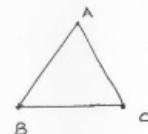


Chapter-15 Properties of Triangles

Exercise-15.1

Solution -01:-



→ By joining of AB, BC and CA figure obtained is triangle ABC. where A, B and C are three non-collinear points.

- (i) the side opposite to $\angle B$ is AC
- (ii) the angle opposite to side AB is $\angle ACB$
- (iii) the vertex opposite to side BC is A
- (iv) the side opposite to vertex B is AC.

Solution -02:-

No, By definition of a triangle

Solution-03:-

Triangle :-

A plane figure formed by three non parallel line segments is called a triangle.



Triangular Region:-

The interior of $\triangle ABC$ together with the $\triangle ABC$ itself, is called the triangular region of $\triangle ABC$.

Solution-04:-

Triangles observed in the figure are $\triangle ACD$, $\triangle ADB$ and $\triangle ABC$.

Total no. of triangles are '3'



Solution-05:-

Eight triangles observed in the figure are

1. $\triangle ABC$
2. $\triangle ABD$
3. $\triangle ABO$
4. $\triangle BCD$
5. $\triangle DCO$
6. $\triangle AOD$
7. $\triangle ACD$
8. $\triangle Bop.$

Solution-06:-

→ A plane figure formed by three non parallel line segments is called a triangle where as triangular Region is the interior of $\triangle ABC$ together with the $\triangle ABC$ itself, is called the triangular region ABC .

Solution -07:-

(i) Triangle:-

A Plane figure formed by three non-parallel line segments is called a triangle.

(ii) Parts or Elements of a triangle:-

The three sides AB, BC, CA and three angles $\angle A, \angle B, \angle C$ of a $\triangle ABC$ are together called the six parts or elements of $\triangle ABC$.

(iii) Scalene triangle:-

A triangle whose no two sides are equal, is called Scalene triangle.

(iv) Isosceles triangle:-

A triangle whose two sides are equal, is called isosceles triangle.

(v) Equilateral triangle:-

A triangle whose all sides are equal, is called Equilateral triangle.



(vi) Acute triangle:-

A triangle whose all the angles are acute is called Acute triangle.

(vii) Right triangle:-

A triangle whose one of the angles is right angle is called Right triangle.

(viii) obtuse triangle:-

A triangle whose one of the angles is obtuse angle is called Obtuse triangle.

(ix) Interior of a Triangle:-

The interior of a triangle is made up of all such points P of the plane, are enclosed by the triangle.

(x) Exterior of a triangle:-

The exterior of a triangle is made up of part of the plane which consists of those points Q, which are neither on the triangle nor in its interior.

Solution - 08:-

$$(i) AB \neq BC \neq CA$$

Scalene triangle

$$(ii) PQ = PR, QR = SCM.$$

Isosceles triangle.

$$(iii) XY = YZ = ZX$$

Equilateral triangle

$$(iv) UV \neq VW \neq UW$$

Scalene triangle

(v) Two sides are equal

→ Isosceles triangle

Solution - 09:-

(i) Angle given is 90°

∴ Right angle triangle

(ii) Angle given is 120° [$120^\circ > 90^\circ$]

∴ Obtuse triangle

(iii) All the angles are acute [$< 90^\circ$ → Acute]

(iv) Right triangle

(v) Obtuse triangle.



- (i) Three
- (ii) Three
- (iii) Three
- (iv) six
- (v) Scalene
- (vi) Isosceles
- (vii) Equilateral
- (viii) Right triangle
- (ix) Acute triangle
- (x). obtuse triangle.





Exercise-15.2

Exercise-15.2 :-

Solution-01:-

Let ABC be a triangle such that $\angle B = 105^\circ$ & $\angle C = 30^\circ$

Then, we have find the measure of the third angle A.

NOW, $\angle B = 105^\circ$ and $\angle C = 30^\circ$

$$\Rightarrow \angle B + \angle C = 105^\circ + 30^\circ = 135^\circ$$

By the Angle sum property of a triangle, we have

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\Rightarrow \angle A + 135^\circ = 180^\circ$$

$$\Rightarrow \angle A = 180^\circ - 135^\circ$$

$$\Rightarrow \angle A = 45^\circ$$

Solution-02:-

Let ABC be a triangle such that $\angle A = 130^\circ$ and

the other two angles $\angle B = \angle C$

By the angle sum property of a triangle, we have

$$\angle A + \angle B + \angle C = 180^\circ$$

[$\angle A = 130^\circ$ and $\angle C = \angle B$]

$$130^\circ + 2\angle C = 180^\circ \Rightarrow 2\angle C = 180^\circ - 130^\circ$$

$$\therefore \angle C = 25^\circ = \angle B$$

$$\therefore \angle A = 130^\circ, \angle B = 25^\circ \text{ & } \angle C = 25^\circ$$

Solution-03:-

Given that,

Three triangles of triangles are equal.

