

Math II Name _____ ID: 1

Exponent Properties (w/fractions) Date _____ Period ____

Simplify.

1) $m^2 \cdot 2m^{\frac{1}{2}} \rightarrow 2m^{2+\frac{1}{2}}$
 $2m^{\frac{5}{2}}$

2) $2x^{\frac{1}{2}} \cdot 2x \rightarrow 2 \cdot 2 \cdot x^{\frac{1}{2}+1}$
 $4x^{\frac{3}{2}}$

3) $p^{\frac{1}{2}} \cdot p^1 \rightarrow p^{\frac{1}{2}+1}$
 $p^{\frac{3}{2}}$

4) $n^{\frac{1}{2}} n^{\frac{1}{2}} \rightarrow n^{\frac{1}{2}+\frac{1}{2}}$
 n^1

5) $\left(\frac{1}{n^2}\right)^{\frac{1}{2}} \rightarrow n^{\left(\frac{1}{2}\right)\left(\frac{1}{2}\right)}$
 $n^{\frac{1}{4}}$

6) $\left(a^{\frac{3}{2}}\right)^{\frac{3}{2}} \rightarrow a^{\left(\frac{3}{2}\right)\left(\frac{3}{2}\right)}$
 $a^{\frac{9}{4}}$

$$7) \left(x^{\frac{3}{2}}\right)^{\frac{3}{2}} \rightarrow x^{\left(\frac{3}{2}\right)\left(\frac{3}{2}\right)}$$

$$\boxed{x^{\frac{9}{4}}}$$

$$8) \left(r^{\frac{1}{2}}\right)^{\frac{3}{2}} \rightarrow r^{\left(\frac{1}{2}\right)\left(\frac{3}{2}\right)}$$

$$\boxed{r^{\frac{3}{4}}}$$

$$9) \frac{1}{2} v^{\frac{3}{2}}$$

$$\frac{1}{2} v^{2 - \frac{3}{2}}$$

$$\boxed{\frac{1}{2} v^{\frac{1}{2}} \text{ or } \frac{v^{\frac{1}{2}}}{2}}$$

$$10) \frac{2x}{x^{\frac{1}{2}}} \rightarrow 2x^{1 - \frac{1}{2}}$$

$$\rightarrow \boxed{2x^{\frac{1}{2}}}$$

11) $\left(\frac{2x^{\frac{3}{2}}}{2x^1}\right) \rightarrow \frac{2}{2} x^{\frac{3}{2}-1}$
 $x^{\frac{1}{2}}$

12) $\frac{n^{\frac{3}{2}}}{n^2} \rightarrow n^{\frac{3}{2}-2}$
 $\rightarrow n^{-\frac{1}{2}}$
 $\rightarrow \frac{1}{n^{\frac{1}{2}}}$

Solve each equation. DO NOT USE A CALCULATOR.

13) $7 = \sqrt{n}$
 $7 = (n)^{\frac{1}{2}}$ cancel $\rightarrow n = 7^2 = 49$
 $(7)^2 = (n)^{\frac{1}{2} \cdot 2}$

14) $3 = x^{\frac{1}{3}}$ cancel
 $(3)^3 = (x^{\frac{1}{3}})^3$
 $x = 27$

15) $27 = x^{\frac{3}{4}}$
 $(3^3)^{\frac{4}{3}} = (x^{\frac{3}{4}})^{\frac{4}{3}}$ cancel
 $3^{(3)(\frac{4}{3})} = x$
 $3^4 = x \rightarrow x = 81$

16) $x^{\frac{3}{2}} = 27$
 $x^{\frac{3}{2}} = 3^3$ cancel
 $(x^{\frac{3}{2}})^{\frac{2}{3}} = (3^3)^{\frac{2}{3}}$
 $x = 3^{(3)(\frac{2}{3})}$
 $x = 3^2 = 9$

17) $\sqrt{b} = 5$
 $(b)^{\frac{1}{2}} = 5$
~~cancel~~ $(b^{\frac{1}{2}})^2 = (5)^2$ → $b = 25$

18) $\sqrt{p} = 9$
 $(p)^{\frac{1}{2}} = 9$
~~cancel~~ $(p^{\frac{1}{2}})^2 = (9)^2$ → $p = 81$

19) $x^{\frac{3}{2}} = 729$
 $x^{\frac{3}{2}} = 9^3$
~~cancel~~ $(x^{\frac{3}{2}})^{\frac{2}{3}} = (9^3)^{\frac{2}{3}}$
 $x = 9^{(3)(\frac{2}{3})}$
 $x = 9^2 = 81$

20) $\sqrt[3]{x} = 5$
 $x^{\frac{1}{3}} = 5$
~~cancel~~ $(x^{\frac{1}{3}})^3 = (5)^3$ → $x = 5^3 = 125$

21) $3 = p^{\frac{1}{2}}$
 $(3)^2 = (p^{\frac{1}{2}})^2$ —cancel
 $p = 9$

22) $243 = m^{\frac{5}{4}}$
 $(3^5) = m^{\frac{5}{4}}$ cancel
 $(3^5)^{\frac{4}{5}} = (m^{\frac{5}{4}})^{\frac{4}{5}}$ → $3^{(5)(\frac{4}{5})} = m$
 $m = 3^4 = 81$

-2-