



Linear Equations

Ex 8A

Definition of a Linear Equation

- A linear equation in one variable x is an equation that can be written in the form
- $ax + b = 0$
- where a and b are real numbers and $a \neq 0$.

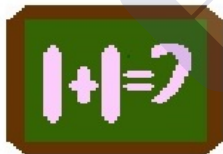
Equation is a mathematical sentence indicating that two expressions are equal. The symbol "=" is used to indicate equality.

Ex.

$2x + 5 = 9$ is a conditional equation

since its truth or falsity depends on the value of x

$2 + 9 = 11$ is identity equation since both of its sides are identical to the same number 11.





Solution Set of a Linear Equation

Example

$$4x + 2 = 10$$

this statement is either true or false

If $x = 1$, then $4x + 2 = 10$

is false because $4(1) + 2$ is $\neq 10$

If $x = 2$, then $4x + 2 = 10$

is true because $4(2) + 2 = 10$

ONE STEP SUBTRACTION EXAMPLE

The Opposite of Subtraction is Addition

$$\begin{array}{rcl} x - 120 & = & 80 \\ +120 & & +120 \\ \hline x & = & 200 \checkmark \end{array}$$

The value which makes the equation true is 200.

$x - 4 = 7$	Original problem
$x - 4 = 7$	We want to remove the minus 4.
$x - 4 + 4 = 7 + 4$	The opposite of minus 4 is plus 4, so I added 4 to BOTH sides of the equation.
$x = 11$	$-4 + 4 = 0$, so x remains on the left and $7 + 4 = 11$; therefore $x = 11$
Check: $x - 4 = 7$ $11 - 4 = 7$	This is a correct statement, so my answer is $x = 11$ is correct!



Solving simple two-step equations

To solve an equation, find the value that makes the equation true.

Solve $2x + 3 = 13$

This means: $x \times 2 \rightarrow + 3 = 13$

To solve, we reverse the process:

$x \times 2 \rightarrow + 3 = 13$
 $x \div 2 \leftarrow - 3 = 13$

Use the opposite (inverse) operation and undo in reverse order.

$$2x + 3 = 13$$

$$- 3$$

$$2x = 10$$

$$\div 2$$

$$x = 5$$

We have solved the equation when we get to a single value of x (here, $x = 5$).

Solve $4x + 6 = 14$

$$4x + 6 = 14$$

$$- 6$$

$$4x = 8$$

$$\div 4$$

$$x = 2$$

Solve $3x - 8 = 19$

$$3x - 8 = 19$$

$$+ 8$$

$$3x = 27$$

$$\div 3$$

$$x = 9$$

Q1

Answer :

$$\begin{aligned}
 8x + 3 &= 27 + 2x \\
 \Rightarrow 8x - 2x &= 27 - 3 \\
 \Rightarrow 6x &= 24 \\
 \Rightarrow x &= \frac{24}{6} = 4 \\
 \therefore x &= 4
 \end{aligned}$$

Q2

Answer :

$$\begin{aligned}
 5x + 7 &= 2x - 8 \\
 \Rightarrow 5x - 2x &= -8 - 7 \\
 \Rightarrow 3x &= -15 \\
 \Rightarrow x &= \frac{-15}{3} = -5 \\
 \therefore x &= -5
 \end{aligned}$$

Q3.

Answer :

$$\begin{aligned}
 2z - 1 &= 14 - z \\
 \Rightarrow 2z + z &= 14 + 1 \\
 \Rightarrow 3z &= 15 \\
 \Rightarrow z &= \frac{15}{3} = 5 \\
 \therefore z &= 5
 \end{aligned}$$

Q4.

Answer :

$$\begin{aligned}
 9x + 5 &= 4(x - 2) + 8 \\
 \Rightarrow 9x + 5 &= 4x - 8 + 8 \\
 \Rightarrow 9x + 5 &= 4x \\
 \Rightarrow 9x - 4x &= -5 \\
 \Rightarrow 5x &= -5 \\
 \Rightarrow x &= \frac{-5}{5} = -1 \\
 \therefore x &= -1
 \end{aligned}$$



Q5.

Answer :

$$\frac{7y}{5} = y - 4$$

By cross multiplication :

$$\Rightarrow 7y = 5(y - 4)$$

$$\Rightarrow 7y = 5y - 20$$

$$\Rightarrow 7y - 5y = -20$$

$$\Rightarrow 2y = -20$$

$$\Rightarrow y = \frac{-20}{2} = -10$$

$$\therefore y = -10$$

Q6.

Answer :

$$3x + \frac{2}{3} = 2x + 1$$

$$\Rightarrow 3x - 2x = 1 - \frac{2}{3}$$

$$\Rightarrow x = \frac{1}{1} - \frac{2}{3} \quad (\text{L. C. M. of 1 and 3 is 3}) \quad \Rightarrow x =$$

$$\frac{3-2}{3}$$

$$\Rightarrow x = \frac{1}{3}$$

$$\Rightarrow x = \frac{1}{3}$$

$$\therefore x = \frac{1}{3}$$

Q7.

Answer :

$$15(y - 4) - 2(y - 9) + 5(y + 6) = 0$$

$$\Rightarrow 15y - 60 - 2y + 18 + 5y + 30 = 0$$

$$\Rightarrow 15y - 2y + 5y - 60 + 18 + 30 = 0$$

$$\Rightarrow 18y - 12 = 0$$

$$\Rightarrow 18y = 12$$

$$\Rightarrow y = \frac{12}{18} = \frac{2}{3}$$

$$\therefore y = \frac{2}{3}$$

Q8.

Answer :

$$3(5x - 7) - 2(9x - 11) = 4(8x - 13) - 17$$

$$\Rightarrow 15x - 21 - 18x + 22 = 32x - 52 - 17$$

$$\Rightarrow 15x - 18x - 21 + 22 = 32x - 69$$

$$\Rightarrow -3x + 1 = 32x - 69$$

$$\Rightarrow 1 + 69 = 32x + 3x$$

$$\Rightarrow 70 = 35x$$

$$\Rightarrow 35x = 70 \quad (\text{by transposition})$$

$$\Rightarrow x = \frac{70}{35} = 2$$

$$\therefore x = 2$$

Q9.