The measured angles be $\angle A = \angle B = \angle C$.

By the angle sum property of a triangle, we have

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + \angle A + \angle A = 180^\circ$$

$$3\angle A = 180^\circ$$

$$\angle A = \frac{180^\circ}{3} = 60^\circ$$

$$\therefore \angle A = \angle B = \angle C = 60^\circ$$

Solution-04:-

Given that,

three angles of a triangle in the ratio 1:2:3

Let the measured angles be $x, 2x$ & $3x$.

By the angle sum property of a triangle

we have

$$x + 2x + 3x = 180^\circ$$

$$6x = 180^\circ$$

$$x = 30^\circ$$

$$1^{\text{st}} \text{ angle} \rightarrow 30^\circ$$

$$2^{\text{nd}} \text{ Angle} \rightarrow 2(30^\circ) \rightarrow 60^\circ$$

[$2x$]

$$3^{\text{rd}} \text{ Angle} \rightarrow 3(30^\circ) \rightarrow 90^\circ$$

[$3x$]

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solution-05:-

Give angles of a triangle are

$$(x-40)^\circ, (x-20)^\circ \text{ & } (\frac{1}{2}x-10)^\circ.$$

By the Angle sum property of a triangle,
we have

$$(x-40)^\circ + (x-20)^\circ + (\frac{1}{2}x-10)^\circ = 180^\circ$$

$$2x - 70^\circ = 180^\circ \Rightarrow \frac{4x+2x-140^\circ}{2} = 180^\circ$$

$$5x - 140^\circ = 360^\circ$$

$$5x = 360^\circ + 140^\circ$$

$$x = \frac{500^\circ}{5}$$

$$\boxed{x = 100^\circ}$$

Required angles are

$$(x-40)^\circ = (100-40)^\circ = 60^\circ$$

$$(x-20)^\circ = (100-20)^\circ = 80^\circ$$

$$(\frac{1}{2}x-10)^\circ = (\frac{100}{2}-10)^\circ$$

$$= (50-10)^\circ$$

$$= 40^\circ$$

∴ Required angles are $60^\circ, 80^\circ$ and 40° .

solution-06:-

Given that,

Angles are arranged in the ascending order say ~~A ≥ B ≥ C~~. $A < B < C$ and difference between two angles is 10° .

Then the measured angles be say

$$x, x+10 \text{ and } x+20.$$

By Angle sum property of a triangle, we have

$$x + x+10 + x+20 = 180^\circ$$

$$3x + 30^\circ = 180^\circ$$

$$3x = 180^\circ - 30^\circ$$

$$x = \frac{150^\circ}{3}$$

$$x = 50^\circ$$

∴ Required angles are $x, x+10$ and $x+20$.

$$\angle A = x = 50^\circ$$

$$\angle B = x+10 = 60^\circ$$

$$\angle C = x+10+10 = x+20^\circ = 50^\circ+20^\circ = 70^\circ$$

∴ Three angles are $50^\circ, 60^\circ, 70^\circ$.


Solution-08:-

Given that,

one angle of a triangle is equal to the sum of the other two

Let the measures of angles be x, y, z

By the Angle sum property of a triangle, we have

$$x + y + z = 180^\circ$$

$$x + z = 180^\circ \quad [x = y + z]$$

$$2x = 180^\circ$$

$$x = 90^\circ$$

If one angle is 90° then the given triangle is a right angle triangle.

Solution-09:-

Given that,

each angle of a triangle is less than the sum of the other two.

measure of angles be x, y and z

$$x < y+z$$

$$y < x+z$$

$$z < x+y$$

$$\therefore x < 90^\circ, y < 90^\circ, z < 90^\circ \quad [\text{By the Angle sum Property of a triangle}]$$

\therefore The triangle is an acute angled.

Solution-10:-

$$(i) 63^\circ + 37^\circ + 80^\circ = 180^\circ$$

[By the angle sum of Properties of a triangle].

Angles form a triangle

$$(ii) 45^\circ + 61^\circ + 73^\circ \neq 180^\circ$$

$$(iii) 59 + 62^\circ + 61^\circ \neq 180^\circ$$

$$(iv) 45^\circ + 45^\circ + 90^\circ = 180^\circ$$

Angles form a triangle.

$$(v) 20^\circ + 20^\circ + 125^\circ \neq 180^\circ$$

Solution-11

Given that,

angles of a triangle in ratio $3:4:5$

measure of Angles be $3x, 4x$ and $5x$

Angle sum property of a triangle, we have

$$3x + 4x + 5x = 180^\circ$$

$$12x = 180^\circ$$

$$x = \frac{180^\circ}{12} = 15^\circ$$

$$\text{smallest angle} = 3x$$

$$= 3(15)^\circ$$

$$= 45^\circ$$


Solution -12:-

Given,

Two acute angles of a right angle triangle are equal.

