## （PI）1．1 Data Representation

## 9618 Computer Science Syllabus requirements：

## Sec 1．1 Data Representation

Candidates should be able to：
© Show understanding of binary magnitudes and the difference between binary prefixes and decimal prefixes
© Show understanding of the basis of different number systems
© Show understanding of the basis of different number systems
© Describe practical applications where Binary Coded Decimal（BCD）and Hexadecimal are used
© Show understanding of and be able to represent character data in its intemal binary form， depending on the character set used
〔 Understand the difference between and use：
－kibi and kilo
－mebi and mega
－gibi and giga
－tebi and tera
〔15 Use the binary，denary，hexadecimal number bases and Binary Coded Decimal（BCD）and one＇s and two＇s complement representation for binary numbers
©
Convert an integer value from one number base／representation to another
Using positive and negative binary integers Show understanding of how overflow can occur Familiar with ASCII（American Standard Code for Information Interchange），extended ASCII and Unicode．Students will not be expected to memorise any particular character codes．

## Denary Number System：

We know decimal or denary number system has（base 10）．This uses digits 0 to 9 and has place values below

| 10000 | 1000 | 100 | 10 | units |
| :---: | :---: | :---: | :---: | :---: |
| 3 | 1 | 4 | 2 | 1 |

## Binary number system：

The binary system on computers uses combinations of 0 s and 1 s and has（base 2）．

| 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left(2^{7}\right)$ | $\left(2^{6}\right)$ | $\left(2^{5}\right)$ | $\left(2^{4}\right)$ | $\left(2^{3}\right)$ | $\left(2^{2}\right)$ | $\left(2^{1}\right)$ | $\left(2^{0}\right)$ |

A typical binary number would be：
1
1
1
0
1
1
1
0
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## Binary place values

You can also break a binary number down into place-value columns, but each column is a power of two instead of a power of ten.
For example, take a binary number like 1001.

| Eights | Fours | Twos | Ones |
| :---: | :---: | :---: | :---: |
| 8 s | 4 s | 2 s | 1 s |
| $\left(2^{\prime}\right)$ | $\left(2^{\prime}\right)$ | $\left(2^{\prime}\right)$ | $\left(2^{\prime}\right)$ |
| 1 | 0 | 0 | 1 |

By looking at the place values, we can calculate the equivalent denary number.
That is: $\quad\left(\mathbf{1} \times \mathbf{2}^{\mathbf{3}}\right)+\left(\mathbf{0} \times \mathbf{2}^{\mathbf{2}}\right)+\left(\mathbf{0} \times \mathbf{2}^{\mathbf{1}}\right)+\left(\mathbf{1} \times \mathbf{2}^{\mathbf{0}}\right)=\mathbf{8}+\mathbf{0}+\mathbf{0}+\mathbf{1}$

$$
(\mathbf{1} \times 8)+(\mathbf{0} \times 4)+(\mathbf{0} \times 2)+(\mathbf{1} \times 1)=8+1
$$

$$
=9
$$

## Converting binary to denary

To calculate a large binary number like $\mathbf{1 0 1 0 1 0 0 0}$ we need more place values of multiples of 2 .

- $2^{7}=128$
- $2^{6}=64$
- $2^{5}=32$
- $2^{4}=16$
- $2^{3}=8$
- $2^{2}=4$
- $2^{1}=2$
- $2^{0}=1$

In denary the sum is calculated as:
$\left(1 \times 2^{7}\right)+\left(0 \times 2^{6}\right)+\left(1 \times 2^{5}\right)+\left(0 \times 2^{4}\right)+\left(1 \times 2^{3}\right)+\left(0 \times 2^{2}\right)+\left(0 \times 2^{1}\right)+\left(0 \times 2^{0}\right)=168$
$(\mathbf{1} \times 128)+(\mathbf{0} \times 64)+(\mathbf{1} \times 32)+(\mathbf{0} \times 16)+(\mathbf{1} \times 8)+(\mathbf{0} \times 4)+(\mathbf{0} \times 2)+(\mathbf{0} \times 1)=128+32$
$+8=168$
The table below shows denary numbers down the left with their equivalent binary numbers marked out below the base 2 columns. Each individual column in the table represents a different place value equivalent to the base 2 powers

