



# Linear Equations in Two Variables

- **Linear Equation in two Variables:** Equation of the form:  $ax + by + c = 0$   
Here,  $a$ ,  $b$  and  $c$  are real numbers, where  $a$  and  $b$  are not both zero.  
Example:  $2x + 3y - 9 = 0$  is a linear equation of two variables because 2, 3 &  $-9$  are all real numbers and also both  $a, b \neq 0$ .
- There are infinitely many solutions for a linear equation of two variables.
- The graph of every linear equation in two variables is a straight line.

## Solution of an Equation in Two Variables

### Example:

Given the equation  $2x + 3y = 18$ , determine if the ordered pair (3, 4) is a solution to the equation.

We substitute 3 in for  $x$  and 4 in for  $y$ .

$$2(3) + 3(4) ? 18$$

$$6 + 12 ? 18$$

$$18 = 18 \text{ True.}$$

**Therefore, the ordered pair (3, 4) is a solution to the equation  $2x + 3y = 18$ .**

## Exercise 8A

### Question 1:

(i) The given equation is  $x = 5$

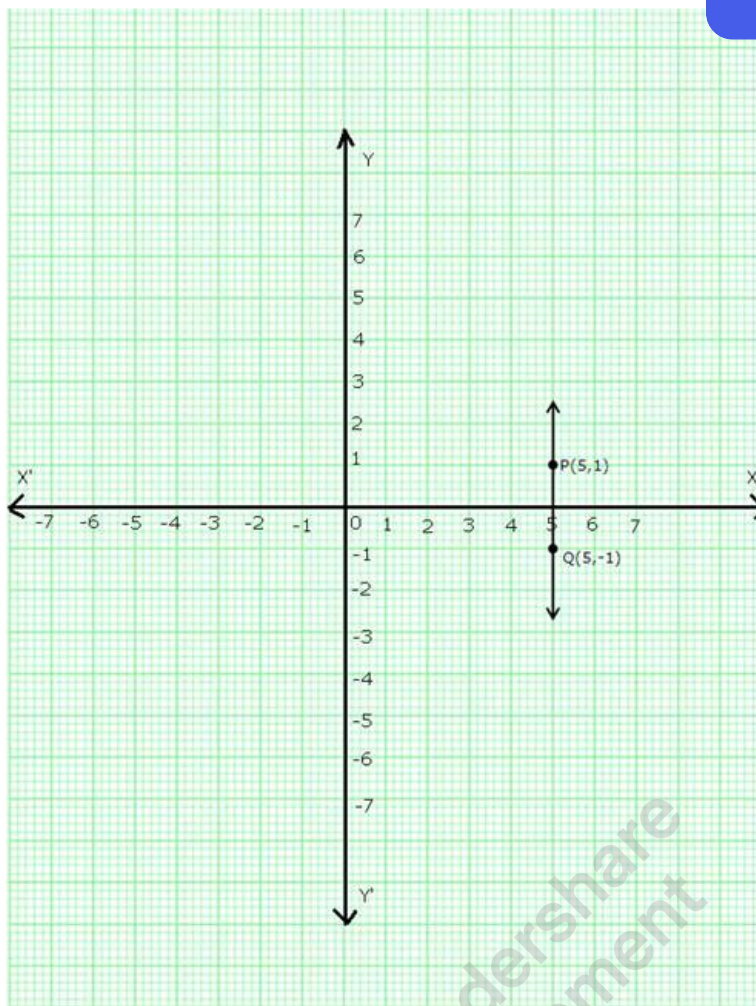
Take two solutions of the given equation as  $x = 5, y = 1$  and  $x = 5, y = -1$

Thus we get the following table:

$x$	5	5
$y$	1	-1

Plot points P(5,1) and Q(5,-1) on the graph paper.

Join PQ. The line PQ is the required graph.



(ii) The given equation is  $y = -2$

Take two solutions of the given equation as  $x = 1, y = -2$  and  $x = 2, y = -2$ .

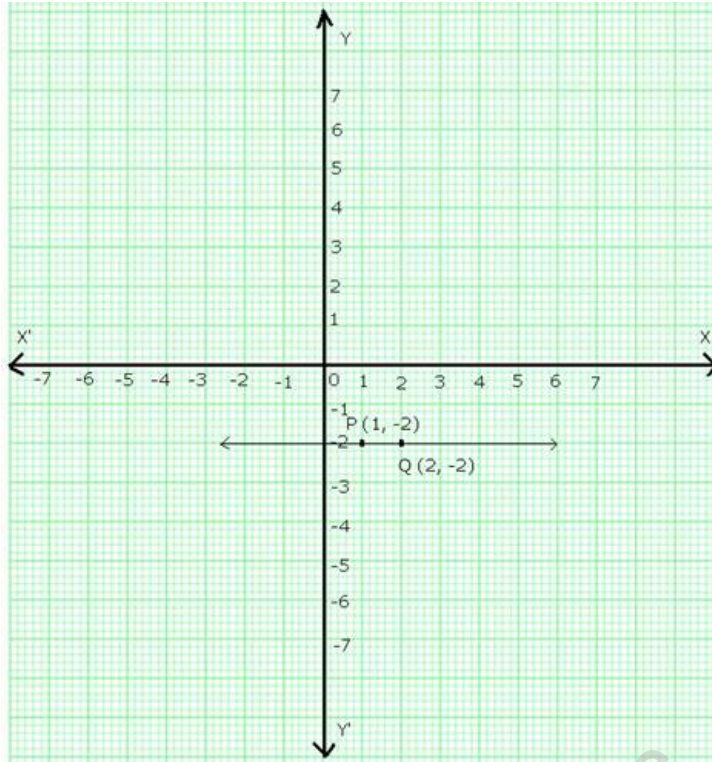
Thus we have the following table:

x	1	2
y	-2	-2

Plot points  $P(1, -2)$  and  $Q(2, -2)$  on the graph paper. Join  $PQ$ . The line  $PQ$  is the required



graph.



