

QUADRILATERALS

EXERCISE 8.1

- **Q.1.** The angles of a quadrilateral are in the ratio 3:5:9:13. Find all the angles of the quadrilateral.
- **Sol.** Suppose the measures of four angles are 3x, 5x, 9x and 13x.

$$\therefore 3x + 5x + 9x + 13x = 360^{\circ}$$
 [Angle sum property of a quadrilateral]

$$\Rightarrow$$
 30x = 360°

$$\Rightarrow$$
 $x = \frac{30}{30}$

$$\Rightarrow 3x = 3 \times 12^{\circ} = 36^{\circ}$$

$$5x = 5 \times 12^{\circ} = 60^{\circ}$$

$$9x = 9 \times 12^{\circ} = 108^{\circ}$$

$$13x = 13 \times 12^{\circ} = 156^{\circ}$$

- : the angles of the quadrilateral are 36°, 60°, 108° and 156° Ans.
- **Q.2.** If the diagonals of a parallelogram are equal, then show that it is a rectangle.
- **Sol. Given :** ABCD is a parallelogram in which AC = BD.

To Prove : ABCD is a rectangle.

Proof : In
$$\triangle ABC$$
 and $\triangle ABD$

$$AB = AB$$

[Common]

$$BC = AD$$

[Opposite sides of a parallelogram]

...(i)

$$AC = BD$$

[Given]

$$\therefore \Delta ABC \cong \Delta BAD$$

[SSS congruence]

[CPCT]

Since, ABCD is a parallelogram, thus,

$$\angle ABC + \angle BAD = 180^{\circ}$$
 ...(ii)

[Consecutive interior angles]

$$\angle ABC + \angle ABC = 180^{\circ}$$

$$\therefore \qquad 2\angle ABC = 180^{\circ} \qquad [From (i) and (ii)]$$

$$\Rightarrow$$
 $\angle ABC = \angle BAD = 90^{\circ}$

This shows that ABCD is a parallelogram one of whose angle is 90°

Hence, ABCD is a rectangle. Proved.

- Q.3. Show that if the diagonals of a quadrilateral bisect each other at right angles, then it is a rhombus.
- D bis Sol. Given: A quadrilateral ABCD, in which diagonals AC and BD bisect each other at right angles.

To Prove : ABCD is a rhombus.





Proof: In $\triangle AOB$ and $\triangle BOC$

$$AO = OC$$

[Diagonals AC and BD bisect each other]

$$\angle AOB = \angle COB$$

 $[Each = 90^{\circ}]$

$$BO = BO$$

[Common]

$$\therefore \Delta AOB \cong \Delta BOC$$

[SAS congruence]

$$AB = BC$$

...(i) [CPCT]

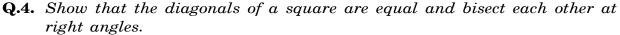
AB = BC

Since, ABCD is a quadrilateral in which

[From (i)]

Hence, ABCD is a rhombus.

: if the diagonals of a quadrilateral bisect each other, then it is a parallelogram and opposite sides of a parallelogram are equal **Proved.**



Sol. Given: ABCD is a square in which AC and BD are diagonals.

To Prove : AC = BD and AC bisects BD at right angles, i.e. $AC \perp BD$.

$$AO = OC, OB = OD$$

Proof: In $\triangle ABC$ and $\triangle BAD$,

$$AB = AB$$

[Common]

$$BC = AD$$

[Sides of a square]

$$\angle ABC = \angle BAD = 90^{\circ}$$

[Angles of a square] [SAS congruence]

[CPCT]

Now in $\triangle AOB$ and $\triangle COD$,

 $\Delta ABC \cong \Delta BAD$

$$AB = DC$$

[Sides of a square]

$$\angle AOB = \angle COD$$

[Vertically opposite angles]

[Alternate angles] [AAS congruence]

$$\triangle AOB \cong \triangle COD$$

 $\angle AO = \angle OC$

[CPCT]

Similarly by taking $\triangle AOD$ and $\triangle BOC$, we can show that OB = OD.