## Convert between denary

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|  |  | Binary pattern |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Place value 128 | Place value 64 | Place value 32 | Place value 16 | Place value 8 | Place value 4 | Place value 2 | Place value 1 |
|  | 0 |  |  |  |  |  |  |  | 0 |
|  | 1 |  |  |  |  |  |  |  | 1 |
|  | 2 |  |  |  |  |  |  | 1 | 0 |
|  | 3 |  |  |  |  |  |  | 1 | 1 |
|  | 4 |  |  |  |  |  | 1 | 0 | 0 |
|  | 5 |  |  |  |  |  | 1 | 0 | 1 |
|  | 6 |  |  |  |  |  | 1 | 1 | 0 |
|  | 7 |  |  |  |  |  | 1 | 1 | 1 |
|  | 8 |  |  |  |  | 1 | 0 | 0 | 0 |
|  | 9 |  |  |  |  | 1 | 0 | 0 | 1 |
|  | 10 |  |  |  |  | 1 | 0 | 1 | 0 |
|  | .... |  |  |  |  |  |  |  |  |
|  | 255 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

## Converting denary to binary: Method 1

There are two methods for converting a denary (base 10) number to binary (base 2).
This is method one.
Divide by two and use the remainder
Divide the starting number by 2 . If it divides evenly, the binary digit is 0 . If it does not if there is a remainder - the binary digit is 1 .

## Worked example: Denary number 83



Put the remainders in reverse order to get the final number: 1010011.

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## Converting denary to binary: Method 2

There are two methods for converting a denary (base 10) number to binary (base 2). This method uses Place Values


Worked example: Denary number 84
We need to check which numbers place values can be added to make 84 . We will put 1 under the numbers to e added and 0 under the numbers which are not added.

1. We select Place value 64 so we put 1 under it.
2. We select place value 16 and put 1 under it
3. We selected place value 4 and put 1 under it.
4. Adding $64+16+4$ gives us $\mathbf{8 4}$ so our number becomes:

| 64 | 32 | 16 | 8 | 4 | 2 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 0 | 1 | 0 | 1 | 0 | 0 |

Adding 64+16+4=84
Result: $\mathbf{8 4}$ in denary is equivalent to $\mathbf{1 0 1 0 1 0 0}$ in binary.

## Bits and binary:

Computers use binary - the digits 0 and 1 - to store data. A binary digit, or bit, is the smallest unit of data in computing. It is represented by a 0 or a 1 .

The circuits in a computer's processor are made up of billions of transistors. A transistor is a tiny switch that is activated by the electronic signals it receives.
The digits $\mathbf{1}$ or $\mathbf{0}$ used in binary reflect the on or off states of a transistor.
All software, music, documents, and any other information that is processed by a computer, is also stored using binary.

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## Bits and bytes



Bits can be grouped together to make them easier to work with. A group of 8 bits is called a byte. Other groupings include:

- Nibble - 4 bits (half a byte)
- Byte - 8 bits
- Kilobyte (KB) - 1024 bytes (or $1024 \times 8$ bits) $=\mathbf{2}^{\mathbf{1 0}}$
- Megabyte (MB) - 1024 kilobytes (or 1048576 bytes) $=\mathbf{2}^{20}$
- Gigabyte (GB) - 1024 megabytes

$$
=2^{30}
$$

- Terabyte (TB) - 1024 gigabytes
- Petabyte (PB) -1024 Terabytes

$$
=2^{40}
$$

- Exabyte (EB) -1024 Petabytes
- Zettabyte (ZB)- 1024 Exabytes

$$
=2^{50}
$$

- Yottabyte (YB) 1024 Zettabytes

$$
=\mathbf{2}^{60}
$$

$$
=\mathbf{2}^{70}
$$

The IEC convention for computer internal memories (including RAM) becomes:
C1 1 kilobyte $=1000$ byte
1 megabyte $=1000000$ bytes
1 gigabyte $=1000000000$ bytes
N 1 terabyte $=1000000000000$ bytes and so on.

