

Functions: Episode I

By the end of this lesson, I will be able to answer the following questions...

1. How do I decide if a **relation** is a function?
2. What is **function notation**?
3. How do I find the **domain** of a function algebraically?
4. What are **difference quotients** and why are they useful?
5. How do I build function based on a scenario and use technology with the function to make predictions?

Vocabulary

1. Function: Every input has one unique output.
2. Domain: The set of inputs for which the function is defined.
3. Range: The set of possible outputs for a given function
4. Piece-Wise Function: A function that is defined by two or more equations over a specific domain.

5. Difference Quotient: $\frac{f(x+h) - f(x)}{h}, h \neq 0$

Prerequisite Skills with Practice

Evaluate the following function for $f(3)$ and $f(-3)$.

$$f(x) = -x^2 + 3x - 3$$

Evaluate the following function for $f(x+1)$

$$f(x) = -x^2 + 3x - 3$$

Algebraic Challenge: Isolate "y" in the follow equation.

$$(x-2)^2 + (y+3)^2 = 25$$

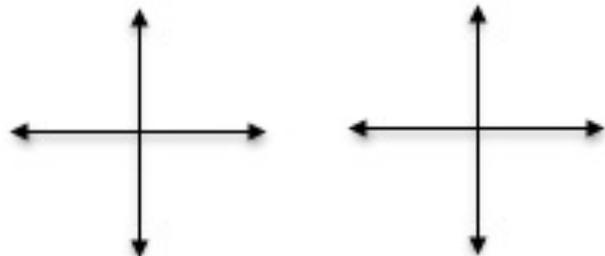
When is a relation a function?

Input	Output
-3	9
-2	4
-1	1
0	0
1	1
2	4

Input	Output
0	0
1	1
1	-1
2	4
2	-4

Vertical Line Test.

Why does it work?



Testing for functions algebraically.

Looking for a sign OR envision the graph...

$x^2 + y = 1$

$x + y^2 = 1$

$y = -3$

$x = \frac{4}{3}$

$y = |x|$

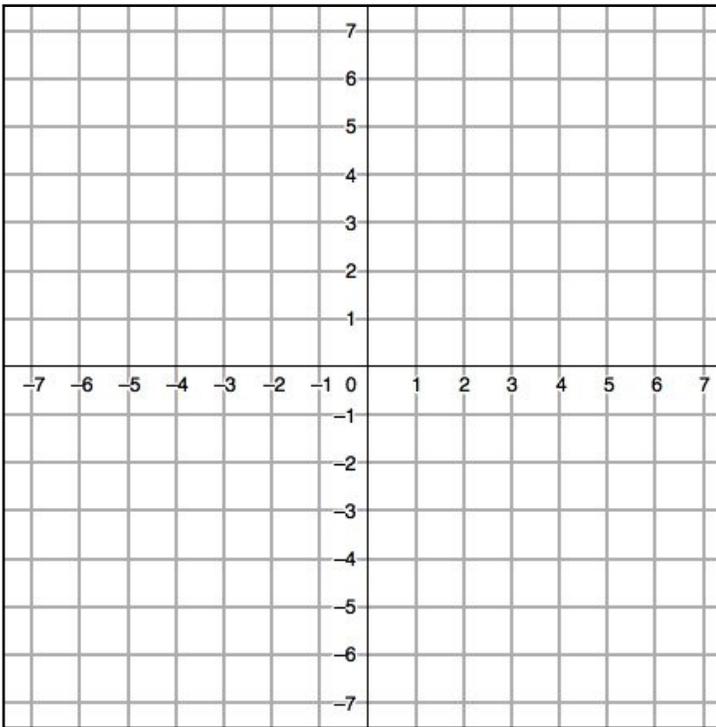
$x = |y|$

Piecewise-Defined Function Evaluating.

