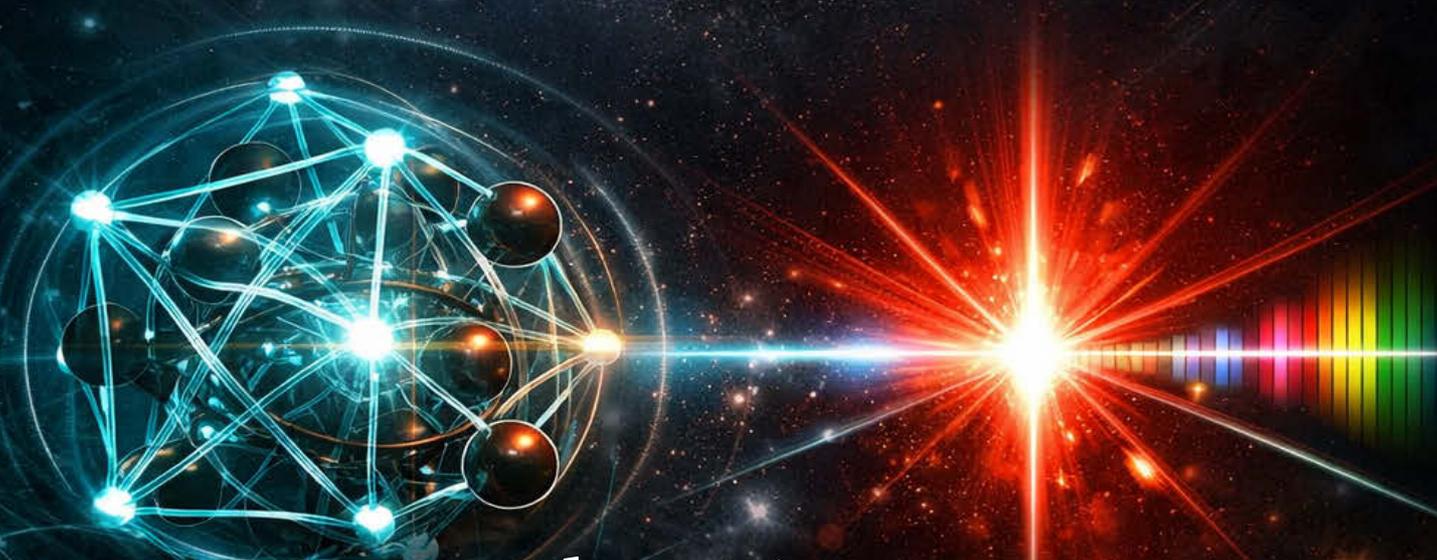


# Atomic Spectra Generation *from Optical Reciprocal Induction*

*Interfluxion Closure, Potentum, and the Optical Remainder*



Joseph P Firmage



# Atomic Spectra Generation from Optical Reciprocal Induction Interfluxion Closure, Potentum, and the Optical Remainder

## Abstract

Atomic spectra constitute the most exact and persistent fingerprints of matter. They are invariant across environment, reproducible to extreme precision, and uniquely characteristic of atomic species. Yet in conventional quantum mechanics, spectra are obtained only indirectly—through eigenvalue problems whose boundary conditions are imposed rather than derived, and whose physical interpretation remains ambiguous.

In this paper we present a first-principles generative account of atomic spectra based on Optical Reciprocal Induction, a geometric-algebraic framework in which atomic structure arises from closure of interfluxive motion between conjugate domains. Spectral lines are shown to be the necessary optical remainder of incomplete closure, not transitions between abstract energy levels.

We re-derive the spectral engine from foundational definitions—Potentum,  $|J|$ , reciprofluxion, and interfluxion—and present a dual-space reporting protocol that distinguishes interfluxion density (cause space) from optical projection (effect space). The method is demonstrated in full for Hydrogen, Carbon, Iron, and Gold, each treated as a worked generative example with platable stages suitable for independent verification.

The purpose of this Abstract is not to promise numerical outcomes in advance, but to state the causal claim the paper will defend: that discrete spectra arise because closure is discrete, and that the optical field is a consequence of what remains unclosed. This places the burden of explanation on the closure mechanism itself rather than on postulated quantization rules.

A second purpose is methodological clarity. The paper is organized so that an independent reader can separate what the model claims is "real inside the atom" (interfluxion density space) from what is only "what propagates out" (Optica). This is essential because many theories conflate internal structure with external radiation, leading to category errors.

Finally, the abstract signals the reporting discipline: plates are referenced explicitly but not embedded. The text is designed so that Canon plates can be dropped in without rewriting prose, and so that plate sequences can be audited without interpretive drift.

The Author has chosen to include instructions employed in the generation of both illustrative plates and "interfluxion density" plates. The latter are *\*all\** generated computationally from solely the combination of the Geometric Algebra of the Hestenes Electron and the Geometric Algebra of Firmage's Reciprocal Induction defining Nuclear structure and thus the overall Atomic mechanism.

By including my instructions to the renderer and computational engine, I hope this document can serve educators at all levels to advance their pedagogical knowledge and asset base for expanded understanding of the future of Physics.

# 1 Introduction: The Missing Optical Symmetry

1 — Orientation: Cause space vs Effect space

Physics has historically advanced by discovering the symmetries that nature actually employs. Translation, rotation, and Lorentz invariance are now foundational. Yet one symmetry—reciprocal inversion through motion—has remained underdeveloped despite its ubiquity in optics, electromagnetism, and matter.

Atomic spectra expose this omission. Spectral lines are not statistical artifacts; they are discrete, stable, and universal. Any theory that claims to explain matter must therefore explain why spectra exist at all, and why their wavelengths are discrete, without fitting.

Optical Reciprocal Induction begins from a simple recognition:

Whenever motion attempts to close upon itself but cannot do so perfectly, the unresolved remainder propagates optically.

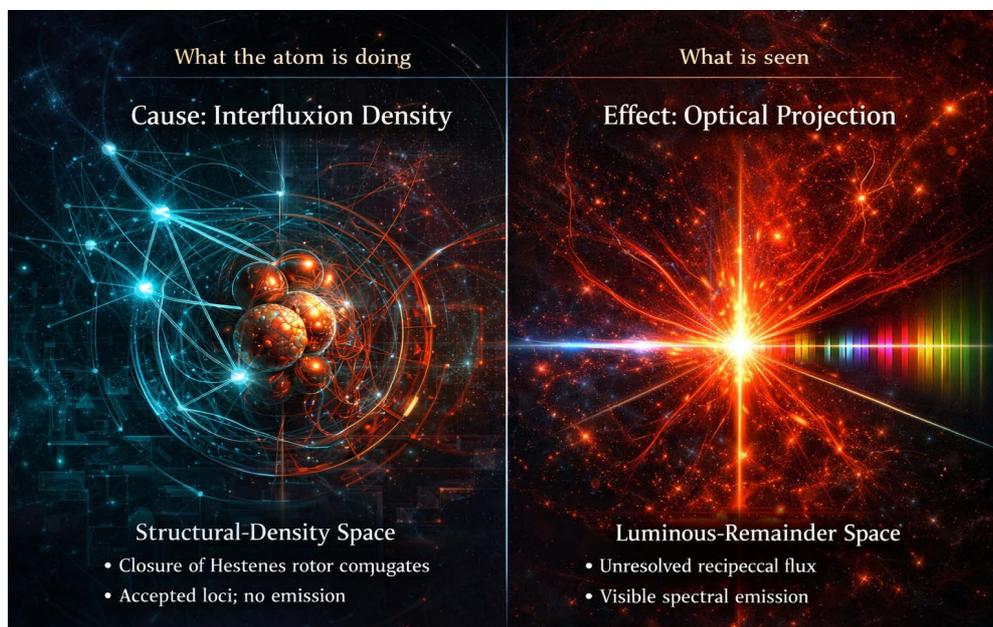
Spectra are not primary objects. They are what closure fails to retain.

To make this precise, we must introduce several foundational concepts that are absent—or only implicit—in conventional formulations.

The pedagogical goal of this Introduction is to re-orient the reader around a single diagnostic question: what physical process makes discreteness unavoidable? In many treatments, discreteness appears as a rule layered on top of dynamics. Here, discreteness is treated as a property of closure itself: only certain closure completions are admissible, and those admissibilities determine what remains.

The phrase "missing optical symmetry" is meant in a strict causal sense. Optics is usually treated as a separate dynamical sector, while atomic structure is treated as another. Optical Reciprocal Induction asserts that, at the level relevant to spectra, optics is not separate: it is induced by the residual temporal structure of incomplete closure.

In plate terms, this section prepares the reader for a disciplined visual separation. Plates associated with this section are not "results" plates; they are conceptual orientation plates. They should show, at minimum, the distinction between an internal closure geometry (cause) and an external propagating remainder (effect), without mixing their semantics.



## 2 Potentum and the Primitive Impulse $|J|$

2 — Definitions: Potentum and the primitive impulse

### 2.1 Potentum

2.1 — Potentum: closed vs unclosed agency

Potentum is defined as unclosed geometric agency: the capacity for motion, curvature, or action that has not yet been bound into a closed structure.

