

Angles, Linesand Triangles

Exercise 4A

Question 1:

- (i) Angle: Two rays having a common end point form an angle.
- (ii) Interior of an angle: The interior of \angle AOB is the set of all points in its plane, which lie on the same side of OA as B and also on same side of OB as A.
- (iii) Obtuse angle: An angle whose measure is more than 90° but less than 180°, is called an obtuse angle.
- (iv) Reflex angle: An angle whose measure is more than 180° but less than 360° is called a reflex angle.
- (v) Complementary angles: Two angles are said to be complementary, if the sum of their measures is 90o.
- (vi) Supplementary angles: Two angles are said to be supplementary, if the sum of their measures is 180° .

Question 2:

∠A =
$$36^{\circ} 27' 46''$$
 and ∠B = $28^{\circ} 43' 39''$
∴ Their sum = $(36^{\circ} 27' 46'') + (28^{\circ} 43' 39'')$
Deg Min Sec
 $36^{\circ} 27' 46''$
 $+ 28^{\circ} 43' 39''$ [1° = 60'; 1' = 60'']
 $65^{\circ} 11' 25''$

Therefore, the sum $\angle A + \angle B = 65^{\circ} 11' 25''$

Question 3:

Let
$$\angle A = 36^{\circ}$$
 and $\angle B = 24^{\circ} 28' 30''$
Their difference = $36^{\circ} - 24^{\circ} 28' 30''$

Thus the difference between two angles is $\angle A - \angle B = 11^{\circ} 31' 30''$

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Question 4:

- (i) Complement of $58^{\circ} = 90^{\circ} 58^{\circ} = 32^{\circ}$
- (ii) Complement of $16^{\circ} = 90 16^{\circ} = 74^{\circ}$
- (iii) $\frac{2}{3}$ of a right angle = $\frac{2}{3} \times 90^{\circ} = 60^{\circ}$

Complement of $60^{\circ} = 90^{\circ} - 60^{\circ} = 30^{\circ}$

(iv)
$$1^{\circ} = 60'$$

Deg	Min
89°	60'
90°	9 '
- 46°	30'
43°	30'

Complement of 46° 30′ = 90° - 46° 30′ = 43° 30′

$$(v) 90^\circ = 89^\circ 59' 60''$$

Deg	Min	Sec
89°	59'	60'
90°	9,	g"
– 52°	43'	20′′
37°	16′	40"

Complement of 52° 43′ 20″ = 90° - 52° 43′ 20″

(vi)
$$90^\circ = 89^\circ 59' 60''$$

Deg 89°	Min 59'	Sec 60''
- 68°	32,	45"
21°	24'	15"

- ∴ Complement of (68° 35′ 45″)
- $= 90^{\circ} (68^{\circ} 35' 45'')$
- = 89° 59′ 60″ (68° 35′ 45″)
- = 21° 24′ 15″

Question 5:

- (i) Supplement of $63^{\circ} = 180^{\circ} 63^{\circ} = 117^{\circ}$
- (ii) Supplement of $138^{\circ} = 180^{\circ} 138^{\circ} = 42^{\circ}$
- (iii) $\frac{3}{5}$ of a right angle = $\frac{3}{5} \times 90^{\circ} = 54^{\circ}$
- : Supplement of $54^{\circ} = 180^{\circ} 54^{\circ} = 126^{\circ}$
- (iv) $1^{\circ} = 60'$
- ⇒ 180° = 179° 60′



	Deg 179°	Min 60'
_	180° 75°	مور 36'
	104°	24'

Supplement of 75° 36′ = 180° - 75° 36′ = 104° 24′

(v)
$$1^{\circ} = 60'$$
, $1' = 60''$

Supplement of 124° 20′ 40″ = 180° - 124° 20′ 40″

(vi)
$$1^\circ = 60'$$
, $1' = 60''$

- : Supplement of $108^{\circ} 48' 32'' = 180^{\circ} 108^{\circ} 48' 32''$
- = 71° 11′ 28″.

Question 6:

(i) Let the required angle be x^{o}

Then, its complement = $90^{\circ} - x^{\circ}$

- \therefore The measure of an angle which is equal to its complement is 45°.
- (ii) Let the required angle be xo

Then, its supplement = $180^{\circ} - x^{\circ}$

: The measure of an angle which is equal to its supplement is 90°.

Question 7:

Let the required angle be xo

Then its complement is $90^{\circ} - x^{\circ}$

$$\Rightarrow \qquad \qquad x^{\circ} = \left(90^{\circ} - x^{\circ}\right) + 36^{\circ}$$

$$\Rightarrow \qquad x^{\circ} + x^{\circ} = 90^{\circ} + 36^{\circ}$$

$$\Rightarrow \qquad 2x^{\circ} = 126^{\circ}$$

$$\Rightarrow \qquad \qquad x = \frac{126}{2} = 63$$

∴ The measure of an angle which is 36° more than its complement is 63°.

Question 8:

Let the required angle be x^o

Then its supplement is $180^{\circ} - x^{\circ}$

$$\Rightarrow \qquad \qquad x^{\circ} = \left(180^{\circ} - x^{\circ}\right) - 25^{\circ}$$

$$\Rightarrow \qquad x^{\circ} + x^{\circ} = 180^{\circ} - 25^{\circ}$$

$$\Rightarrow \qquad 2x = 155$$

$$\Rightarrow \qquad x = \frac{155}{2} = 77\frac{1}{2}$$



∴ The measure of an angle which is 25° less than its supplement is

Question 9:

Let the required angle be xo

Then, its complement = $90^{\circ} - x^{\circ}$

$$\Rightarrow \qquad \qquad x^{\circ} = 4 \Big(90^{\circ} - x^{\circ} \Big)$$

$$\Rightarrow \qquad x^0 = 360^0 - 4x^0$$

$$\Rightarrow \qquad 5x = 360$$

$$\Rightarrow \qquad \qquad X = \frac{360}{5} = 72$$

∴ The required angle is 72°.

Question 10:

Let the required angle be xo

Then, its supplement is $180^{\circ} - x^{\circ}$

$$\Rightarrow \qquad \qquad x^{\circ} = 5 \Big(180^{\circ} - x^{\circ} \Big)$$

$$\Rightarrow \qquad \qquad x^{\circ} = 900^{\circ} - 5x^{\circ}$$

$$\Rightarrow \qquad \qquad x + 5x = 900$$

$$\Rightarrow \qquad \qquad 6x = 900$$

$$\begin{array}{ccccc}
\Rightarrow & & & & & & & \\
x^0 & = 5\left(180^\circ - x^\circ\right) \\
\Rightarrow & & & & & \\
x^0 & = 900^\circ - 5x^\circ \\
\Rightarrow & & & & & \\
x + 5x & = 900 \\
\Rightarrow & & & & \\
6x & = 900 \\
\Rightarrow & & & & \\
x & = \frac{900}{6} = 150.
\end{array}$$

∴ The required angle is 150°.

Question 11:

Let the required angle be xo

Then, its complement is 90° – x° and its supplement is 180° –

That is we have,

$$3x = 180$$

 $x = \frac{180}{3} = 60^{\circ}$

∴ The required angle is 60°.