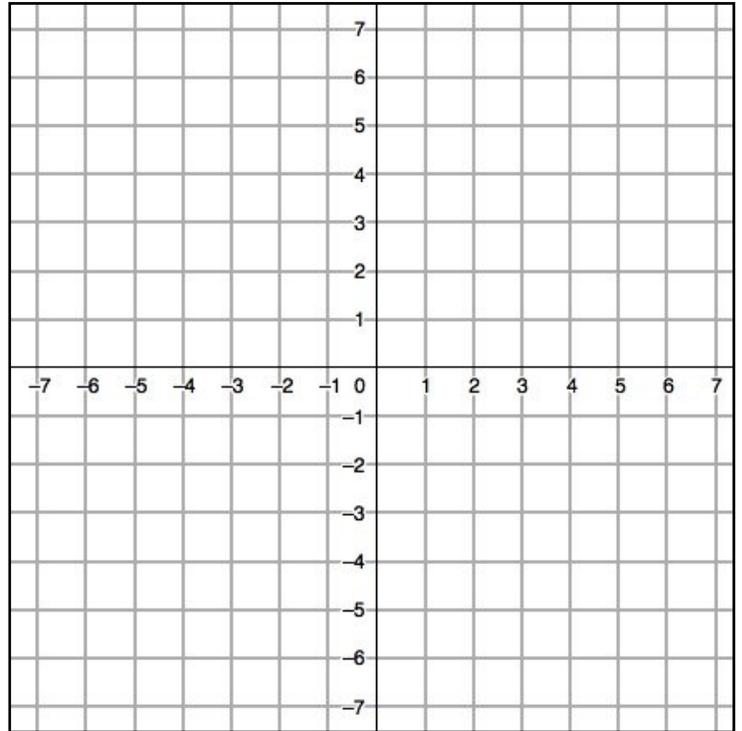
Evaluate $f(-2)$, $f(0)$, $f(3)$ given $f(x) = \begin{cases} 5 - 2x^2, & x < 0 \\ 2x + 5, & x \geq 0 \end{cases}$

Piecewise-Defined Function Sketching.

Filled in point ● for \leq or \geq . Open point ○ for $<$ or $>$



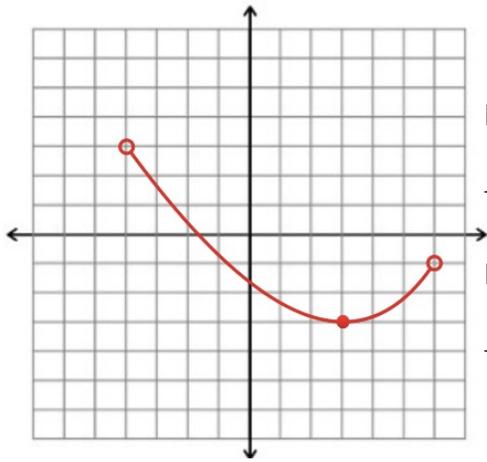
$$f(x) = \begin{cases} -2x + 1, & x < 2 \\ x + 3, & x \geq 2 \end{cases}$$



$$g(x) = \begin{cases} x + 1, & x < -3 \\ 2, & -3 \leq x \leq 0 \\ -x + 3, & x \geq 0 \end{cases}$$

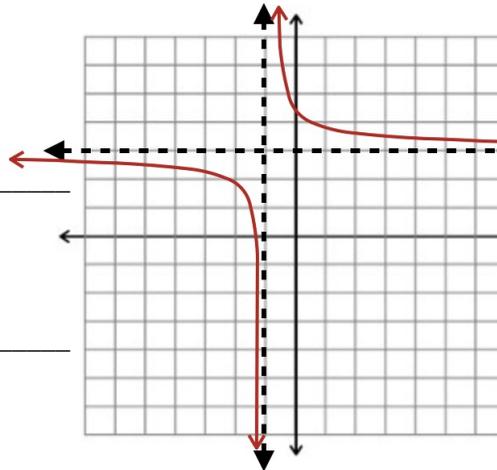
Using Interval Notation to State Domain and Range.

Open Interval $\rightarrow (\text{ or })$ Closed Interval $\rightarrow [\text{ or }]$ Union $\rightarrow \cup$



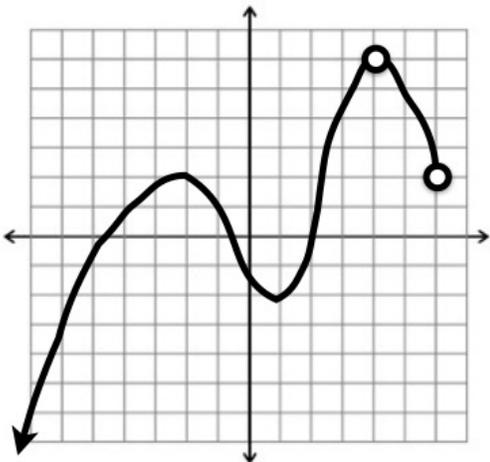
Domain:

Range:



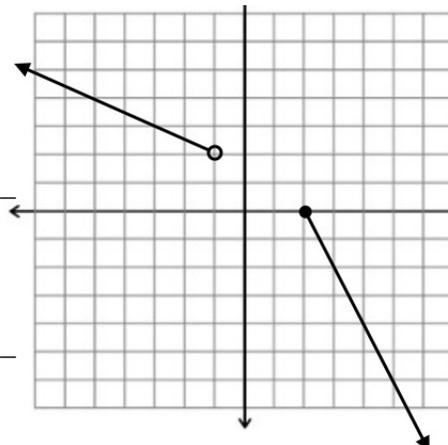
Domain:

Range:



Domain:

Range:



Domain:

Range:

Determining Domains of Functions.