Closed Potentum appears as mass, inertia, and memory

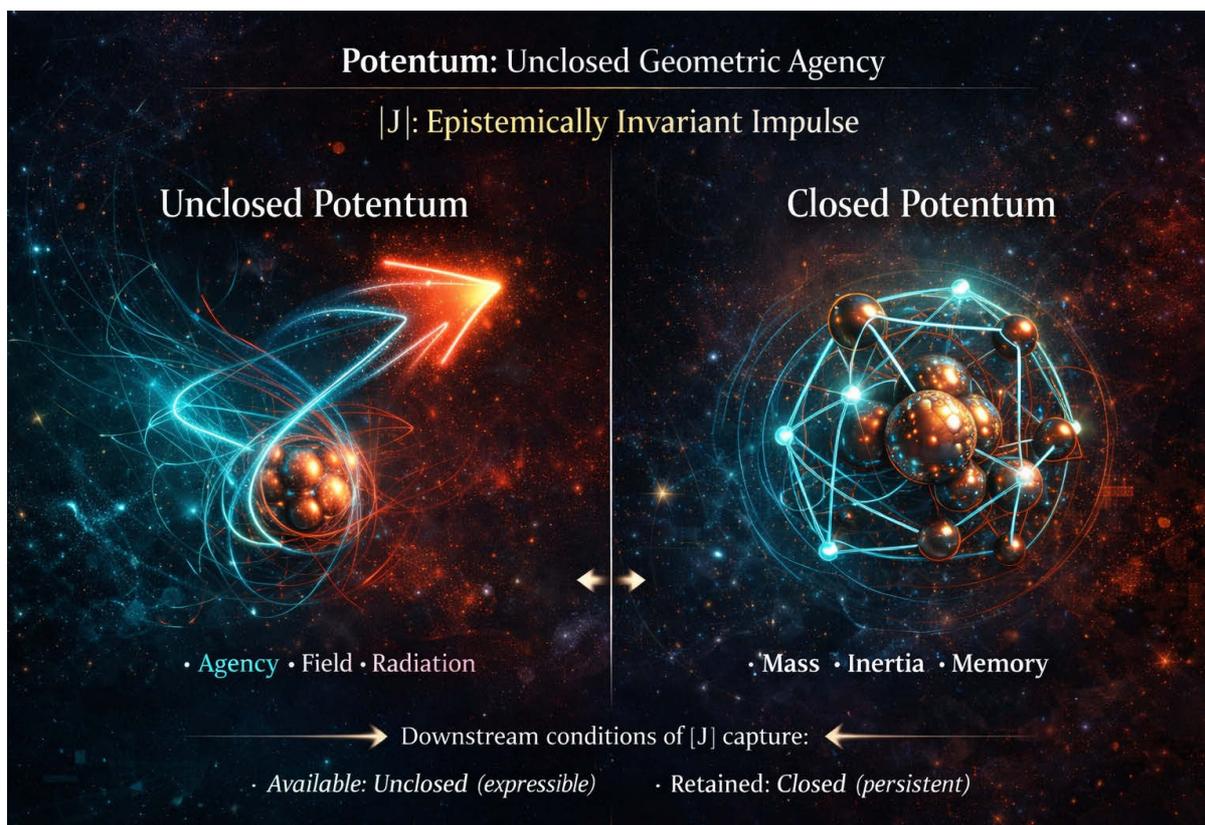
Unclosed Potentum appears as agency, field, and radiation

Potentum is not energy. It is the pre-energetic condition of possible action, geometrically realized.

Pedagogically, Potentum is introduced to prevent a familiar mistake: treating "energy" as the primitive explanation for structure. In this framework, energy is downstream. What is primitive is whether geometric agency is closed (retained) or unclosed (available to propagate).

The distinction "closed versus unclosed" is not rhetorical. It defines two different causal roles. Closed Potentum is what stabilizes an atomic scaffold and gives persistence. Unclosed Potentum is what remains available to express as field behavior and, in the spectral case, as radiative remainder.

A plate following this subsection should be understood as a definitional plate: it can depict closure versus remainder schematically, or it can depict a simple rotor closure event and label what is being called Potentum. The plate is not asked to show element-specific features; it is asked to make the ontological distinction visually legible.



## 2.2 The Primitive Impulse $|J|$

2.2 —  $|J|$ : epistemically invariant impulse

We posit a single irreducible magnitude,  $|J|$ , representing the elemental impulse of geometric agency.

$|J|$  is:

Not derived from mass, charge, or energy

Epistemically invariant across formalisms

The same impulse whether encountered as attraction or repulsion

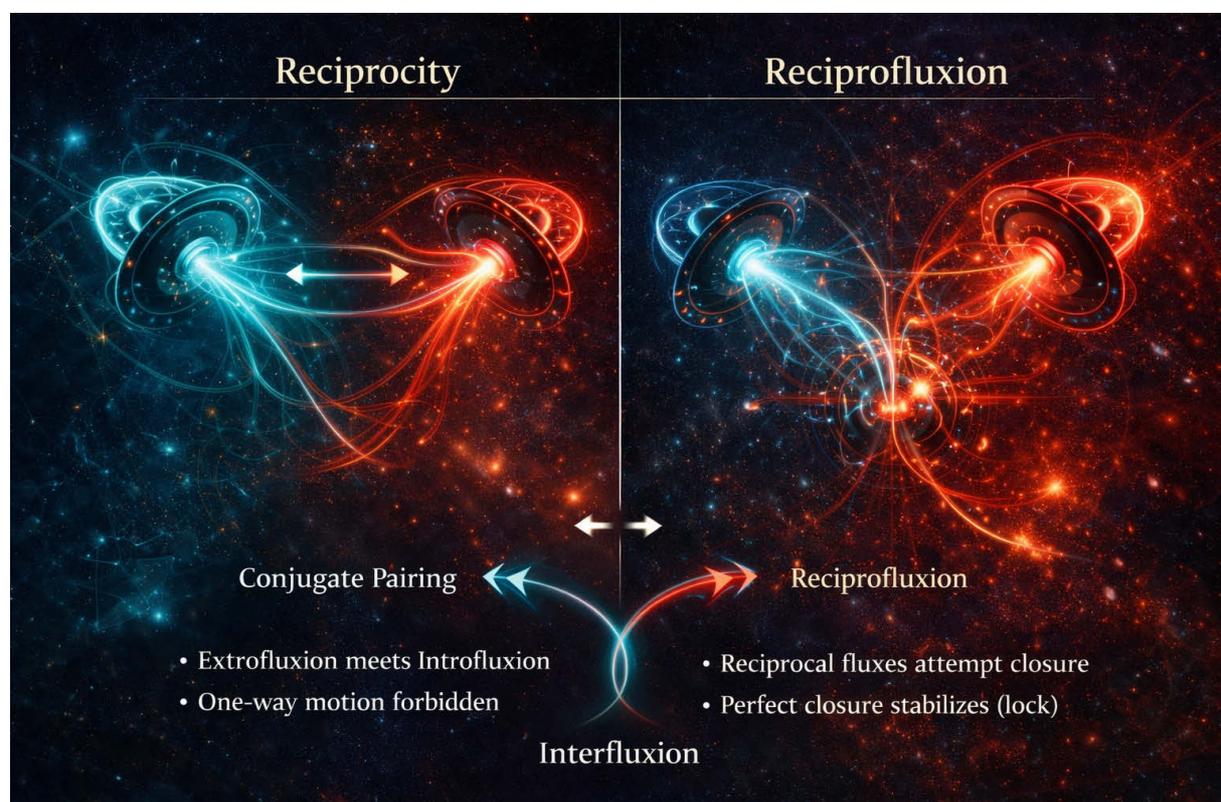
All atomic structure emerges from how  $|J|$  is captured, redirected, or left unclosed.

Pedagogically,  $|J|$  functions as the minimal "given" required to avoid infinite regress.

If one tries to build the theory from mass, charge, or energy, one inherits the same interpretive ambiguities the paper aims to resolve.  $|J|$  is introduced so that closure can be the primary generative act.

The phrase "epistemically invariant" is important: it means that regardless of whether an investigator starts from classical, quantum, or field-theoretic language, there will remain an irreducible repulsive/impulsive content that must be accounted for.  $|J|$  names that content without prematurely committing to a derived interpretation.

A plate following this subsection should show how a single magnitude can appear under dual aspects (e.g., what is called attraction and repulsion in different frames) while remaining a single primitive in the closure engine. This is a plate of interpretive unification, not of numerical comparison.