Question 12:

Let the required angle be xo

Then, its complement is 90° – x° and its supplement is 180° – x°

$$90^{\circ} - x^{\circ} = \frac{1}{3} \left(180^{\circ} - x^{\circ} \right)$$

$$90 - x = 60 - \frac{1}{3} \times x$$

$$4x + \frac{1}{3} \times x = 90 - 60$$

$$2x + \frac{1}{3} \times x = 30$$

$$8x + \frac{30 \times 3}{2} = 45$$

$$\Rightarrow \qquad 90 - x = 60 - \frac{1}{3}x$$

$$\Rightarrow \qquad \qquad \times -\frac{1}{2} \times = 90 - 60$$

$$\Rightarrow \frac{2}{3}x = 30$$

$$\times = \frac{30 \times 3}{2} = 48$$

∴ The required angle is 45°.

Question 13:

Let the two required angles be xo and 180o - xo.

$$\frac{x^0}{180^0 - x^0} = \frac{3}{2}$$

$$\Rightarrow$$
 2x = 3(180 - x)

$$\Rightarrow$$
 2x = 540 - 3x

$$\Rightarrow$$
 3x + 2x = 540

$$\Rightarrow 5x = 540$$

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 \Rightarrow x = 108

Thus, the required angles are 108° and 180° – x° = 180° – 108° = 72° .

Question 14:

Let the two required angles be x^0 and $90^0 - x^0$.

Then

$$\frac{x^{\circ}}{90^{\circ}-x^{\circ}}=\frac{4}{5}$$

$$\Rightarrow$$
 5x = 4(90 - x)

$$\Rightarrow 5x = 360 - 4x$$

$$\Rightarrow 5x + 4x = 360$$

$$\Rightarrow$$
 9x = 360

$$\Rightarrow x = \frac{360}{9} = 40$$

Thus, the required angles are 40° and 90° – x° = 90° – 40° = 50° .

Question 15:

Let the required angle be xo.

Then, its complementary and supplementary angles are $(90^{\circ} - x)$ and $(180^{\circ} - x)$ respectively.

Then, $7(90^{\circ} - x) = 3(180^{\circ} - x) - 10^{\circ}$

$$\Rightarrow$$
 630° - 7x = 540° - 3x - 10°

$$\Rightarrow$$
 7x - 3x = 630° - 530°

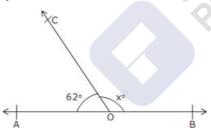
$$\Rightarrow$$
 4x = 100°

$$\Rightarrow$$
 x = 25°

Thus, the required angle is 25°.

Exercise 4B

Question 1:



Since ∠BOC and ∠COA form a linear pair of angles, we have

$$\Rightarrow$$
 $x^0 + 62^0 = 180^0$

$$\Rightarrow$$
 x = 180 - 62

∴
$$x = 118^{\circ}$$

Question 2:

Since, ∠BOD and ∠DOA form a linear pair.

$$\therefore$$
 ZBOD + **Z**DOC + **Z**COA = 180°

$$\Rightarrow$$
 (x + 20)° + 55° + (3x - 5)° = 180°

$$\Rightarrow$$
 x + 20 + 55 + 3x - 5 = 180

$$\Rightarrow$$
 4x + 70 = 180

$$\Rightarrow$$
 4x = 180 - 70 = 110

$$\Rightarrow x = \frac{110}{4} = 27.5$$

$$\therefore$$
 ZAOC = $(3 \times 27.5 - 5)^{\circ} = 82.5 - 5 = 77.5^{\circ}$

And,
$$\angle BOD = (x + 20)^{\circ} = 27.5^{\circ} + 20^{\circ} = 47.5^{\circ}$$
.



Question 3:

Since ∠BOD and ∠DOA from a linear pair of angles.

$$\Rightarrow$$
 ZBOD + **Z**DOA = 180°

$$\Rightarrow$$
 ZBOD + **Z**DOC + **Z**COA = 180°

$$\Rightarrow$$
 x° + (2x - 19)° + (3x + 7)° = 180°

$$\Rightarrow$$
 6x = 180 + 12 = 192

$$\Rightarrow x = \frac{192}{6} = 32$$

⇒
$$\angle$$
AOC = $(3x + 7)^{\circ}$ = $(332 + 7)^{\circ}$ = 103°

⇒
$$\angle$$
COD = $(2x - 19)^{\circ}$ = $(232 - 19)^{\circ}$ = 45°

and **Z**BOD =
$$x^0 = 32^0$$

Question 4:

The sum of their ratios = 5 + 4 + 6 = 15

But
$$x + y + z = 180^{\circ}$$

[Since, XOY is a straight line]

So, if the total sum of the measures is 15, then the measure of x is 5.

If the sum of angles is 180° , then, measure of $x = \frac{3}{15} \times 180 = 60$

And, if the total sum of the measures is 15, then the measure of y is 4.

If the sum of the angles is 180° , then, measure of $y = \overline{15} \times 180 = 48$

And
$$\angle z = 180^{\circ} - \angle x - \angle y$$

$$= 180^{\circ} - 108^{\circ} = 72^{\circ}$$

$$\therefore$$
 x = 60, y = 48 and z = 72.

Question 5:

AOB will be a straight line, if two adjacent angles form a linear pair.

$$\Rightarrow$$
 $(4x - 36)^{\circ} + (3x + 20)^{\circ} = 180^{\circ}$

$$\Rightarrow$$
 4x - 36 + 3x + 20 = 180

$$\Rightarrow$$
 7x - 16 = 180°

$$\Rightarrow$$
 7x = 180 + 16 = 196

$$\Rightarrow x = \frac{196}{7} = 28$$

∴ The value of x = 28.

Question 6:

Since **Z**AOC and **Z**AOD form a linear pair.

∠AOD and ∠BOC are vertically opposite angles.

∠BOD and ∠AOC are vertically opposite angles.

Question 7:

ave, Millione ain a service and a service an Since ∠COE and ∠DOF are vertically opposite angles, we have,



 \Rightarrow \angle z = 50°

Also ∠BOD and ∠COA are vertically opposite angles.

So, **Z**BOD = **Z**COA

 \Rightarrow \angle t = 90°

As **Z**COA and **Z**AOD form a linear pair,

∠COA + ∠AOD = 180°

$$\Rightarrow$$
 \angle COA + \angle AOF + \angle FOD = 180° [\angle t = 90°]

$$\Rightarrow$$
 t + x + 50° = 180°

$$\Rightarrow$$
 90° + x° + 50° = 180°

Since ∠EOB and ∠AOF are vertically opposite angles

$$\Rightarrow$$
 y = x = 40

Thus,
$$x = 40 = y = 40$$
, $z = 50$ and $t = 90$

Question 8:

Since ∠COE and ∠EOD form a linear pair of angles.

$$\Rightarrow$$
 5x + \angle EOA + 2x = 180

$$\Rightarrow$$
 5x + \angle BOF + 2x = 180

[∴ ∠EOA and BOF are vertically opposite angles so, ∠EOA = ∠BOF]

$$\Rightarrow$$
 5x + 3x + 2x = 180

$$\Rightarrow 10x = 180$$

Now
$$\angle AOD = 2x^0 = 2 \times 18^0 = 36^0$$

$$\angle$$
COE = $5x^{0} = 5 \times 18^{0} = 90^{0}$

and,
$$\angle EOA = \angle BOF = 3x^{0} = 3 \times 18^{0} = 54^{0}$$

Question 9:

Let the two adjacent angles be 5x and 4x.

Now, since these angles form a linear pair.