## VS

© 1 kibibyte $(1 \mathrm{KiB})=1024$ bytes
1 mebibyte $(\mathbf{1 ~ M i B})=1048576$ bytes
1 gibibyte $(\mathbf{1 ~ G i B})=\mathbf{1 0 7 3 7 4 1 8 2 4}$ bytes
1 tebibyte $(1 \mathrm{TiB})=1099511627776$ bytes and so on.
However, the IEC terms are not universally used and we still use the more conventional terms shown above. This also ties up with the Cambridge International Examinations computer science syllabus which uses the same terminology as in example above.

## Binary addition (unsigned binary number)

Adding binary numbers is similar to adding denary numbers.

## Example: Adding the binary numbers 011 and 100.

Write the numbers out using the column method. Start from the right, and simply add the binary number 3 to binary number 4.

$$
\begin{array}{r}
011 \\
+100 \\
\hline 111
\end{array}
$$

$111=7$ if converted back to denary.

## Example: Adding two 1s in the same column.

Sometimes a binary addition will require you to carry over values into the next highest placevalue column, eg when finding the sum of the binary numbers 0010 and 0111:

When adding two ones in the same column. In binary, $\mathbf{1 + 1}=\mathbf{1 0}$ ( $\mathbf{2}$ in denary) - it has to become 0 in sum and with 1 carried over.

$1001=9$ if converted back to denary. $2+7=9$ in denary.

## + ve and -ve binary numbers (signed numbers)

When computer stores binary numbers, we have to differentiate +ve binary numbers from - ve binary numbers. Unfortunately (-) or (+) sign cannot be displayed rather only $\mathbf{0 / 1}$ can be used in binary.

## (MSB) Most significant bit and LSB least significant bit:

In a binary number, the bit furthest to the left is called the most significant bit (MSB) and the bit furthest to the right is called the least significant bit (LSB).

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The MSB gives the sign of the number (sign bit), $\mathbf{0}$ for positive and $\mathbf{1}$ for negative. MSB
$\begin{array}{llllllll}0 & 1 & 0 & 1 & 1 & 0 & 1 & 1\end{array}$

## Rules of + ve and -ve binary numbers:

(1) Positive binary number always starts with 0 in MSB (Most significant bit)

Negative binary number always starts with 1 in MSB (Most significant bit)
e.g +ve number: 01010010
-ve number: 10010110
-128 $6432 \begin{array}{llllll}16 & 8 & 4 & 2 & 1\end{array}$ Place Values
Number becomes
$\underset{\downarrow}{\mathbf{V}} \underset{\sim}{1} 0 \mathbf{0} 0010$ so number is $0+64+16+2=82$
Sign bit + ve part of number
Negative binary number always starts with 1 in MSB (Most significant bit)
-128 643216842181 Place Values
Number becomes

Sign bit + ve part of number

## Conversion of -ve denary number to binary:

## What is - $\mathbf{6 5} \mathbf{1 0}$ in binary?

Two's complement allows us to represent signed negative values in binary,

## Binary addítion and subtraction

Up until now we have assumed all binary numbers have positive values. There are a number of methods to represent both positive and negative numbers. We will consider:

One's complement
Two's complement.
In one's complement, each digit in the binary number is inverted (in other words, 0 becomes 1and 1 becomes 0). For example,
Step 1
$65=01000001$ in binary
Step 2: invert 1 to 0 and 0 to 1 we get: 01000001 to its one's complement as below:

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$01000001=10111110$
In two's complement,binary digit 1 is added to one's compliment Step 3: Convert 10111110 Binary to its two's complement by adding 1 to the one's complement.


Two's compliment of a positive number will make it a negative number
-128 6432168421 Place values
1001111111 = Two's complement

$$
=-128+32+16+8+4+2+1=-65
$$

10111111 is $\mathbf{- 6 5}$ in binary. We know this it true because if we add 01000001 (+65) to 10111111b (-65) and ignore the carry bit, the sum $=0$.
which is what we obtain if we add $+65+(-65)=0$.