### 3 Reciprocity, Reciprofluxion, and Interfluxion

3 — Concept triad: reciprocity → circulation → density

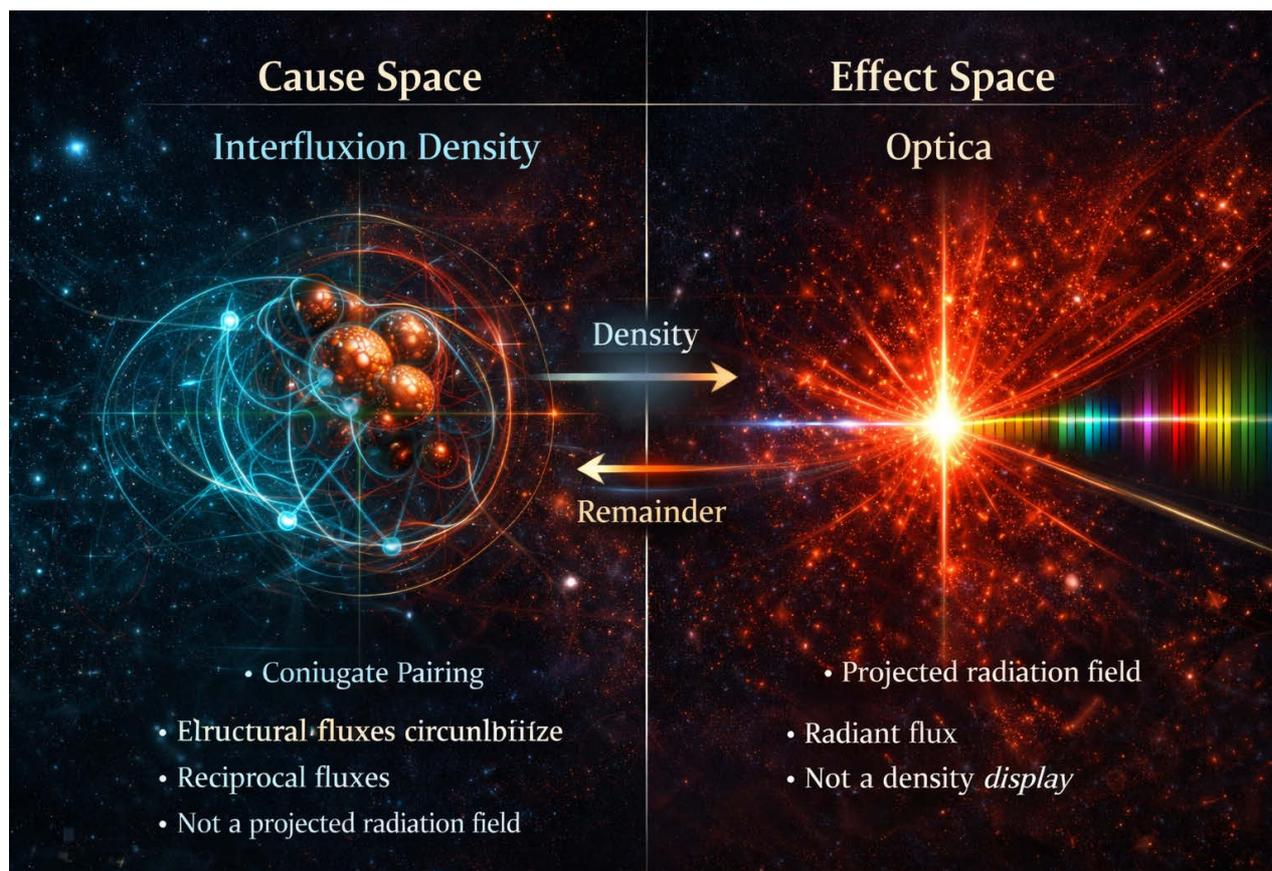
#### 3.1 Reciprocity

3.1 — Reciprocity: paired extro/intro

Reciprocity is the requirement that every extrofluxive motion admits a conjugate introfluxive response. Motion is never unilateral; it is always paired.

Pedagogically, reciprocity is introduced to fix the directionality of explanation. In many stories, radiation is treated as an emission from a localized source. Here, radiation is treated as a failure of mutual satisfaction between conjugate motions: extrofluxion is incomplete unless it is met by a conjugate introfluxion.

A plate for reciprocity should emphasize pairing. It can show two conjugate channels, or two conjugate rotors, or paired flux directions, but it must make clear that "one-way motion" is not a stable primitive. The goal is for the reader to see why closure requires a mutual relation.



## 3.2 Reciprofluxion

3.2 — Reciprofluxion: closure vs residual channel

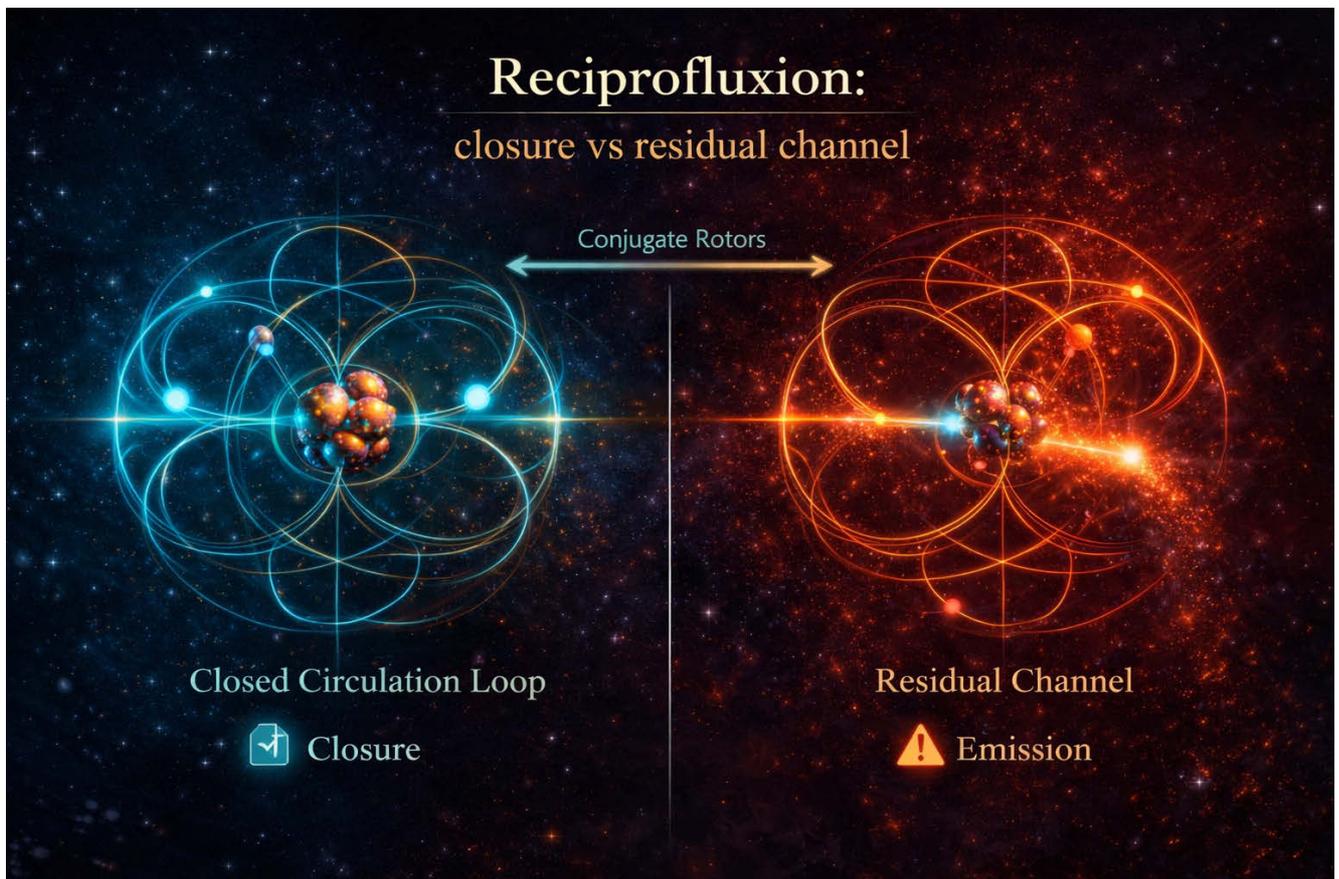
Reciprofluxion is the closed or partially closed circulation formed by conjugate fluxes attempting mutual satisfaction.

Perfect reciprofluxion yields stable structure

Imperfect reciprofluxion yields residual propagation

Pedagogically, the term ``reciprofluxion'' is introduced to describe not a field in space but a circulation condition. If the circulation completes, the system retains structure. If it does not, the remainder must express itself. This ties structure and radiation to the same attempted act: closure.

A plate here can be more concrete: it can depict a circulation loop, a closure boundary, or an interlocking rotor pair. The plate should aim to show the difference between a fully rechordeed circulation and one with a residual channel.



### 3.3 Interfluxion

3.3 — Interfluxion density: cause-space discipline

Interfluxion is the internal circulation density of reciprocal flux within a closed or partially closed system.

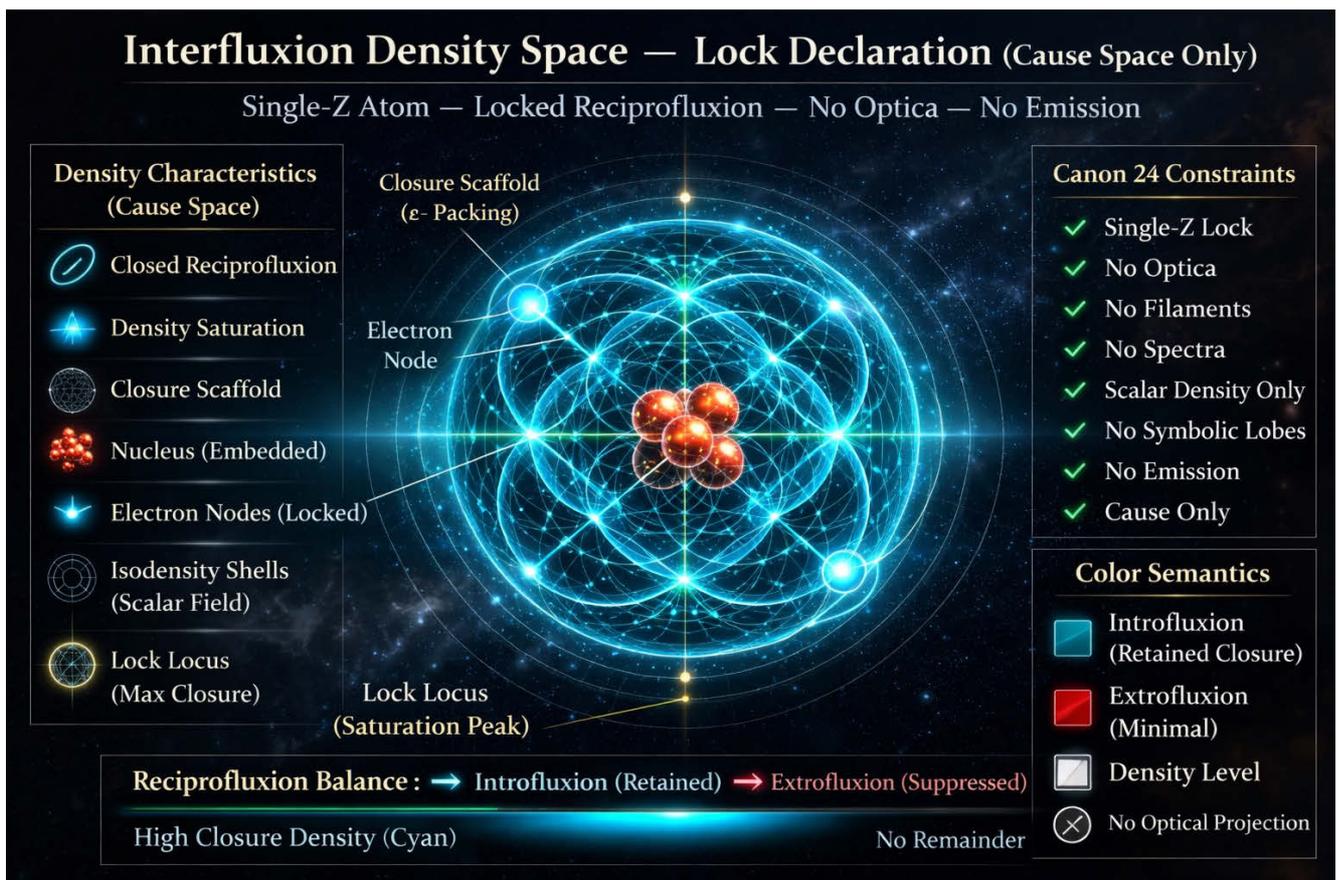
Interfluxion density is ontological.