So,
$$5x + 4x = 180^{\circ}$$

$$\Rightarrow$$
 9x = 180°

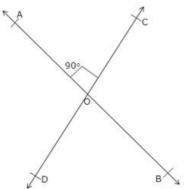
$$\Rightarrow x = \frac{180}{9} = 20$$

 \therefore The required angles are $5x = 5x = 520^{\circ} = 100^{\circ}$

and
$$4x = 4 \times 20^{\circ} = 80^{\circ}$$

Question 10:

Let two straight lines AB and CD intersect at O and let ∠AOC = 90°.



Now, $\angle AOC = \angle BOD$ [Vertically opposite angles]

AOC = 90°.

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⇒ **∠**BOD = 90°

Also, as ∠AOC and ∠AOD form a linear pair.

⇒ 90° + ∠AOD = 180°

 \Rightarrow **Z**AOD = $180^{\circ} - 90^{\circ} = 90^{\circ}$

Since, $\angle BOC = \angle AOD$ [Vertically opposite angles]

⇒ **∠**BOC = 90°

Thus, each of the remaining angles is 90°.

Question 11:

Since, ∠AOD and ∠BOC are vertically opposite angles.

∴ ∠AOD = ∠BOC

Now, ∠AOD + ∠BOC = 280° [Given]

 \Rightarrow \angle AOD + \angle AOD = 280°

⇒ 2**∠**AOD = 280°

 \Rightarrow \angle AOD = $\frac{280}{2}$ = 140°

⇒ ∠BOC = ∠AOD = 140°

As, **Z**AOC and **Z**AOD form a linear pair.

So, $\angle AOC + \angle AOD = 180^{\circ}$

⇒∠AOC + 140° = 180°

⇒ ∠AOC = 180° - 140° = 40°

Since, **Z**AOC and **Z**BOD are vertically opposite angles.

 \therefore **Z**AOC = **Z**BOD

⇒ **∠**BOD = 40°

 \therefore **Z**BOC = 140°, **Z**AOC = 40°, **Z**AOD = 140° and **Z**BOD = 40°

Question 12:

Since ∠COB and ∠BOD form a linear pair

So, \angle COB + \angle BOD = 180°

⇒ ∠BOD = 180° - ∠COB (1)

Also, as **Z**COA and **Z**AOD form a linear pair.

So, **Z**COA + **Z**AOD = 180°

⇒ ∠AOD = 180° - ∠COA

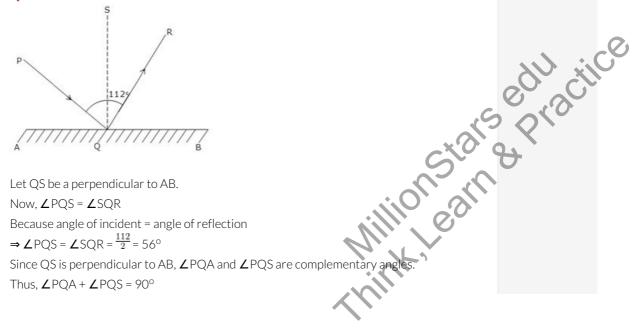
⇒ ∠AOD = 180° - ∠COB (2)

[Since, OC is the bisector of \angle AOB, \angle BOC = \angle AOC]

From (1) and (2), we get,

 \angle AOD = \angle BOD (Proved)

Question 13:

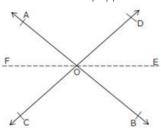




 \Rightarrow **Z**PQA = 90° - 56° = 34°

Question 14:

Given : AB and CD are two lines which are intersecting at O. OE is a ray bisecting the \angle BOD. OF is a ray opposite to ray OE.



To Prove: ∠AOF = ∠COF

Proof : Since \overrightarrow{OE} and \overrightarrow{OF} are two opposite rays, \overrightarrow{EF} is a straight line passing through O.

∴∠AOF = ∠BOE

and ∠COF = ∠DOE

[Vertically opposite angles]

But ∠BOE = ∠DOE (Given)

∴ ∠AOF = ∠COF

Hence, proved.

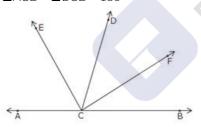
Question 15:

Given: \overrightarrow{CF} is the bisector of \angle BCD and \overrightarrow{CE} is the bisector of \angle ACD.

To Prove: ∠ECF = 90°

Proof: Since ∠ACD and ∠BCD forms a linear pair.

∠ACD + ∠BCD = 180°



ZACE + ZECD + ZDCF + ZFCB = 180°

∠ECD + ∠ECD + ∠DCF + ∠DCF = 180°

because **Z**ACE = **Z**ECD

and **Z**DCF = **Z**FCB

 $2(\angle ECD) + 2(\angle CDF) = 180^{\circ}$

2(**∠**ECD + **∠**DCF) = 180°

 \angle ECD + \angle DCF = $\frac{180}{2}$ = 90°

∠ECF = 90° (Proved)

Exercise 4C

Question 1:

Since AB and CD are given to be parallel lines and t is a transversal.

So, $\angle 5 = \angle 1 = 70^{\circ}$ [Corresponding angles are equal]

 $\angle 3 = \angle 1 = 70^{\circ}$ [Vertically opp. Angles]

 $\angle 3 + \angle 6 = 180^{\circ}$ [Co-interior angles on same side]

 \therefore **Z**6 = 180° - **Z**3

= 180° - 70° = 110°

versal.



∠6 = ∠8 [Vertically opp. Angles]

⇒∠8 = 110°

 \Rightarrow $\angle 4 + \angle 5 = 180^{\circ}$ [Co-interior angles on same side]

 $\angle 4 = 180^{\circ} - 70^{\circ} = 110^{\circ}$

 $\angle 2 = \angle 4 = 110^{\circ}$ [Vertically opposite angles]

 $\angle 5 = \angle 7$ [Vertically opposite angles]

So, $\angle 7 = 70^{\circ}$

 \therefore **\(\Lambda\)** 2 = 110°, **\(\Lambda\)** 3 = 70°, **\(\Lambda\)** 4 = 110°, **\(\Lambda\)** 5 = 70°, **\(\Lambda\)** 6 = 110°, **\(\Lambda\)** 7 = 70° and **\(\Lambda\)** 8 = 110°.

Question 2:

Since $\angle 2 : \angle 1 = 5 : 4$.

Let $\angle 2$ and $\angle 1$ be 5x and 4x respectively.

Now, $\angle 2 + \angle 1 = 180^{\circ}$, because $\angle 2$ and $\angle 1$ form a linear pair.

So, $5x + 4x = 180^{\circ}$

 \Rightarrow 9x = 180°

 \Rightarrow x = 20°

 \therefore **\(1** = 4x = 4 \times 20^{\tilde{0}} = 80^{\tilde{0}}

And $\angle 2 = 5x = 5 \times 20^{\circ} = 100^{\circ}$

 $\angle 3 = \angle 1 = 80^{\circ}$ [Vertically opposite angles]

And $\angle 4 = \angle 2 = 100^{\circ}$ [Vertically opposite angles]

 $\angle 1 = \angle 5$ and $\angle 2 = \angle 6$ [Corresponding angles]

So, $\angle 5 = 80^{\circ}$ and $\angle 6 = 100^{\circ}$

 $\angle 8 = \angle 6 = 100^{\circ}$ [Vertically opposite angles]

And $\angle 7 = \angle 5 = 80^{\circ}$ [Vertically opposite angles]

Thus, $\angle 1 = 80^{\circ}$, $\angle 2 = 100^{\circ}$, $\angle 3 = \angle 80^{\circ}$, $\angle 4 = 100^{\circ}$, $\angle 5 = 80^{\circ}$, $\angle 6 = 100^{\circ}$, $\angle 7 = 80^{\circ}$ and

∠8 = 100°.