Answer :

$$\frac{x-5}{2} - \frac{x-3}{5} = \frac{1}{2}$$

$$\Rightarrow 10\left(\frac{x-5}{2}\right) - 10\left(\frac{x-3}{5}\right) = 10\left(\frac{1}{2}\right) \quad (\text{multiplying throughout by 10, which is}$$

$$\text{the L. C. M. of 2, 2 and 5}) \Rightarrow 5(x - 5) - 2(x - 3) = 5 \Rightarrow 5x - 25 - 2x + 6 = 5 \Rightarrow 5x - 2x - 25 + 6 = 5 \Rightarrow 3x - 19 = 5 \Rightarrow 3x = 5 + 19 \Rightarrow 3x = 24 \Rightarrow x$$

$$= \frac{24}{3} = 8 \therefore x = 8$$

Q10.



Answer :

$$\begin{aligned}\frac{3t-2}{4} - \frac{2t+3}{3} &= \frac{2}{3} - t \\ \Rightarrow \frac{3t-2}{4} - \frac{2t+3}{3} &= \frac{2-3t}{3} \quad \left(3 \text{ is the L.C.M. of } 1 \text{ and } 3\right) \\ \Rightarrow 12 \left(\frac{3t-2}{4}\right) - 12 \left(\frac{2t+3}{3}\right) &= 12 \left(\frac{2-3t}{3}\right) \quad \left(\text{multiplying throughout by } 12, \text{ which}\right. \\ &\left.\text{is the L.C.M. of } 4, 3 \text{ and } 3\right) \\ \Rightarrow 3(3t-2) - 4(2t+3) &= 4(2-3t) \\ \Rightarrow 9t-6-8t-12 &= 8-12t \\ \Rightarrow 9t-8t-6-12 &= 8-12t \\ \Rightarrow t-18 &= 8-12t \\ \Rightarrow t+12t &= 18+8 \\ \Rightarrow 13t &= 26 \\ \Rightarrow t &= \frac{26}{13} = 2 \\ \therefore t &= 2\end{aligned}$$

Q11.

Answer :

$$\begin{aligned}\frac{2x+7}{5} - \frac{3x+11}{2} &= \frac{2x+8}{3} - 5 \\ \Rightarrow \frac{2x+7}{5} - \frac{3x+11}{2} &= \frac{2x+8-15}{3} \quad \left(\text{L.C.M. of } 3 \text{ and } 1 \text{ is } 3\right) \\ \Rightarrow 30 \left(\frac{2x+7}{5}\right) - 30 \left(\frac{3x+11}{2}\right) &= 30 \left(\frac{2x+8-15}{3}\right) \\ \left(\text{multiplying throughout by } 30, \text{ which is the L.C.M. of } 5, 2 \text{ and } 3\right) \\ \Rightarrow 6(2x+7) - 15(3x+11) &= 10(2x+8-15) \Rightarrow 12x+42-45x-165 \\ &= 20x-70 \Rightarrow 12x-45x+42-165 = 20x-70 \Rightarrow -33x-123 = 20x-70 \Rightarrow \\ -33x-20x &= 123-70 \Rightarrow -53x = 53 \Rightarrow x = \frac{53}{-53} \Rightarrow x = -1 \therefore x = -1\end{aligned}$$

Q12.

Answer :

$$\begin{aligned}\frac{5x-4}{6} &= 4x+1 - \frac{3x+10}{2} \\ \Rightarrow \frac{5x-4}{6} &= \frac{2(4x+1)-3x-10}{2} \quad \left(\text{L.C.M. of } 1 \text{ and } 2 \text{ is } 2\right) \\ \Rightarrow \frac{5x-4}{6} &= \frac{8x+2-3x-10}{2} \\ \Rightarrow \frac{5x-4}{6} &= \frac{8x-3x+2-10}{2} \\ \Rightarrow \frac{5x-4}{6} &= \frac{5x-8}{2} \\ \Rightarrow 2(5x-4) &= 6(5x-8) \\ \Rightarrow 10x-8 &= 30x-48 \\ \Rightarrow 10x-30x &= -48+8 \\ \Rightarrow -20x &= -40 \\ \Rightarrow x &= \frac{-40}{-20} = 2 \\ \therefore x &= 2\end{aligned}$$

Q13.

**Answer :**

$$\begin{aligned}
5x - \frac{1}{3}(x+1) &= 6\left(x + \frac{1}{30}\right) \\
\Rightarrow 5x - \frac{1(x+1)}{3} &= 6\left(\frac{30x+1}{30}\right) \quad \left(\text{L.C.M. of 1 and 30 is 30}\right) \\
\Rightarrow 5x - \frac{(x+1)}{3} &= \frac{30x+1}{5} \\
\Rightarrow \frac{15x-x-1}{3} &= \frac{30x+1}{5} \quad \left(\text{L.C.M. of 1 and 3 is 3}\right) \\
\Rightarrow \frac{14x-1}{3} &= \frac{30x+1}{5} \\
\Rightarrow 5(14x-1) &= 3(30x+1) \quad \left(\text{by cross multiplication}\right) \\
\Rightarrow 70x-5 &= 90x+3 \\
\Rightarrow 70x-90x &= 3+5 \\
\Rightarrow -20x &= 8 \\
\Rightarrow x &= \frac{8}{-20} = \frac{-2}{5} \\
\therefore x &= -\frac{2}{5}
\end{aligned}$$

Q14.

Answer :

$$\begin{aligned}
4 - \frac{2(z-4)}{3} &= \frac{1}{2}(2z+5) \\
\Rightarrow \frac{12-2(z-4)}{3} &= \frac{1(2z+5)}{2} \quad \left(\text{L.C.M. of 1 and 3 is 3}\right) \\
\Rightarrow \frac{12-2z+8}{3} &= \frac{2z+5}{2} \\
\Rightarrow \frac{20-2z}{3} &= \frac{2z+5}{2} \\
\Rightarrow 2(20-2z) &= 3(2z+5) \quad \left(\text{by cross multiplication}\right) \\
\Rightarrow 40-4z &= 6z+15 \\
\Rightarrow 40-15 &= 6z+4z \\
\Rightarrow 25 &= 10z \\
\Rightarrow 10z &= 25 \quad \left(\text{by transposition}\right) \\
\Rightarrow z &= \frac{25}{10} = \frac{5}{2} \\
\therefore z &= \frac{5}{2}
\end{aligned}$$

Q15.