In
$$\triangle ABC$$
, $\angle BAC + \angle BCA = 90^{\circ}$

In
$$\triangle ABC$$
, $\angle BAC + \angle BCA = 90^{\circ}$ [: $\angle B = 90^{\circ}$] $\Rightarrow 2\angle BAC = 90^{\circ}$ [$\angle BAC = \angle BCA$, as $BC = AD$]

$$\Rightarrow \angle BCA = 45^{\circ} \text{ or } \angle BCO = 45^{\circ}$$

Similarly $\angle CBO = 45^{\circ}$

In ΔBCO.

$$\angle BCO + \angle CBO + \angle BOC = 180^{\circ}$$

$$\Rightarrow 90^{\circ} + \angle BOC = 180^{\circ}$$

$$\Rightarrow \angle BOC = 90^{\circ}$$

$$\Rightarrow$$
 BO \perp OC \Rightarrow BO \perp AC

Hence, AC = BD, $AC \perp BD$, AO = OC and OB = OD. Proved.

Q.5. Show that if the diagonals of a quadrilateral are equal and bisect each other at right angles, then it is a square.

Sol. Given: A quadrilateral ABCD, in which diagonals AC and BD are equal and bisect each other at right angles,

To Prove : ABCD is a square.





Proof: Since ABCD is a quadrilateral whose diagonals bisect each other, so it is a parallelogram. Also, its diagonals bisect each other at right angles, therefore, ABCD is a rhombus.

$$\Rightarrow$$
 AB = BC = CD = DA

[Sides of a rhombus]

In $\triangle ABC$ and $\triangle BAD$, we have

$$AB = AB$$

[Common]

$$BC = AD$$

[Sides of a rhombus]

$$AC = BD$$

[Given]

$$\therefore \qquad \Delta ABC \cong \Delta BAD$$

[SSS congruence]

$$\therefore \qquad \angle ABC = \angle BAD$$

[CPCT]

But,
$$\angle ABC + \angle BAD = 180^{\circ}$$

[Consecutive interior angles]

$$\angle ABC = \angle BAD = 90^{\circ}$$

 \Rightarrow ABCD is a rhombus whose angles are of 90° each.

Hence, ABCD is a square. Proved.

 $\angle A = \angle B = \angle C = \angle D = 90^{\circ}$

Q.6. Diagonal AC of a parallelogram ABCD bisects ∠A (see Fig.). Show that

- (i) it bisects $\angle C$ also,
- (ii) ABCD is a rhombus.

Given : A parallelogram ABCD, in which A^{\neq} diagonal AC bisects \angle A, i.e., \angle DAC = \angle BAC.

To Prove: (i) Diagonal AC bisects

 \angle C i.e., \angle DCA = \angle BCA

(ii) ABCD is a rhomhus.

Proof:

(i) $\angle DAC = \angle BCA$

$$\angle BAC = \angle DCA$$

But,
$$\angle DAC = \angle BAC$$

Hence, AC bisects ∠DCB

Or, AC bisects ∠C **Proved.**

(ii) In $\triangle ABC$ and $\triangle CDA$

$$AC = AC$$

[Common]

[Given]

$$\angle BAC = \angle DAC$$

[Given]

and
$$\angle BCA = \angle DAC$$

[Proved above]

$$\therefore$$
 $\triangle ABC \cong \triangle ADC$

[ASA congruence]

[Alternate angles]

$$\therefore$$
 BC = DC

[CPCT]

But
$$AB = DC$$

[Given]

$$\therefore$$
 AB = BC = DC = AD

Hence, ABCD is a rhombus **Proved.**

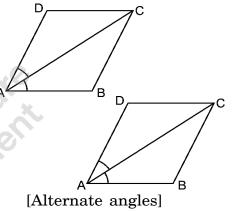
[∵ opposite angles are equal]