Question 3:

Given: AB | CD and AD | BC

To Prove: ∠ADC = ∠ABC

Proof: Since AB | CD and AD is a transversal. So sum of consecutive interior angles is

180°.

⇒ ∠BAD + ∠ADC = 180°(i)

Also, AD || BC and AB is transversal.

So, **Z**BAD + **Z**ABC = 180°(ii)

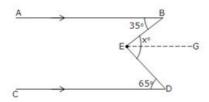
From (i) and (ii) we get:

ZBAD + ZADC = ZBAD + ZABC

⇒ ∠ADC = ∠ABC (Proved)

Question 4:

(i) Through E draw EG || CD. Now since EG||CD and ED is a transversal.



So, \angle GED = \angle EDC = 65° [Alternate interior angles]

Since EG || CD and AB || CD,

 $\mathsf{EG}||\mathsf{AB} \ \mathsf{and} \ \mathsf{EB} \ \mathsf{is} \ \mathsf{transversal}.$

So, \angle BEG = \angle ABE = 35° [Alternate interior angles]

So, $\angle DEB = x^0$

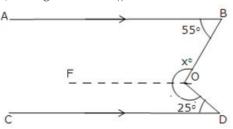




⇒ \angle BEG + \angle GED = 35° + 65° = 100°.

Hence, x = 100.

(ii) Through O draw OF||CD.



Now since OF || CD and OD is transversal.

ZCDO + **Z**FOD = 180°

[sum of consecutive interior angles is 180°]

$$\Rightarrow$$
 ZFOD = 180° - 25° = 155°

As OF || CD and AB || CD [Given]

Thus, OF || AB and OB is a transversal.

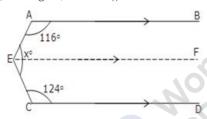
So, \angle ABO + \angle FOB = 180° [sum of consecutive interior angles is 180°]

$$\Rightarrow$$
 ZFOB = 180° - 55° = 125°

Now,
$$x^0 = \angle FOB + \angle FOD = 125^0 + 155^0 = 280^\circ$$
.

Hence, x = 280.

(iii) Through E, draw EF || CD.



Now since EF || CD and EC is transversal.

[sum of consecutive interior angles is 180°]

$$\Rightarrow$$
 ZFEC = $180^{\circ} - 124^{\circ} = 56^{\circ}$

Since EF || CD and AB || CD

So, EF | AB and AE is a trasveral.

[sum of consecutive interior angles is 180°]

Thus
$$x^0 = /FFA + /FFC$$

$$= 64^{\circ} + 56^{\circ} = 120^{\circ}$$
.

So,
$$\angle$$
ABC = \angle BCD [atternate interior angles

$$\Rightarrow$$
 70° = x° + \angle FCD (i)

$$\Rightarrow$$
 ∠ECD = 180° - 130° = 50°



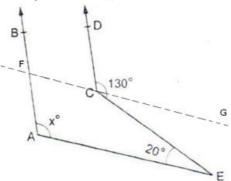
Putting ∠ECD = 50° in (i) we get,

 $70^{\circ} = x^{\circ} + 50^{\circ}$

 \Rightarrow x = 70 - 50 = 20

Question 6:

Through C draw FG || AE



Now, since CG || BE and CE is a transversal.

So, \angle GCE = \angle CEA = 20° [Alternate angles]

∴∠DCG = 130° - ∠GCE

 $= 130^{\circ} - 20^{\circ} = 110^{\circ}$

Also, we have AB || CD and FG is a transversal.

So, \angle BFC = \angle DCG = 110° [Corresponding angles]

As, FG | AE, AF is a transversal.

∠BFG = ∠FAE

[Corresponding angles]

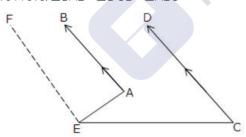
 $\therefore x^{\circ} = \angle FAE = 110^{\circ}$.

Hence, x = 110

Question 7:

Given: AB || CD

To Prove: ∠BAE - ∠DCE = ∠AEC



Construction: Through Edraw EF | AB

Proof: Since EF | AB, AE is a transversal.

So, ∠BAE + ∠AEF = 180^O(i)

[sum of consecutive interior angles is 180°]

As EF || AB and AB || CD [Given]

So, EF || CD and EC is a transversal.

So, ∠FEC + ∠DCE = 180°(ii)

[sum of consecutive interior angles is 180°]

From (i) and (ii) we get,

∠BAE + ∠AEF = ∠FEC + ∠DCE

 \Rightarrow \angle BAE - \angle DCE = \angle FEC - \angle AEF = \angle AEC [Proved]

Question 8:

Since AB || CD and BC is a transversal.

So, \angle BCD = \angle ABC = x° [Alternate angles]

As BC || ED and CD is a transversal.





∠BCD + ∠EDC = 180°

⇒ ∠BCD + 75° = 180°

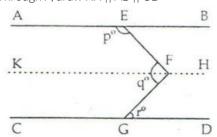
 \Rightarrow ∠BCD = 180° - 75° = 105°

 \angle ABC = 105° [since \angle BCD = \angle ABC] \therefore x° = \angle ABC = 105°

Hence, x = 105.

Question 9:

Through F, draw KH || AB || CD



Now, KF || CD and FG is a transversal.

$$\Rightarrow$$
 \angle KFG = \angle FGD = r° (i)

[alternate angles]

Again AE || KF, and EF is a transversal.

$$\angle$$
KFE = 180° - p° (ii)

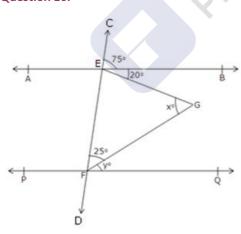
Adding (i) and (ii) we get,

$$\Rightarrow$$
 ZEFG = 180 - p + r

$$\Rightarrow$$
 q = 180 - p + r

i.e.,
$$p + q - r = 180$$

Question 10:



Since AB || PQ and EF is a transversal.

So, \angle CEB = \angle EFQ [Corresponding angles]

⇒ ∠EFQ = 75°

⇒ ∠EFG + ∠GFQ = 75°

 \Rightarrow 25° + y° = 75°

 \Rightarrow y = 75 - 25 = 50

Also, \angle BEF + \angle EFQ = 180° [sum of consecutive interior angles is 180°]

∠BEF = 180° - ∠EFQ

= 180° - 75°

∠BEF = 105°

∴ ∠FEG + ∠GEB = ∠BEF = 105°

⇒ \angle FEG = 105° - \angle GEB = 105° - 20° = 85°

gles is 180°]



In \triangle EFG we have,

$$x^{\circ} + 25^{\circ} + \angle FEG = 180^{\circ}$$

 $\Rightarrow x^{\circ} + 25^{\circ} + 85^{\circ} = 180^{\circ}$
 $\Rightarrow x^{\circ} + 110^{\circ} = 180^{\circ}$
 $\Rightarrow x^{\circ} = 180^{\circ} - 110^{\circ}$
 $\Rightarrow x^{\circ} = 70^{\circ}$

Hence, x = 70.

