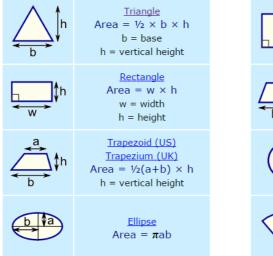
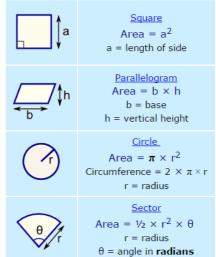




Area

Exercise 10A





Question 1:

Area of
$$\triangle ABD = \frac{1}{2} \times base \times height$$

A 5 cm B

$$= \left(\frac{1}{2} \times 5 \times 7\right) \text{ cm}^2 = \frac{35}{2} \text{ cm}^2$$
Area of $\triangle \text{CBD} = \left(\frac{1}{2} \times 5 \times 7\right) \text{ cm}^2 = \frac{35}{2} \text{ cm}^2$

Since the diagonal BD divides ABCD into two triangles of equal area.

- ∴ ABCD is a parallelogram.
- .. Area of parallelogram = Area of ΔABD+Area of ΔCBD

$$= \left(\frac{35}{2} + \frac{35}{2}\right) \text{ cm}^2 = \frac{70}{2} \text{ cm}^2$$
$$= 35 \text{ cm}^2$$

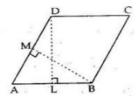
∴ Area of parallelogram = 35 cm²





Question 2:

Since ABCD is a parallelogram and DL is perpendicular to AB.



So, its area = AB
$$\times$$
 DL
=(10 \times 6) cm²
= 60 cm²

Also, in parallelogram ABCD,

BM⊥AD

:, Area of parallelogram ABCD = AD x BM

$$60 = AD \times 8cm$$

$$AD \times 8 = 60$$

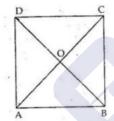
$$AD = \frac{60}{8} = 7.5 \text{ cm}$$

AD = 7.5 cm

Question 3:

ABCD is a rhombus in which diagonal AC=24 cm and BD = 16 cm

These diagonals intersect at O



Since diagonals of a rhombus are perpendicular to each other. So, in A ACD,

OD is its altitude and AC is its base.

So, area of
$$\triangle$$
 ACD $=\frac{1}{2} \times AC \times OD$

$$=\frac{1}{2} \times 24 \times \frac{BD}{2}$$

$$=\left(\frac{1}{2} \times 24 \times 8\right) \text{ cm}^2 \quad [\because BD = 16 \text{ cm}]$$

$$=96 \text{ cm}^2$$
Area of \triangle ABC $=\frac{1}{2} \times AC \times OB$

$$=\left(\frac{1}{2} \times 24 \times 8\right) \text{ cm}^2 = 96 \text{ cm}^2$$
Now, area of r hombus = Area of \triangle ACD + Area of \triangle ABC
$$=(96 + 96) \text{ cm}^2$$

$$= 192 \text{ cm}^2$$

⇒ Area of
$$\triangle$$
ABC = $\frac{1}{2}$ × AC × OB
= $\left(\frac{1}{2}$ × 24 × 8 $\right)$ cm² = 96 cm²

Now, area of rhombus = Area of \triangle ACD + Area of \triangle ABC

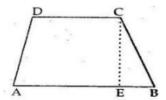
$$=(96+96) \text{ cm}^2$$

= 192 cm²



Question 4:

ABCD is a trapezium in which, AB ||CD $AB = 9 \, \text{cm}$ and $CD = 6 \, \text{cm}$ CE is a perpendicular drawn to AB through C and CE = 8 cm



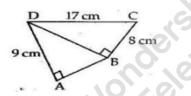
Area of trapezium= $\frac{1}{2}$ (sum of parallel sides)×distancebetween them

$$= \left[\frac{1}{2}(9+6) \times 8\right] \text{ cm}^2$$
$$= \left(\frac{1}{2} \times 15 \times 8\right) \text{ cm}^2 = 60 \text{ cm}^2$$

∴Area of trapezium = 60 cm²

Question 5:

(i) ABCD is a quadrilateral.