- **Q.7.** ABCD is a rhombus. Show that diagonal AC bisects $\angle A$ as well as $\angle C$ and diagonal BD bisects $\angle B$ as well as $\angle D$.
- Sol. Given: ABCD is a rhombus, i.e.,

$$AB = BC = CD = DA.$$

To Prove :
$$\angle DAC = \angle BAC$$
,







$$\angle ADB = \angle CDB$$
, $\angle ABD = \angle CBD$

Proof: In
$$\triangle ABC$$
 and $\triangle CDA$, we have

Similarly, $\angle ADB = \angle CDB$ and $\angle ABD = \angle CBD$.

Hence, diagonal AC bisects $\angle A$ as well as $\angle C$ and diagonal BD bisects $\angle B$ as well as $\angle D$. **Proved.**

- **Q.8.** ABCD is a rectangle in which diagonal AC bisects $\angle A$ as well as $\angle C$. Show that:
 - (i) ABCD is a square (ii) diagonal BD bisects $\angle B$ as well as $\angle D$.
- **Sol. Given :** ABCD is a rectangle in which diagonal AC bisects $\angle A$ as well as $\angle C$.

(ii) Diagonal BD bisects $\angle B$ as well as $\angle D$.



(i) In \triangle ABC and \triangle ADC, we have

$$\angle BAC = \angle DAC$$
 [Given]
 $\angle BCA = \angle DCA$ [Given]
 $AC = AC$

$$\therefore \Delta ABC \cong \Delta ADC$$
 [ASA congruence]

$$\therefore$$
 AB = AD and CB = CD [CPCT]

But, in a rectangle opposite sides are equal,

i.e.,
$$AB = DC$$
 and $BC = AD$

$$\therefore$$
 AB = BC = CD = DA

Hence, ABCD is a square **Proved.**

(ii) In $\triangle ABD$ and $\triangle CDB$, we have

$$AD = CD$$

$$AB = CD$$

$$BD = BD$$

$$ABD = BD$$

$$ABD \cong \Delta CBD$$

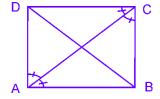
$$So, \angle ABD = \angle CBD$$

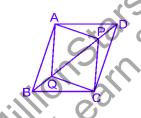
$$\angle ADB = \angle CDB$$

$$ABD = \angle CDB$$

Hence, diagonal BD bisects $\angle B$ as well as $\angle D$ **Proved.**

- **Q.9.** In parallelogram ABCD, two points P and Q are taken on diagonal BD such that DP = BQ (see Fig.). Show that :
 - (i) $\triangle APD \cong \triangle CQB$
 - (ii) AP = CQ
 - (iii) $\Delta AQB \cong \Delta CPD$
 - (iv) AQ = CP
 - (v) APCQ is a parallelogram







Sol. Given: ABCD is a parallelogram and P and Q are points on diagonal BD such that DP = BQ.

To Prove: (i) $\triangle APD \cong \triangle CQB$

- (ii) AP = CQ
- (iii) $\triangle AQB \cong \triangle CPD$
- (iv) AQ = CP
- (v) APCQ is a parallelogram

Proof:

(i) In \triangle APD and \triangle CQB, we have

$$AD = BC$$

[Opposite sides of a ||gm]

$$DP = BQ$$

[Given]

 $\angle ADP = \angle CBQ$

[Alternate angles]

$$\therefore \Delta APD \cong \Delta CQB$$

[SAS congruence]

(ii)
$$\therefore$$
 AP = CQ

[CPCT]

(iii) In $\triangle AQB$ and $\triangle CPD$, we have

$$AB = CD$$

[Opposite sides of a ||gm]

$$DP = BQ$$

[Given]

 $\angle ABQ = \angle CDP$

[Alternate angles]

$$\therefore \Delta AQB \cong \Delta CPD$$

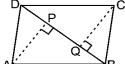
[SAS congruence]

(iv)
$$\therefore$$
 AQ = CP

[CPCT]

(v) Since in APCQ, opposite sides are equal, therefore it is a parallelogram. Proved.