## Iwo's complement sums:

Using two's complement, the CPU can perform arithmetic using binary addition. For example:
-7 + 7 in two's complement binary would be calculated as:

$$
\begin{array}{r}
1001 \\
+\quad \begin{array}{r}
0111 \\
\times 0000
\end{array}
\end{array}
$$

In two's complement, if the final result overflows the remaining carry number is simply discarded. For example:
-3 + 4 in two's complement binary would be calculated as:

$$
\begin{array}{r}
1101 \\
+\quad 0100
\end{array}
$$

Consider the two's complement binary number 10110001.
Method 1:
© Convert to the 1 's compliment gives 01001110 and keep the minus sign with it
© Converting to two's complement gives us 01001111.
© You ignore the leading zero in MSB as it is not a positive number and apply one of the methods to convert the remaining binary to denary which gives 79.
© You add the minus sign to give -79 .
Method 2: Sum the individual place values but treat the most significant bit as a negative value
You follow the approach illustrated in Table 1.02 to convert the original binary number 10110001 as follows:

| Place | $-2^{7}$ <br> $=$ <br> value | $2^{6}$ <br> $=$ <br> 64 | $2^{5}$ <br> $=$ <br> 32 | $2^{4}$ <br> $=$ <br> 16 | $2^{3}$ <br> $=$ <br> 8 | $2^{2}$ <br> $=$ <br> 4 | $2^{1}$ <br> $=$ <br> 2 | $2^{0}$ <br> 1 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Digit | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 1 |
| Product | -128 | 0 | 32 | 16 | 0 | 0 | 0 | 1 |

You now add the values in the bottom row to get -79 .

## Binary Subtractions

What is Binary Subtraction? Subtraction of binary numbers is an arithmetic operation similar to the subtraction of decimal numbers or base 10 numbers. For example, $1+1+1=3$ in base 10 and $1+1+1=11$.

When you add and subtract binary numbers, you will need to be careful when borrowing as these will take place more often. When 1 is to be subtracted from 0 , the result is 1 where 1 is borrowed from the next highest order bit or digit.
Method 1: Binary subtraction using binary numbers
Binary Subtraction Table:

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The subtraction of binary numbers is given by:

| Binary Number | Subtraction Value |
| :--- | :--- |
| $0-0$ | 0 |
| $1-0$ | 1 |
| $0-1$ | 1 (Borrow 1 from next high order digit) |
| $1-1$ | 0 |

## Procedure to do Binary Subtraction:

## Example 1:

$$
0011010-0001100
$$

## Solution:

$$
2 \text { - } 1 \text { = } 1 \text { (denary) }
$$



$$
\begin{array}{lllllll}
0 & 0 & 0 & 1 & 1 & 1 & 0
\end{array}
$$

Decimal Equivalent :
$0011010=26$
$0001100=12$
Therefore, $26-12=14$
The binary resultant 0001110 is equivalent to the 14

## Example 2:

$$
0100010-0001010
$$

Solution:

$$
\begin{aligned}
& \left.\right) \\
& 0 \quad 0 \quad 1 \quad 1 \quad 0 \quad 0 \quad 0 \quad=\quad 24_{10}
\end{aligned}
$$

Method 2: Binary subtraction converting denary numbers to binary numbers


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The additional ninth bit is simply ignored leaving the binary number 00011011 (denary equivalent of 27, which is the correct result of the subtraction).

## Overflow :-

A CPU with a capacity of 8 bits has a capacity of up to 11111111 in binary. If one more bit was added there would be an overflow error.

## Example: 8-bit overflow:

An example of an 8-bit overflow occurs in the binary sum $11111111+1$ (denary: $255+1$ ).

$$
\begin{array}{r}
11111111 \\
+\quad \begin{array}{r}
0001001 \\
\hline 100000000
\end{array}
\end{array}
$$

The total is a number bigger than 8 digits, and when this happens the CPU drops the overflow digit because the computer cannot store it anywhere, and the computer thinks $255+\mathbf{1}=\mathbf{0}$.


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Overflow errors happen when the largest number that a register can hold is exceeded. The number of bits that it can handle is called the word size.

Most CPUs use a much bigger word size than 8 bits. Many PCs have a 64 -bit CPU. A 64-bit CPU can handle numbers larger than 18 quintillion (18,446,744,073,709,551,615 to be precise).