Answer :

$$\begin{aligned}
\frac{3(y-5)}{4} - 4y &= 3 - \frac{(y-3)}{2} \\
\Rightarrow \frac{3y-15}{4} - 4y &= 3 - \frac{y-3}{2} \\
\Rightarrow \frac{3y-15-16y}{4} &= 3 - \frac{y-3}{2} \quad \left(\text{L.C.M. of 4 and 1 is 4}\right) \\
\Rightarrow \frac{-13y-15}{4} &= \frac{6-y+3}{2} \\
\Rightarrow \frac{-13y-15}{4} &= \frac{9-y}{2} \\
\Rightarrow 2(-13y-15) &= 4(9-y) \\
\Rightarrow -26y-30 &= 36-4y \\
\Rightarrow -26y+4y &= 36+30 \\
\Rightarrow -22y &= 66 \\
\Rightarrow 22y &= -66 \quad \left(\text{multiplying both the sides with a -ve sign}\right) \\
\Rightarrow y &= \frac{-66}{22} = -3 \\
\therefore y &= -3
\end{aligned}$$

Q16.

**Answer :**

$$\frac{8x-3}{3x} = 2$$

$$\Rightarrow 8x - 3 = 2(3x) \quad (\text{by cross multiplication})$$

$$\Rightarrow 8x - 3 = 6x$$

$$\Rightarrow 8x - 6x = 3$$

$$\Rightarrow 2x = 3$$

$$\Rightarrow x = \frac{3}{2}$$

$$\therefore x = \frac{3}{2}$$

Q17.

Answer :

$$\frac{9x}{7-6x} = 15$$

$$\Rightarrow \frac{9x}{7-6x} = \frac{15}{1}$$

$$\Rightarrow 1(9x) = 15(7-6x) \quad (\text{by cross multiplication})$$

$$\Rightarrow 9x = 105 - 90x$$

$$\Rightarrow 9x + 90x = 105$$

$$\Rightarrow 99x = 105$$

$$\Rightarrow x = \frac{105}{99} = \frac{35}{33}$$

$$\therefore x = \frac{35}{33}$$

Q18.

Answer :

$$\frac{3x}{5x+2} = -4$$

$$\Rightarrow \frac{3x}{5x+2} = \frac{-4}{1}$$

$$\Rightarrow 1(3x) = -4(5x+2) \quad (\text{by cross multiplication})$$

$$\Rightarrow 3x = -20x - 8$$

$$\Rightarrow 3x + 20x = -8$$

$$\Rightarrow 23x = -8$$

$$\Rightarrow x = \frac{-8}{23}$$

$$\therefore x = \frac{-8}{23}$$

Q20.

Answer :

$$\frac{2-9z}{17-4z} = \frac{4}{5}$$

$$\Rightarrow 5(2-9z) = 4(17-4z) \quad (\text{by cross multiplication})$$

$$\Rightarrow 10 - 45z = 68 - 16z$$

$$\Rightarrow 10 - 68 = 45z - 16z$$

$$\Rightarrow -58 = 29z$$

$$\Rightarrow 29z = -58 \quad (\text{by transposition})$$

$$\Rightarrow z = \frac{-58}{29} = -2$$

$$\therefore z = -2$$

Q21.

Answer :

$$\frac{4x+7}{9-3x} = \frac{1}{4}$$

$$\Rightarrow 4(4x+7) = 1(9-3x) \quad (\text{by cross multiplication})$$

$$\Rightarrow 16x + 28 = 9 - 3x$$

$$\Rightarrow 16x + 3x = 9 - 28$$

$$\Rightarrow 19x = -19$$

$$\Rightarrow x = \frac{-19}{19} = -1$$

$$\therefore x = -1$$

Q22.

**Answer :**

$$\begin{aligned}\frac{7y+4}{y+2} &= \frac{-4}{3} \\ \Rightarrow 3(7y+4) &= -4(y+2) && \text{(by cross multiplication)} \\ \Rightarrow 21y+12 &= -4y-8 \\ \Rightarrow 21y+4y &= -8-12 \\ \Rightarrow 25y &= -20 \\ \Rightarrow y &= \frac{-20}{25} = \frac{-4}{5} \\ \therefore y &= \frac{-4}{5}\end{aligned}$$

Q23.

Answer :

$$\begin{aligned}\frac{15(2-y)-5(y+6)}{1-3y} &= 10 \\ \Rightarrow \frac{30-15y-5y-30}{1-3y} &= 10 \\ \Rightarrow \frac{-20y}{1-3y} &= 10 \\ \Rightarrow 1(-20y) &= 10(1-3y) && \text{(by cross multiplication)} \\ \Rightarrow -20y &= 10-30y \\ \Rightarrow -20y+30y &= 10 \\ \Rightarrow 10y &= 10 \\ \Rightarrow y &= \frac{10}{10} = 1 \\ \therefore y &= 1\end{aligned}$$

Q24.

Answer :

$$\begin{aligned}\frac{2x-(7-5x)}{9x-(3+4x)} &= \frac{7}{6} \\ \Rightarrow \frac{2x-7+5x}{9x-3-4x} &= \frac{7}{6} \\ \Rightarrow \frac{7x-7}{5x-3} &= \frac{7}{6} \\ \Rightarrow 6(7x-7) &= 7(5x-3) && \text{(by cross multiplication)} \\ \Rightarrow 42x-42 &= 35x-21 \\ \Rightarrow 42x-35x &= 42-21 \\ \Rightarrow 7x &= 21 \\ \Rightarrow x &= \frac{21}{7} = 3 \\ \therefore x &= 3\end{aligned}$$

Q25.

Answer :

$$\begin{aligned}m - \frac{(m-1)}{2} &= 1 - \frac{(m-2)}{3} \\ \Rightarrow \frac{2m-m+1}{2} &= 1 - \frac{(m-2)}{3} && \text{(L.C.M. of 1 and 2 is 2)} \\ \Rightarrow \frac{m+1}{2} &= \frac{3-m+2}{3} && \text{(L.C.M. of 1 and 3 is 3)} \\ \Rightarrow \frac{m+1}{2} &= \frac{5-m}{3} \\ \Rightarrow 3(m+1) &= 2(5-m) && \text{(by cross multiplication)} \\ \Rightarrow 3m+3 &= 10-2m \\ \Rightarrow 3m+2m &= 10-3 \\ \Rightarrow 5m &= 7 \\ \Rightarrow m &= \frac{7}{5} \\ \therefore m &= \frac{7}{5}\end{aligned}$$

Q26.

**Answer :**

$$\frac{3x+5}{4x+2} = \frac{3x+4}{4x+7}$$

$$\Rightarrow (4x+7)(3x+5) = (4x+2)(3x+4) \quad (\text{by cross multiplication})$$

$$\Rightarrow 12x^2 + 20x + 21x + 35 = 12x^2 + 16x + 6x + 8$$

$$\Rightarrow 12x^2 + 41x + 35 = 12x^2 + 22x + 8$$

$$\Rightarrow 12x^2 - 12x^2 + 41x - 22x = 8 - 35$$

$$\Rightarrow 19x = -27$$

$$\Rightarrow x = \frac{-27}{19}$$

$$\therefore x = \frac{-27}{19}$$

Q27.