It describes what the atom is doing, not what is observed.

This distinction is essential and will be preserved throughout.

Pedagogically, this subsection exists to enforce a strict rule that will govern the entire paper: internal density is not the same as external observation. The reader must be trained to resist interpreting interfluxion plates as images of light, and to resist interpreting Optica plates as images of structure.

A plate following this subsection is a disciplinary plate. It should label the space as cause space and show that what is being visualized is an internal density measure, not a projected radiation field. This prevents category collapse later, especially during model-to-data comparisons.



## 4 Optical Reciprocal Induction

4 — Induction: closure geometry → induced optical remainder

Optical Reciprocal Induction states:

When reciprocal flux closes only partially, the unresolved temporal residue induces propagating optical modes whose frequencies are determined by the geometry of closure.

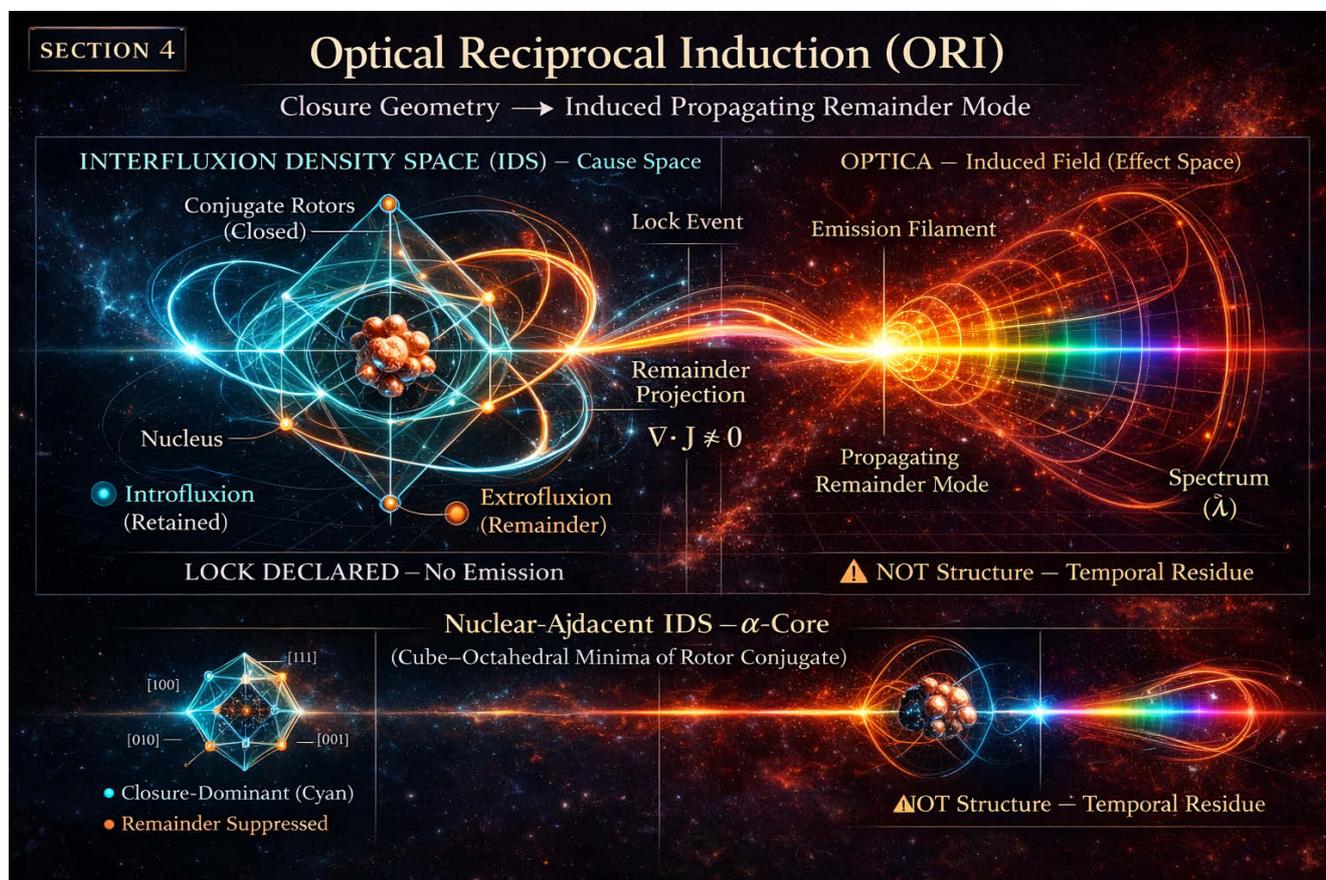
Optics is not imposed. It is induced.

Light is therefore not an independent field added to matter; it is the temporal shadow of incomplete geometric closure.

Pedagogically, the key word is "induces." The claim is not that light is always present as a background ingredient, but that light emerges as a necessary consequence when closure cannot complete. This makes optical emission an explanatory output, not a starting axiom.

The phrase "temporal residue" is also deliberate. The remainder is not merely spatial leakage; it is the time-structured failure to fully close. Therefore the induced modes are frequencies. In this view, frequency is the natural language of incomplete closure because it is the natural language of temporal remainder.

A plate after this section should illustrate induction in the causal sense. If you drop a Canon plate here, it should be one that shows (i) closure geometry in interfluxion space and (ii) the onset of a propagating remainder mode in Optica space derived from the same lock event, without modifying the underlying geometry.



# 5 The Atomic Closure Engine

5 — Engine roadmap / lock hinge

The atomic engine proceeds in a strict causal order:

Primitive impulse  $|J|$  seeks closure

Conjugate rotor structures form (electron clock, proton inversion)

Reciprofluxive circulation attempts closure

A discrete interfluxion scaffold locks

Residual Potentum remains

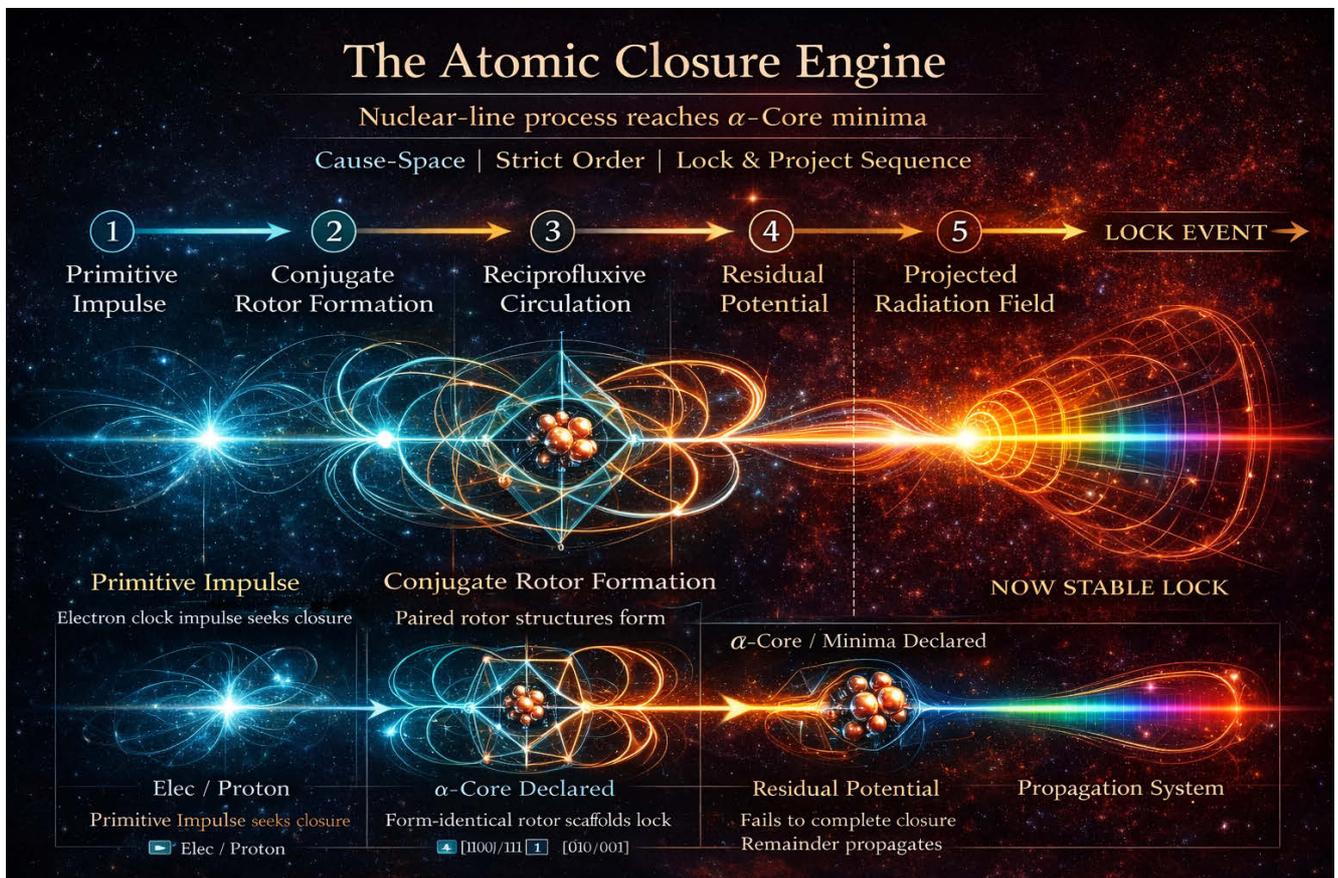
Residual Potentum propagates optically as discrete modes

No step is optional. No spectra are assumed.