Question 11:

Since AB || CD and AC is a transversal.

So, \angle BAC + \angle ACD = 180° [sum of consecutive interior angles is 180°]

$$= 180^{\circ} - 75^{\circ} = 105^{\circ}$$

∠ECF = 105°

Now in ΔCEF.

$$\Rightarrow 105^{\circ} + x^{\circ} + 30^{\circ} = 180^{\circ}$$

$$\Rightarrow$$
 x = 180 - 30 - 105 = 45

Hence, x = 45.

Question 12:

Since AB || CD and PQ a transversal.

So, ∠PEF = ∠EGH [Corresponding angles]

⇒ **∠**EGH = 85°

∠EGH and ∠QGH form a linear pair.

⇒
$$\angle$$
QGH = 180° - 85° = 95°

Similarly, ∠GHQ + 115° = 180°

$$\Rightarrow$$
 ZGHQ = 180° - 115° = 65°

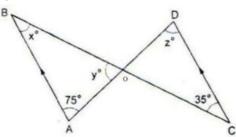
In Δ GHQ, we have,

$$x^{0} + 65^{0} + 95^{0} = 180^{0}$$

$$\Rightarrow$$
 x = 180 - 65 - 95 = 180 - 160

 $\therefore x = 20$

Question 13:



Since AB || CD and BC is a transversal.

$$\Rightarrow$$
 x = 35

Also, AB || CD and AD is a transversal.

$$\Rightarrow$$
 z = 75

In \triangle ABO, we have,

$$\Rightarrow$$
 $x^0 + 75^0 + y^0 = 180^0$

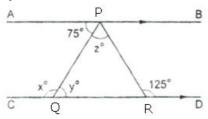
$$\Rightarrow$$
 35 + 75 + y = 180

$$\Rightarrow$$
 y = 180 - 110 = 70



 \therefore x = 35, y = 70 and z = 75.

Question 14:



Since AB | CD and PQ is a transversal.

So, y = 75

[Alternate angle]

Since PQ is a transversal and AB || CD, so x + APQ = 180°

[Sum of consecutive interior angles]

$$\Rightarrow$$
 $x^0 = 180^0 - APQ$

Also, AB | CD and PR is a transversal.

So, **Z**APR = **Z**PRD

[Alternate angle]

$$\Rightarrow$$
 \angle APQ + \angle QPR = \angle PRD [Since \angle APR = \angle APQ + \angle QPR]

$$\Rightarrow$$
 75° + z° = 125°

$$\Rightarrow$$
 z = 125 - 75 = 50

$$\therefore$$
 x = 105, y = 75 and z = 50.

Question 15:

 $\angle PRQ = x^0 = 60^\circ$ [vertically opposite angles]

Since EF | GH, and RQ is a transversal.

So,
$$\angle x = \angle y$$
 [Alternate angles]

AB | CD and PR is a transversal.

So,
$$\angle PRD = \angle APR$$
 [Alternate angles]

$$\Rightarrow$$
 \angle PRQ + \angle QRD = \angle APR [since \angle PRD = \angle PRQ + \angle QRD]

$$\Rightarrow x + \angle QRD = 110^{\circ}$$

$$\Rightarrow$$
 ∠QRD = 110° - 60° = 50°

In \triangle QRS, we have,

$$\angle QRD + t^{0} + y^{0} = 180^{0}$$

$$\Rightarrow$$
 50 + t + 60 = 180

Since, AB || CD and GH is a transversal

So, $z^{\circ} = t^{\circ} = 70^{\circ}$ [Alternate angles]

$$\therefore$$
 x = 60, y = 60, z = 70 and t = 70

Question 16:

(i) Lines I and m will be parallel if 3x - 20 = 2x + 10

[Since, if corresponding angles are equal, lines are parallel]

$$\Rightarrow$$
 3x - 2x = 10 + 20

(ii) Lines will be parallel if $(3x + 5)^{\circ} + 4x^{\circ} = 180^{\circ}$

[if sum of pairs of consecutive interior angles is 180°, the lines are parallel]

So,
$$(3x + 5) + 4x = 180$$

$$\Rightarrow$$
 3x + 5 + 4x = 180

$$\Rightarrow$$
 7x = 180 - 5 = 175

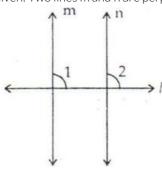
$$\Rightarrow$$
 x = $\frac{175}{7}$ = 25

s are parallel]



Question 17:

Given: Two lines m and n are perpendicular to a given line l.



To Prove: m || n

Proof: Since m ⊥ I

Again, since n ⊥ l

$$\therefore$$
 \(\) 1 = **\(\)** 2 = 90°

But $\angle 1$ and $\angle 2$ are the corresponding angles made by the transversal I with lines m and n and they are proved to be equal.

Thus, m || n.

Exercise 4D

Question 1:

Since, sum of the angles of a triangle is 180°

$$\Rightarrow$$
 $\angle A + 76^{\circ} + 48^{\circ} = 180^{\circ}$

$$\Rightarrow$$
 ZA = 180° - 124° = 56°

Question 2:

Let the measures of the angles of a triangle are $(2x)^{\circ}$, $(3x)^{\circ}$ and $(4x)^{\circ}$.

Then, 2x + 3x + 4x = 180 [sum of the angles of a triangle is 180°]

$$\Rightarrow$$
 9x = 180

$$\Rightarrow x = \frac{180}{9} = 20$$

∴ The measures of the required angles are:

$$2x = (2 \times 20)^{\circ} = 40^{\circ}$$

$$3x = (3 \times 20)^{\circ} = 60^{\circ}$$

$$4x = (4 \times 20)^{\circ} = 80^{\circ}$$

Question 3:

Let
$$3\angle A = 4\angle B = 6\angle C = x \text{ (say)}$$

Then,
$$3\angle A = x$$

$$\Rightarrow \angle A = \frac{x}{3}$$

$$\Rightarrow \angle B = \frac{x}{4}$$

and
$$6\angle C = x$$

$$\Rightarrow \angle C = \frac{x}{6}$$



$$\Rightarrow \frac{\frac{x}{3} + \frac{x}{4} + \frac{x}{6} = 180}{\Rightarrow \frac{4x + 3x + 2x}{12} = 180}$$

$$\Rightarrow \frac{9x = 180 \times 12}{\Rightarrow x = \frac{180 \times 12}{9} = 240$$

$$\therefore \angle^{A} = \frac{x}{3} = \frac{240}{3} = 80^{\circ}$$

$$\angle B = \frac{x}{4} = \frac{240}{4} = 60^{\circ}$$

$$\angle^{C} = \frac{\times}{6} = \frac{240}{6} = 40^{\circ}$$

Question 4:

But as ∠A, ∠B and ∠C are the angles of a triangle,

$$\Rightarrow$$
 C = 180° - 108° = 72°

Also,
$$\angle B + \angle C = 130^{\circ}$$
 [Given]

$$\Rightarrow$$
 ∠B + 72° = 130°

$$\Rightarrow$$
 ZB = 130° - 72° = 58°

$$\Rightarrow$$
 \angle A + 58° = 108°

$$\Rightarrow$$
 $\angle A = 108^{\circ} - 58^{\circ} = 50^{\circ}$

∴
$$\angle A = 50^{\circ}$$
, $\angle B = 58^{\circ}$ and $\angle C = 72^{\circ}$.