(iii) The given equation is

$$x + 6 = 0$$

$$\Rightarrow x = -6$$

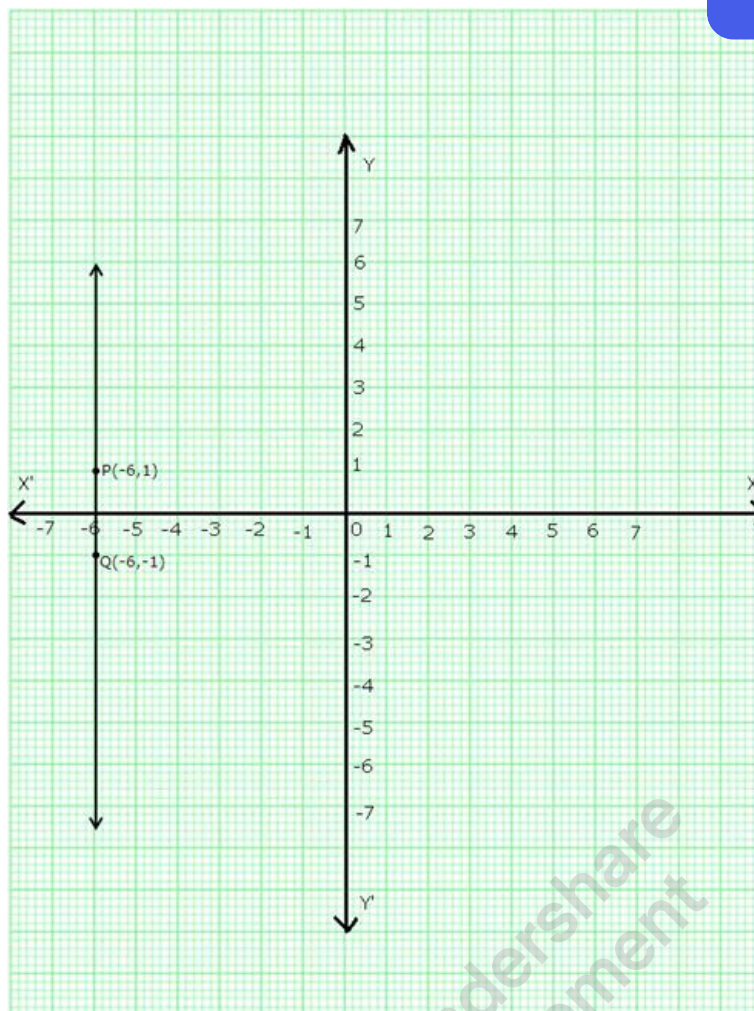
$$\text{Let } x = -6 \text{ \& } y = 1$$

$$x = -6 \text{ \& } y = -1$$

x	-6	-6
y	1	-1

Plot points P(-6,1) and Q(-6,-1) on the graph paper. Join PQ. The line PQ is the required graph.





(iv) The given equation is

$$x + 7 = 0$$

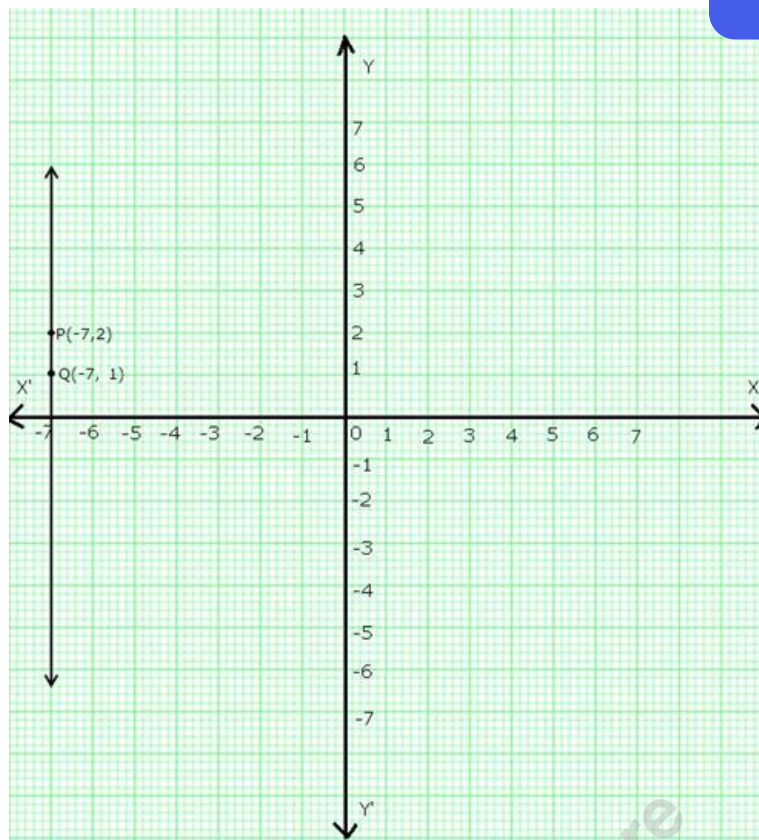
$$\Rightarrow x = -7$$

Let  $x = -7, y = 2$  and  $x = -7, y = 1$

Thus we have the following table:

x	-7	-7
y	2	1

Plot points  $P(-7, 2)$  and  $Q(-7, 1)$  on the graph paper. Join PQ. The line PQ is the required graph.