Pedagogically, this section is a roadmap. It tells the reader where each later concept belongs and in what sequence it is allowed to appear. The discipline "no step is optional" is meant to prevent smuggling spectra in early as assumptions.

The engine order also implies where computation and verification belong. The lock event is the hinge: it is where the system transitions from "seeking closure" to "having a stable scaffold." Only after this lock does it make sense to compute the remainder and project it optically.

A plate following this section should be a process plate: a staged depiction of the engine, or a sequence snapshot, or a lock certificate representation. The plate should orient an auditor to where, exactly, the interfluxion plate set begins and where the Optica plate set begins.



## 6 Interfluxion Density Space (Cause Space)

6 — IDS density plate (no wavelengths)

We define an interfluxion density field:

representing the squared magnitude of satisfied reciprocal flux at each locus for atomic number  $Z$ .

Closure is obtained by minimizing a closure residual functional:  
subject to conjugacy and reciprocity constraints.

A lock occurs when further redistribution of  $|J|$  fails to reduce .

This lock defines:

The nuclear scaffold

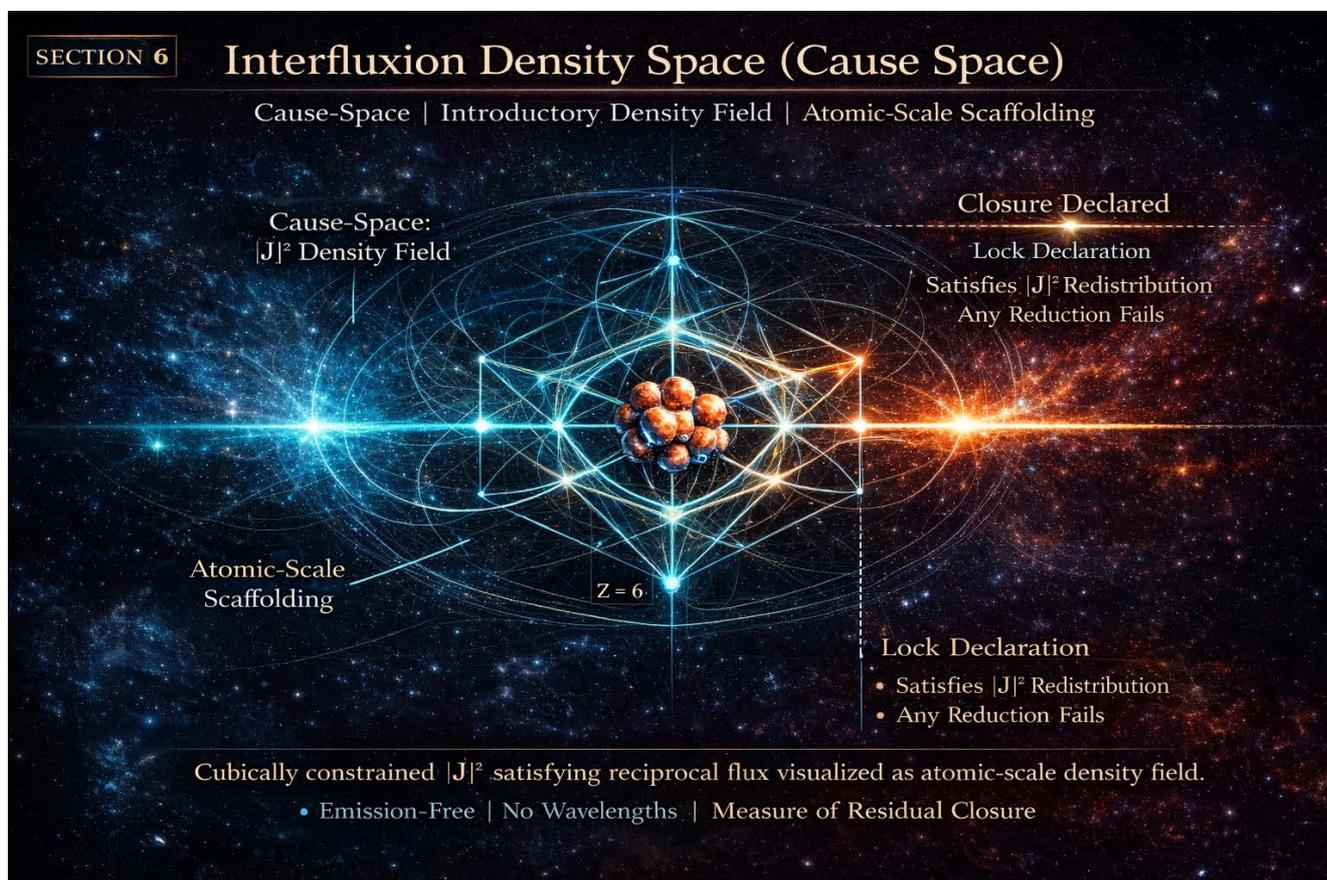
The atom-scale interfluxion density

The admissible transition loci

Pedagogically, the purpose of introducing an explicit density field is to ensure the theory is testable in a constructive way. A density field can be computed, visualized, and compared across solver implementations without requiring interpretive leaps.

The closure residual functional should be understood as a computable measure of "how unclosed" the system remains. Minimizing is the formal expression of the physical act "seeking closure." The lock event is not chosen by hand; it is declared when further minimization fails.

A plate after this section should show the cause-space density itself. It should include enough annotation (in the plate footer, not necessarily in the figure) to identify  $Z$ , the basin/lock, and the fact that wavelengths are not present here. The entire point is to make structure visible before emission.



## 7 EZ Spacing and Integer Phase Admissibility

7 — Discrete admissibility / loci plate

Closure admits only integer phase transitions:

Each admissible transition corresponds to a dimensionless EZ spacing factor:

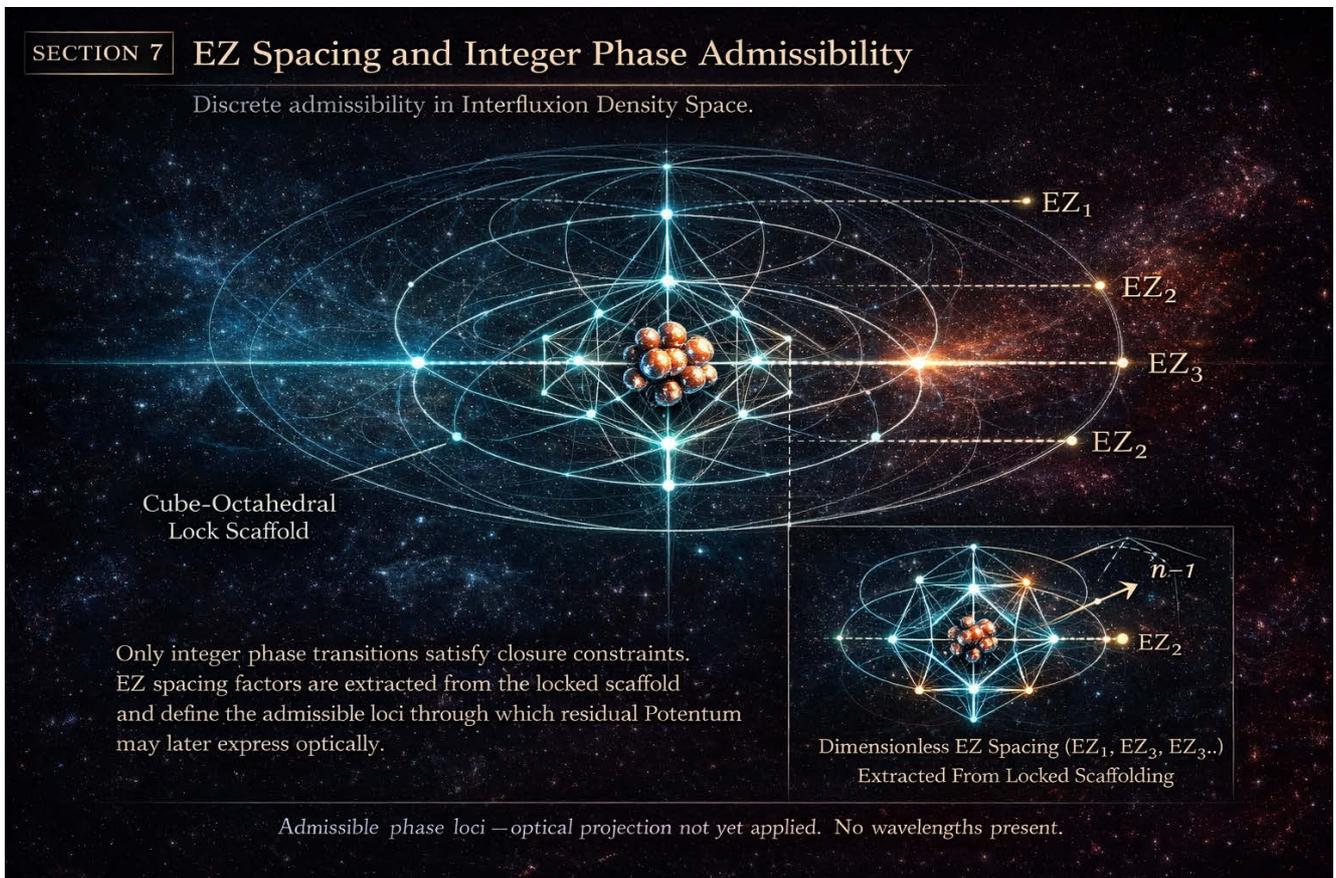
These spacings are extracted from geometry, not fitted.