Question 5:

Since. ∠A, ∠B and ∠C are the angles of a triangle.

So,
$$\angle A + \angle B + \angle C = 180^{\circ}$$

Now,
$$\angle A + \angle B = 125^{\circ}$$
 [Given]

$$125^{\circ} + \angle C = 180^{\circ}$$

$$\Rightarrow$$
 \angle C = 180° - 125° = 55°

$$\Rightarrow$$
 $\angle A + 55^{\circ} = 113^{\circ}$

$$\Rightarrow$$
 $\angle A = 113^{\circ} - 55^{\circ} = 58^{\circ}$

$$\Rightarrow$$
 ZB = 125° - 58° = 67°

∴
$$\angle A = 58^{\circ}$$
, $\angle B = 67^{\circ}$ and $\angle C = 55^{\circ}$.

Question 6:

Since, $\angle P$, $\angle Q$ and $\angle R$ are the angles of a triangle.

So,
$$\angle P + \angle Q + \angle R = 180^{\circ}(i)$$

$$\Rightarrow$$
 $\angle P = 42^{\circ} + \angle Q \dots (ii)$

and
$$\angle Q - \angle R = 21^{\circ}$$
 [Given]

Substituting the value of $\angle P$ and $\angle R$ from (ii) and (iii) in (i), we get,

$$\Rightarrow 42^{\circ} + \angle Q + \angle Q + \angle Q - 21^{\circ} = 180^{\circ}$$

$$\Rightarrow 3\angle Q + 21^{\circ} = 180^{\circ}$$

$$\Rightarrow 3\angle Q = 180^{\circ} - 21^{\circ} = 159^{\circ}$$

$$\angle O = \frac{159}{3} = 53^{\circ}$$

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$$\therefore \angle P = 42^{\circ} + \angle Q$$

$$=42^{\circ}+53^{\circ}=95^{\circ}$$

$$=53^{\circ}-21^{\circ}=32^{\circ}$$

Question 7:

Given that the sum of the angles A and B of a ABC is 116° , i.e., $\angle A + \angle B = 116^{\circ}$.

Since,
$$\angle A + \angle B + \angle C = 180^{\circ}$$

So,
$$116^{\circ} + \angle C = 180^{\circ}$$

$$\Rightarrow$$
 LC = $180^{\circ} - 116^{\circ} = 64^{\circ}$

Also, it is given that:

Putting,
$$\angle A = 24^{\circ} + \angle B$$
 in $\angle A + \angle B = 116^{\circ}$, we get,

$$\Rightarrow 24^{\circ} + \angle B + \angle B = 116^{\circ}$$

$$\Rightarrow 2\angle B + 24^{\circ} = 116^{\circ}$$

$$\Rightarrow 2\angle B = 116^{\circ} - 24^{\circ} = 92^{\circ}$$

$$\angle B = \frac{92}{2} = 46^{\circ}$$

Therefore,
$$\angle A = 24^{\circ} + 46^{\circ} = 70^{\circ}$$

∴
$$\angle A = 70^{\circ}$$
, $\angle B = 46^{\circ}$ and $\angle C = 64^{\circ}$.

Question 8:

Let the two equal angles, A and B, of the triangle be x^0 each.

We know,

$$\Rightarrow$$
 $x^0 + x^0 + \angle C = 180^0$

$$\Rightarrow 2x^{\circ} + \angle C = 180^{\circ}(i)$$

Also, it is given that,

$$\angle C = x^0 + 18^0 \dots (ii)$$

Substituting ∠C from (ii) in (i), we get,

$$\Rightarrow 2x^{0} + x^{0} + 18^{0} = 180^{0}$$

$$\Rightarrow$$
 3x° = 180° - 18° = 162°

$$x = \frac{162}{3} = 54^{\circ}$$

Thus, the required angles of the triangle are 54° , 54° and $x^{\circ} + 18^{\circ} = 54^{\circ} + 18^{\circ} = 72^{\circ}$.

Question 9:

Let ∠C be the smallest angle of ABC.

Then,
$$\angle A = 2\angle C$$
 and $B = 3\angle C$

So,
$$\angle A = 2\angle C = 2(30^{\circ}) = 60^{\circ}$$

$$\angle B = 3\angle C = 3 (30^{\circ}) = 90^{\circ}$$

∴ The required angles of the triangle are 60°, 90°, 30°.

Question 10:

Let ABC be a right angled triangle and $\angle C = 90^{\circ}$

Since,
$$\angle A + \angle B + \angle C = 180^{\circ}$$

$$\Rightarrow$$
 $\angle A + \angle B = 180^{\circ} - \angle C = 180^{\circ} - 90^{\circ} = 90^{\circ}$

Suppose $\angle A = 53^{\circ}$





Then, $53^{\circ} + \angle B = 90^{\circ}$

 \Rightarrow **\angle**B = 90° - 53° = 37°

∴ The required angles are 53°, 37° and 90°.

Question 11:

Let ABC be a triangle.

Given, $\angle A + \angle B = \angle C$

We know, ∠A + ∠B + ∠C = 180°

⇒ ∠C + ∠C = 180°

⇒2**∠**C = 180°

 \Rightarrow $\angle C = \frac{180}{2} = 90^{\circ}$

So, we find that ABC is a right triangle, right angled at C.

Question 12:

Given: \triangle ABC in which \angle A = 90°, AL \perp BC

To Prove: **Z**BAL = **Z**ACB

Proof:

In right triangle \triangle ABC,

⇒∠ABC+∠BAC+∠ACB = 180°

⇒ ∠ABC + 90° + ∠ACB = 180°

⇒ ∠ABC + ∠ACB = 180° - 90°

 \therefore **Z**ABC + **Z**ACB = 90°

 \Rightarrow **Z** ACB = 90° - **Z**ABC(1)

.iat, Similarly since \triangle ABL is a right triangle, we find that,

 $∠BAL = 90^{\circ} - ∠ABC$...(2)

Thus from (1) and (2), we have

 \therefore **Z**BAL = **Z**ACB (Proved)

Question 13:

Let ABC be a triangle.

So, ∠A < ∠B + ∠C

Adding A to both sides of the inequality,

 $\Rightarrow 2\angle A < \angle A + \angle B + \angle C$

 $\Rightarrow 2\angle A < 180^{\circ}$ [Since $\angle A + \angle B + \angle C = 180^{\circ}$]

 \Rightarrow $\angle A < \frac{180}{2} = 90^{\circ}$

Similarly, ∠B < ∠A + ∠C

⇒**∠**B<90°

and $\angle C < \angle A + \angle B$

⇒ **∠**C < 90°

 \triangle ABC is an acute angled triangle.

Question 14:

Let ABC be a triangle and **L**B > **L**A + **L**C

Since, $\angle A + \angle B + \angle C = 180^{\circ}$

⇒ ∠A + ∠C = 180° - ∠B

Therefore, we get

ZB > 180° - **Z**B

Adding **Z**B on both sides of the inequality, we get,

⇒ ∠B + ∠B > 180° - ∠B + ∠B

⇒2**∠**B > 180°

 \Rightarrow $\angle B > \frac{180}{2} = 90^{\circ}$

i.e., $\angle B > 90^{\circ}$ which means $\angle B$ is an obtuse angle.





ΔABC is an obtuse angled triangle.

Question 15:

Since ∠ACB and ∠ACD form a linear pair.