(v)  $y = 0$  represents the x-axis

(vi)  $x = 0$  represents the y-axis.

### Question 2:

The given equation is  $y = 3x$ .

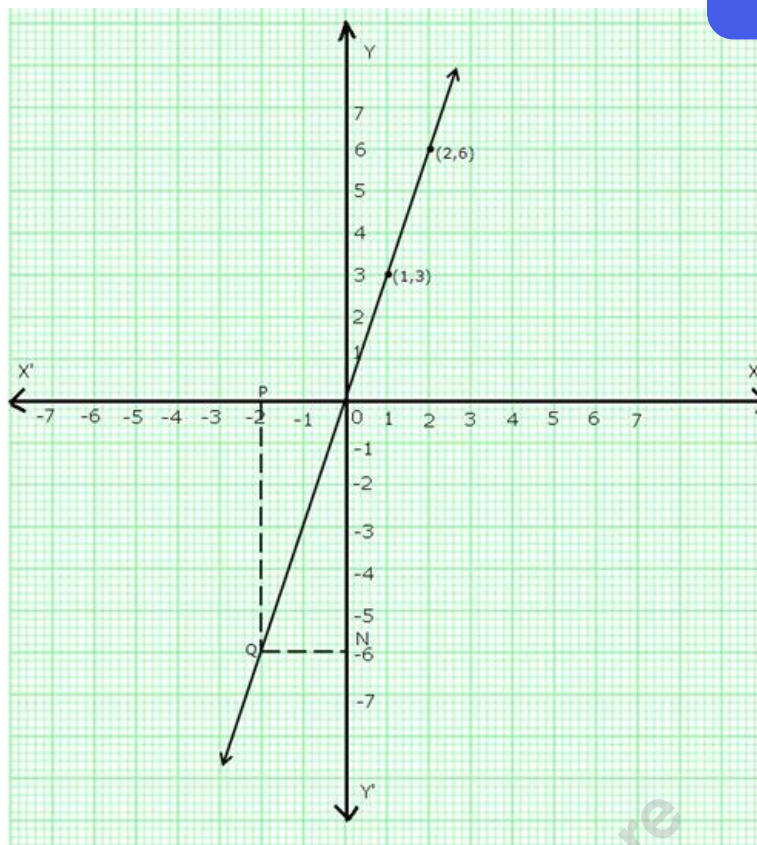
Putting  $x = 1$ ,  $y = 3(1) = 3$

Putting  $x = 2$ ,  $y = 3(2) = 6$

Thus, we have the following table:

x	1	2
y	3	6

Plot points (1,3) and (2,6) on a graph paper and join them to get the required graph.



Take a point P on the left of y-axis such that the distance of point P from the y-axis is 2 units.

Draw PQ parallel to y-axis cutting the line  $y = 3x$  at Q. Draw QN parallel to x-axis meeting y-axis at N.

So,  $y = ON = -6$ .

### Question 3:

The given equation is,

$$x + 2y - 3 = 0$$

$$\Rightarrow x = 3 - 2y$$

$$\text{Putting } y = 1, x = 3 - (2 \times 1) = 1$$

$$\text{Putting } y = 0, x = 3 - (2 \times 0) = 3$$

Thus, we have the following table:

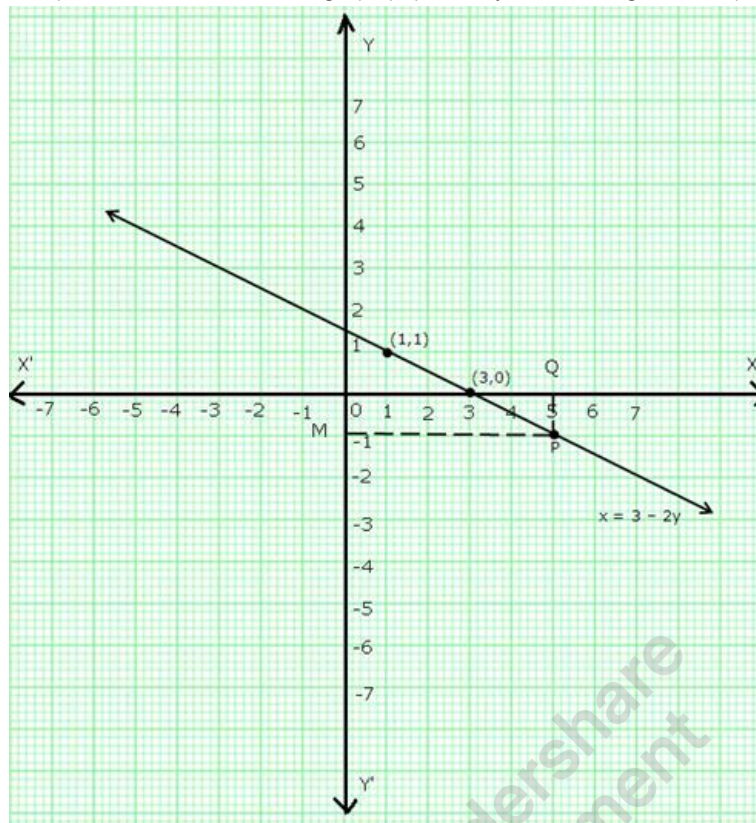
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x	1	3
y	1	0

Plot points (1,1) and (3,0) on a graph paper and join them to get the required graph.