Pedagogically, this section explains why discreteness is expected rather than surprising. If closure were continuous, spectra would be continuous. The fact that closure is phase-admissible only in integers is what enforces discrete families of remainder modes.

The EZ spacing factors are introduced as a bridge between structure and wavelength without collapsing the two. They are dimensionless geometric quantities extracted from the locked scaffold, and they function as the admissible "slots" through which the remainder can express itself.

A plate after this section is ideally a "spacing" plate: transition loci marked on a structural density map, or a schematic of admissible phase steps, still without producing wavelengths. The reader should see the discrete admissibility before seeing optical projection.

### Electron Zone Geometry is Optical Extroversion of Nuclear Structure



## 8 Optica: The Projection of the Remainder (Effect Space)

8 — First true Optica plate (derived from same lock)

Optical wavelengths arise from the unresolved temporal residue of closure:

Where:

$\tau$  is a single universal temporal conversion constant

No element-specific tuning is permitted

Optica is consequential, not ontological.

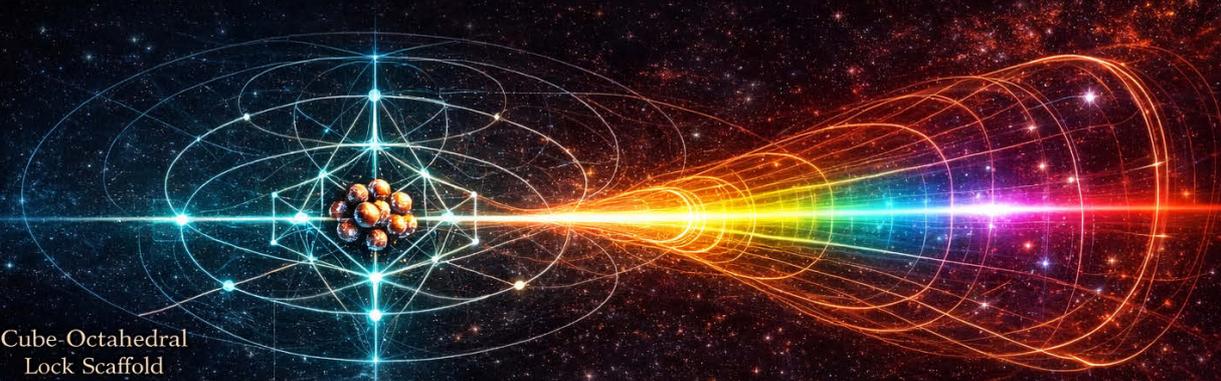
It is a projection of interfluxion remainder into propagating modes.

Pedagogically, this section teaches the reader how to interpret the optical side without reifying it as structure. Optica is a projection: it is what becomes visible to an observer because a remainder exists and must propagate.

The statement "no element-specific tuning" is essential for falsifiability. If each element required its own temporal constant, then the model would be a fitting engine. Instead, the model claims that element-to-element diversity arises from closure geometry, not from tuned optical parameters.

A plate after this section should be the first true Optica plate: it should depict the projected field or spectrum derived from the same lock as the cause plate. It should communicate that it is an effect-space image, not a cause-space density.

**SECTION 8** **Optica: The Projection of the Remainder (Effect Space)**  
Quantized Emission Projected from Unresolved Temporal Remainder



Cube-Octahedral Lock Scaffold

Optical Projection

Propagated Spectrum  $\lambda$

Quantized wavelengths arise as an effect-space spectrum projected from the same closure lock defined previously in cause space.

- Spectral emission – remainder is projected
- Derived from same lock / lockpath sequence
- Effect-Space Image

Quantized wavelengths arise as an effect-space spectrum projected from the same closure lock defined previously in cause space.

## 9 Dual-Space Reporting Protocol

9 — Protocol plate: two parallel plate sequences

For every element, results are presented in two parallel plate sequences derived from the same lock:

Interfluxion Density Plates

Closure basin

Locked scaffold

Atom-scale density

Transition loci (no wavelengths)

Optica Plates

Optical field projection

Emergent wavelengths

Visible-band extraction

MODEL  $\leftrightarrow$  NIST comparison (comparison only)

This prevents category collapse.

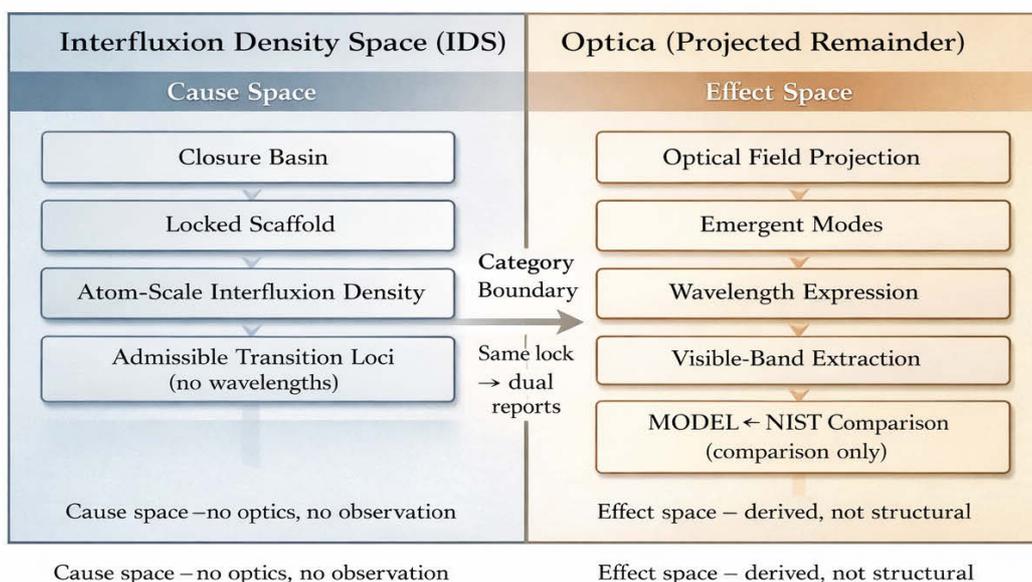
Pedagogically, this protocol is the enforcement mechanism for clarity. Many confusions in physics come from mixing a model's internal variables with what is directly observed. The dual-space protocol forces a separation so that each plate set answers one question at a time.

The Interfluxion series answers: what is the closure geometry and where are its admissible loci? The Optica series answers: given that geometry, what remainder propagates and at what wavelengths? The comparison to NIST is explicitly postponed to the end, so that observation does not sneak into structure.

A plate after this section should be a protocol plate: a simple two-column depiction of the workflow, or a plate index showing which figures belong to cause space and which belong to effect space. It is a reader-aid that makes the later element sections easier to audit.

— SECTION 9 —

### Dual-Space Reporting Protocol



## 10 Worked Example I: Hydrogen ( $Z=1$ )

10 — Hydrogen: IDS left / Optica right archetype pair

Hydrogen demonstrates the archetype:

A single closure

Multiple optical modes

No degeneracy excuses

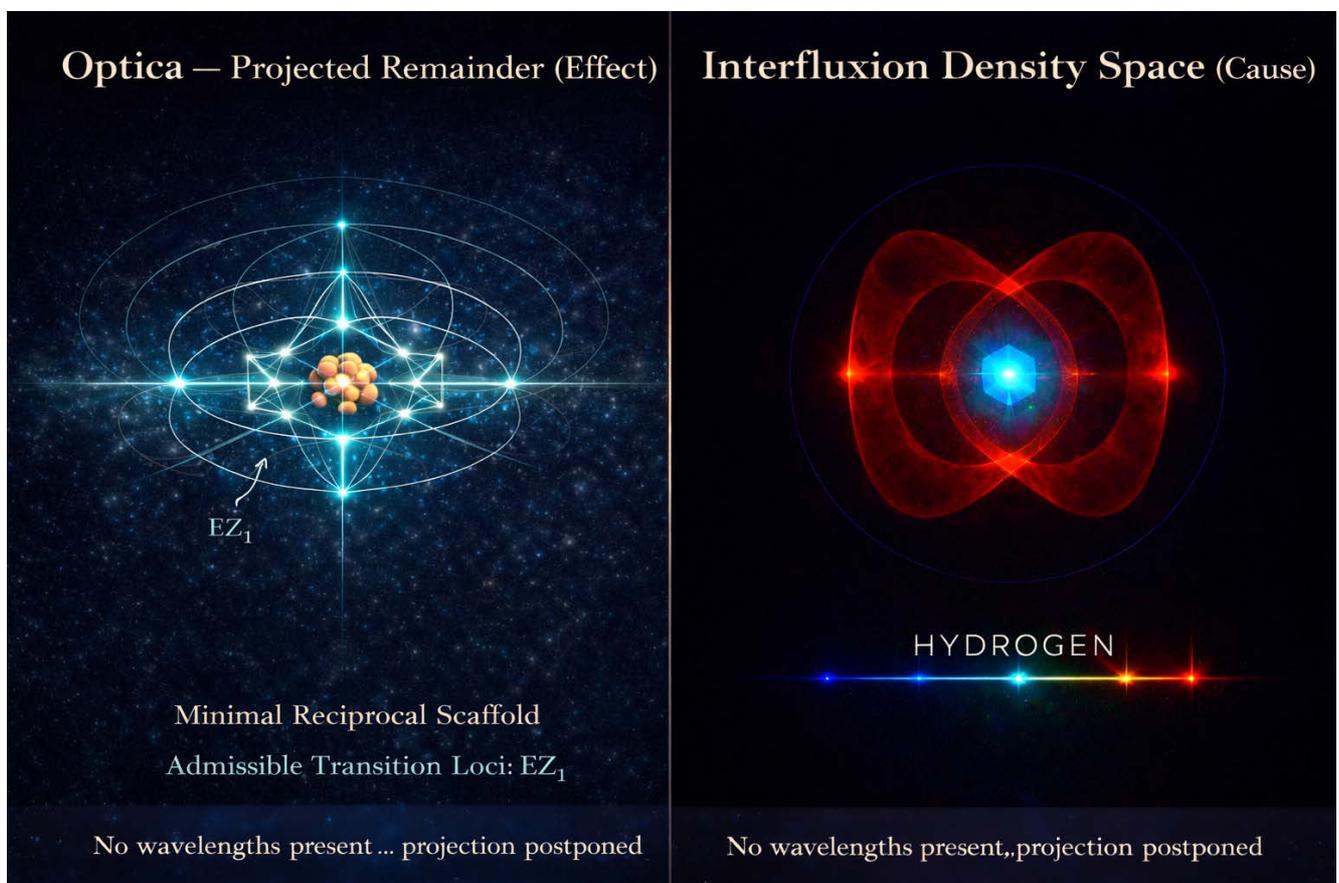
Interfluxion density shows a minimal reciprocal scaffold.