Now in right angled ∆ DBC

DB² = DC² - CB²
=
$$17^2 - 8^2$$

= $289 - 64 = 225 \text{ cm}^2$
∴ DB = $\sqrt{225} = 15 \text{ cm}$
So, area of Δ DBC = $\left(\frac{1}{2} \times 15 \times 8\right) \text{ cm}^2 = 60 \text{ cm}^2$
Again, in right angled Δ DAB,

AB² = DB² - AD²
=
$$15^2 - 9^2$$

= $225 - 81 = 144 \text{ cm}^2$
AB = $\sqrt{144} = 12 \text{ cm}$
area of $\Delta DAB = \left(\frac{1}{2} \times 12 \times 9\right) \text{ cm}^2 = 54 \text{ cm}^2$

So, area of quadrilateral ABCD

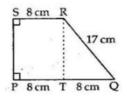
= Area of ΔDBC + Area of ΔDAB

 $= (60 + 54) \text{ cm}^2 = 114 \text{ cm}^2$

: area of quadrilateral ABCD = 114 cm²



(ii)



RT
$$\perp$$
PQ
In right angled \triangle RTQ
RT² = RQ² - TQ²
= 17² - 8²
= 289 - 64= 225 cm²
RT = $\sqrt{225}$ = 15 cm

:. Area of trapezium = $\frac{1}{2}$ (sum of parallel sides) x distance

between them

$$= \frac{1}{2} \times (PQ + SR) \times RT$$

$$= \frac{1}{2} \times (16 + 8) \times 15$$

$$= \left(\frac{1}{2} \times 24 \times 15\right) \text{ cm}^2 = 180 \text{ cm}^2$$

.: area of trapezium = 180 cm²

Question 7:

Given: ABCD is a quadrilateral and BD is one of

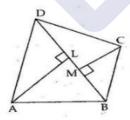
its diagonals.

AL_BD and CM_BD

To Prove: area (quad. ABCD)

$$=\frac{1}{2}\times BD\times (AL+CM)$$

Proof:



Area of
$$\triangle$$
 BAD = $\frac{1}{2} \times BD \times AL$

Area of
$$\triangle$$
 CBD = $\frac{1}{2} \times BD \times CM$

:. Area of quard. ABCD = Area of \triangle ABD + Area of \triangle CBD

$$= \frac{1}{2} \times BD \times AL + \frac{1}{2} \times BD \times CM$$

:. Area of quard. ABCD =
$$\frac{1}{2} \times BD[AL + CM]$$

of ACBD
M

Cital

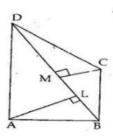


Question 8:

Area of
$$\triangle BAD = \frac{1}{2} \times BD \times AL$$

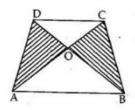
$$= \left(\frac{1}{2} \times 14 \times 8\right) \text{ cm}^2 = 56 \text{ cm}^2$$
Area of $\triangle CBD = \frac{1}{2} \times BD \times CM$

$$= \left(\frac{1}{2} \times 14 \times 6\right) \text{ cm}^2 = 42 \text{ cm}^2$$



$$\therefore$$
 area of quad. ABCD = Area of \triangle ABD + Area of \triangle CBD = $(56 + 42)$ cm² = 98 cm²

Question 9:



Consider Δ ADC and Δ DCB. We find they have the same base CD and lie between two parallel lines DC and AB.

Triangles on the same base and between the same parallels are equal in area.

So ΔCDA and ΔCDB are equal in area.

.: area (ΔCDA) = area (ΔCDB)

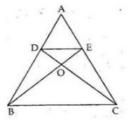
Now, $\operatorname{area}(\Delta AOD) = \operatorname{area}(\Delta ADC) - \operatorname{area}(\Delta OCD)$ and $\operatorname{area}(\Delta BOC) = \operatorname{area}(\Delta CDB) - \operatorname{area}(\Delta OCD)$

 $= \operatorname{area}(\Delta \operatorname{ADC}) - \operatorname{area}(\Delta \operatorname{OCD})$

 \Rightarrow area(\triangle AOD)= area(\triangle BOC)



Question 10:



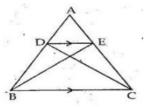
 (i) \(\Delta \text{DBE} \) and \(\Delta \text{DCE} \) have the same base DE and lie between parallel lines BC and DE.