Q.10. ABCD is a parallelogram and AP and CQ are perpendiculars from vertices A and C on diagonal BD (see Fig.). Show that



(i)
$$\triangle APB \cong \triangle CQD$$

(ii)
$$AP = CQ$$

Sol. Given: ABCD is a parallelogram and AP and CQ are perpendiculars from vertices A and C on BD.

- **To Prove :** (i) $\triangle APB \cong \triangle CQD$
 - (ii) AP = CQ

Proof:

(i) In \triangle APB and \triangle CQD, we have

$$\angle ABP = \angle CDQ$$

[Alternate angles]

AB = CD [Opposite sides of a parallelogram]

$$\angle APB = \angle CQD$$

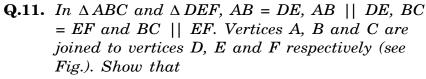
 $[Each = 90^{\circ}]$

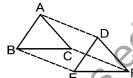
$$\therefore \Delta APB \cong \Delta CQD$$

[ASA congruence]

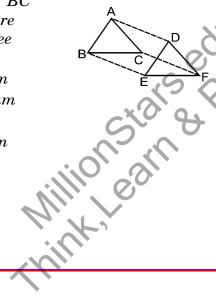
(ii) So,
$$AP = CQ$$

[CPCT] Proved.



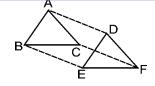


- (i) quadrilateral ABED is a parallelogram
- (ii) quadrilataeral BEFC is a parallelogram
- (iii) $AD \mid\mid CF \text{ and } AD = CF$
- (iv) quadrilateral ACFD is a parallelogram
- (v) AC = DF
- (vi) $\triangle ABC \equiv \triangle DEF$





Sol. Given: In DABC and DDEF, AB = DE, AB | | DE, BC = EF and BC | | EF. Vertices A, B and C are joined to vertices D, E and F.



To Prove: (i) ABED is a parallelogram

- (ii) BEFC is a parallelogram
- (iii) $AD \mid\mid CF \text{ and } AD = CF$
- (iv) ACFD is a parallelogram
- (v) AC = DF
- (vi) $\triangle ABC \cong \triangle DEF$

Proof: (i) In quadrilateral ABED, we have

 \Rightarrow ABED is a parallelogram.

[One pair of opposite sides is parallel and equal]

(ii) In quadrilateral BEFC, we have

[Given]

 \Rightarrow BEFC is a parallelogram.

[One pair of opposite sides is parallel and equal]

(iii) BE = CF and BE | | BECF [BEFC is parallelogram] [ABED is a parallelogram] $AD = BE \text{ and } AD \mid \mid BE \mid$

$$\Rightarrow$$
 AD = CF and AD | | CF

(iv) ACFD is a parallelogram.

[One pair of opposite sides is parallel and equal]

[Opposite sides of parallelogram ACFD] (v) AC = DF

(vi) In $\triangle ABC$ and $\triangle DEF$, we have

$$AB = DE$$

[Given]

$$BC = EF$$

[Given]

$$AC = DF$$

[Proved above]

$$\therefore \Delta ABC \cong \Delta DEF$$

[SSS axiom] **Proved.**

Q.12. ABCD is a trapezium in which AB

$$|| CD \ and \ AD = BC \ (see Fig.).$$
 Show that

(i)
$$\angle A = \angle B$$

(ii)
$$\angle C = \angle D$$

(iii)
$$\triangle ABC \cong \triangle BAD$$

$$(iv)$$
 diagonal AC = diagonal BD

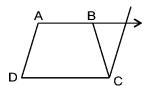


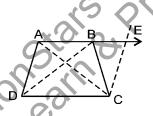
To Prove : (i)
$$\angle A = \angle B$$

(ii)
$$\angle C = \angle D$$

(iii)
$$\triangle ABC \cong \triangle BAD$$

Constructions: Join AC and BD. Extend AB and draw a line through C parallel to DA meeting AB produced at E.