Right triangle:-

Triangle whose one of the angle is right angle.

measured angles be $x, x, 90^\circ$

By Angle sum property of a triangle, we have

$$x+x+90^\circ = 180^\circ$$

$$2x = 180^\circ - 90^\circ$$

$$x = \frac{90^\circ}{2} \Rightarrow x = 45^\circ$$

The two angles are $45^\circ, 45^\circ$.

Solution -13:-

Angle of a triangle is greater than the sum of the other two.

measure of angles be x, y and z .

$$x > y+z \text{ (or)}$$

$$y > x+z \text{ (or)}$$

$$z > x+y.$$

x (or) y (or) $z > 90^\circ$ which is obtuse.

\therefore triangle is a obtuse angle.

Solution -14:-

$$\angle AFB + \angle ABC + \angle BCD + \angle CDE + \angle DEF + \angle EFA.$$

We know that the sum of angles of a triangle is 180° .

\therefore In $\triangle ABC$, we have

$$\angle CAB + \angle ABC + \angle BCA = 180^\circ \dots (i)$$

In $\triangle ACD$, we have

$$\angle PAC + \angle ACD + \angle CPA = 180^\circ \dots (ii)$$

In $\triangle ADE$, we have

$$\angle PAD + \angle ADE + \angle DAE = 180^\circ \dots (iii)$$

In $\triangle AEF$, we have

$$\angle FAE + \angle AEF + \angle EFA = 180^\circ \dots (iv)$$

Adding (i), (ii), (iii) and (iv), we get

$$\begin{aligned} & (\angle CAB + \angle ABC + \angle BCA) + (\angle PAC + \angle ACD + \angle CPA) \\ & + (\angle PAD + \angle ADE + \angle DAE) + (\angle FAE + \angle AEF + \angle EFA) \\ & = 720^\circ \end{aligned}$$

$$\therefore \angle AFB + \angle ABC + \angle BCD + \angle CDE + \angle DEF + \angle EFA = 720^\circ$$

$$\angle AFB = \angle CAB + \angle PAC + \angle PAD + \angle FAE;$$

$$\angle ABC = \angle BCA + \angle ACD;$$

$$\angle BCD = \angle CPA + \angle DAE;$$

$$\angle CDE = \angle AEF + \angle DAE; \quad \angle DEF = \angle EFA.$$

$$\therefore \angle AFB = \angle CAB + \angle BCA + \angle CPA + \angle DAE + \angle AEF + \angle EFA.$$

Solution - 15 :- .

(i) By Angle Sum Property of a triangle we have

$$\angle 4^\circ + \angle 3^\circ + \angle z = 180^\circ$$

$$\angle z = 180^\circ - 70^\circ$$

$$\angle z = 110^\circ.$$

 $\angle z$ and 40° are corresponding angles

$$\angle x = 40^\circ$$

 $\angle y$ and 30° are corresponding angles

$$\angle y = 30^\circ$$

(ii) By Angle Sum Property of a triangle, we have

 In $\triangle ABC$

$$x^\circ + 40^\circ + 90^\circ = 180^\circ$$

$$x^\circ = 180^\circ - 130^\circ$$

$$x^\circ = 50^\circ$$

 In $\triangle ACD$

$$45^\circ + 90^\circ + y^\circ = 180^\circ$$

$$y^\circ = 180^\circ - 135^\circ$$

$$y^\circ = 45^\circ$$

 (iii) By Angle sum Property of a $\triangle ABC$, we have

 In $\triangle ABC$

$$50^\circ + 90^\circ + x^\circ = 180^\circ$$

$$x^\circ = 180^\circ - 140^\circ$$

$$x^\circ = 80^\circ$$

~~(iv)~~ x° and y° is a linear pair

$$\angle x^\circ + \angle y^\circ = 180^\circ$$

$$80^\circ + y^\circ = 180^\circ$$

$$y^\circ = 100^\circ$$

(iv) By Angle sum Property of triangle, we have

 In $\triangle ADE$

$$x^\circ + 50^\circ + 40^\circ = 180^\circ$$

$$x^\circ = 180^\circ - 90^\circ$$

$$x^\circ = 90^\circ$$

$$\angle y = 50^\circ \quad [\text{corresponding angles}]$$

$$\angle z = 40^\circ \quad [\text{corresponding angles}]$$



Solution-16:-

Given that angle $\theta = 60^\circ$

Let the other angles be x and $2x$

[\because two angles are in the ratio $1:2$]