So, area (\triangle DBE) = area(\triangle DCE)....(1) Adding area(\triangle ADE) on both sides, we get $ar(\triangle$ DBE) + $ar(\triangle$ ADE) = $ar(\triangle$ DCE) + $ar(\triangle$ ADE) \Rightarrow $ar(\triangle$ ABE) = $ar(\triangle$ ACD)

(ii) Since $ar(\Delta DBE) = ar(\Delta DCE)$ [from (1)] Subtracting $ar(\Delta ODE)$ from both sides we get $ar(\Delta DBE) - ar(\Delta ODE) = ar(\Delta DCE) - ar(\Delta ODE)$ $\Rightarrow ar(\Delta OBD) = ar(\Delta OCE)$

Question 11:

Given: A \triangle ABC in which points D and E lie on AB and AC, such that $ar(\triangle$ BCE) = $ar(\triangle$ BCD)



To Prove: DE || BC

Proof : As \triangle BCE and \triangle BCD have same base BC, and are equal in area, they have same altitudes.

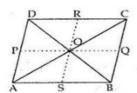
This means that they lie between two parallel lines.

DE | BC

Question 12:



Given: A parallelogram ABCD in which O is a point inside it To Prove: (i) $ar(\Delta OAB) + ar(\Delta OCD) = \frac{1}{2}ar(\parallel gm ABCD)$ (ii) ar (\triangle OAD)+ar(\triangle OBC) = $\frac{1}{2}$ ar(\parallel gm ABCD)



Construction: Through O draw PQ || AB and RS || AD Proof: (i) Δ AOB and parallelogram ABQP have same base AB and lie between parallel lines AB and PQ. If a triangle and a parallelogram are on the same base, and between the same parallels, then the area of the triangle is equal to half the area of the parallelogram.

$$\text{in} (\Delta AOB) = \frac{1}{2} \text{ar} (\|\text{gm ABQP})$$
 Similarly,
$$\text{ar} (\Delta COD) = \frac{1}{2} \text{ar} (\|\text{gm PQCD})$$
 So,
$$\text{ar} (\Delta AOB) + \text{ar} (\Delta COD)$$

$$= \frac{1}{2} \text{ar} (\|\text{gm ABQP}) + \frac{1}{2} \text{ar} (\|\text{gm PQCD})$$

$$= \frac{1}{2} \left[\text{ar} (\|\text{gm ABQP}) + \text{ar} (\|\text{gm PQCD}) \right]$$

$$= \frac{1}{2} \left[\text{ar} \|\text{gm ABCD} \right]$$

(ii) Δ AOD and \parallel gm ASRD have the same base AD and lie between same parallel lines AD and RS.

So,
$$\operatorname{ar}(\Delta \mathsf{AOD}) = \frac{1}{2}\operatorname{ar}(\|\mathsf{gm}\ \mathsf{ASRD})$$

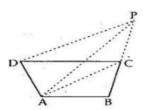
Similarly, $\operatorname{ar}(\Delta \mathsf{BOC}) = \frac{1}{2}\operatorname{ar}(\|\mathsf{gm}\ \mathsf{RSBC})$
 $\therefore \operatorname{ar}(\Delta \mathsf{AOD}) + \operatorname{ar}(\Delta \mathsf{BOC}) = \frac{1}{2}\left[\operatorname{ar}(\|\mathsf{gm}\ \mathsf{ASRD}) + \operatorname{ar}(\|\mathsf{gmRSBC})\right]$

$$= \frac{1}{2} [ar (\parallel gmABCD)]$$

Question 13:

Given: ABCD is a quadrilateral in which through D. a line is drawn parallel to AC which meets BC produced in P.