(i) Since AB || DC

 \Rightarrow AE || DC ...(i)

and AD || CE ...(ii) [Construction]

 \Rightarrow ADCE is a parallelogram [Opposite pairs of sides are parallel

 $\angle A + \angle E = 180^{\circ}$...(iii)

[Consecutive interior angles]

 $\angle B + \angle CBE = 180^{\circ}$...(iv) [Linear pair]

AD = CE ...(v) [Opposite sides of a ||gm|]

AD = BC ...(vi) [Given]

 \Rightarrow BC = CE [From (v) and (vi)]

 \Rightarrow \angle E = \angle CBE ...(vii) [Angles opposite to equal sides]

 $\therefore \angle B + \angle E = 180^{\circ}$...(viii) [From (iv) and (vii)

Now from (iii) and (viii) we have

 $\angle A + \angle E = \angle B + \angle E$

 \Rightarrow $\angle A = \angle B$ **Proved.**

(ii) $\angle A + \angle D = 180^{\circ}$ $\angle B + \angle C = 180^{\circ}$ [Consecutive interior angles]

 $\Rightarrow \angle A + \angle D = \angle B + \angle C$ $[\because \angle A = \angle B]$

 \Rightarrow $\angle D = \angle C$

Or $\angle C = \angle D$ **Proved.**

(iii) In \triangle ABC and \triangle BAD, we have

AD = BC [Given]

 $\angle A = \angle B$ [Proved]

AB = CD [Common]

 $\therefore \Delta ABC \cong \Delta BAD$

[ASA congruence]

(iv) diagonal AC = diagonal BD

[CPCT] Proved.

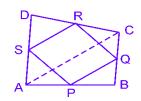
Millions are a practice



QUADRILATERALS

EXERCISE 8.2

Q.1. ABCD is a quadrilateral in which P, Q, R and S are mid-points of the sides AB, BC, CD and DA respectively. (see Fig.). AC is a diagonal. Show that:

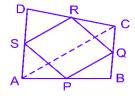


(i)
$$SR \mid\mid AC \text{ and } SR = \frac{1}{2}AC$$

(ii)
$$PQ = SR$$

(iii) PQRS is a parallelogram.

Given: ABCD is a quadrilateral in which P, Q, R and S are mid-points of AB, BC, CD and DA. AC is a diagonal.



To Prove: (i) SR || AC and SR = $\frac{1}{2}$ AC

(ii)
$$PQ = SR$$

(iii) PQRS is a parallelogram

(i) In $\triangle ABC$, P is the mid-point of AB and Q is the mid-point **Proof:** of BC.

$$\therefore$$
 PQ || AC and PQ = $\frac{1}{2}$ AC ...(1)

[Mid-point theorem]

In ΔADC, R is the mid-point of CD and S is the mid-point of AD

$$\therefore$$
 SR || AC and SR = $\frac{1}{2}$ AC ...(2)

[Mid-point theorem]

(ii) From (1) and (2), we get $PQ \parallel SR$ and PQ = SR

Millions are a practice (iii) Now in quadrilateral PQRS, its one pair of opposite sides PQ and SR is equal and parallel.

.: PQRS is a parallelogram. **Proved.**



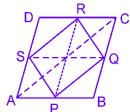
- **Q.2.** ABCD is a rhombus and P, Q, R and S are the mid-points of the sides AB, BC, CD and DA respectively. Show that the quadrilateral PQRS is a rectangle.
- **Sol. Given :** ABCD is a rhombus in which P, Q, R and S are mid points of sides AB, BC, CD and DA respectively :

To Prove: PQRS is a rectangle.

Construction: Join AC, PR and SQ.