$$60^\circ + 2x + x = 180^\circ$$

$$60^\circ + 3x = 180^\circ$$

$$x = \frac{120^\circ}{3}$$

$$x = 40^\circ$$

two angles are $40^\circ, 80^\circ$

Solution-17:-

Given one angle of a triangle $= 100^\circ$

the two angles are in the ratio $= 2:3$

measures of angles be $2x$ and $3x$

respectively

$$2x + 3x + 100^\circ = 180^\circ$$

$$5x + 100^\circ = 180^\circ$$

$$5x = 180 - 100$$

$$x = 16^\circ$$

\therefore two angles are $32^\circ = 2(16)^\circ$

$$3(16)^\circ = 48^\circ$$

Solution-18:-

In a $\triangle ABC$

By Angle sum property of a triangle, we have

$$3\angle A + 4\angle B + 6\angle C = 180^\circ$$

$$3\angle A + 3\angle A + 3\angle A = 180^\circ$$

$$[\because 3\angle A = 4\angle B = 6\angle C]$$

$$9\angle A = 180^\circ$$

$$\angle A = 20^\circ$$

$$3\angle A = 3(20^\circ) = 60^\circ$$

$$4\angle B = 60^\circ \Rightarrow \angle B = 15^\circ$$

$$6\angle C = 60^\circ \Rightarrow \angle C = \frac{60^\circ}{6} = 10^\circ$$

Solution-20:-

Given $\angle A = 100^\circ$

$\angle PAB = 50^\circ, \angle P = 90^\circ$

$$\therefore \angle B + \angle PAB + \angle P = 180^\circ$$

$$\angle B = 180^\circ - 140^\circ = 40^\circ$$



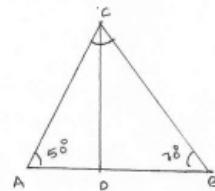


Solution - 21 :-

Given that,

$$\angle A = 50^\circ, \angle B = 70^\circ$$

By, Angle sum property of a triangle, we have .



$$\angle A + \angle B + \angle C = 180^\circ$$

$$50^\circ + 70^\circ + \angle C = 180^\circ$$

$$\angle C = 180^\circ - 120^\circ$$

$$\angle C = 60^\circ$$

Given that CD bisects AB in D.

In $\triangle ACD$

$$\angle ACD + \angle ADC + \angle A = 180^\circ \quad [A.S.P]$$

$$30^\circ + 30^\circ + \angle ADC = 180^\circ$$

$$\therefore \angle ADC = 120^\circ$$

In $\triangle DCB$

$$\angle B + \angle C + \angle DCB = 180^\circ$$

$$70^\circ + 30^\circ + \angle DCB = 180^\circ$$

$$\angle DCB = 180^\circ - 100^\circ$$

$$\therefore \angle DCB = 80^\circ$$

$$\therefore \angle DCB = 80^\circ, \angle ADC = 120^\circ$$

Solution - 22 :-

Given,

In $\triangle ABC, \angle A = 60^\circ, \angle B = 80^\circ$

i) By Angle sum property of a triangle, we have

$$\angle A + \angle B + \angle C = 180^\circ$$

$$60^\circ + 80^\circ + \angle C = 180^\circ$$

$$\angle C = 180^\circ - 140^\circ$$

$$\angle C = 40^\circ$$

ii) In $\triangle BOC$, we have

By Angle sum property of a triangle, we have

$$\angle B = 40^\circ, \angle C = 20^\circ, \angle BOC = ?$$

$$\angle B + \angle C + \angle BOC = 180^\circ \quad [A.S.P]$$

$$40^\circ + 20^\circ + \angle BOC = 180^\circ$$

$$\angle BOC = 180^\circ - 60^\circ$$

$$\angle BOC = 120^\circ$$



Solution - 23 :-

Given that,

The bisectors of the acute angles of a right angle meet at O.

$$\angle B = 90^\circ$$

$$\angle A + \angle C = 90^\circ$$

$$\angle A + \angle C = 90^\circ$$

$$\therefore \angle CAO + \angle COA = \frac{90^\circ}{2} = 45^\circ \quad [\text{bisectors}]$$

In $\triangle OAC$, we have

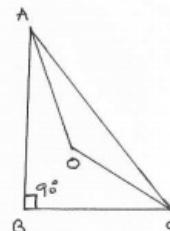
By Angle Sum Property of a triangle

$$\angle CAO + \angle COA + \angle COA = 180^\circ$$

$$45^\circ + \angle COA = 180^\circ$$

$$\angle COA = 180^\circ - 45^\circ$$

$$\angle COA = 135^\circ$$



Exercise-15.3

Exercise-15.3

Solution-01:-

(i) The interior adjacent angle of $\angle B$ is

$$\angle A \text{ and } \angle C$$

(ii) $\angle BAC$, $\angle ACB$:

$$\angle ABC, \angle ACB$$

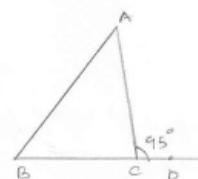
interior opposite angles to exterior $\angle B$.