Take a point Q on x-axis such that  $OQ = 5$ .

Draw QP parallel to y-axis meeting the line ( $x = 3 - 2y$ ) at P.

Through P, draw PM parallel to x-axis cutting y-axis at M.

So,  $y = OM = -1$ .

#### Question 4:

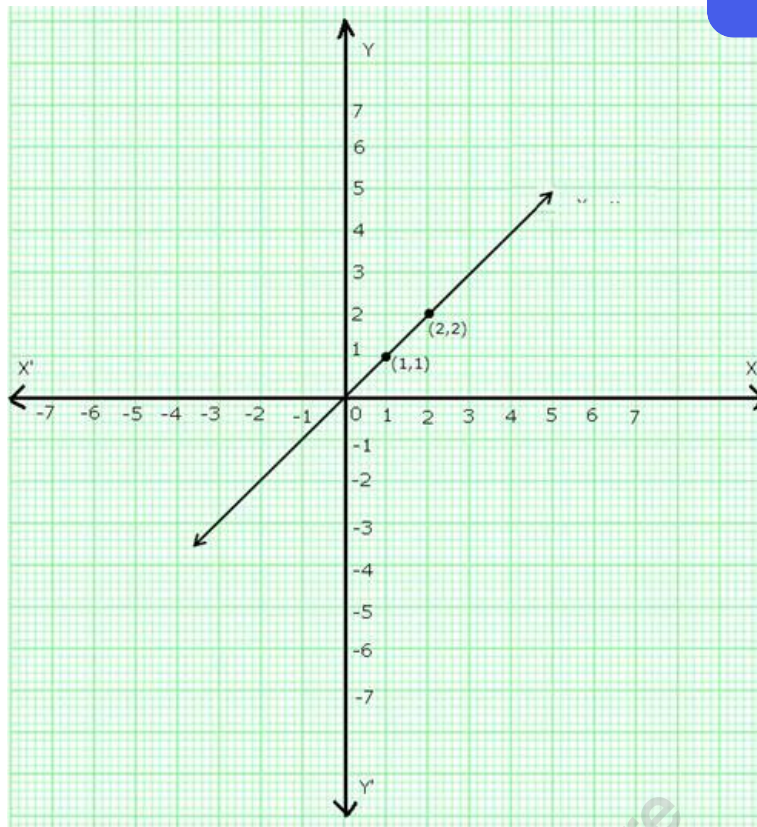
(i) The given equation is  $y = x$

Let  $x = 1$ , then  $y = 1$  and let  $x = 2$ , then  $y = 2$

Thus, we have the following table:

x	1	2
y	1	2

Plot points (1,1) and (2,2) on a graph paper and join them to get the required graph.



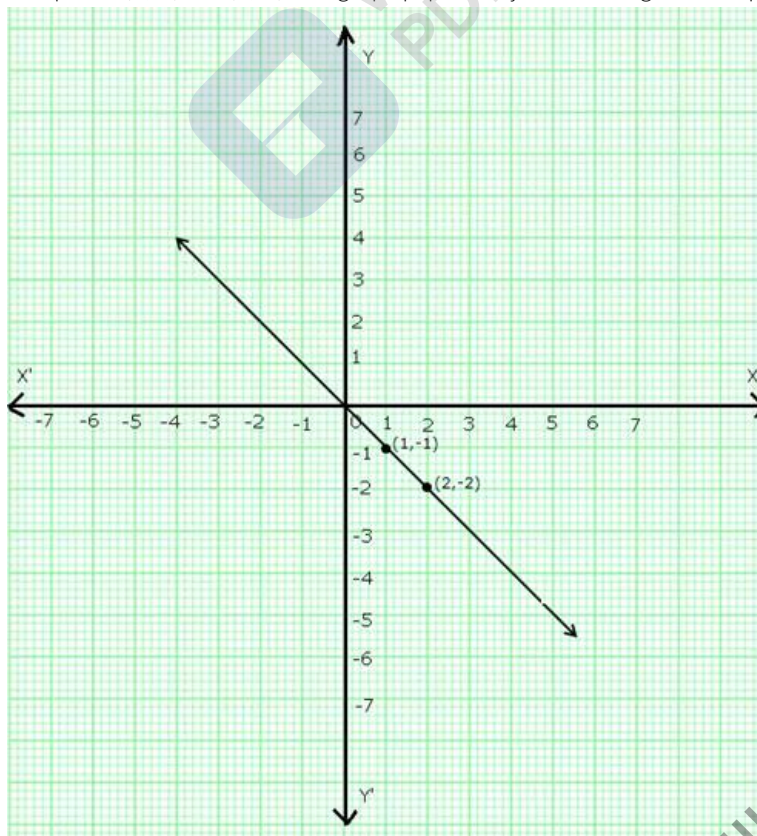
(ii) The given equation is  $y = -x$

Now, if  $x = 1$ ,  $y = -1$  and if  $x = 2$ ,  $y = -2$

Thus, we have the following table:

x	1	2
y	-1	-2

Plot points  $(1, -1)$  and  $(2, -2)$  on a graph paper and join them to get the required graph.