Proof: In ∆ABC

P is mid point of AB [Given] Q is mid point of BC [Given]



 \Rightarrow PQ || AC and PQ = $\frac{1}{2}$ AC ...(i) [Mid point theorem] Similarly, in ΔDAC,

SR || AC and SR =
$$\frac{1}{2}$$
 AC ...(ii)

From (i) and (ii), we have PQ | | SR and PQ = SR

⇒ PQRS is a parallelogram

[One pair of opposite sides is parallel and equal]

Since ABQS is a parallelogram

 \Rightarrow AB = SQ [Opposite sides of a || gm]

Similarly, since PBCR is a parallelogram.

 \Rightarrow BC = PR

Thus, SQ = PR [AB = BC]

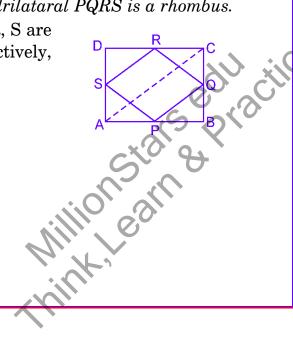
Since SQ and PR are diagonals of parallelogram PQRS, which are equal.

 \Rightarrow PQRS is a rectangle. **Proved.**

- **Q.3.** ABCD is a rectangle and P, Q, R and S are mid-points of the sides AB, BC, CD and DA respectively. Show that the quadrilateral PQRS is a rhombus.
- **Sol. Given:** A rectangle ABCD in which P, Q, R, S are the mid-points of AB, BC, CD and DA respectively, PQ, QR, RS and SP are joined.

To Prove: PQRS is a rhombus.

Construction: Join AC









Proof: In $\triangle ABC$, P and Q are the mid-points of the sides AB and BC.

$$\therefore$$
 PQ || AC and PQ = $\frac{1}{2}$ AC

...(i) [Mid point theorem]

Similarly, in $\triangle ADC$,

SR || AC and SR =
$$\frac{1}{2}$$
 AC

...(ii)

From (i) and (ii), we get

$$PQ \mid \mid SR \text{ and } PQ = SR$$

...(iii)

Now in quadrilateral PQRS, its one pair of opposite sides PQ and SR is parallel and equal [From (iii)]

∴PQRS is a parallelogram.

Now
$$AD = BC$$

...(iv)

[Opposite sides of a rectangle ABCD]

$$\therefore \frac{1}{2} AD = \frac{1}{2} BC$$

$$\Rightarrow$$

$$AS = BQ$$

In $\triangle APS$ and $\triangle BPQ$

$$AP = BP$$

$$AS = BQ$$

$$\angle PAS = \angle PBQ$$

 $\triangle APS \cong \triangle BPQ$

$$PS = PQ$$

P is the mid-point of AB]

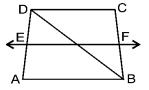
[Proved above]

 $[Each = 90^{\circ}]$

From (iii) and (v), we have

PQRS is a rhombus **Proved.**

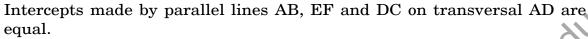
Q.4. ABCD is a trapezium in which AB || DC, BD is a diagonal and E is the mid-point of AD. A line is drawn through E parallel to AB intersecting BC at F (see Fig.). Show that F is the mid-point of BC.



Sol. Given: A trapezium ABCD with AB | DC, E is the mid-point of AD and EF || AB.

To Prove : F is the mid-point of BC.

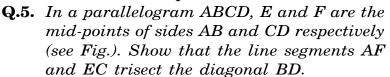
$$\Rightarrow$$
 AB, EF and DC are parallel.

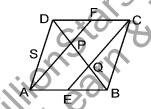


:. Intercepts made by those parallel lines on transversal BC are also egual.

i.e.,
$$BF = FC$$

$$\Rightarrow$$
 F is the mid-point of BC.







Given: A parallelogram ABCD, in which E and F are mid-points of sides AB and DC respectively.