Solution-02:-

Given,

exterior angle of a vertex $= 95^\circ$

interior opposite angle $= 55^\circ$



Let ABC be a triangle whose side BC produced to D to form a exterior angle $\angle ACD$ such that $\angle ACD = 95^\circ$.

Let $\angle B = 55^\circ$. By exterior angle theorem, we have

$$\angle ACD = \angle B + \angle A$$

$$95^\circ = 55^\circ + \angle A$$

$$\angle A = 95^\circ - 55^\circ$$

$$\angle A = 40^\circ$$

NOW, By using Angle sum property of a triangle, we have

$$\angle A + \angle B + \angle C = 180^\circ$$

$$40^\circ + 55^\circ + \angle C = 180^\circ$$

$$\angle C = 180^\circ - 95^\circ$$

$$\angle C = 85^\circ$$

The angles of a triangle are $40^\circ, 55^\circ$ and 85° .

**Solution-06:-**

Given

$$\angle ACD = 105^\circ$$

$$\angle EAF = 45^\circ$$

 $\angle ACD$ and $\angle ACB$ is a Linear pair

$$\angle ACD + \angle ACB = 180^\circ$$

$$105^\circ + \angle ACB = 180^\circ$$

$$\angle ACB = 180^\circ - 105^\circ$$

$$\angle ACB = 75^\circ.$$

since $\angle CAB$ and $\angle EAF$ are vertically opposite angles

$$\angle CAB = \angle EAF = 45^\circ$$

By using Angle sum Property of a triangle, we have

$$\angle CAB + \angle ACB + \angle ABC = 180^\circ$$

$$45^\circ + 75^\circ + \angle ABC = 180^\circ$$

$$\angle ABC = 180^\circ - 120^\circ$$

$$\angle ABC = 60^\circ$$

Solution-07:-

Given

$$\angle A : \angle B : \angle C = 3 : 2 : 1$$

By Angle sum property of a triangle, we have

measure of angles be $3x$, $2x$ and x

$$x + 2x + 3x = 180^\circ$$

$$6x = 180^\circ$$

$$x = 30^\circ$$

$$\angle A = 30^\circ \angle B = 90^\circ$$

$$\angle B = 60^\circ$$

$$\angle C = 30^\circ$$

$$\begin{aligned} \text{ACB} + \angle ACE + \angle ECD &= 180^\circ && [\text{Linear Pair}] \\ 90^\circ + 30^\circ + \angle ECD &= 180^\circ \end{aligned}$$

$$\angle ECD = 180^\circ - 120^\circ$$

$$\angle ECD = 60^\circ$$

Solution-08:-No, since sum of interior angles A and B
 $= 183^\circ > 180^\circ$.



Solution-09 :-

Given $\angle FCD = 50^\circ$.

$\angle BAD = ?$.

In $\triangle ABD$, we have

$$\angle ADB = 90^\circ.$$

$\angle FCD$ and $\angle BAD$ are vertically opposite angles

$$\angle FCD = \angle BAD$$

$$\therefore \angle BAD = 50^\circ.$$

Solution-10 :-

Given

$$\angle FDB = 60^\circ,$$

$$\angle FDC = 90^\circ$$

$$\angle BCF = ?.$$

$$\angle CFB + \angle FDC + \angle DCF = 180^\circ \quad [A.S.P]$$

$$\angle DCF = 180^\circ - 60^\circ - 90^\circ = 30^\circ$$

$$\angle DCF + x^\circ = 180^\circ \Rightarrow x^\circ = 180^\circ - 30^\circ = 150^\circ$$

[Linear pair] $\therefore x^\circ = 150^\circ$

Here,

$$\angle AED + 120^\circ = 180^\circ \quad (\text{Linear pair})$$

$$\Rightarrow \angle AED = 180^\circ - 120^\circ = 60^\circ$$

We know that the sum of all angles of a triangle is 180° .

