## Research Awards Screening Test, 2005

## KEY

## Section 1: Algebra 3.7 open 3.8 closed, connected 1.1 5 3.9 nowhere dense 1.2 5 3.10 closed, compact, connected 1.3 $\alpha = -1/2, \beta = 1, \gamma = 1/2$ Section 4: Applied Mathematics 1.4 2 1.5 4 $4.1 \ 4\pi$ 1.6 124.2 01.7 (a), (b) $4.3 \pi^2$ 1.8 (a) (c) 4.4 01.9 (a) (c) (d) $4.5 \ 3$ 1.10 (a) (c) (d) 4.6 174.7 elliptic Section 2: Analysis $4.8 \pi$ $2.1 \int_0^1 f(t)dt$ 4.9 $\int_{\Omega} f(x,y) dx dy = 0$ $2.2 \infty$ $4.10 \ \ h = 2r$ $[2.3 \ ]1, \infty[$ 2.4 1Section 5: Miscellaneous 2.5 05.1 29 2.6 0 $5.2 \ n2^{n-1}$ 2.7 (b) (c) 5.3 1 2.8 (b) (c) $5.4 \ 3\sqrt{3}/4$ 2.9 None 5.5 2 2.10 (b) 5.6 parallelogram Section 3: Topology 5.7 0 $5.8 \ 2/\pi$ 3.1 uniformly continuous 5.9 True 3.2 0 $5.10 \ 2e - 1$ 3.3 1 Note: Correct answers to Qns. 2.1, 2.3 and 4.9 3.4 infinite in any other equivalent notation can, obviously, 3.5 open, dense

3.6 compact, connected

be accepted!!!