Proof: Since E and F are mid-points of AB and DC respectively.

$$\Rightarrow$$
 AE = $\frac{1}{2}$ AB and CF = $\frac{1}{2}$ DC ...(i)

[Opposite sides of a parallelogram]

$$\therefore$$
 AE = CF and AE || CF.

$$\Rightarrow$$
 AECF is a parallelogram.

[One pair of opposite sides is parallel and equal]

In $\triangle BAP$,

E is the mid-point of AB

EQ || AP

 \Rightarrow Q is mid-point of PB [Converse of mid-point theorem]

$$\Rightarrow$$
 PQ = QB ...(iii)

Similarly, in ΔDQC ,

P is the mid-point of DQ

$$DP = PQ$$
 ...(iv

From (iii) and (iv), we have

$$DP = PQ = QB$$

or line segments AF and EC trisect the diagonal BD. Proved.

Q.6. Show that the line segments joining the mid-points of the opposite sides of a quadrilateral bisect each other.



To Prove: EG and FH bisect each other.

Construction: Join EF, FG, GH, HE and AC.

Proof: In $\triangle ABC$, E and F are mid-points of AB and BC respectively.

$$\therefore EF = \frac{1}{2}AC \text{ and } EF \mid\mid AC \qquad ...(i)$$

In ΔADC, H and G are mid-points of AD and CD respectively.

$$\therefore HG = \frac{1}{2}AC \text{ and } HG \mid\mid AC \qquad ...(ii)$$

From (i) and (ii), we get

EF = HG and $EF \mid \mid HG$

: EFGH is a parallelogram.

 $[\cdot \cdot \cdot]$ a quadrilateral is a parallelogram if its one pair of opposite sides is equal and parallel

Now, EG and FH are diagonals of the parallelogram EFGH.

: EG and FH bisect each other.

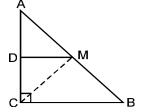
[Diagonal of a parallelogram bisect each other] Proved.



- **Q.7.** ABC is a triangle right angled at C. A line through the mid-point M of hypotenuse AB and parallel to BC intersects AC at D. Show that
 - (i) D is the mid-point of AC.
 - (ii) $MD \perp AC$

(iii)
$$CM = MA = \frac{1}{2}AB$$

- **Sol. Given:** A triangle ABC, in which $\angle C = 90^{\circ}$ and M is the mid-point of AB and BC || DM.
 - **To Prove:** (i) D is the mid-point of AC [Given]
 - (ii) DM \(\pm \) BC
 - (iii) $CM = MA = \frac{1}{2}AB$



Construction: Join CM.

Proof: (i) In $\triangle ABC$,

M is the mid-point of AB.

[Given] [Given]

BC || DM

D is the mid-point of AC

[Converse of mid-point theorem] **Proved.**

(ii)
$$\angle ADM = \angle ACB$$

[: Coresponding angles]

But
$$\angle ACB = 90^{\circ}$$

[Given]

$$\therefore$$
 $\angle ADM = 90^{\circ}$

But
$$\angle ADM + \angle CDM = 180^{\circ}$$

[Linear pair]

$$\therefore$$
 \angle CDM = 90°

Hence, $MD \perp AC$ Proved.

(iii)
$$AD = DC \dots (1)$$

 $[\cdot \cdot \cdot]$ D is the mid-point of AC]

Now, in $\triangle ADM$ and $\triangle CMD$, we have

$$\angle ADM = \angle CDM$$

 $[Each = 90^{\circ}]$

$$AD = DC$$

[From (1)]

$$DM = DM$$

[Common]

$$\therefore$$
 $\triangle ADM \cong \triangle CMD$

[SAS congruence]

$$\Rightarrow$$
 CM = MA

 \dots (2) [CPCT]

Since M is mid-point of AB,

$$\therefore \qquad MA = \frac{1}{2}AB$$

⇒ CM = MA ...(2) [CPCT]
Since M is mid-point of AB,

∴ MA =
$$\frac{1}{2}$$
AB ...(3)

Hence, CM = MA = $\frac{1}{2}$ AB Proved. [From (2) and (3)]