## Hexadecimal Number System:

We often have to deal with large positive binary numbers. For instance, consider that computers connect to the Internet using a Network Interface Card (NIC). Every NIC in the world is assigned a unique 48-bit identifier as an Ethernet address. The intent is that no two NICs in the world will have the same address.

A sample Ethernet address might be:

## 000000000100011101011110011111111001001000110110

Fortunately, large binary numbers can be made much more compactand hence easier to work with.
©
You may wonder: Binary numbers would also be more compact if represented in base-10—why not just convert them to decimal?
© The answer, as you will soon see, is that converting between binary and hexadecimal is exceedingly easy.

## The Hexadecimal Number System

$(0,1,2,3,4,5,6,7,8,9, A, B, C, D, E, F)_{16}$
The base 16 hexadecimal has 16 digits. Note that the single hexadecimal symbol $A=10, B=11$, $C=12, D=13, E=14$ and $F=15$.

Just as with decimal notation or binary notation, we again write a number as a string of symbols, but now each symbol is one of the 16 possible hexadecimal digits ( 0 through F). To interpret a hexadecimal number, we multiply each digit by the power of 16 associated with that digit's position.

## Hexadecimal Place value:

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| 1048576 | 65536 | 4096 | 256 | 16 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $(165)$ | $(164)$ | $\left(16^{3}\right)$ | $\left(16^{2}\right)$ | $(161)$ | $(160)$ |

-H denotes hex prefix.
For example, consider the hexadecimal number 1 A 9 B.
Examples:

$$
\begin{aligned}
1 \text { A } 9 B_{16} & =1 A 9 B_{H} \\
& =1 \times 16^{3}+10 \times 16^{2}+9 \times 16^{1}+11 \times 16^{0} \\
& =4096+2560+144+11=6811_{10}
\end{aligned}
$$

(i) $2 \mathrm{~F} 16=2 \mathrm{~F}_{\mathrm{H}}=2 \times 16+15 \times 1=47$
(ii) $\quad \mathrm{BC} 1216=\mathrm{BC} 12_{\mathrm{H}}=11 \times 16^{3}+12 \times 16^{2}+1 \times 16^{1}+2 \times 16^{0}=48146$

## Hexadecimal Numbers in Computing

There are two ways in which hex makes life easier.
© The first is that it can be used to write down very large integers in a compact form.
© For example, ( A D 4 5) ${ }_{16}$ is shorter than its decimal equivalent (44357) 10 and as values increase the difference in length becomes even more pronounced.

## Converting Binary Numbers to Hexadecimal Numbers.

Let's assume we have a binary number of: 01010111
The binary number is 01010111
We will break number into 4 bits each as 01010111

Then we will start with the right side 4 bits
Starting from extreme right number
for 0101
for 0111
$0 \times 2^{3}+1 \times 2^{2}+0 \times 2^{1}+1 \times 2^{0}$
$0 \times 2^{3}+1 \times 2^{2}+1 \times 2^{1}+1 \times 2{ }^{0}$
$0 \times 8+1 \times 4+0 \times 2+1 \times 1$
$0+4+0+1=5$

5
$0 \times 8+1 \times 4+1 \times 2+1 \times 1$
$0+4+2+1=7$

7

So Hexadecimal number is 57

## Converting Hexadecimal Numbers to Binary Numbers

To convert a hexadecimal number to a binary number, we reverse the above procedure. We separate every digit of hexadecimal number and find its equivalent binary number and then we write it together.

## Example 1:

To convert the hexadecimal number 9F216 to binary, each hex digit is converted into binary form.

$$
\begin{aligned}
& 9 \text { F } 216=\left(\begin{array}{ll}
(10011110010
\end{array}\right)_{2} \\
& 9=1001 \quad F=1111 \quad 2=0010
\end{aligned}
$$

So Binary equivalent of Hexadecimal number is: 9F2=100111110010
Work on the given question below :
Convert hexadecimal 2BF9 to its binary equivalent.
Convert binary 110011100001 to its hexadecimal equivalent.