(iii) The given equation is  $y + 3x = 0$

$$\Rightarrow y = -3x$$

Now, if  $x = -1$ , then  $y = -3(-1) = 3$



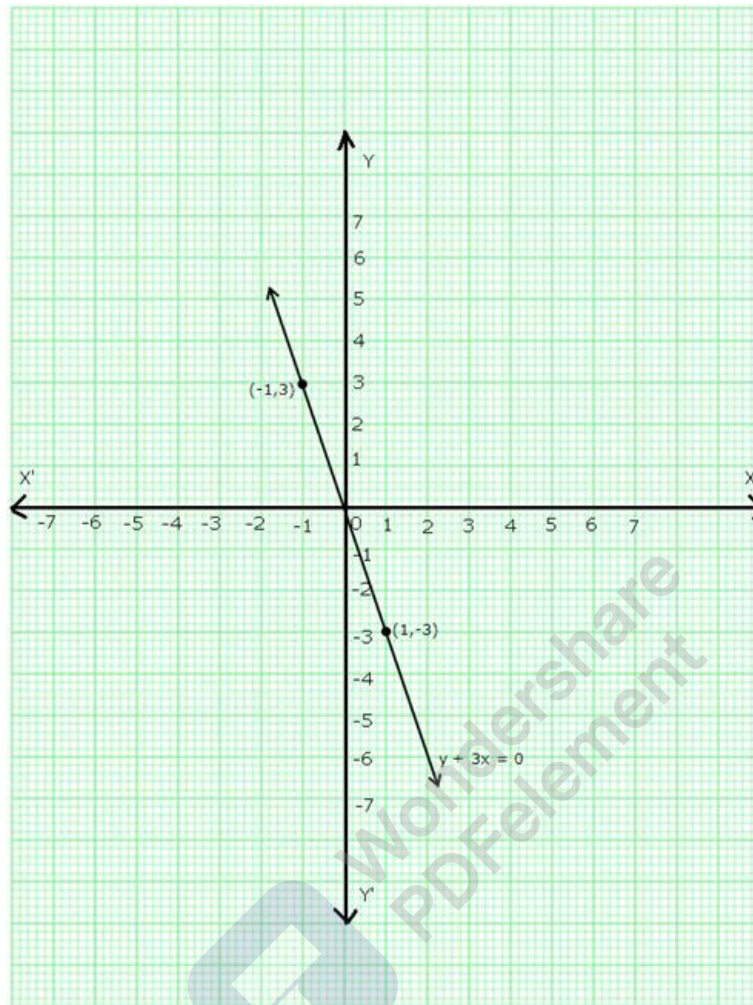


And, if  $x = 1$ , then  $y = -3(1) = -3$

Thus we have the following table:

x	1	-1
y	-3	3

Plot points  $(1, -3)$  and  $(-1, 3)$  on a graph paper and join them to get the required graph.



(iv) The given equation is  $2x + 3y = 0$

$$\Rightarrow y = \frac{-2}{3}x$$

Now, if  $x = 3$ , then

$$y = \frac{-2}{3} \times 3 = -2$$

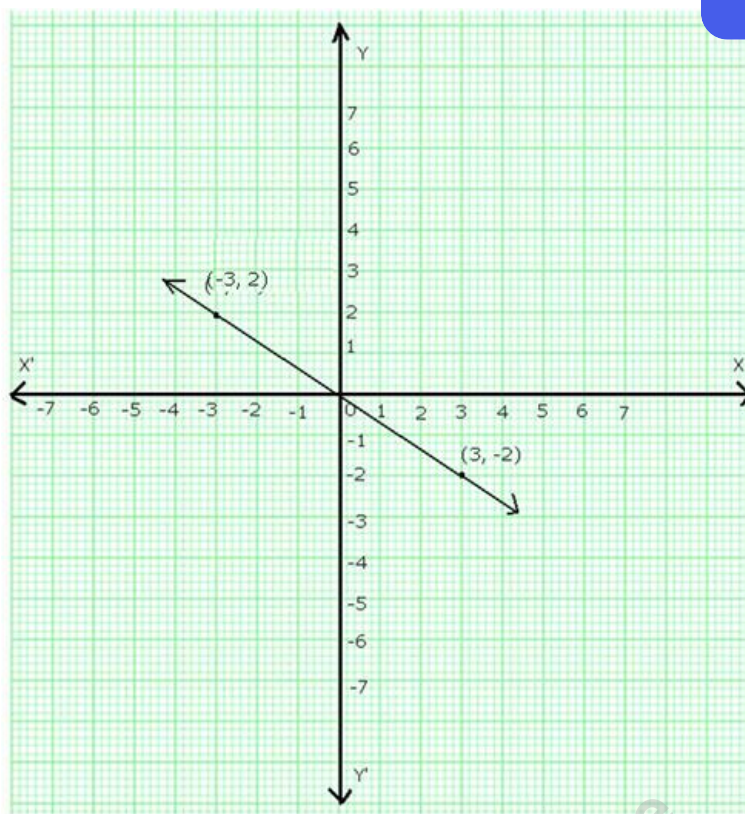
And, if  $x = -3$ , then

$$y = \frac{-2}{3} \times (-3) = 2$$

Thus, we have the following table

x	3	-3
y	-2	2

Plot points  $(3, -2)$  and  $(-3, 2)$  on a graph paper and join them to get the required graph.