To Prove: $ar(\triangle ABP) = ar(quad.ABCD)$



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$$\therefore$$
 ar(\triangle ACP) = ar(\triangle ACD)

Adding $ar(\Delta ABC)$ on both sides, we get;

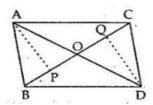
$$ar(\Delta ACP) + ar(\Delta ABC) = ar(\Delta ACD) + ar(\Delta ABC)$$

$$\Rightarrow$$
 ar(\triangle ABP) = ar(quad.ABCD)

Question 14:



Given: Two triangles, i.e. \triangle ABC and \triangle DBC which have same base BC and points A and D lie on opposite sides of BC and ar(\triangle ABC) = ar(\triangle BDC)



To Prove: OA = OD

Construction: Draw AP ⊥BC and DQ ⊥BC

Proof: We have

$$ar(\Delta ABC) = \frac{1}{2} \times BC \times AP \text{ and}$$
$$ar(\Delta BCD) = \frac{1}{2} \times BC \times DQ$$

So,
$$\frac{1}{2} \times BC \times AP = \frac{1}{2} \times BC \times DQ$$
 [from (1)]
 $\Rightarrow AP = DQ \dots (2)$

Now, in $\triangle AOP$ and $\triangle QOD$, we have

 $\angle APO = \angle DQO = 90^{\circ}$

and

 $\angle AOP = \angle DOQ$ [vertically opp. angles] AP = DQ [from (2)]

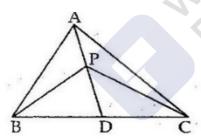
Thus, by Angle-Angle-Side criterion of congruence, we have

 $\triangle AOP \cong \triangle QOD$ [AAS]

The corresponding parts of the congruent triangles are equal.

Question 15:

Given: A \triangle ABC in which AD is the median and P is a point on AD.



To Prove: (i) $ar(\Delta BDP) = ar(\Delta CDP)$

(ii) $ar(\Delta ABP) = ar(\Delta APC)$

Proof :(i) In Δ BPC, PD is the median. Since median of a triangle divides the triangle into two triangles of equal areas

So,
$$ar(\Delta BPD) = ar(\Delta CDP).....(1)$$

(ii) In ΔABC, AD is the median

So, $ar(\triangle ABD) = ar(\triangle ADC)$

But, $ar(\Delta BPD) = ar(\Delta CDP)$ [from (1)]

Subtracting $ar(\Delta BPD)$ from both the sides

of the equation, we have

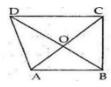
 $\therefore \operatorname{ar}(\triangle \operatorname{ABD}) - \operatorname{ar}(\triangle \operatorname{BPD}) = \operatorname{ar}(\triangle \operatorname{ADC}) - \operatorname{ar}(\triangle \operatorname{BPD})$ $= \operatorname{ar}(\triangle \operatorname{ADC}) - \operatorname{ar}(\triangle \operatorname{CDP}) \text{ from (1)}$

 \Rightarrow ar($\triangle ABP$) = ar($\triangle ACP$).

Question 16:



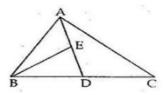
Given: A quadrilateral ABCD in which diagonals AC and BD intersect at O and BO = OD



To Prove : $ar(\Delta ABC) = ar(\Delta ADC)$ Proof: Since OB = OD [Given] So, AO is the median of ΔABD \therefore $ar(\Delta AOD) = ar(\Delta AOB)$ (i) As OC is the median of ΔCBD $ar(\Delta DOC) = ar(\Delta BOC)$ (ii) Adding both sides of (i) and (ii), we get $ar(\Delta AOD) + ar(\Delta DOC) = ar(\Delta AOB) + ar(\Delta BOC)$ \therefore $ar(\Delta ADC) = ar(\Delta ABC)$

Question 17:

Given: A \triangle ABC in which AD is a median and E is the mid – point of AD



To Prove: $ar(\Delta BED) = \frac{1}{4}ar(\Delta ABC)$ Proof: Since, $ar(\Delta ABD) = ar(\Delta ACD)$ [: AD is the median]

i.e. $ar(\triangle ABD) = \frac{1}{2}ar(\triangle ABC)$ (1)