Therefore, for $\triangle ADE$, we can say that :

$$\angle ADE + \angle AED + \angle DAE = 180^\circ$$

$$\Rightarrow 60^\circ + \angle ADE + 30^\circ = 180^\circ$$

Or,

$$\angle ADE = 180^\circ - 60^\circ - 30^\circ = 90^\circ$$

From the given figure, we can also say that :

$$\angle FDC + 90^\circ = 180^\circ \quad (\text{Linear pair})$$

$$\Rightarrow \angle FDC = 180^\circ - 90^\circ = 90^\circ$$

Using the above rule for $\triangle CDF$, we can say that :

$$\angle CDF + \angle DCF + \angle DFC = 180^\circ$$

$$\Rightarrow 90^\circ + \angle DCF + 60^\circ = 180^\circ$$

$$\angle DCF = 180^\circ - 60^\circ - 90^\circ = 30^\circ$$

Also,

$$\angle DCF + x = 180^\circ \quad (\text{Linear pair})$$

$$\Rightarrow 30^\circ + x = 180^\circ$$

Or,

$$x = 180^\circ - 30^\circ = 150^\circ$$

Q11

(i)

Here,

$$\angle BAF + \angle FAD = 180^\circ \text{ (Linear pair)}$$

$$\Rightarrow \angle FAD = 180^\circ - \angle BAF = 180^\circ - 90^\circ = 90^\circ$$

Also,

$$\angle AFE = \angle ADF + \angle FAD \text{ (Exterior angle property)}$$

$$\angle ADF + 90^\circ = 130^\circ$$

$$\angle ADF = 130^\circ - 90^\circ = 40^\circ$$

(ii)

We know that the sum of all the angles of a triangle is 180° .

Therefore, for $\triangle BDE$, we can say that :

$$\angle BDE + \angle BED + \angle DBE = 180^\circ.$$

$$\Rightarrow \angle DBE = 180^\circ - \angle BDE - \angle BED = 180^\circ - 90^\circ - 40^\circ = 50^\circ \dots (i)$$

Also,

$$\angle FAD = \angle ABC + \angle ACB \text{ (Exterior angle property)}$$

$$\Rightarrow 90^\circ = 50^\circ + \angle ACB$$

Or,

$$\angle ACB = 90^\circ - 50^\circ = 40^\circ$$

(iii) $\angle ABC = \angle DBE = 50^\circ$ [From (i)]

Solution -11:-

$$\text{Given } \angle AFE = 130^\circ$$

$$\angle CAB = 90^\circ$$

$$\angle PFB = 90^\circ$$

$$(i) \quad \angle BPE$$

$$\angle AFE = 130^\circ$$

$$\angle ACB = 40^\circ$$

$$\therefore \angle BAE + \angle ACB + \angle ABC = 180^\circ$$

$$\angle ABC = 180^\circ - 130^\circ - 40^\circ$$

$$\angle ABC = 50^\circ$$

$$(ii) \quad \angle BDE = 180^\circ - 50^\circ - 90^\circ$$

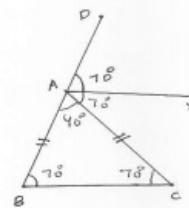
$$= 40^\circ$$

$$(iii) \quad \angle BCA = 40^\circ$$

$$(iv) \quad \angle ABC = 50^\circ$$



Solution-12:-



Given,

$$\angle BAX = 70^\circ$$

AX bisects exterior angle BAC

$$\text{so, } \angle BAX = \angle BAC$$

$$\therefore \angle BAC = 70^\circ$$

$\angle BAX$, $\angle BAC$ and $\angle BAC$ is linear pair

$$\angle BAX + \angle BAC + \angle BAC = 180^\circ$$

$$70^\circ + 70^\circ + \angle BAC = 180^\circ$$

$$\angle BAC = 180^\circ - 140^\circ$$

$$\angle BAC = 40^\circ.$$

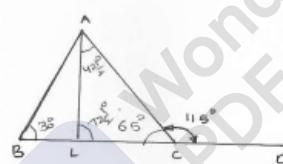
$$\text{Let } \angle B = \angle C = x.$$