Optica reveals the Balmer series as the unavoidable remainder.

Pedagogically, Hydrogen is treated first because it has the least room for interpretive escape. If discreteness and induced spectra are real consequences of closure, Hydrogen should show it with maximal transparency.

The interfluxion plates for Hydrogen should therefore be spare and legible: a minimal scaffold, a clear lock, and transition loci that are few enough to inspect by eye. The Optica plates should then show how multiple optical modes arise from that single structural closure.

A plate after this section should be the Hydrogen pair: one cause-space density plate and one Optica plate from the same lock. If you also use a comparison plate, it belongs at the end of the Optica sequence, clearly labeled as comparison only.



## 11 Worked Example II: Carbon ( $Z=6$ )

11 — Carbon: tetrahedral IDS then downstream Optica

Carbon introduces structural chemistry.

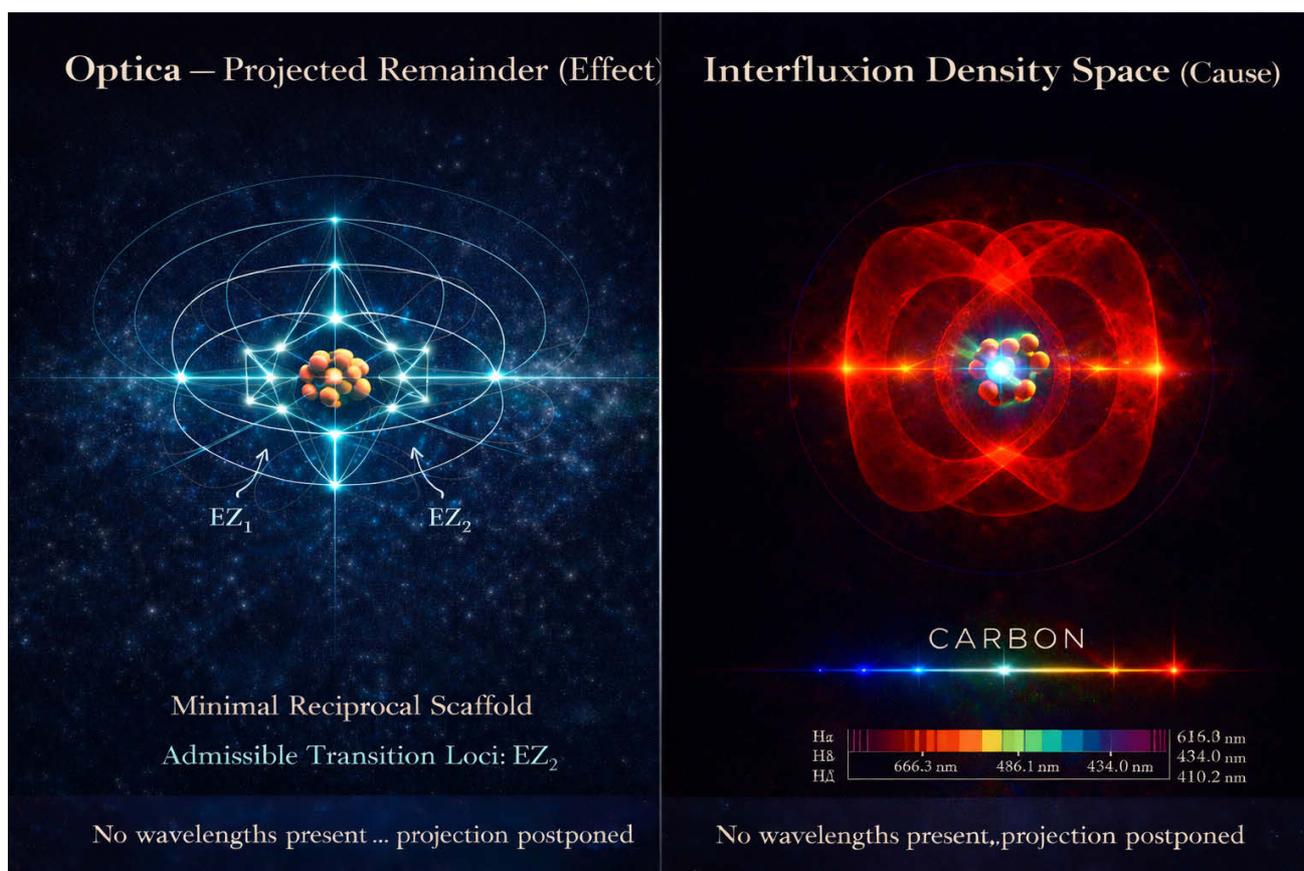
Interfluxion density reveals tetrahedral symmetry before spectra appear.

Optical lines follow as projections, not causes.

Pedagogically, Carbon is where ``structure'' becomes unavoidably chemical. The reader should see that the same closure logic that generated Hydrogen's scaffold now generates a tetrahedral organization that has immediate interpretive relevance to bonding.

The key teaching point is temporal ordering: tetrahedral symmetry appears in cause space before any optical projection is computed. This prevents the common confusion of thinking that spectral lines ``explain'' geometry. In this framework, geometry explains the spectrum.

A plate after this section should show Carbon's tetrahedral interfluxion density plate (cause space) and then an Optica projection plate derived from the same lock. The reader should be able to see that the optical field is downstream and does not feed back into the tetrahedral organization.



## 12 Worked Example III: Iron ( $Z = 26$ )

12 — Iron: dense IDS scaffold + crowded Optica

Iron exhibits dense closure and memory accumulation.

Spectral crowding is shown to arise from geometric multiplicity, not stochastic transitions.

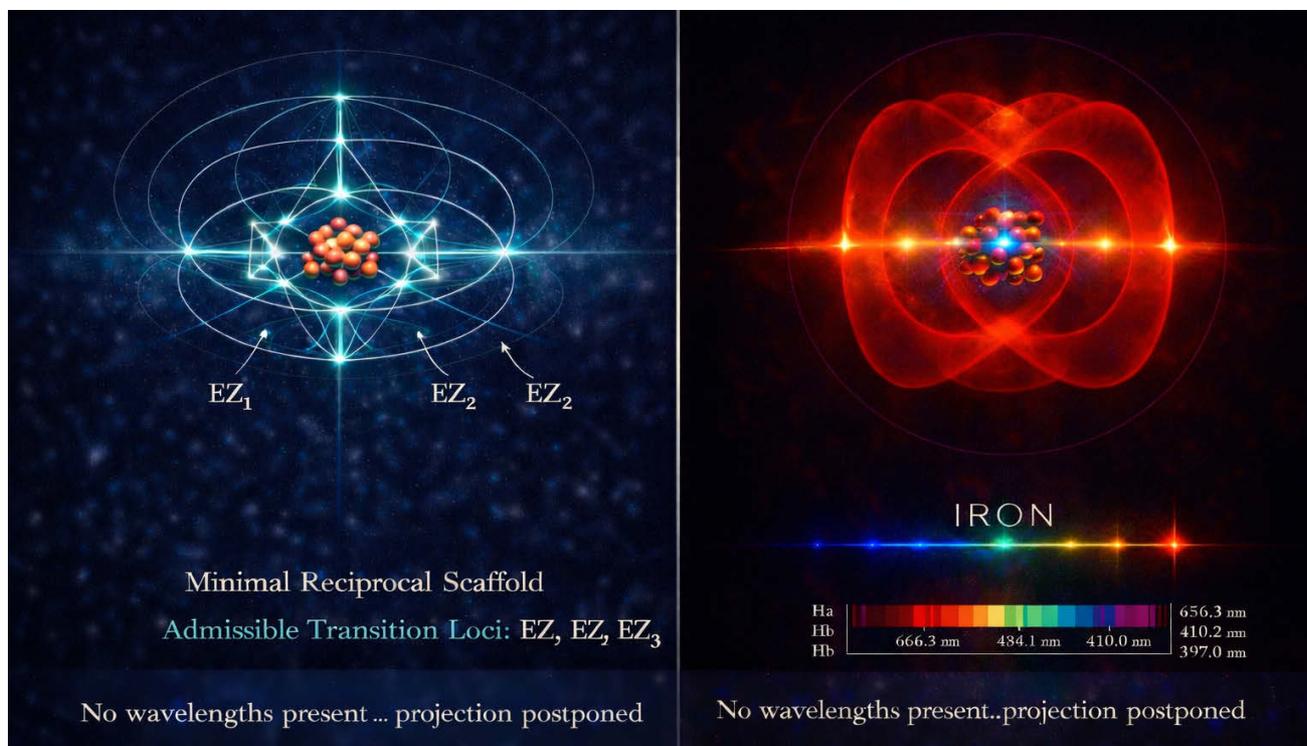
Pedagogically, Iron is the entry point to "spectral density" as a structural phenomenon. The reader must learn to interpret line crowding not as randomness, but as many admissible remainder modes emerging from a highly articulated closure scaffold.