 $[\because ar(\triangle ABC) = ar(\triangle ABD) + ar(\triangle ADC)]$

Now, as BE is the median of \triangle ABD

 $ar(\Delta ABE) = ar(\Delta BED) \dots (2)$

Since $ar(\Delta ABD) = ar(\Delta ABE) + ar(\Delta BED) \dots (3)$

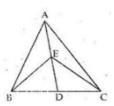
ar (ΔBED) = ar (ΔABE) [from (2)] = $\frac{1}{2}$ ar (ΔABD) [from (2) and (3)] = $\frac{1}{2} \left[\frac{1}{2}$ ar (ΔABC) [from (1)]

 $=\frac{1}{4}ar(\Delta ABC)$

Question 18:



Given: A \triangle ABC in which E is the mid – point of line segment AD where D is a point on BC.



To Prove:
$$ar(\Delta BEC) = \frac{1}{2}ar(\Delta ABC)$$

Proof: Since BE is the median of \triangle ABD So, $ar(\triangle BDE) = ar(\triangle ABE)$

$$\therefore \qquad \text{ar}(\Delta BDE) = \frac{1}{2} \text{ar}(\Delta ABD) \qquad \dots (i)$$

As, CE is median of Δ ADC

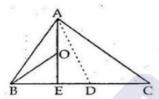
So,
$$ar(\Delta CDE) = \frac{1}{2}ar(\Delta ACD)$$
(ii)

Adding (i) and (ii), we get

$$\begin{split} \operatorname{ar}(\Delta \operatorname{BDE}) + \operatorname{ar}(\Delta \operatorname{CDE}) &= \frac{1}{2}\operatorname{ar}\left(\Delta \operatorname{ABD}\right) + \frac{1}{2}\operatorname{ar}\left(\Delta \operatorname{ACD}\right) \\ \operatorname{ar}(\Delta \operatorname{BEC}) &= \frac{1}{2}\left[\operatorname{ar}\left(\Delta \operatorname{ABD}\right) + \operatorname{ar}\left(\Delta \operatorname{ACD}\right)\right] \\ &= \frac{1}{2}\operatorname{ar}\left(\Delta \operatorname{ABC}\right). \end{split}$$

Question 19:

Given: A \triangle ABC in which AD is the median and E is the mid-point of BD. O is the mid-point of AE.



To Prove :
$$ar(\Delta BOE) = \frac{1}{8}ar(\Delta ABC)$$

Proof: Since O is the midpoint of AE.

So, BO is the median of Δ BAE

$$\therefore \qquad \operatorname{ar}(\Delta BOE) = \frac{1}{2}\operatorname{ar}(\Delta ABE) \dots (1)$$

Now, E is the mid-point of BD

So AE divides \triangle ABD into two triangles of equal area.

$$\therefore \qquad \operatorname{ar}(\Delta A BE) = \frac{1}{2} \operatorname{ar}(\Delta A BD) \dots (2)$$

As D is the mid point of BC

So
$$\operatorname{ar}(\Delta A BD) = \frac{1}{2}\operatorname{ar}(\Delta ABC)....(3)$$

$$\Rightarrow \operatorname{ar}(\Delta BOE) = \frac{1}{2}\operatorname{ar}(\Delta ABE) \quad [from (1)]$$

$$= \frac{1}{2}\left[\frac{1}{2}\operatorname{ar}(\Delta A BD)\right] \quad [from (2)]$$

$$= \frac{1}{4}\operatorname{ar}(\Delta A BD)$$

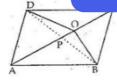
$$= \frac{1}{4} \times \frac{1}{2}\operatorname{ar}(\Delta ABC) \quad [from (3)]$$

$$= \frac{1}{8}\operatorname{ar}(\Delta ABC)$$

Question 20:



Given: A parallelogram ABCD in which O is any point on the diagonal AC.



To Prove: $ar(\Delta AOB) = ar(\Delta AOD)$.

Construction: Join BD which intersects AC at P.

