

## Using Patterns and Formulas Assignment

Use the **difference of two squares** pattern  $A^2 - B^2 = (A - B)(A + B)$  to FACTOR the following.

$$\begin{aligned} x^2 - 49 \\ (x)^2 - (7)^2 \\ (A)^2 - (B)^2 &= (A - B)(A + B) \\ &= (x - 7)(x + 7) \end{aligned}$$

$$\begin{aligned} 5x^2 - 80 \\ 5(x^2 - 16) \\ 5((x)^2 - (4)^2) \\ A^2 - B^2 \rightarrow (A - B)(A + B) \\ 5(x - 4)(x + 4) \end{aligned}$$

$$\begin{aligned} 64x^2 - 9y^2 \\ (8x)^2 - (3y)^2 \\ A^2 - B^2 \rightarrow (A - B)(A + B) \\ (8x - 3y)(8x + 3y) \end{aligned}$$

$$\begin{aligned} 4x^2 - 81 \\ (2x)^2 - (9)^2 \\ A^2 - B^2 \rightarrow (A - B)(A + B) \\ (2x - 9)(2x + 9) \end{aligned}$$

$$\begin{aligned} x^4 - 16 \\ (x^2)^2 - (4)^2 \\ A^2 - B^2 \rightarrow (A - B)(A + B) \\ (x^2 - 4)(x^2 + 4) \\ (x^2 - 2^2)(x^2 + 4) \\ \text{diff of squares again!} \rightarrow (x - 2)(x + 2)(x^2 + 4) \end{aligned}$$

$$\begin{aligned} -x^2 + 25 \\ -(x^2 - 25) \\ -((x)^2 - (5)^2) \\ A^2 - B^2 \rightarrow (A - B)(A + B) \\ -(x - 5)(x + 5) \end{aligned}$$

Use the **perfect square trinomial** pattern  $(A + B)^2 = A^2 + 2AB + B^2$  to EXPAND the following.

$$\begin{aligned} (2x + 3)^2 \\ (A + B)^2 = A^2 + 2AB + B^2 \\ = (2x)^2 + 2(2x)(3) + (3)^2 \\ = 4x^2 + 12x + 9 \end{aligned}$$

$$\begin{aligned} (-5x + 1)^2 \\ (A + B)^2 = A^2 + 2AB + B^2 \\ = (-5x)^2 + 2(-5x)(1) + (1)^2 \\ = 25x^2 - 10x + 1 \end{aligned}$$

$$\begin{aligned} (7x - y)^2 \\ (A + B)^2 = A^2 + 2AB + B^2 \\ = (7x)^2 + 2(7x)(-y) + (-y)^2 \\ = 49x^2 - 14xy + y^2 \end{aligned}$$

$$\begin{aligned} (x^4 + 2)^2 \\ (A + B)^2 = A^2 + 2AB + B^2 \\ = (x^4)^2 + 2(x^4)(2) + (2)^2 \\ = x^8 + 4x^4 + 4 \end{aligned}$$

$$\begin{aligned} (3x^3 - y)^2 \\ (A + B)^2 = A^2 + 2AB + B^2 \\ = (3x^3)^2 + 2(3x^3)(-y) + (-y)^2 \\ = 9x^6 - 6x^3y + y^2 \end{aligned}$$

$$\begin{aligned} (2x^2 + 5y^2)^2 \\ (A + B)^2 = A^2 + 2AB + B^2 \\ = (2x^2)^2 + 2(2x^2)(5y^2) + (5y^2)^2 \\ = 4x^4 + 20x^2y^2 + 25y^4 \end{aligned}$$

Use the SUM or DIFFERENCE of Cubes to Expand the following

**SUM OF CUBES**

**DIFFERENCE OF CUBES**

$$A^3 + B^3 = (A+B)(A^2 - AB + B^2) \quad A^3 - B^3 = (A-B)(A^2 + AB + B^2)$$

$$x^3 + 125$$

$$(x)^3 + (5)^3$$

$$A^3 + B^3 \rightarrow (A+B)(A^2 - AB + B^2)$$

$$\rightarrow (x+5)(x^2 - (x)(5) + (5)^2)$$

$$\rightarrow (x+5)(x^2 - 5x + 25)$$

$$2x^3 + 54$$

$$2(x^3 + 27)$$

$$2((x)^3 + (3)^3)$$

$$A^3 + B^3 \rightarrow (A+B)(A^2 - AB + B^2)$$

$$2(x+3)(x^2 - (x)(3) + (3)^2)$$

$$2(x+3)(x^2 - 3x + 9)$$

$$8x^3 - 1$$

$$(2x)^3 - (1)^3$$

$$A^3 - B^3 \rightarrow (A-B)(A^2 + AB + B^2)$$

$$(2x-1)((2x)^2 + (2x)(1) + (1)^2)$$

$$(2x-1)(4x^2 + 2x + 1)$$

$$27x^3 - y^3$$

$$(3x)^3 - (y)^3$$

$$A^3 - B^3 \rightarrow (A-B)(A^2 + AB + B^2)$$

$$(3x-y)((3x)^2 + (3x)(y) + (y)^2)$$

$$(3x-y)(9x^2 + 3xy + y^2)$$

$$16x^3 - 2$$

$$2(8x^3 - 1)$$

$$2((2x)^3 - (1)^3)$$

$$A^3 - B^3 \rightarrow (A-B)(A^2 + AB + B^2)$$

$$2(2x-1)((2x)^2 + (2x)(1) + (1)^2)$$

$$2(2x-1)(4x^2 + 2x + 1)$$

Challenge

$$x^6 - y^6$$

$$(x^2)^3 - (y^2)^3$$

$$A^3 - B^3 \rightarrow (A-B)(A^2 + AB + B^2)$$

$$(x^2 - y^2)((x^2)^2 + (x^2)(y^2) + (y^2)^2)$$

difference of squares

$$(x^2 - y^2)(x^4 + x^2y^2 + y^4)$$

$$(x-y)(x+y)(x^4 + x^2y^2 + y^4)$$