By using Angle sum property of a triangle
we have, In $\triangle ABC$

$$40^\circ + x + x = 180^\circ \Rightarrow 2x = 180^\circ - 40^\circ = 140^\circ$$

$$\therefore \angle B = \angle C = 70^\circ$$

Solution-13:-



Given,

$$\angle BAC = 35^\circ \text{ & } \angle ACD = 115^\circ.$$

We have, In $\triangle ABC$

By using Angle sum property of a triangle

$$35^\circ + 65^\circ + \angle BAC = 180^\circ$$

$$\angle BAC = 180^\circ - 90^\circ$$

$$\angle BAC = 42\frac{1}{2}^\circ + 42\frac{1}{2}^\circ$$

$$\Rightarrow \angle BAL + \angle CAL = 42\frac{1}{2}^\circ + 42\frac{1}{2}^\circ$$

$$\therefore \angle BAL = 42\frac{1}{2}^\circ = \angle CAL.$$

By using Angle sum property of a triangle,
we have,

$$65^\circ + 42\frac{1}{2}^\circ + \angle ALC = 180^\circ$$

$$\angle ALC = 107\frac{1}{2}^\circ + 180^\circ$$

$$\angle ALC = 182\frac{1}{2}^\circ.$$



$$\angle APO = ?.$$

By using Angle Sum property of a triangle we have

In $\triangle ABC$,

$$60^\circ + 80^\circ + \angle C = 180^\circ$$

$$\angle C = 180^\circ - 140^\circ$$

$$\angle C = 40^\circ$$

In $\triangle ADC$,

$$40^\circ + 40^\circ + \angle ADC = 180^\circ$$

$$\angle ADC = 180^\circ - 80^\circ - 40^\circ$$

$$\angle ADC = 100^\circ$$

$$\angle APP + \angle POC = 100^\circ$$

$$\angle APP = 100^\circ - 15^\circ$$

$$= 85^\circ.$$

By using Angle sum property of a triangle we have

$$\angle APP + \angle ADP + \angle PAP = 180^\circ$$

$$[\angle A = \angle ADC +$$

$$\angle AOP = 180^\circ - 85^\circ - 40^\circ$$

$$[\angle AOP = \angle ADC]$$

$$\angle AOP = 180^\circ - 125^\circ$$

$$[\angle AOP = \angle ADP]$$

$$\angle AOP = 55^\circ.$$

Solution-15:-

(i) $\angle ACD$ and $\angle ACO$ is a Linear pair

$$75^\circ + \angle ACD = 180^\circ$$

$$\angle ACD = 105^\circ$$

[BC produced is
Let O]

By using Angle sum property of a triangle we have

In $\triangle ABC$,

$$\angle A + \angle B + \angle ACB = 180^\circ$$

$$\angle B = 180^\circ - 75^\circ - 40^\circ$$

$$\angle B = 180^\circ - 115^\circ$$

$$\angle B = 70^\circ$$

Solution-15 (ii)-

K'ABC Let AB produced is O.

$\angle BAC$ and $\angle BAC'$ is a linear pair

$$\angle BAC + \angle BAC' = 180^\circ$$

$$\angle BAC' = 180^\circ - 80^\circ$$

$$\angle BAC' = 100^\circ$$

By using Angle sum property of a triangle we have

$$\angle BAC' + \angle ABC + \angle C = 180^\circ$$

$$\angle ABC = 180^\circ - 100^\circ - 30^\circ$$

$$\angle ABC = 50^\circ.$$



Solution-15-(ii) :-

By using Angle sum property of a \triangle we have
In $\triangle ACD$,

$$\angle CAD + \angle ACD + \angle CDA = 180^\circ$$

$$\angle CDA = 180^\circ - 100^\circ - 38^\circ$$

$$\angle CDA = 50^\circ$$

$\angle BCD$ and $\angle ACB$ is a Linear pair

$$\angle ACD + \angle ACB = 180^\circ$$

$$\angle ACB = 180^\circ - 50^\circ = 130^\circ$$

$$\angle ACB = 80^\circ$$

By using Angle sum property of a \triangle we have

$$\angle BAC + 45^\circ + 80^\circ = 180^\circ$$

$$\angle BAC = 180^\circ - 125^\circ$$

$$\angle BAC = 55^\circ$$

$$x = 55^\circ, y = 50^\circ$$

Solution-15-(iv) :-

By using Angle sum property of a \triangle , we have
 $\angle PBC + \angle PCA + \angle PDC = 180^\circ$