Proof: As diagonals of a parallelogram bisect each other,

so, OP is the median of Δ ODB $ar(\Delta ODP) = ar(\Delta OBP).$

Also, APis the median of △ABD

 $ar(\Delta ADP) = ar(\Delta ABP)$

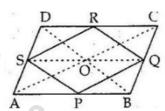
Adding both sides, we get

 $ar(\Delta ODP) + ar(\Delta ADP) = ar(\Delta OBP) + ar(\Delta ABP)$

 $ar(\Delta AOD) = ar(\Delta AOB).$

Question 21:

Given: ABCD is a parallelogram and P,Q,R and S are the midpoints of AB,BC,CD and DA respectively.



To Prove: PQRS is a parallelogram and ar (||gmPQRS)

$$=\frac{1}{2}$$
ar (\parallel gm ABCD)

Construction: Join AC, BD and SQ.

Proof: As S and R are the midpoints of AD and CD.So, in △ADC

By mid point theorem SR | AC

Also, as P and Q are the midpoints of AB and BC.So, in △ABC,

PQ | AC

 $\mathsf{PQ} \parallel \mathsf{AC} \parallel \mathsf{SR}$

PQ || SR

Similarly, we can prove SP | RQ.

Thus PQRS is a parallelogram as its opposite sides are parallel since diagonals of a parallelogram bisect each other. So in $\triangle ABD$,

O is the midpoint of AC and S is the midpoint of AD.

OS || AB By midpoint theorem

Similarly in ABC, we can prove that,

OQ ||AB

SQ | AB i.e.

Thus, ABQS is a parallelogram.

Now,
$$ar(\Delta SPQ) = \frac{1}{2}ar(\|gm ABQS)$$
(i)

Allin Stars & Practice [∵∆SPQ and ||gm ABQS have the same base and lie] between same parallel lines

Similarly, we can prove that;

$$ar(\Delta SRQ) = \frac{1}{2}ar(\parallel gmSQCD)$$
(ii

Adding (i) and (ii) we get

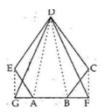
$$ar(\Delta SPQ) + ar(\Delta SRQ) = \frac{1}{2} [ar(\|gmABQS) + ar(\|gmSQCD)]$$

$$\therefore \qquad \operatorname{ar}(\|\operatorname{gmPQRS}) = \frac{1}{2}\operatorname{ar}(\|\operatorname{gmABCD})$$

Question 22:



Given: ABCDE is a pentagon. EG, drawn parallel to DA, meets BA produced at G, and CF, drawn parallel to DB, meets AB produced at F.



To Prove: $ar(Pentagon ABCDE) = ar(\Delta DGF)$

Proof:

Triangles on the same base and between the same parallels are equal in area. Since \triangle DGA and \triangle AED have same base AD and lie between

parallel lines AD and EG $ar(\Delta DGA) = ar(\Delta AED)....(1)$

Similarly, Δ DBC and Δ BFD have same baseDB and lie between parallel lines BD and CF.

 $ar(\Delta DBF) = ar(\Delta DBC)....(2)$

Adding both the sides of the equations (1) and (2), we have

 \therefore ar(\triangle DGA)+ ar(\triangle DBF)=ar(\triangle AED)+ar(\triangle BCD)

Adding $ar(\Delta ABD)$ to both sides, we get, $ar(\Delta DGA) + ar(\Delta DBF) + ar(\Delta ABD)$

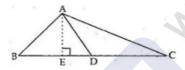
 $= ar(\Delta AED) + ar(\Delta BCD) + ar(\Delta ABD)$

 \therefore ar (\triangle DGA) = ar (pentagon ABCDE)

Question 23:

Felemei Given: ABC is a triangle in which AD is the median.

To Prove: $ar(\triangle ABD) = ar(\triangle ACD)$ Construction: Draw AE ⊥ BC



Proof:
$$ar(\triangle ABD) = \frac{1}{2} \times BD \times AE$$

and,
$$ar(\Delta ADC) = \frac{1}{2} \times DC \times AE$$

Since,
$$BD = DC$$
 [Since D is the median]

So,
$$\operatorname{ar} (\Delta \operatorname{ABD}) = \frac{1}{2} \times \operatorname{BD} \times \operatorname{AE}$$

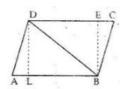
$$= \frac{1}{2} \times \operatorname{DC} \times \operatorname{AE} = \operatorname{ar} (\Delta \operatorname{ADC})$$

$$\therefore \quad ar(\Delta ABD) = ar(\Delta ACD)$$

Question 24:

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Given: ABCD is a parallelogram in which BD is its diagonal.