Answer :

$$\frac{9x-7}{3x+5} = \frac{3x-4}{x+6}$$

$$\Rightarrow (x+6)(9x-7) = (3x+5)(3x-4)$$

(by cross multiplication)

$$\Rightarrow 9x^2 - 7x + 54x - 42 = 9x^2 - 12x + 15x - 20$$

$$\Rightarrow 9x^2 + 47x - 42 = 9x^2 + 3x - 20$$

$$\Rightarrow 9x^2 - 9x^2 + 47x - 3x = -20 + 42$$

$$\Rightarrow 44x = 22$$

$$\Rightarrow x = \frac{22}{44} = \frac{1}{2}$$

$$\therefore x = \frac{1}{2}$$

Q28.

Answer :

$$\frac{2-7x}{1-5x} = \frac{3+7x}{4+5x}$$

$$\Rightarrow (4+5x)(2-7x) = (1-5x)(3+7x) \quad (\text{by cross multiplication})$$

$$\Rightarrow 8 - 28x + 10x - 35x^2 = 3 + 7x - 15x - 35x^2$$

$$\Rightarrow -35x^2 - 18x + 8 = -35x^2 - 8x + 3$$

$$\Rightarrow -35x^2 + 35x^2 - 18x + 8x = 3 - 8$$

$$\Rightarrow -10x = -5$$

$$\Rightarrow x = \frac{-5}{-10} = \frac{1}{2}$$

$$\therefore x = \frac{1}{2}$$



Linear Equations

Ex 8B

Definition of a Linear Equation

- A linear equation in one variable x is an equation that can be written in the form
- $ax + b = 0$
- where a and b are real numbers and $a \neq 0$.

ONE STEP SUBTRACTION EXAMPLE

The Opposite of Subtraction is Addition

$$x - 120 = 80$$

$$+120 \quad +120$$

$$x = 200 \checkmark$$

The value which makes the equation true is 200.

$x - 4 = 7$	Original problem
$x - 4 = 7$	We want to remove the minus 4.
$x - 4 + 4 = 7 + 4$	The opposite of minus 4 is plus 4, so I added 4 to BOTH sides of the equation.
$x = 11$	$-4 + 4 = 0$, so x remains on the left and $7 + 4 = 11$; therefore $x = 11$
Check: $x - 4 = 7$ $11 - 4 = 7$	This is a correct statement, so my answer is $x = 11$ is correct!



Solving simple two-step equations

To solve an equation, find the value that makes the equation true.

Solve $2x + 3 = 13$

This means: $x \times 2 \rightarrow + 3 = 13$

To solve, we reverse the process:

$x \times 2 \rightarrow + 3 = 13$

$x \leftarrow \div 2 \leftarrow - 3 = 13$

Use the opposite (inverse) operation and undo in reverse order.

$2x + 3 = 13$

$2x = 10$

$x = 5$

We have solved the equation when we get to a single value of x (here, $x = 5$).

Solve $4x + 6 = 14$

$4x + 6 = 14$

$4x = 8$

$x = 2$

$- 6$
 $\div 4$

Solve $3x - 8 = 19$

$3x - 8 = 19$

$3x = 27$

$x = 9$

$+ 8$
 $\div 3$

Q1

Answer :

Let the numbers be $8x$ and $3x$.

$8x + 3x = 143$

$\Rightarrow 11x = 143$

$\Rightarrow x = \frac{143}{11}$

$\Rightarrow x = 13$

$\therefore \text{One number} = 8x = 8 \times 13 = 104$

$\text{Other number} = 3x = 3 \times 13 = 39$

Q2.

Answer :

Let the original number be x .

$\frac{2}{3}$ of the number is 20 less than the original number.

$\therefore \frac{2}{3}x = x - 20$

$\Rightarrow \frac{2x}{3} = x - 20$

$\Rightarrow 2x = 3(x - 20)$ (by cross multiplication)

$\Rightarrow 2x = 3x - 60$

$\Rightarrow 2x - 3x = -60$

$\Rightarrow -x = -60$

$\Rightarrow x = 60$

Therefore, the original number is 60.

Q3.

Answer :

Let the number be x .

Four fifths of the number is 10 more than two thirds of the number.

$\therefore \frac{4}{5}x = 10 + \frac{2}{3}x$

$\Rightarrow \frac{4x}{5} = 10 + \frac{2x}{3}$

$\Rightarrow \frac{4x}{5} = \frac{30 + 2x}{3}$ (L.C.M. of 1 and 3 is 3)

$\Rightarrow 3(4x) = 5(30 + 2x)$ (by cross multiplication)

$\Rightarrow 12x = 150 + 10x$

$\Rightarrow 12x - 10x = 150$

$\Rightarrow 2x = 150$

$\Rightarrow x = \frac{150}{2} = 75$

Therefore, the number is 75.

Q4.

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Let one part be x .

7 times the first part = $7x$

Let the other part be $(24 - x)$.

5 times the second part = $5(24 - x)$

$$\therefore 7x + 5(24 - x) = 146$$

$$\Rightarrow 7x + 120 - 5x = 146$$

$$\Rightarrow 7x - 5x = 146 - 120$$

$$\Rightarrow 2x = 26$$

$$\Rightarrow x = \frac{26}{2} = 13$$

Therefore, one part is 13.

Other part = $(24 - x) = (24 - 13) = 11$

Q5. Answer :

Let the number be x .

Fifth part increased by 5 = $\frac{x}{5} + 5$

Fourt part diminished by 5 = $\frac{x}{4} - 5$

$$\therefore \frac{x}{5} + 5 = \frac{x}{4} - 5$$

$$\Rightarrow 5 + 5 = \frac{x}{4} - \frac{x}{5}$$

$$\Rightarrow 10 = \frac{5x - 4x}{20}$$

$$\Rightarrow 10 = \frac{x}{20}$$

$$\Rightarrow 200 = x$$

$$\Rightarrow x = 200$$

Therefore, the number is 200.

Q6. Answer :

Let the common multiple for the given three numbers be x .

Then, the three numbers would be $4x$, $5x$ and $6x$.

$$\therefore 4x + 6x = 5x + 55$$

$$\Rightarrow 10x = 5x + 55$$

$$\Rightarrow 10x - 5x = 55$$

$$\Rightarrow 5x = 55$$

$$\Rightarrow x = \frac{55}{5} = 11$$

$$\therefore \text{Smallest number} = 4x = 4(11) = 44$$

$$\text{Largest number is} = 6x = 6(11) = 66$$

$$\text{Third number} = 5x = 5(11) = 55$$

Therefore, the three numbers are 44, 55 and 66.

