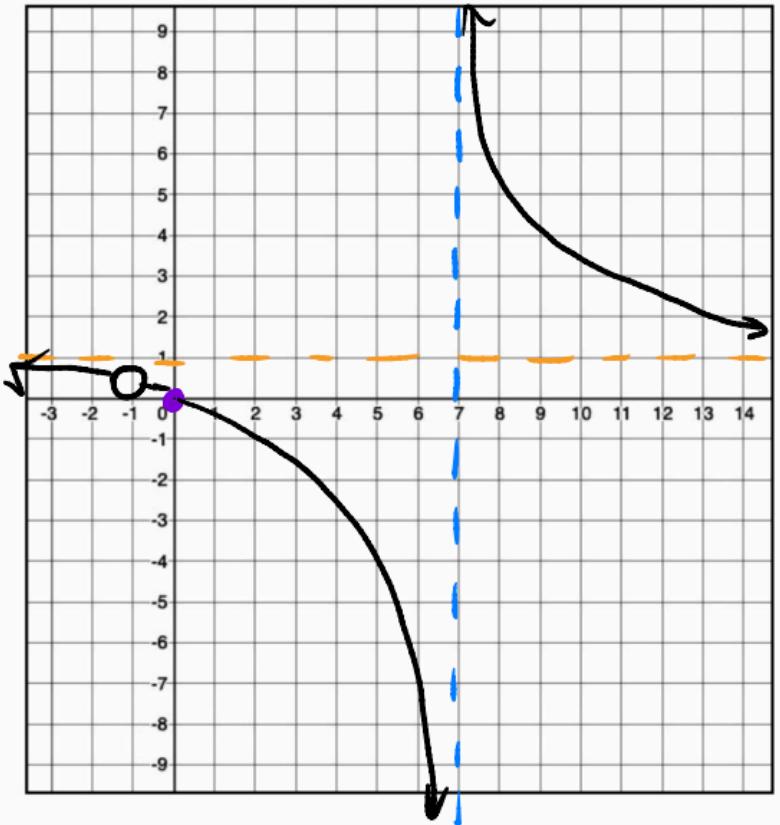
strategic points

$$f(-4) = -\frac{4}{7}$$

$$f(-1) = \frac{1}{8}$$

$$f(1) = -\frac{1}{8}$$

$$f(4) = \frac{4}{7}$$

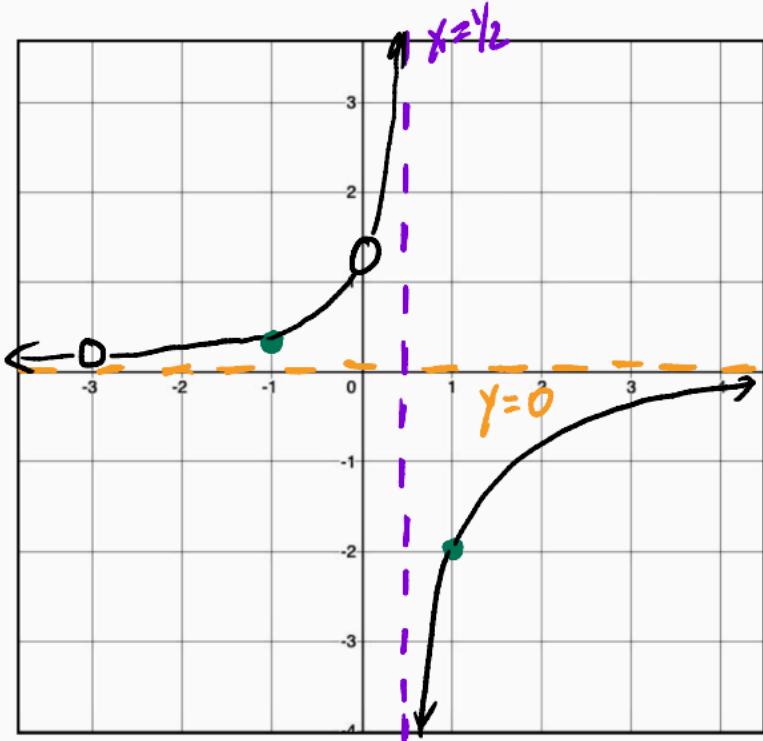


$$f(x) = \frac{x^2 + x}{x^2 - 6x - 7} \rightarrow \frac{x(x+1)}{(x-7)(x+1)}$$

| | |
|------------------------|---------------------|
| x -intercepts: | $(0, 0)$ |
| Vertical Asymptotes: | $x = 7$ |
| Horizontal Asymptotes: | $y = 1$ |
| Holes: | $\text{at } x = -1$ |
| y -Intercept(s): | $(0, 0)$ |
| Domain: | |
| Range: | |

X-int $x=0$ vertical asymptote $x-7=0$ horizontal asymptote $y=1$

holes y-int
 $x+1=0$ $f(0) = \frac{(0)^2 + (0)}{(0)^2 - 6(0) - 7} = 0$
 $x=-1$



Strategic points

$$f(-1) = \frac{2}{5}$$

$$f(1) = -2$$

$$f(x) = \frac{-2x(x+3)}{x(2x-1)(x+3)}$$

$$\frac{-2(4)}{(1)(1)(4)}$$

| | |
|------------------------|--------------------|
| x-intercepts: | none |
| Vertical Asymptotes: | $x=\frac{1}{2}$ |
| Horizontal Asymptotes: | $y=0$ |
| Holes: | @ $x=0$ and $x=-3$ |
| y-Intercept(s): | none |
| Domain: | |
| Range | |

x-int vertical asymptote horizontal asymptote
 $-2 \neq 0$ $2x-1=0$ $y=0$
 $x=\frac{1}{2}$

holes

$$x=0 \quad x+3=0 \quad x=-3$$

y-int

$f(0)$ is a hole so no y-int.