(v) The given equation is  $3x - 2y = 0$

$$\Rightarrow y = \frac{3}{2}x$$

Now, if  $x = 2$ ,

$$y = \frac{3}{2} \times 2 = 3$$

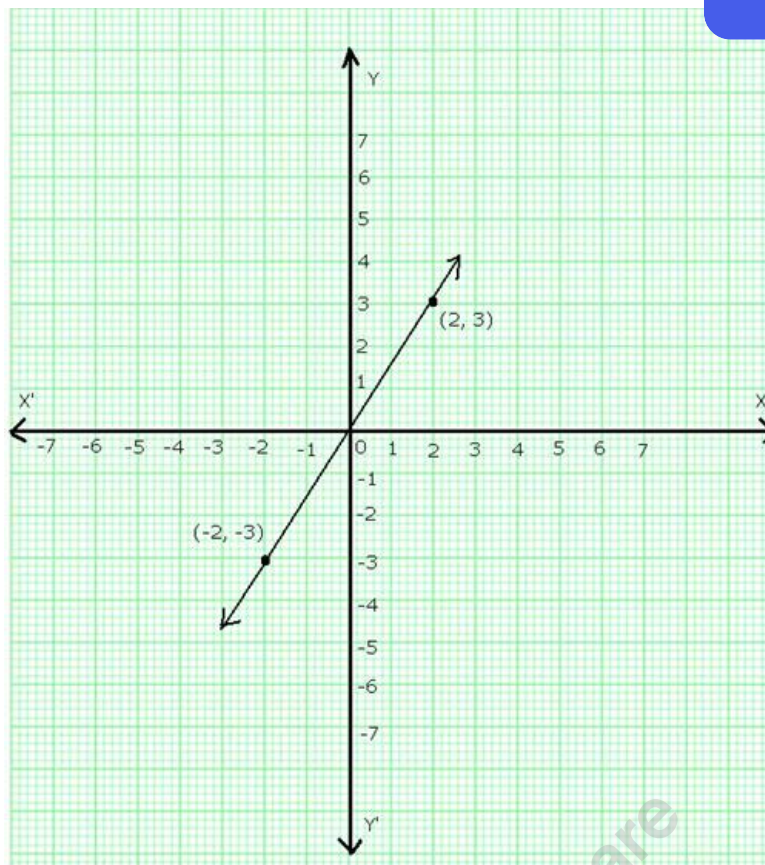
And, if  $x = -2$ ,

$$y = \frac{3}{2} \times (-2) = -3$$

Thus, we have the following table:

x	2	-2
y	3	-3

Plot points (2,3) and (-2,-3) on a graph paper and join them to get the required graph.



(vi) The given equation is  $2x + y = 0$

$$\Rightarrow y = -2x$$

Now, if  $x = 1$ , then  $y = -2 \cdot 1 = -2$

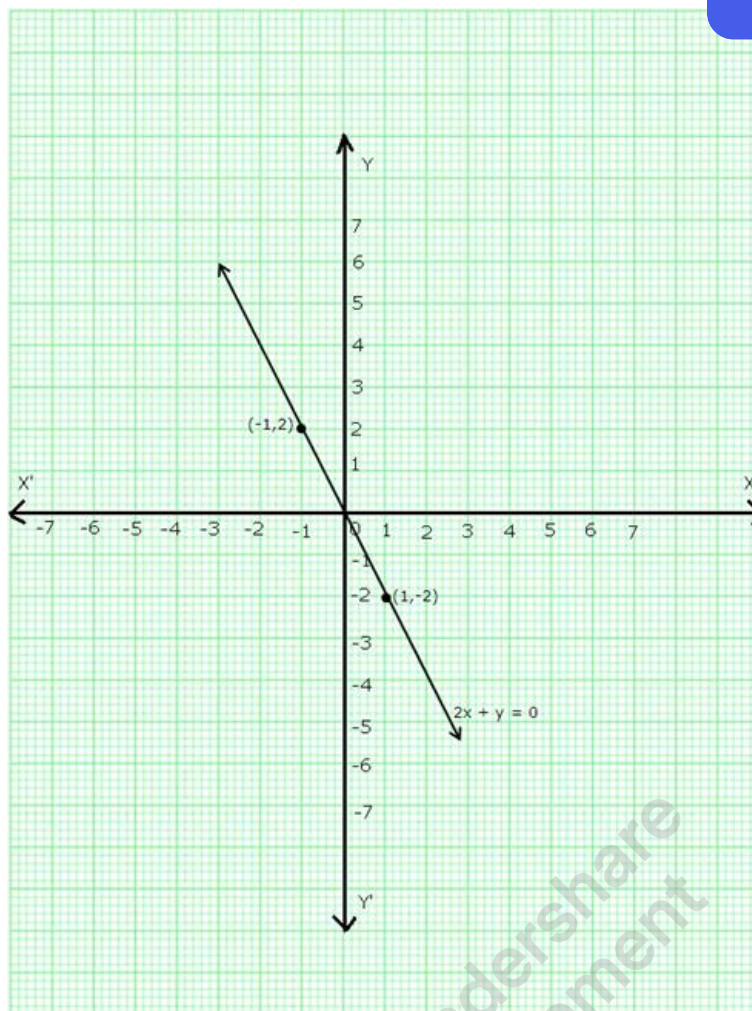
And, if  $x = -1$ , then  $y = -2 \cdot (-1) = 2$

Thus, we have the following table:

x	1	-1
y	-2	2

Plot points  $(1, -2)$  and  $(-1, 2)$  on a graph paper and join them to get the required graph.