Q7. Answer :

Let the number be x .

$$\therefore 10 + 4x = 5x - 5$$

$$\Rightarrow 10 + 5 = 5x - 4x$$

$$\Rightarrow 15 = x$$

$$\Rightarrow x = 15 \text{ (by transposition)}$$

Therefore, the number is 15.

Q8.

Answer :

Let us consider x as the common multiple of both the number.

Then, first number = $3x$

Second number = $5x$

$$\therefore \frac{3x + 10}{5x + 10} = \frac{5}{7}$$

$$\Rightarrow 7(3x + 10) = 5(5x + 10) \quad (\text{by cross multiplication})$$

$$\Rightarrow 21x + 70 = 25x + 50$$

$$\Rightarrow 21x - 25x = 50 - 70$$

$$\Rightarrow -4x = -20$$

$$\Rightarrow x = \frac{-20}{-4} = 5$$

Therefore, the common multiple of both the numbers is 5.

First number = $3x = 3 \times 5 = 15$

Second number = $5x = 5 \times 5 = 25$



Q9.

Answer :Let the first odd number be x .Let the second odd number be $(x + 2)$.Let the third odd number be $(x + 4)$.

$$\therefore x + (x + 2) + (x + 4) = 147$$

$$\Rightarrow x + x + 2 + x + 4 = 147$$

$$\Rightarrow 3x + 6 = 147$$

$$\Rightarrow 3x = 147 - 6$$

$$\Rightarrow 3x = 141$$

$$\Rightarrow x = \frac{141}{3} = 47$$

Therefore, the first odd number is 47.

$$\text{Second odd number} = (x + 2) = (47 + 2) = 49$$

$$\text{Third odd number} = (x + 4) = (47 + 4) = 51$$

Q10.

Answer :Let the first even number be x .Let the second even number be $x + 2$.Let the third even number be $x + 4$.

$$\therefore x + x + 2 + x + 4 = 234$$

$$\Rightarrow x + x + 2 + x + 4 = 234$$

$$\Rightarrow 3x + 6 = 234$$

$$\Rightarrow 3x = 234 - 6$$

$$\Rightarrow 3x = 228$$

$$\Rightarrow x = \frac{228}{3} = 76$$

$$\therefore \text{First even number} = x = 76$$

$$\text{Second even number} = x + 2 = 76 + 2 = 78$$

$$\text{Third even number} = x + 4 = 80$$

Q11. **Answer :**Let the digit in *the* units place be x .

$$\text{Digit in the tens place} = (12 - x)$$

$$\therefore \text{Original number} = 10(12 - x) + x = 120 - 9x$$

On reversing the digits, we have x at the tens place and $(12 - x)$ at the units place.

$$\therefore \text{New number} = 10x + 12 - x = 9x + 12$$

$$\text{New number} - \text{Original number} = 54$$

$$\Rightarrow 9x + 12 - (120 - 9x) = 54$$

$$\Rightarrow 9x + 12 - 120 + 9x = 54$$

$$\Rightarrow 18x - 108 = 54$$

$$\Rightarrow 18x = 54 + 108$$

$$\Rightarrow 18x = 162$$

$$\Rightarrow x = \frac{162}{18} = 9$$

Therefore, the digit in *the* units place is 9.

$$\text{Digit in tens place} = (12 - x) = (12 - 9) = 3$$

Therefore, the original number is 39.

Check :

The original number is 39.

$$\text{Sum of the digits in the original number} = (3 + 9) = 12$$

$$\text{New number obtained on reversing the digits} = 93$$

$$\text{New number} - \text{Original number} = (93 - 39) = 54$$

Thus, both the given conditions are satisfied by 39.

Hence, the original number is 39.



Q12.

Answer :Let the digit in *the* units place be x .Digit in *the* tens place = $3x$

$$\text{Original number} = 10(3x) + x = 30x + x$$

On reversing the digits, we have x at the tens place and $(3x)$ at the units place.

$$\therefore \text{New number} = 10(x) + 3x = 10x + 3x$$

$$\text{New number} = \text{Original number} - 36$$

$$\Rightarrow 10x + 3x = 30x + x - 36$$

$$\Rightarrow 13x = 31x - 36$$

$$\Rightarrow 36 = 31x - 13x$$

$$\Rightarrow 36 = 18x$$

$$\Rightarrow 18x = 36$$

$$\Rightarrow x = \frac{36}{18} = 2$$

Therefore, the digit in *the* units place is 2.

$$\text{Digit in } \textit{the} \text{ tens place} = (3x) = 3 \times 2 = 6$$

Therefore, the original number is 62.

Check :

$$\text{New number} + 36 = \text{Original Number}$$

$$26 + 36 = 62$$

Hence, both the conditions are satisfied.

Therefore, the original number *is* 62.

Q13.

Answer :Let the numerator be x .

The denominator is greater than the numerator by 7.

$$\therefore (x+7)$$

$$\therefore \frac{x+17}{(x+7)-6} = 2$$

$$\Rightarrow \frac{x+17}{x+1} = 2$$

$$\Rightarrow x + 17 = 2(x + 1) \quad (\text{by cross multiplication})$$

$$\Rightarrow x + 17 = 2x + 2$$

$$\Rightarrow x - 2x = 2 - 17$$

$$\Rightarrow -x = -15$$

$$\Rightarrow x = 15$$

Therefore, the numerator is 15.

$$\text{Denominator} = (x+7) = (15+7) = 22$$

$$\therefore \text{Original number} = \frac{15}{22}$$

Q14.



Denominator, $d = x$

It is given that twice the numerator is equal to two more than the denominator.

$$\therefore \text{Twice of numerator, } 2n = x + 2$$

$$\therefore \text{Numerator, } n = \frac{x+2}{2}$$

$$\therefore \frac{n+3}{d+3} = \frac{2}{3}$$

$$\Rightarrow 3(n+3) = 2(d+3) \quad (\text{by cross multiplication})$$

$$\Rightarrow 3n + 9 = 2d + 6$$

$$\Rightarrow 3n - 2d = 6 - 9$$

$$\Rightarrow 3n - 2d = -3$$

On replace d by x and n by $\frac{x+2}{2}$:

$$\Rightarrow 3\left(\frac{x+2}{2}\right) - 2x = -3$$

$$\Rightarrow \frac{3x+6-4x}{2} = -3 \quad (\text{taking the L.C.M. of 2 and 1 as 2})$$

$$\Rightarrow 6 - x = -6 \quad (\text{by cross multiplication})$$

$$\Rightarrow -x = -6 - 6$$

$$\Rightarrow x = 12$$

The denominator is 12.

$$\therefore \text{Numerator} = \frac{x+2}{2} = \frac{12+2}{2} = \frac{14}{2} = 7$$

$$\therefore \text{Original fraction} = \frac{7}{12}$$

Q15.