To Prove: $ar(\triangle ABD) = ar(\triangle BCD)$

Construction : Draw DL ⊥ AB and BE ⊥ CD

Proof:
$$ar(\Delta ABD) = \frac{1}{2} \times AB \times DL$$
(i)

and,
$$\operatorname{ar}(\Delta CBD) = \frac{1}{2} \times CD \times BE$$
(ii)

Now, since ABCD is a parallelogram.

$$\therefore$$
 AB || CD and AB = CD(iii)

Since distance between two parallel

lines is constant,

$$\Rightarrow$$
 DL = BE(iv)

Form (i),(ii), (iii), and (iv) we have

$$ar(\Delta ABD) = \frac{1}{2} \times AB \times DL$$

 $= \frac{1}{2} \times CD \times BE = ar(\Delta CBD)$
 $ar(\Delta ABD) = ar(\Delta CBD)$

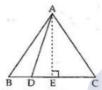
Question 25:

Given: A \(\Delta ABC in \) which D is a point on BC such that;

$$BD = \frac{1}{2}DC$$

:
ABC in which D is a point on BC such that;

To Prove:
$$ar(\Delta ABD) = \frac{1}{3} ar(\Delta ABC)$$



Consruction: Draw AE ⊥ BC

Proof:
$$ar(\triangle ABD) = \frac{1}{2} \times BD \times AE \dots (1)$$

and,
$$\operatorname{ar}(\Delta ABC) = \frac{1}{2} \times BC \times AE \dots (2)$$

Given that $BD = \frac{1}{2}BC$

So,
$$BC = BD + DC = BD + 2BD = 3BD$$

$$\therefore BD = \frac{1}{3}BC \qquad(3)$$

From (1),

$$\begin{split} \text{ar} \left(\Delta \, \mathsf{ABD} \right) &= \frac{1}{2} \times \mathsf{BD} \times \mathsf{AE} \\ &= \frac{1}{2} \times \frac{\mathsf{BC}}{3} \times \mathsf{AE} \end{split} \qquad \text{[from (3)]}$$

$$\therefore \operatorname{ar}(\Delta \mathsf{ABD}) = \frac{1}{3} \times \left(\frac{1}{2} \times \mathsf{BC} \times \mathsf{AE}\right)$$

$$= \frac{1}{3} \times \operatorname{ar}(\Delta \mathsf{ABC}) \qquad [\mathsf{from}(2)]$$

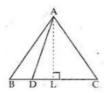
$$\therefore \operatorname{ar}(\Delta \mathsf{ABD}) = \frac{1}{3} \times \operatorname{ar}(\Delta \mathsf{ABC})$$

Question 26:



Given: ABC is a triangle in which D is a point on BC such

BD:DC = m:n



 $ar(\Delta ABD): ar(\Delta ACD)$ To Prove:

= m : n

 $ar(\triangle ABD) = \frac{1}{2} \times BD \times AL$ Proof:

and, $ar(\Delta ADC) = \frac{1}{2} \times DC \times AL$

Now, BD:DC = m:n

$$\therefore \qquad \qquad BD = DC \times \frac{m}{n}$$

$$\therefore \text{ ar}(\Delta ABD) = \frac{1}{2} \times BD \times AL$$

$$= \frac{1}{2} \times (DC \times \frac{m}{n}) \times AL$$

$$= \frac{m}{n} \times (\frac{1}{2} \times DC \times AL)$$

$$= \frac{m}{n} \times \text{ar}(\Delta ADC)$$

$$\Rightarrow \frac{\text{ar}(\Delta ABD)}{\text{ar}(\Delta ADC)} = \frac{m}{n}$$

$$\Rightarrow \text{ar}(\Delta ABD) : \text{ar}(\Delta ADC) = m : n$$

 $\frac{\text{ar}(\Delta \text{ABD})}{\text{ar}(\Delta \text{ADC})}$

 $ar(\Delta ABD) : ar(\Delta ADC) = m : n$