**Question 5:**

The given equation is,  $2x - 3y = 5$

$$\Rightarrow y = \frac{2x-5}{3}$$

Now, if  $x = 4$ , then

$$y = \frac{2(4)-5}{3} = \frac{8-5}{3} = 1$$

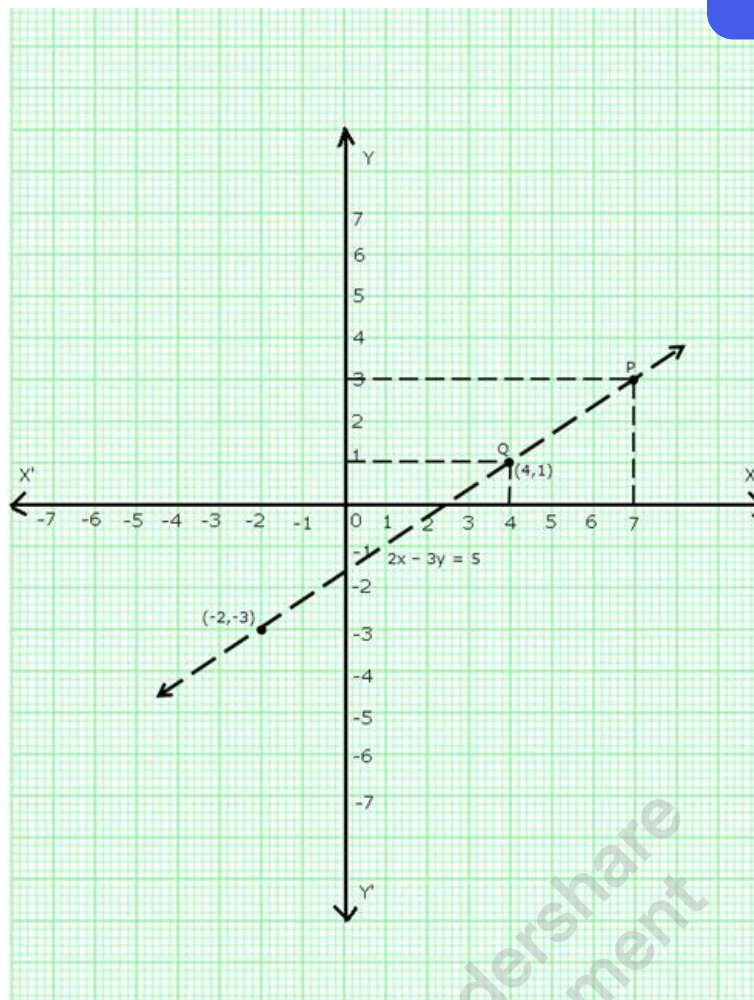
And, if  $x = -2$ , then

$$y = \frac{2(-2)-5}{3} = \frac{-4-5}{3} = \frac{-9}{3} = -3$$

Thus, we have the following table:

x	4	-2
y	1	-3

Plot points  $(4, 1)$  and  $(-2, -3)$  on a graph paper and join them to get the required graph.



(i) When  $x = 4$ , draw a line parallel to  $y$ -axis at a distance of 4 units from  $y$ -axis to its right cutting the line at  $Q$  and through  $Q$  draw a line parallel to  $x$ -axis cutting  $y$ -axis which is found to be at a distance of 1 units above  $x$ -axis.

Thus,  $y = 1$  when  $x = 4$ .

(ii) When  $y = 3$ , draw a line parallel to  $x$ -axis at a distance of 3 units from  $x$ -axis and above it, cutting the line at point  $P$ . Through  $P$ , draw a line parallel to  $y$ -axis meeting  $x$ -axis at a point which is found to be 7 units to the right of  $y$  axis.

Thus, when  $y = 3$ ,  $x = 7$ .