Need to consider the values for which the function is defined and the real world implications of the function.

$$f : \{(-3,0), (-1,5), (0,7), (3,5), (6,7)\}$$

$$k(x) = \sqrt{4 - 3x}$$

$$h(x) = \frac{1}{x+5}$$

$$g(x) = -3x^2 + 4x + 5$$

$$m(x) = \sqrt{x^2 + 2x - 8}$$

$$l(x) = \frac{1}{x^2 - 3x + 2}$$

The volume of a sphere: $V(r) = \frac{4}{3}\pi r^3$

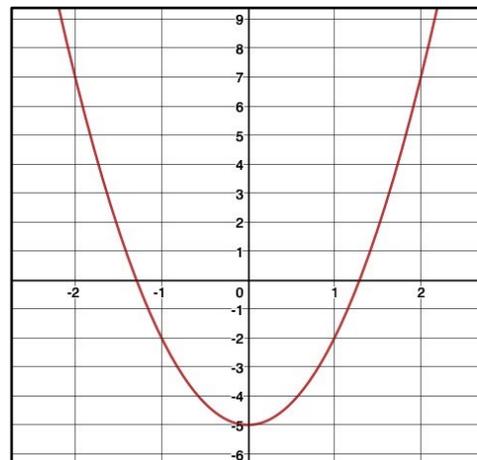
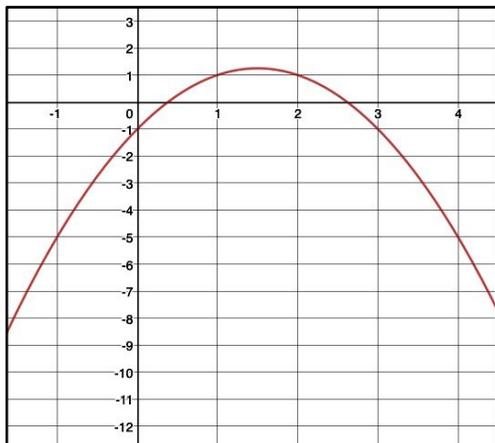
Find the ***Difference Quotient*** for the functions below and simplify your answer.

$$f(x) = -x^2 + 3x - 1$$

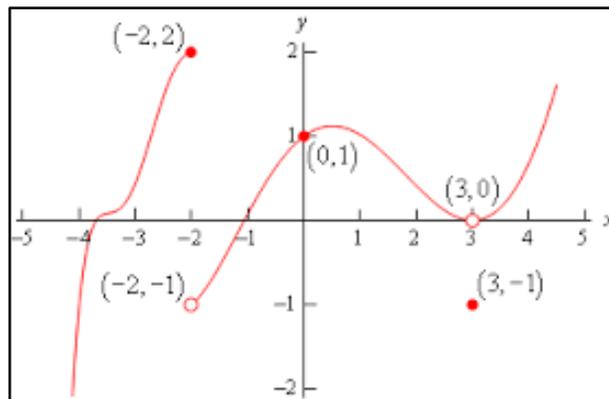
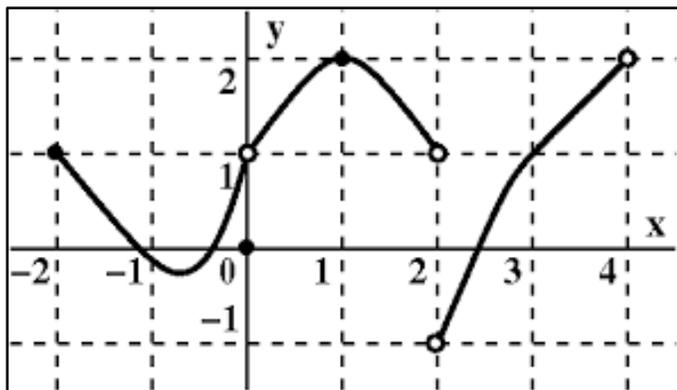
$$\frac{f(x+h) - f(x)}{h}, h \neq 0$$

$$f(x) = 3x^2 - 5$$

Difference Quotient



Reading Points from Graphs



$$f(-2) = ? \quad \underline{\hspace{2cm}}$$

$$f(0) = ? \quad \underline{\hspace{2cm}}$$

$$f(2) = ? \quad \underline{\hspace{2cm}}$$

$$f(?) = 2 \quad \underline{\hspace{2cm}}$$

$$f(-2) = ? \quad \underline{\hspace{2cm}}$$

$$f(0) = ? \quad \underline{\hspace{2cm}}$$

$$f(3) = ? \quad \underline{\hspace{2cm}}$$