Answer :

Let the breadth of the original rectangle be x cm.

Then, its length will be $(x+7)$ cm.

The area of the rectangle will be $(x)(x+7)$ cm².

$$\therefore (x+3)(x+7-4) = (x)(x+7)$$

$$\Rightarrow (x+3)(x+3) = x^2 + 7x$$

$$\Rightarrow x^2 + 3x + 3x + 9 = x^2 + 7x$$

$$\Rightarrow x^2 + 6x + 9 = x^2 + 7x$$

$$\Rightarrow 9 = x^2 - x^2 + 7x - 6x$$

$$\Rightarrow 9 = x$$

$$\Rightarrow x = 9 \quad (\text{by transposition})$$

Breadth of the original rectangle = 9 cm

$$\text{Length of the original rectangle} = (x+7) = (9+7) = 16 \text{ cm}$$

Q16.

Answer :

Let the width of the rectangle be x cm.

It is $\frac{2}{3}$ of the length of the rectangle.

This means that the length of the rectangle will be $\frac{3}{2}x$.

$$\text{Perimeter of the rectangle} = 2(x) + 2\left(\frac{3}{2}x\right) = 180 \text{ m}$$

$$\therefore 2x + \frac{6x}{2} = 180$$

$$\Rightarrow \frac{4x+6x}{2} = 180 \quad (\text{taking the L.C.M. of 1 on the L.H.S. of the equation})$$

$$\Rightarrow 10x = 2 \times 180 \quad (\text{by cross multiplication})$$

$$\Rightarrow 10x = 360$$

$$\Rightarrow x = \frac{360}{10} = 36$$

Therefore, the width of the rectangle is 36 m.

$$\text{Length of the rectangle will be} = \frac{3}{2}x = \frac{3}{2}(36) = 54 \text{ m}$$

Q17.



Let the length of the base of the triangle be x cm.

Then, its altitude will be $\frac{5}{3}x$ cm.

$$\text{Area of the triangle} = \frac{1}{2}(x)\left(\frac{5}{3}x\right) = \frac{5}{6}x^2$$

$$\therefore \frac{1}{2}(x-2)\left(\frac{5}{3}x+4\right) = \frac{5}{6}x^2$$

$$\Rightarrow \left(\frac{x-2}{2}\right)\left(\frac{5x+12}{3}\right) = \frac{5x^2}{6}$$

$$\Rightarrow \frac{(x-2)(5x+12)}{6} = \frac{5x^2}{6}$$

$$\Rightarrow \frac{5x^2 + 12x - 10x - 24}{6} = \frac{5x^2}{6}$$

$$\Rightarrow 5x^2 + 2x - 24 = 5x^2 \quad \left(\text{cancelling the denominators from both the sides since they are same}\right)$$

$$\Rightarrow 5x^2 - 5x^2 + 2x = 24$$

$$\Rightarrow 2x = 24$$

$$\Rightarrow x = \frac{24}{2} = 12 \text{ m}$$

Therefore, the base of the triangle is 12 m.

$$\text{Altitude of the triangle} = \frac{5}{3}x = \frac{5}{3}(12) = 20 \text{ m}$$

Q18

Answer :

Let the common multiple of all the three angles be x .

Then, the first angle will be $4x$.

And the second angle will be $5x$.

In a triangle, sum of all the three angles will be equal to 180° .

$$\therefore \text{Third angle} = 180 - (4x + 5x) = 180 - 9x$$

$$\therefore 4x + 5x = 180 - 9x$$

$$\Rightarrow 9x = 180 - 9x$$

$$\Rightarrow 9x + 9x = 180$$

$$\Rightarrow 18x = 180$$

$$\Rightarrow x = \frac{180}{18} = 10$$

$$\text{First angle} = 4x = 4 \times 10 = 40^\circ$$

$$\text{Second angle} = 5x = 5 \times 10 = 50^\circ$$

$$\text{Third angle} = 4x + 5x = 9x = 9 \times 10 = 90^\circ$$

Q19

Answer :

Let the speed of the steamer in still water be x km/h.

Speed (downstream) = $(x + 1)$ km/h

Speed (upstream) = $(x - 1)$ km/h

Distance covered in 9 hours while going downstream = $9(x + 1)$ km

Distance covered in 10 hours while going upstream = $10(x - 1)$ km

But both of these distances will be same.

$$9(x + 1) = 10(x - 1)$$

$$\Rightarrow 9x + 9 = 10x - 10$$

$$\Rightarrow 9 + 10 = 10x - 9x$$

$$\Rightarrow 19 = x$$

$$\Rightarrow x = 19$$

Therefore, the speed of the steamer in still water is 19 km/h.

$$\text{Distance between the ports} = 9(x + 1) = 9(19 + 1) = 9 \times 20 = 180 \text{ km}$$

Q20



Answer :

Let the speed of one motorcyclist be x km/h.

So, the speed of the other motorcyclist will be $(x + 7)$ km/h.

Distance travelled by the first motorcyclist in 2 hours = $2x$ km

Distance travelled by the second motorcyclist in 2 hours = $2(x + 7)$ km

Therefore,

$$300 - (2x + (2x + 14)) = 34$$

$$\Rightarrow 300 - (2x + 2x + 14) = 34$$

$$\Rightarrow 300 - 4x - 14 = 34$$

$$\Rightarrow 286 - 4x = 34$$

$$\Rightarrow 286 - 34 = 4x$$

$$\Rightarrow 252 = 4x$$

$$\Rightarrow x = \frac{252}{4} = 63$$

Therefore, the speed of the first motorcyclist is 63 km/h.

The speed of the second motorcyclist is $(x + 7) = (63 + 7) = 70$ km/h.

Check :

The distance covered by the first motorcyclist in 2 hours = $63 \times 2 = 126$ km

The distance covered by the second motorcyclist in 2 hours = $70 \times 2 = 140$ km

The distance between the motorcyclists after 2 hours = $300 - (126 + 140) =$

34 km (which is the same as given)

Therefore, the speeds of the motorcyclists are 63 km/h and 70 km/h, respectively.