#### Question 6:

The given equation is  $2x + y = 6$

$$\Rightarrow y = 6 - 2x$$

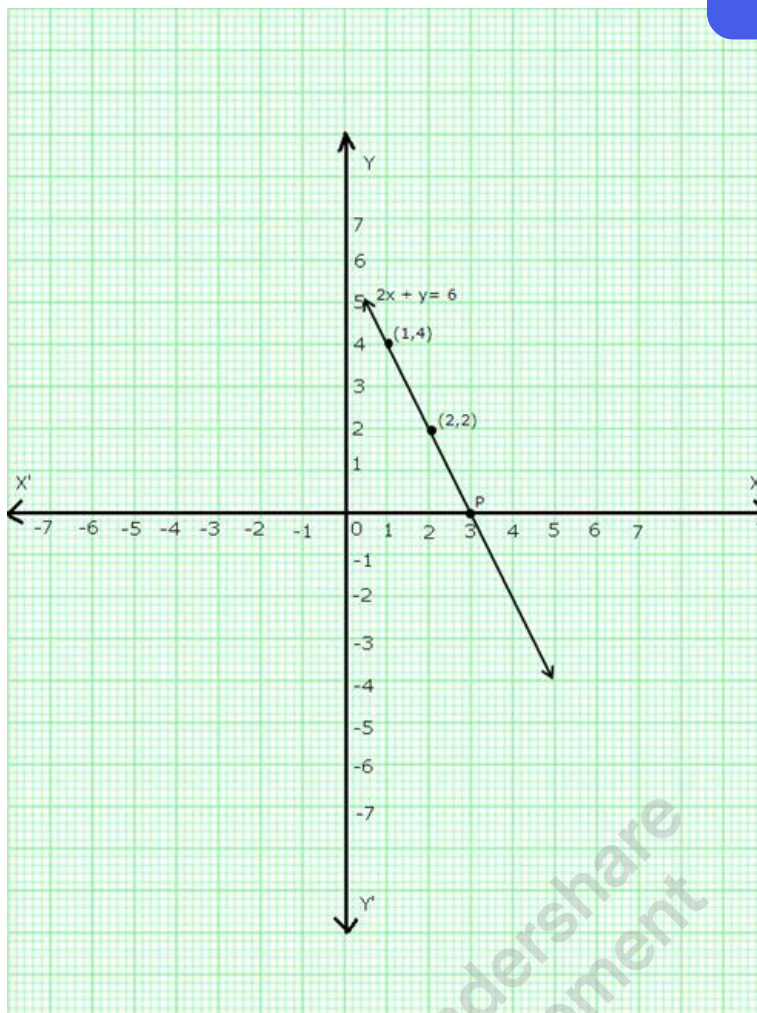
Now, if  $x = 1$ , then  $y = 6 - 2(1) = 4$

And, if  $x = 2$ , then  $y = 6 - 2(2) = 2$

Thus, we have the following table:

$x$	1	2
$y$	4	2

Plot points  $(1, 4)$  and  $(2, 2)$  on a graph paper and join them to get the required graph.



We find that the line cuts the x-axis at a point P which is at a distance of 3 units to the right of y-axis.

So, the co-ordinates of P are (3,0).

#### Question 7:

The given equation is  $3x + 2y = 6$

$$\Rightarrow 2y = 6 - 3x$$

$$\Rightarrow y = \frac{6-3x}{2}$$

Now, if  $x = 2$ , then

$$y = \frac{6-3(2)}{2} = 0$$

And, if  $x = 4$ , then

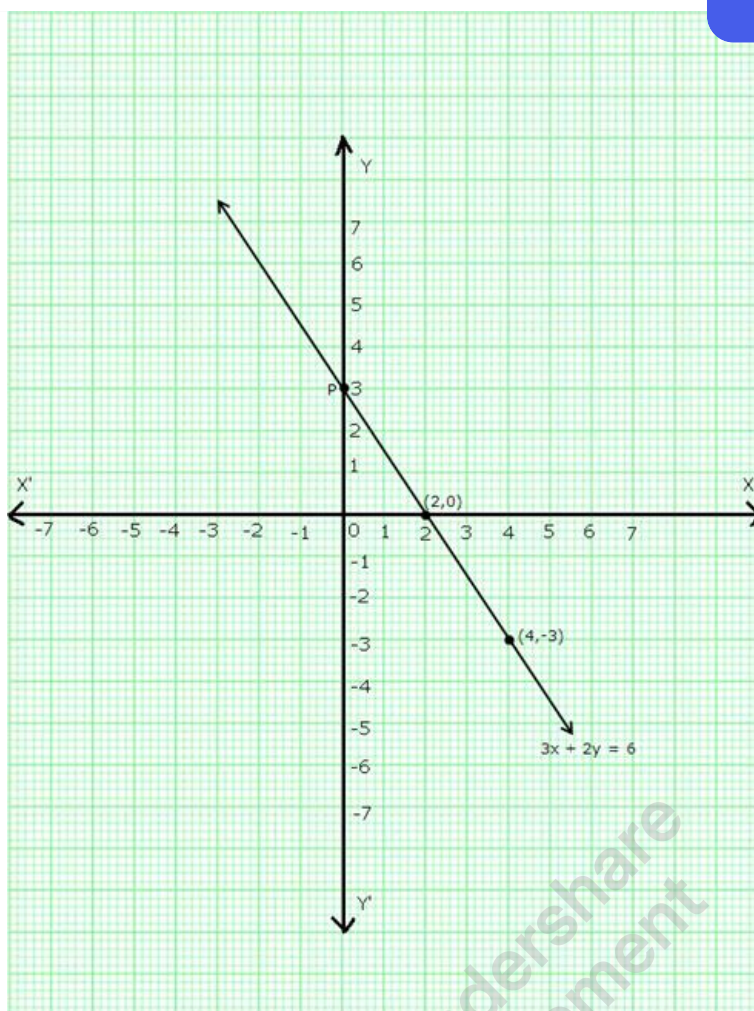
$$y = \frac{6-3(4)}{2} = \frac{-6}{2} = -3$$

Thus, we have the following table:

x	2	4
y	0	-3

Plot points (2, 0) and (4, -3) on a graph paper and join them to get the required graph.





We find that the line  $3x + 2y = 6$  cuts the y-axis at a point P which is 3 units above the x-axis.

So, co-ordinates of P are (0,3).