## Converting a Hexadecimal Number to a (Denary) Decimal Number

To convert a hexadecimal number to a decimal number, write the hexadecimal number as a sum of powers of 16. For example, considering the hexadecimal number 1A9B above, we convert this to decimal as:

| $\mathbf{1}$ | $\mathbf{A}$ | $\mathbf{9}$ | $\mathbf{B}$ |
| :---: | :---: | :---: | :---: |
| $16^{3}$ | $16^{2}$ | $16^{1}$ | $16^{0}$ |

$$
\begin{aligned}
1 A 9 B & =1\left(16^{3}\right)+A\left(16^{2}\right)+9\left(16^{1}\right)+B\left(16^{0}\right) \\
& =4096+10(256)+9(16)+11(1)=6811
\end{aligned}
$$

So 1A9B $_{16}=6811_{10}$
Converting a (Denary) Decimal Number into Hexadecimal Number

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The easiest way to convert from decimal to hexadecimal is to use the same division algorithm that you used to convert from decimal to binary, but repeatedly dividing by 16 instead of by 2 . As before, we keep track of the remainders.

For example, to convert the decimal number $\mathbf{7 4 6}$ to hexadecimal, we proceed as follows:

## Remainder

16| 746

| $\mid 46$ | $-10=$ | $A$ |
| :--- | ---: | :--- |
| 12 | $14=$ | $E$ |
| 10 |  | 2 |$|$

We read the number as last is first and first is last. The denary $746=2 \mathrm{EA}$ in hexadecimal

## BCD Binary Coded Decimals:

In computing and electronic systems, binary-coded decimal (BCD) is a class of binary encodings of decimal numbers where each decimal digit is represented by a fixed number of bits, usually four or eight. Special bit patterns are sometimes used for a sign or for other indications (e.g., error or overflow).
$0000=0$
$0101=5$
0001 = 1
$0110=6$
$0010=2$
$0111=7$
0011 = 3
$1000=8$
$0100=4$
$1001=9$

BCD was used in many early decimal computers, and is implemented in the instruction set of machines such as the IBM System/360 series and its descendants
and Digital's VAX. Although BCD per se is not as widely used as in the past and is no longer implemented in computers' instruction sets dubious discuss] , decimal fixed-point and floating-point formats are still important and continue to be used in financial, commercial, and industrial computing

As most computers deal with data in 8-bit bytes, it is possible to use one of the following methods to encode a BCD number:

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Unpacked: each numeral is encoded into one byte, with four bits representing the numeral and the remaining bits having no significance.

Packed: two numerals are encoded into a single byte, with one numeral in the least significant nibble (bits 0 through 3 ) and the other numeral in the most significant nibble

The Denary number 8503 could be represented by one BCD digit per byte

000010000000010100000000000000011 (Unpacked)Denary
Number $8 \quad 5 \quad 0 \quad 3$ represented by One BCD per nibble
1000010100000011 (Packed)
e.g. 398602 in BCD

Answer: $3=00119=10018=10006=01100=00002=0010$ So
$398602=001110011000011000000010$ (in BCD)
Method 1: four single bytes

| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 |
| 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 |

5

## Method 2: two bytes

| 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 1 | 0 | 0 | 1 | 0 | 1 |

31
65

Note: All the zeros are essential otherwise you can't read it back.

But do not get confused, binary coded decimal is not the same as hexadecimal. Whereas a 4-bit hexadecimal number is valid up to $\mathrm{F}_{16}$ representing binary 11112, (decimal 15), binary coded decimal numbers stop at 9 binary $1001_{2}$

## Uses of BCD:

There are a number of applications where BCD can be used.
© The obvious type of application is where denary digits are to be displayed, for instance on the screen of a calculator or in a digital time display.

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A somewhat unexpected application is for the representation of currency values. When a currency value is written in a format such as $\$ 300.25$ it is as a fixed-point decimal number (ignoring the dollar sign). It might be expected that such values would be stored as real numbers but this cannot be done accurately.

## ASCII code:

If text is to be stored in a computer it is necessary to have a coding scheme that provides a unique binary code for each distinct individual component item of the text.