Q21

Answer :

Let the first number be x .

Then, the second number will be $\frac{5}{6}x$.

Third number = $\frac{4}{5}(\frac{5}{6}x) = \frac{2}{3}x$

$$\therefore x + \frac{5x}{6} + \frac{2x}{3} = 150$$

$$\Rightarrow \frac{6x + 5x + 4x}{6} = 150 \quad (\text{multiplying the L.H.S. by 6, which is the L.C.M. of 1, 6 and 3})$$

$$\Rightarrow 15x = 150 \times 6 \quad (\text{by cross multiplication})$$

$$\Rightarrow 15x = 900$$

$$\Rightarrow x = \frac{900}{15} = 60$$

Therefore, the first number is 60.

$$\text{Second number} = \frac{5}{6}x = \frac{5}{6}(60) = 50$$

$$\text{Third number} = \frac{2}{3}x = \frac{2}{3}(60) = 40$$

Q22

Answer :

Let the first part be x .

Let the second part be $(4500 - x)$.

$$\therefore 5\% \text{ of } x = 10\% \text{ of } (4500 - x)$$

$$\Rightarrow \left(\frac{5}{100}\right)x = \left(\frac{10}{100}\right)(4500 - x)$$

$$\Rightarrow \frac{5x}{100} = \frac{45000 - 10x}{100}$$

$$\Rightarrow 5x = 45000 - 10x \quad (\text{by cancellation of same denominators from both the sides}) \Rightarrow 5x + 10x = 45000 \Rightarrow 15x = 45000 \Rightarrow x = \frac{45000}{15} = 3000$$

$$\text{Therefore, the first part is 3000. Second part} = (4500 - x) = (4500 - 3000) = 1500$$

Q23



Answer :

Let the present age of Rakhi be x .

Then, the present age of Rakhi's mother will be $4x$.

After five years, Rakhi's age will be $(x + 5)$.

After five years, her mother's age will be $(4x + 5)$.

$$4x + 5 = 3(x + 5)$$

$$\Rightarrow 4x + 5 = 3x + 15$$

$$\Rightarrow 4x - 3x = 15 - 5$$

$$\Rightarrow x = 10$$

Present age of Rakhi = 10 years

Present age of Rakhi's mother = $4(x) = 4 \times 10 = 40$ years

Q24

Answer :

Let the age of Monu's father be x years.

The age of Monu's grandfather will be $(x + 26)$.

Then, the age of Monu will be $(x - 29)$.

$$\therefore x + (x + 26) + (x - 29) = 135$$

$$\Rightarrow x + x + 26 + x - 29 = 135$$

$$\Rightarrow 3x - 3 = 135$$

$$\Rightarrow 3x = 135 + 3$$

$$\Rightarrow 3x = 138$$

$$\Rightarrow x = \frac{138}{3} = 46$$

\therefore Age of Monu's father = 46 years

Age of Monu's grandfather = $(x + 26) = (46 + 26) = 72$ years

Age of Monu = $(x - 29) = 46 - 29 = 17$ years

Q25

Answer :

Let the age of the grandson be x years.

Then, his grandfather's age will be $10x$.

Also, the grandfather is 54 years older than his grandson.

\therefore Age of the grandson = $x + 54$

$$10x = x + 54$$

$$\Rightarrow 10x - x = 54$$

$$\Rightarrow 9x = 54$$

$$\Rightarrow x = \frac{54}{9} = 6$$

Therefore, the grandson's age is 6 years.

Grandfather's age = $10(x) = 10 \times 6 = 60$ years

Q26

Answer :

Let the age of the younger cousin be x .

Then, the age of the elder cousin will be $(x + 10)$.

15 years ago :

Age of the younger cousin = $(x - 15)$

Age of elder cousin = $(x + 10 - 15)$

$$= (x - 5)$$

$$\therefore (x - 5) = 2(x - 15)$$

$$\Rightarrow x - 5 = 2x - 30$$

$$\Rightarrow x - 2x = -30 + 5$$

$$\Rightarrow -x = -25$$

$$\Rightarrow x = 25$$

Therefore, the present age of the younger cousin is 25 years.

Present age of elder cousin = $(x + 10) = (25 + 10) = 35$ years

Q27



Answer :

Let the number of deer in the herd be x .

The number of deer grazing in the field is $\left(\frac{1}{2}\right)x$.

$$\text{Remaining deer} = x - \frac{x}{2} = \frac{x}{2}$$

$$\text{Number of deer playing nearby} = \frac{3}{4} \left(\frac{x}{2}\right) = \frac{3}{8}x$$

The number of deer drinking water from the pond is 9.

$$\therefore 9 + \frac{3}{8}x + \frac{1}{2}x = x$$

$$\Rightarrow \frac{72 + 3x + 4x}{8} = x \quad \left(\text{multiplying the L.H.S. by 8, which is the L.C.M. of 1, 8 and 2}\right)$$

$$\Rightarrow 72 + 7x = 8x \quad \left(\text{by cross multiplication}\right) \Rightarrow 72 = 8x - 7x \Rightarrow 72 =$$

$$x \Rightarrow x = 72 \text{ Total number of deer in the herd} = 72$$



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Linear Equations

Ex 8C

Q1

Answer :

(c) 5

$$\begin{aligned}2x - 3 &= x + 2 \\ \Rightarrow 2x - x &= 3 + 2 \\ \Rightarrow x &= 5\end{aligned}$$

Q2

Answer :

(b) -5

$$\begin{aligned}5x + \frac{7}{2} &= \frac{3}{2}x - 14 \\ \Rightarrow \frac{10x + 7}{2} &= \frac{3x - 28}{2} \\ \Rightarrow 10x + 7 &= 3x - 28 \\ \Rightarrow 10x - 3x &= -28 - 7 \\ \Rightarrow 7x &= -35 \\ \Rightarrow x &= \frac{-35}{7} = -5\end{aligned}$$

Q3

Answer :

(a) 40

$$\begin{aligned}z &= \frac{4}{5}(z + 10) \\ \Rightarrow 5z &= 4(z + 10) \\ \Rightarrow 5z &= 4z + 40 \\ \Rightarrow 5z - 4z &= 40 \\ \Rightarrow z &= 40\end{aligned}$$

Q4

Answer :(c) $\frac{4}{5}$

$$\begin{aligned}3m &= 5m - \frac{8}{5} \\ \Rightarrow 3m &= \frac{25m - 8}{5} \\ \Rightarrow 15m &= 25m - 8 \\ \Rightarrow 15m - 25m &= -8 \\ \Rightarrow -10m &= -8 \\ \Rightarrow m &= \frac{-8}{-10} = \frac{4}{5}\end{aligned}$$