So, ∠ACB + ∠ACD = 180°

⇒ ∠ACB + 128° = 180°

⇒ **∠**ACB = 180° - 128 = 52°

Also, **Z**ABC + **Z**ACB + **Z**BAC = 180°

 \Rightarrow 43° + 52° + **Z**BAC = 180°

⇒ 95° + ∠BAC = 180°

 \Rightarrow **Z**BAC = $180^{\circ} - 95^{\circ} = 85^{\circ}$

 \therefore **Z**ACB = 52° and **Z**BAC = 85°.

Question 16:

As ∠DBA and ∠ABC form a linear pair.

So. **Z**DBA + **Z**ABC = 180°

 \Rightarrow 106° + \angle ABC = 180°

 \Rightarrow **Z**ABC = $180^{\circ} - 106^{\circ} = 74^{\circ}$

Also, ∠ACB and ∠ACE form a linear pair.

So, **Z**ACB + **Z**ACE = 180°

⇒∠ACB + 118° = 180°

 \Rightarrow **Z**ACB = $180^{\circ} - 118^{\circ} = 62^{\circ}$

In ∠ABC, we have,

ZABC + ZACB + ZBAC = 180°

 $74^{\circ} + 62^{\circ} + \angle BAC = 180^{\circ}$

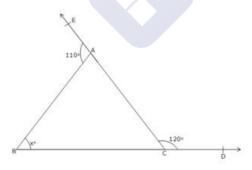
⇒ 136° + ∠BAC = 180°

⇒ ∠BAC = 180° - 136° = 44°

∴ In triangle ABC, \angle A = 44°, \angle B = 74° and \angle C = 62°

Question 17:

(i) ∠EAB + ∠BAC = 180° [Linear pair angles]



110° + **Z**BAC = 180°

⇒ ∠BAC = 180° - 110° = 70°

Again, ∠BCA + ∠ACD = 180°[Linear pair angles]

⇒ ∠BCA + 120° = 180°

 \Rightarrow **Z**BCA = $180^{\circ} - 120^{\circ} = 60^{\circ}$

Now, in **∆**ABC,

∠ABC + ∠BAC + ∠ACB = 180°

 $x^{0} + 70^{0} + 60^{0} = 180^{0}$

 \Rightarrow x + 130° = 180°

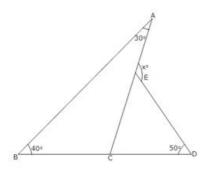
 \Rightarrow x = 180° - 130° = 50°

∴ x = 50

(ii)







In ΔABC,

$$\Rightarrow$$
 LC = $180^{\circ} - 70^{\circ} = 110^{\circ}$

Now ∠BCA + ∠ACD = 180° [Linear pair]

$$\Rightarrow$$
 ZACD = $180^{\circ} - 110^{\circ} = 70^{\circ}$

In **Δ**ECD,

$$\Rightarrow$$
 70° + 50° + **Z**CED = 180°

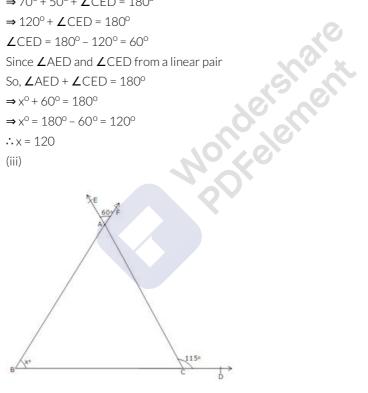
$$\angle$$
CED = $180^{\circ} - 120^{\circ} = 60^{\circ}$

Since ∠AED and ∠CED from a linear pair

$$\Rightarrow$$
 $x^{0} + 60^{0} = 180^{0}$

$$\Rightarrow$$
 $x^{\circ} = 180^{\circ} - 60^{\circ} = 120^{\circ}$

(iii)



∠EAF = ∠BAC [Vertically opposite angles]

In \triangle ABC, exterior \angle ACD is equal to the sum of two opposite interior angles.

$$\Rightarrow 115^{\circ} = 60^{\circ} + x^{\circ}$$

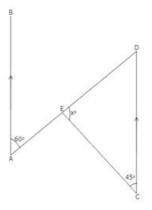
$$\Rightarrow$$
 $x^{\circ} = 115^{\circ} - 60^{\circ} = 55^{\circ}$

(iv)

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Since AB | CD and AD is a transversal.

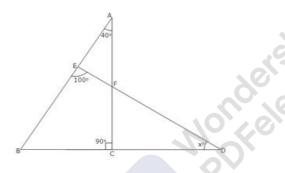
In ∠ECD, we have,

$$\Rightarrow$$
 $x^{0} + 45^{0} + 60^{0} = 180^{0}$

$$\Rightarrow$$
 $x^{0} + 105^{0} = 180^{0}$

$$\Rightarrow$$
 $x^{\circ} = 180^{\circ} - 105^{\circ} = 75^{\circ}$

(v)



In **Δ**AEF,

Exterior **Z**BED = **Z**EAF + **Z**EFA

$$\Rightarrow 100^{\circ} = 40^{\circ} + \angle EFA$$

$$\Rightarrow$$
 ∠EFA = 100° - 40° = 60°

Also, ∠CFD = ∠EFA [Vertically Opposite angles]

Now in \triangle FCD.

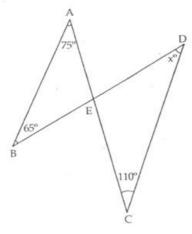
Exterior **Z**BCF = **Z**CFD + **Z**CDF

$$\Rightarrow 90^{\circ} = 60^{\circ} + x^{\circ}$$

$$\Rightarrow$$
 $x^{\circ} = 90^{\circ} - 60^{\circ} = 30^{\circ}$

(vi)





In **∆**ABE, we have,

$$\Rightarrow$$
 75° + 65° + \angle E = 180°

$$\Rightarrow$$
 ZE = 180° - 140° = 40°

Now, ∠CED = ∠AEB [Vertically opposite angles]

Now, in \triangle CED, we have,

$$\Rightarrow 110^{\circ} + 40^{\circ} + x^{\circ} = 180^{\circ}$$

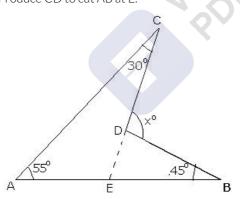
$$\Rightarrow 150^{\circ} + x^{\circ} = 180^{\circ}$$

$$\Rightarrow$$
 $x^{0} = 180^{\circ} - 150^{\circ} = 30^{\circ}$

$$\therefore x = 30$$

Question 18:

Produce CD to cut AB at E.



Now, in \triangle BDE, we have,

Exterior ∠CDB = ∠CEB + ∠DBE

$$\Rightarrow$$
 x° = \angle CEB + 45°(i)

In \triangle AEC, we have,

Exterior **Z**CEB = **Z**CAB + **Z**ACE

$$= 55^{\circ} + 30^{\circ} = 85^{\circ}$$

Putting \angle CEB = 85° in (i), we get,

$$x^0 = 85^0 + 45^0 = 130^0$$

$$\therefore x = 130$$

Question 19:

The angle \angle BAC is divided by AD in the ratio 1:3.

Let ${\bf \angle}$ BAD and ${\bf \angle}$ DAC be y and 3y, respectively.