The concept "memory accumulation" is introduced as a closure property: as  $Z$  increases, closure has more ways to stabilize and more constraints to satisfy, producing richer internal topology. The remainder does not become arbitrary; it becomes more numerous because the closure geometry is more numerous.

A plate after this section should show Iron's interfluxion density plate with clear scaffolding features, followed by an Optica plate showing crowded lines. The reader should be encouraged (by plate organization) to look for correspondence between geometric multiplicity and optical multiplicity.

**Emission structure as  
optical extroversion of  
Nuclear structure's excess**

**Closure of interfluxion  
establishing conserved  
analog resonant memory**



### 13 Worked Example IV: Gold ( $Z = 79$ )

13 — Gold: stress-test IDS + Optica richness

Gold stress-tests the framework.

Despite high complexity, closure remains discrete.

Optical richness is shown to be a projection artifact, not a failure of order.

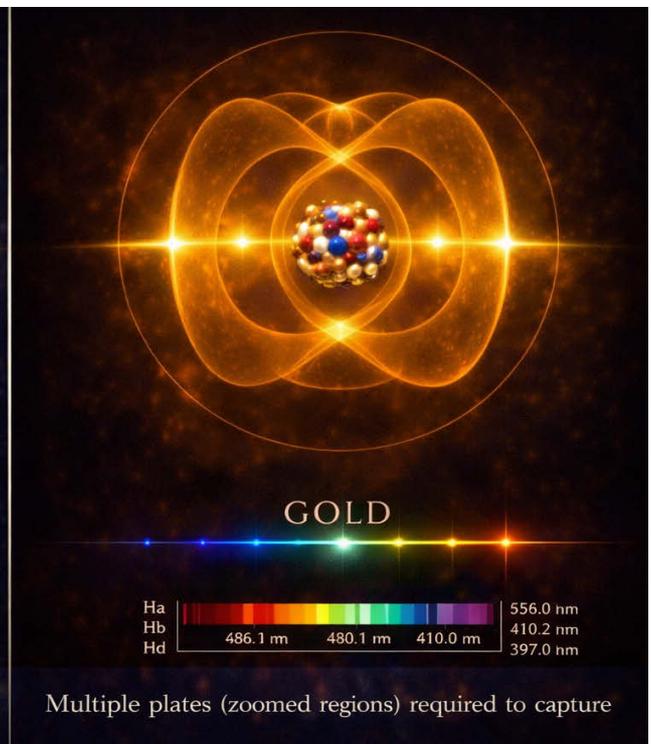
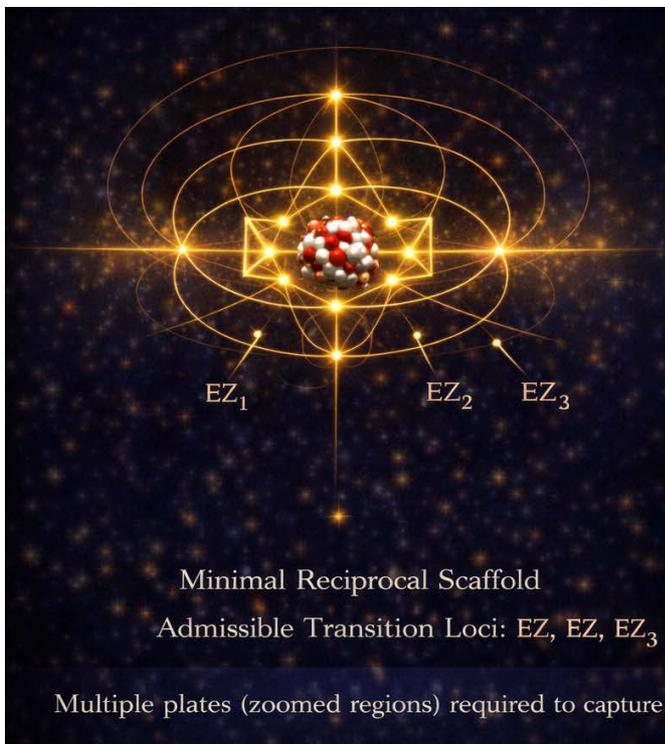
Pedagogically, Gold is included to show scalability. A theory that only ``works'' at low  $Z$  is not a generative theory of matter. The Gold example is therefore a test of whether the closure engine continues to produce discrete scaffolds without introducing new ad hoc rules.

The teaching emphasis is that increased complexity should not be mistaken for loss of lawfulness. Optical richness is the observer-facing appearance of many remainder modes. The underlying cause space remains a locked scaffold produced by the same closure logic.

A plate after this section should show a Gold cause-space density plate and its Optica projection. If visual complexity threatens readability, the protocol is to provide multiple plates (zoomed regions) rather than to compress interpretation.

#### Emission structure as optical extroversion of Nuclear structure's excess

#### Closure of interfluxion establishing conserved analog resonant memory



# 1 Conclusion

Atomic spectra are not mysterious emissions from abstract states, nor are they signals of probabilistic transitions between imposed eigenlevels. They are the optical remainder of geometric closure.

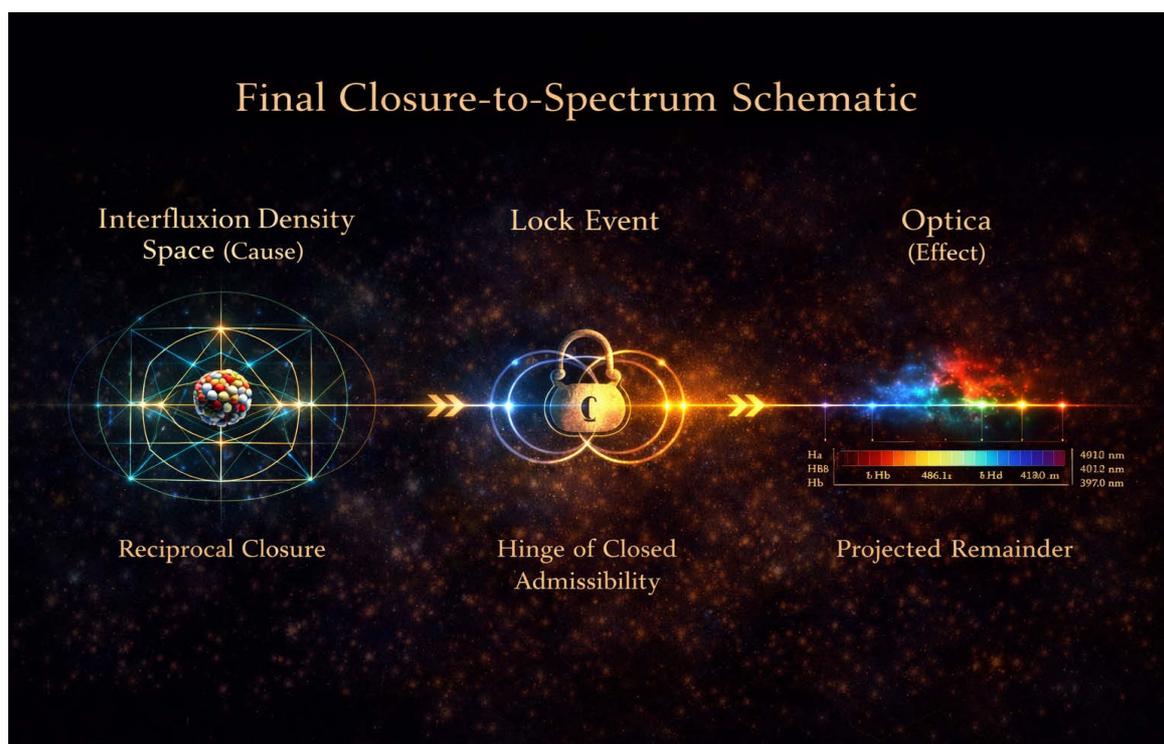
In the framework developed in this paper, atomic structure arises from reciprocal geometric induction. Primitive impulse seeks closure; closure locks discretely according to admissible geometric constraints. When closure cannot retain all agency, a remainder necessarily propagates. That propagation is optical. Spectral lines are therefore not primary causes but required witnesses of what closure could not fully contain.

This framework restores a lawful causal chain without introducing auxiliary postulates. Discreteness does not arise from quantization rules imposed on otherwise continuous systems; it arises from closure itself. Spectral regularity does not require eigenstates; it follows from the finite set of admissible remainder modes permitted by a locked geometric scaffold.

A central methodological safeguard of this work is the strict separation of cause-space and effect-space. Interfluxion Density Space represents the generative closure geometry. Optica represents the observer-facing projection of the remainder. By construction, this separation prevents accidental tuning of structure to match spectra. Structure is resolved before any optical comparison is permitted.

The atom is thus revealed as a doubly-closed generator. One closure stabilizes matter; the second closure governs what must be released. Spectra are not decorations added to atoms—they are the necessary testimony of incomplete retention.

Pedagogically, this conclusion compresses the full argument of the paper into a single lawful narrative: geometry gives rise to closure, closure locks discretely, remainder propagates optically, and that propagation is what we catalog as atomic spectra. Nothing further is assumed.



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