Such a code is referred to as a character code.
The scheme which has been used for the longest time is the ASCII (American Standard Code for Information Interchange) coding scheme.
[1] This is an internationally agreed standard. There are some variations on ASCII coding schemes but the major one is the 7-bit code. It is customary to present the codes in a table for which a number of different designs have been used.
© The full table shows the 27 (128) different codes available for a 7-bit code. You should not try to remember any of the individual codes but there are certain aspects of the coding scheme which you need to understand.
© Computers store text documents, both on disk and in memory, using ASCII codes. For example, if you use Notepad in Windows OS to create a text file containing the words, "Four score and seven years ago," Notepad would use 1 byte of memory per character (including 1 byte for each space character between the words
[1] It is worth emphasizing here that these codes for numbers are exclusively for use in the context of stored, displayed or printed text.
© All of the other coding schemes for numbers are for internal use in a computer system and would not be used in a text.

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e] There are some special features that make the coding scheme easy to use in certain circumstances.

- The first is that the codes for numbers and for letters are in sequence in each case so that, for example,
- if 1 is added to the code for seven the code for eight is produced.
- The second is that the codes for the upper-case letters differ from the codes for the corresponding lower-case letters only in the value of bit 6.
- This makes conversion of upper case to lower case, or the reverse, a simple operation.

| Dec | Hex | Char | Dec | Hex | Char | Dec | Hex | Char |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 32 | 20 | <SPACE> | 64 | 40 | @ | 96 | 60 | - |
| 33 | 21 | ! | 65 | 41 | A | 97 | 61 | a |
| 34 | 22 | " | 66 | 42 | B | 98 | 62 | b |
| 35 | 23 | \# | 67 | 43 | C | 99 | 63 | c |
| 36 | 24 | \$ | 68 | 44 | D | 100 | 64 | d |
| 37 | 25 | \% | 69 | 45 | E | 101 | 65 | e |
| 38 | 26 | \& | 70 | 46 | F | 102 | 66 | f |
| 39 | 27 | , | 71 | 47 | G | 103 | 67 | g |
| 40 | 28 | ( | 72 | 48 | H | 104 | 68 | h |
| 41 | 29 | ) | 73 | 49 | I | 105 | 69 | i |
| 42 | 2A | * | 74 | 4A | J | 106 | 6A | j |
| 43 | 2B | + | 75 | 4B | K | 107 | 6B | k |
| 44 | 2C | , | 76 | 4C | L | 108 | 6C | l |
| 45 | 2D | - | 77 | 4D | M | 109 | 6D | m |
| 46 | 2 E | . | 78 | 4 E | N | 110 | 6E | n |
| 47 | 2 F | / | 79 | 4F | 0 | 111 | 6F | 0 |

Notice the storage of characters with uppercase and lowercase. For example:

| a | 1 | 1 | 0 | 0 | 0 | 0 | 1 | hex 61 (lower case) |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| A | 1 | 0 | 0 | 0 | 0 | 0 | 1 | hex 41 (upper case) |
| y | 1 | 1 | 1 | 1 | 0 | 0 | 1 | hex 79 (lower case) |
| Y | 1 | 0 | 1 | 1 | 0 | 0 | 1 | hex 59 (uppercase) |

## Unicode:

Despite still being widely used, the ASCII codes are far from adequate for many purposes.

Unicode is an international encoding standard for use with different languages and scripts.

## (PI) 1.1 Data Representation

It works by providing a unique number for every character, this creates a consistent encoding, representation, and handling of text.

Basically Unicode is like a Universal Alphabet that covers the majority of different languages across the world, it transforms characters into numbers.

It achieves this by using character encoding, which is to assign a number to every character that can be used.

## What's an example of a Unicode?

Unicode has its own special terminology. For example, a character code is referred to as a 'code point'.

In any documentation there is a special way of identifying a code point. An example is U+0041 which is the code point corresponding to the alphabetic character A.