Q5

Answer :

(b) -1

$$\begin{aligned}5t - 3 &= 3t - 5 \\ \Rightarrow 5t - 3t &= 3 - 5 \\ \Rightarrow 2t &= -2 \\ \Rightarrow t &= \frac{-2}{2} = -1\end{aligned}$$

Q6

Answer :(d) $\frac{7}{3}$

$$\begin{aligned}2y + \frac{5}{3} &= \frac{26}{3} - y \\ \Rightarrow \frac{6y + 5}{3} &= \frac{26 - 3y}{3} \\ \Rightarrow 6y + 5 &= 26 - 3y \\ \Rightarrow 6y + 3y &= 26 - 5 \\ \Rightarrow 9y &= 21 \\ \Rightarrow y &= \frac{21}{9} = \frac{7}{3}\end{aligned}$$

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Answer :

(b) -1

$$\begin{aligned}\frac{6x+1}{3} + 1 &= \frac{x-3}{6} \\ \Rightarrow \frac{6x+1+3}{3} &= \frac{x-3}{6} \\ \Rightarrow 6(6x+4) &= 3(x-3) \\ \Rightarrow 36x+24 &= 3x-9 \\ \Rightarrow 36x-3x &= -24-9 \\ \Rightarrow 33x &= -33 \\ \Rightarrow x &= \frac{-33}{33} = -1\end{aligned}$$

Q8

Answer :

(c) 36

$$\begin{aligned}\frac{n}{2} - \frac{3n}{4} + \frac{5n}{6} &= 21 \\ \Rightarrow \frac{6n-9n+10n}{12} &= 21 \\ \Rightarrow 7n &= 21 \times 12 \\ \Rightarrow 7n &= 252 \\ \Rightarrow n &= \frac{252}{7} = 36\end{aligned}$$

Q9

Answer :

(d) $\frac{1}{2}$

$$\begin{aligned}\frac{x+1}{2x+3} &= \frac{3}{8} \\ \Rightarrow 8(x+1) &= 3(2x+3) \\ \Rightarrow 8x+8 &= 6x+9 \\ \Rightarrow 8x-6x &= 9-8 \\ \Rightarrow 2x &= 1 \\ \Rightarrow x &= \frac{1}{2}\end{aligned}$$

Q10

Answer :

(c) 8

$$\begin{aligned}\frac{4x+8}{5x+8} &= \frac{5}{6} \\ \Rightarrow 6(4x+8) &= 5(5x+8) \\ \Rightarrow 24x+48 &= 25x+40 \\ \Rightarrow 24x-25x &= -48+40 \\ \Rightarrow -x &= -8 \\ \Rightarrow x &= 8\end{aligned}$$

Q11

Answer :

(d) 12

$$\begin{aligned}\frac{n}{n+15} &= \frac{4}{9} \\ \Rightarrow 9n &= 4(n+15) \\ \Rightarrow 9n &= 4n+60 \\ \Rightarrow 9n-4n &= 60 \\ \Rightarrow 5n &= 60 \\ \Rightarrow n &= \frac{60}{5} = 12\end{aligned}$$

Q12

Answer :

(a) -2

$$\begin{aligned}3(t-3) &= 5(2t+1) \\ \Rightarrow 3t-9 &= 10t+5 \\ \Rightarrow 3t-10t &= 9+5 \\ \Rightarrow -7t &= 14 \\ \Rightarrow -t &= \frac{14}{7} = 2 \\ \Rightarrow t &= -2\end{aligned}$$

Q13

**Answer :**

(c) 80

Let the number be x .

$$\therefore \frac{4}{5}x = \frac{3}{4}x + 4$$

$$\Rightarrow \frac{4x}{5} = \frac{3x+16}{4}$$

$$\Rightarrow 16x = 15x + 80$$

$$\Rightarrow 16x - 15x = 80$$

$$\Rightarrow x = 80$$

Q14

Answer :

(b) 28 years

Let x be the common multiple of the ages of A and B.Then, the ages of A and B would be $5x$ and $7x$, respectively.

$$\therefore \frac{5x+4}{7x+4} = \frac{3}{4}$$

$$\Rightarrow 4(5x+4) = 3(7x+4)$$

$$\Rightarrow 20x + 16 = 21x + 12$$

$$\Rightarrow 16 - 12 = 21x - 20x$$

$$\Rightarrow 4 = x$$

$$\Rightarrow x = 4$$

$$\therefore \text{Age of B} = 7(x) = 7 \times 4 \\ = 28 \text{ years}$$

Q15

Answer :

(b) 5 cm

Let the equal side of the isosceles triangle be x .Then, the perimeter of the triangle would be $(x + x + 6)$.

$$\therefore 2x + 6 = 16$$

$$\Rightarrow 2x = 16 - 6$$

$$\Rightarrow 2x = 10$$

$$\Rightarrow x = \frac{10}{2} = 5$$

$$\therefore \text{Length of each equal side} = 5 \text{ cm}$$

Q16

Answer :

(d) 17

Let the three consecutive integers be x , $x+1$ and $x+2$.

$$\text{Equation} = x + x + 1 + x + 2 = 51$$

$$\Rightarrow 3x + 3 = 51$$

$$\Rightarrow 3x = 51 - 3$$

$$\Rightarrow 3x = 48$$

$$\Rightarrow x = \frac{48}{3} = 16$$

$$\text{Middle integer} = x + 1 = 16 + 1 = 17$$

Q17

Answer :

(a) 40

Let the numbers be x and $x + 15$.

$$\therefore x + x + 15 = 95$$

$$\Rightarrow 2x + 15 = 95$$

$$\Rightarrow 2x = 95 - 15$$

$$\Rightarrow 2x = 80$$

$$\Rightarrow x = 40$$

The smaller number is 40.

Q18



Answer :

(c) 48

Let the number of boys in the class be x .

Then, the number of girls will be $(x - 8)$.

The equation becomes :

$$\frac{x}{x-8} = \frac{7}{5}$$

$$\Rightarrow 5x = 7x - 56$$

$$\Rightarrow 5x - 7x = -56$$

$$\Rightarrow -2x = -56$$

$$\Rightarrow x = \frac{-56}{-2} = 28$$

Therefore, the number of boys is 28.

$$\text{Number of girls} = (x - 8) = 28 - 8 = 20$$

$$\text{Total strength of the class} = 28 + 20 = 48$$



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