As BAE is a straight line,

∠BAC + ∠CAE = 180° [linear pair]



 \Rightarrow **Z**BAD + **Z**DAC + $_{\mathbf{Z}}$ CAE = 180°

 \Rightarrow y + 3y + 108° = 180°

 \Rightarrow 4y = 180° - 108° = 72°

 \Rightarrow $y = \frac{72}{4} = 18^{\circ}$

Now, in **∆**ABC,

ZABC + ZBCA + ZBAC = 180°

 $y + x + 4y = 180^{\circ}$

[Since, \angle ABC = \angle BAD (given AD = DB) and \angle BAC = y + 3y = 4y]

 \Rightarrow 5y + x = 180

 \Rightarrow 5 × 18 + x = 180

 \Rightarrow 90 + x = 180

 $\therefore x = 180 - 90 = 90$

Question 20:

Given: A \triangle ABC in which BC, CA and AB are produced to D, E and F respectively.

To prove: Exterior ∠DCA + Exterior ∠BAE + Exterior ∠FBD = 360°

Proof: Exterior **Z**DCA = **Z**A + **Z**B(i)

Exterior ∠FAE = ∠B + ∠C(ii)

Exterior **Z**FBD = **Z**A + **Z**C(iii)

Adding (i), (ii) and (iii), we get,

Ext. **Z**DCA + Ext. **Z**FAE + Ext. **Z**FBD

 $-\omega + \angle C$) = $2 \times 180^{\circ}$ [Since, in triangle the sum of all three angle is 180°] = 360° Hence, proved.

Question 21:

In \triangle ACE, we have,

 $\angle A + \angle C + \angle E = 180^{\circ}...(i)$

In \triangle BDF, we have,

 $\angle B + \angle D + \angle F = 180^{\circ}(ii)$

Adding both sides of (i) and (ii), we get,

 $\angle A + \angle C + \angle E + \angle B + \angle D + \angle F = 180^{\circ} + 180^{\circ}$

 \Rightarrow $\angle A + \angle B + \angle C + \angle D + \angle E + \angle F = 360^{\circ}$.

Question 22:

Given: In \triangle ABC, bisectors of \angle B and \angle C meet at O and \angle A = 70°

In \triangle BOC, we have,



$$\Rightarrow \angle BOC + \frac{1}{2} \angle B + \frac{1}{2} \angle C = 180^{\circ}$$

$$\Rightarrow \angle BOC = 180^{\circ} - \frac{1}{2} \angle B - \frac{1}{2} \angle C$$

$$= 180^{\circ} - \frac{1}{2} (\angle B + \angle C)$$

$$= 180^{\circ} - \frac{1}{2} \left[180^{\circ} - \angle A \right]$$

$$\left[\because \angle A + \angle B + \angle C = 180^{\circ} \right]$$

$$= 180^{\circ} - \frac{1}{2} \left[180^{\circ} - 70^{\circ} \right]$$
$$= 180^{\circ} - \frac{1}{2} \times 110^{\circ}$$

Question 23:

We have a \triangle ABC whose sides AB and AC have been procued to D and E. A = 40° and bisectors of ∠CBD and ∠BCE meet at O.

In \triangle ABC, we have,

Exterior **Z**CBD = C + 40°

$$\Rightarrow$$

$$\angle CBO = \frac{1}{2} Ext. \angle CBD$$

= $\frac{1}{2} \left(\angle C + 40^{\circ} \right)$
= $\frac{1}{2} \angle C + 20^{\circ}$

And exterior \angle BCE = B + 40°

$$= \frac{1}{2} \text{ Ext. } \angle \text{CBD}$$

$$= \frac{1}{2} \left(\angle \text{C} + 40^{\circ} \right)$$

$$= \frac{1}{2} \angle \text{C} + 20^{\circ}$$

$$\angle \text{BCO} = \frac{1}{2} \text{ Ext. } \angle \text{BCE}$$

$$= \frac{1}{2} \left(\angle \text{B} + 40^{\circ} \right)$$

$$= \frac{1}{2} \angle \text{B} + 20^{\circ}.$$
CO

Now, in \triangle BCO, we have,

$$\angle B \text{ OC} = 180^{\circ} - \angle CBO - \angle B \text{ CO}$$

$$= 180^{\circ} - \frac{1}{2} \angle C - 20^{\circ} - \frac{1}{2} \angle B - 20^{\circ}$$

$$= 180^{\circ} - \frac{1}{2} \angle C - \frac{1}{2} \angle B - 20^{\circ} - 20^{\circ}$$

$$= 180^{\circ} - \frac{1}{2} \angle C - \frac{1}{2} \angle B - 20^{\circ} - 20^{\circ}$$

$$= 180^{\circ} - \frac{1}{2} (\angle B + \angle C) - 40^{\circ}$$

$$= 140^{\circ} - \frac{1}{2} (\angle B + \angle C)$$

$$= 140^{\circ} - \frac{1}{2} [180^{\circ} - \angle A]$$

$$= 140^{\circ} - 90^{\circ} + \frac{1}{2} \angle A$$

$$= 50^{\circ} + \frac{1}{2} \angle A$$
$$= 50^{\circ} + \frac{1}{2} \times 40^{\circ}$$

$$=50^{\circ}+20^{\circ}$$

Question 24:

In the given \triangle ABC, we have,

Let
$$\angle A = 3x$$
, $\angle B = 2x$, $\angle C = x$. Then,

$$\Rightarrow$$
 3x + 2x + x = 180°

$$\Rightarrow$$
 6x = 180°

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 $\Rightarrow x = 30^{\circ}$

 $\angle A = 3x = 330^{\circ} = 90^{\circ}$

 $\angle B = 2x = 230^{\circ} = 60^{\circ}$

and, $\angle C = x = 30^{\circ}$

Now, in \triangle ABC, we have,

Ext $\angle ACE = \angle A + \angle B = 90^{\circ} + 60^{\circ} = 150^{\circ}$

ZACD + **Z**ECD = 150°

⇒∠ECD = 150° - ∠ACD

 \Rightarrow ZECD = 150° - 90° [since, AD \perp CD, ZACD = 90°]

⇒∠ECD=60°

Question 25:

In \triangle ABC, AN is the bisector of \angle A and AM \perp BC.

Now in \triangle ABC we have;

$$\angle A = 180^{\circ} - \angle B - \angle C$$

$$\Rightarrow$$
 $\angle A = 180^{\circ} - 65^{\circ} - 30^{\circ}$

$$= 180^{\circ} - 95^{\circ}$$

= 85°

Now, in \triangle ANC we have;

Ext.
$$\angle$$
 MNA = \angle NAC + 30°

$$= \frac{1}{2} \angle A + 30^{\circ}$$

$$= \frac{85^{\circ}}{2} + 30^{\circ}$$

$$= \frac{85^{\circ} + 60^{\circ}}{2}$$

$$= \frac{145^{\circ}}{2}$$

Therefore,
$$\angle MNA = \frac{145^{\circ}}{2}$$

In A MAN. we have;

=
$$180^{\circ}$$
 - 90° - MNA [since AM \perp BC, \angle AMN = 90°]

=
$$90^{\circ} - \frac{145^{\circ}}{2}$$
 [since $\angle MNA = \frac{145^{\circ}}{2}$]
= $\frac{180^{\circ} - 145^{\circ}}{2}$
= $\frac{35^{\circ}}{2}$
= 17. 5°

Thus, ∠MAN =

Question 26:

(i) False (ii) True (iii) False (iv) False (v) True (vi) True.

Million Stars Practice
William Realth