The 0041 are hexadecimal characters representing two bytes. The interesting point is that in a text where the coding has been identified as Unicode it is only necessary to use a one-byte representation for the 128 codes corresponding to ASCII. To ensure such a code cannot be misinterpreted, the codes where more than one byte is needed have restrictions applied.

| FE8D | $\lfloor$ <br> FE8E | $\tilde{1}$ <br> FE81 | $L$ <br> FE82 |
| :---: | :---: | :---: | :---: |
| $\pm$ FE8F | $\underset{\text { FE91 }}{\boldsymbol{\rightharpoonup}}$ | $\stackrel{+}{+}$ | $\underbrace{\text { + }}_{\text {FE90 }}$ |
| $\underbrace{+}_{\text {FB56 }}$ | $\underset{\mathrm{Fb} 58}{\stackrel{\rightharpoonup}{7}}$ | $\underset{\text { FB59 }}{\stackrel{1}{*}}$ | $\underset{\text { FB57 }}{4}$ |


|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Đ | ð |  | t t | + |  | š |  |  |  |  | b b | b | Ż |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | 1/2 | 1/4 |  | 3/4 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | ! |  |  | \$ | \$ |  | \& |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 2 |  | 34 | 4 |  | 6 | 7 | 8 | 9 |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| @ | A | B |  | C D | D E |  | F | G | H |  |  |  |  |  |  |
| P | Q | R |  | T | T U | U | V | W | X ${ }^{0050}$ | Y Z |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | a | b |  | d | d |  |  | g | h |  |  |  |  |  |  |
|  | $\mathrm{q}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Ä | A | C |  | É Ṅ | N Ö |  | Ü | á | à |  |  |  |  |  |  |
| $\hat{\mathrm{e}}$ | éf |  |  |  |  |  | ñ | ód |  |  | ö õ |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\dagger$ |  | ¢ |  | £ § | § |  | 1 | B | - | (c) ${ }^{\text {T}}$ | тм |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | $\leq$ |  | \# | * |  | $\partial$ | $\Sigma$ | П | $\pi$ J | $\int^{\text {a }}$ |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

At its core, Unicode is like ASCII: a list of characters that people want to type into a computer. Every character gets a numeric codepoint, whether it's capital A, lowercase or lambda.

$$
\begin{aligned}
& A=65 \\
& \lambda=923
\end{aligned}
$$

So Unicode says things like, -Allright, this character exists, we assigned it an official name and a codepoint, here are its lowercase or uppercase equivalents (if any), and here's a picture of what it could look like. Font designers, it's up to you to draw this in your font if you want to.

Just like ASCII, Unicode strings (imagine -codepoint 121, codepoint 111...II) have to be encoded to ones and zeros before you can store or transmit them. But unlike ASCII, Unicode has more than a million possible codepoints, so they can't possibly all fit in one byte. And unlike ASCII, there's no One True Way to encode it.

## (PI) 1.1 Data Representation

What can we do? One idea would be to always use, say, 3 bytes per character. That would be nice for string traversal, because the 3rd codepoint in a string would always start at the 9th byte. But it would be inefficient when it comes to storage space and bandwidth.Instead, the most common solution is an encoding called UTF-8.

## UTF-8 :

UTF-8 gives you four templates to choose from: a one-byte template, a two-byte template, a three-byte template, and a four-byte template.

## 0xxxxxxx

## 110xxxxx 10xxxxxx

## 1110xxxx 10xxxxxx 10xxxxxx

## 11110xxx 10xxxxxx 10xxxxxx 10xxxxxx

Each of those templates has some headers which are always the same (shown here in red) and some slots where your code point data can go (shown here as black).

The four-byte template gives us 21 bits for our data, which would let us represent 2,097,151 different values. There are only about 128,000 codepoints right now, so UTF-8 can easily encode any Unicode codepoint for the foreseeable future.Unicode to represent any possible text in code form.

Unicode is a computing industry standard for the consistent encoding, representation, and handling of text expressed in most of the world's writing systems.

Developed in conjunction with the Universal Coded Character Set (UCS) standard and published as The Unicode Standard, the latest version of Unicode contains a repertoire of more than 128,000 characters covering 135 modern and historic scripts, as well as multiple symbol sets..

As of June 2016, the most recent version is Unicode 9.0. The standard is maintained by the Unicode Consortium.

Unicode's success at unifying character sets has led to its widespread and predominant use in the internationalization and localization of computer software. The standard has been implemented in many recent technologies, including modern operating systems, XML, Java (and other programming languages), and the .NET Framework

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