$$\angle PBC = 180^\circ - 30^\circ - 50^\circ = 100^\circ$$

$\angle PBC$ and $\angle PBA$ is a Linear pair

$$\angle PBC + \angle PBA = 180^\circ$$

$$\angle PBA = 180^\circ - 100^\circ$$

$$= 80^\circ$$

$$x = 80^\circ$$

In $\triangle AEB$

$$\angle EAB + \angle AEB + \angle ABE = 180^\circ$$

$$30^\circ + 80^\circ + \angle AEB = 180^\circ$$

$$\angle AEB = 180^\circ - 110^\circ$$

$$\angle AEB = 70^\circ$$

$\angle AEB$ and $\angle AED$ is a Linear pair

$$70^\circ + \angle AED = 180^\circ$$

$$\angle AED = 180^\circ - 70^\circ$$

$$= 110^\circ$$

$$x = 80^\circ, y = 110^\circ$$

Solution-16 :-

(i) $\angle BAE$ and $\angle BAC$ is a Linear pair

$$\angle BAE + \angle BAC = 180^\circ$$

$$\angle BAC = 180^\circ - 120^\circ$$

$$\angle BAC = 60^\circ$$

$\angle ACB$ and $\angle ACD$ is a Linear pair

$$\angle ACB + \angle ACD = 180^\circ$$

$$\angle ACB = 180^\circ - 112^\circ$$

$$\angle ACB = 68^\circ$$

A.S.P

$$\Rightarrow \angle BAC + \angle BCA + \angle ABC = 180^\circ$$

$$\Rightarrow x^\circ = 180^\circ - 60^\circ - 68^\circ = 52^\circ$$



Solution-16:-

(ii) $\angle ACD$ and $\angle ACB$ is a Linear pair

$$\angle ACD + \angle ACB = 180^\circ$$

$$116^\circ + \angle ACB = 180^\circ$$

$$\angle ACB = 180^\circ - 116^\circ$$

$$\angle ACB = 70^\circ$$

$\angle EBA$ and $\angle ABC$ is a Linear pair

$$\angle EBA + \angle ABC = 180^\circ$$

$$\angle ABC = 180^\circ - 120^\circ$$

$$\angle ABC = 60^\circ$$

By using Angle sum property of a triangle, we have

$$\angle ACB + \angle ABC + \angle BAC = 180^\circ$$

$$70^\circ + 60^\circ + \angle BAC = 180^\circ$$

$$\angle BAC = 180^\circ - 130^\circ = 50^\circ \therefore x = 50^\circ$$

(iii) $\angle BAD$ and $\angle ADC$ are vertically opposite angles

$$\angle BAD = \angle ADC = 50^\circ$$

By using Angle sum property of a triangle, we have

$$\angle ADC = \angle EDC.$$

$$\text{In } \triangle EDC, \angle EDC + \angle ECD + \angle CED = 180^\circ$$

$$50^\circ + 40^\circ + x = 180^\circ$$

$$x = 180^\circ - 50^\circ - 40^\circ$$

$$x = 180^\circ - 90^\circ$$

$$x = 80^\circ.$$

Solution 16 :-

Ques

Given $\angle ABC = 45^\circ$,
 $\angle BCD = 50^\circ$,
 $\angle BAD = 35^\circ$.

Construction:- Extend line DC and it intersects AB at 'E'.

Required to find $\angle ADC$

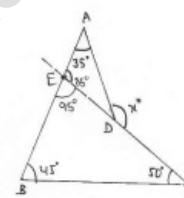
In $\triangle BCE$,

$$\angle ECB + \angle BCE + \angle CEB = 180^\circ \quad (\text{Sum of angles in a triangle is } 180^\circ)$$

$$\angle ABC + \angle BCD + \angle CEB = 180^\circ \quad (\because \angle ECB = \angle ABC) \\ 45^\circ + 50^\circ + \angle CEB = 180^\circ$$

$$\angle CEB = 180^\circ - 95^\circ$$

$$\angle CEB = 85^\circ$$



Consider line AB and line EG.

$\angle BEC$ and $\angle AEG$ form a linear pair.

$$\therefore \angle BEC + \angle AEG = 180^\circ$$

$$85^\circ + \angle AEG = 180^\circ$$

$$\angle AEG = 180^\circ - 85^\circ$$

$$= 95^\circ$$

$$\therefore \angle AEG = 95^\circ$$

In $\triangle AED$, $\angle ADC$ is exterior angle.

$\therefore \angle ADC = \text{Sum of two opposite interior angles}$

$$\angle ADC = \angle DAE + \angle AED$$

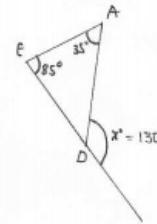
$$x^\circ = 35^\circ + \angle AEC$$

$$= 35^\circ + 90^\circ$$

$$= 130^\circ$$

$\therefore \angle ADC = 130^\circ$

$\therefore x^\circ = 130^\circ$





Exercise-15.4

Remove Watermark



Exercise-15.4.

i) Solution:-

(i) we have,

$$5+7 > 4, 5+9 > 7, 9+7 > 5$$

That is, the sum of any two of the given numbers is greater than the third number.

So, 5cm, 7cm & 9cm can be the lengths of the sides of a triangle

(ii) we have,

$$2+10 \neq 15$$

so, the given numbers cannot be the lengths of the sides of a triangle

(iii) we have.

$$3+4 > 5, 4+5 > 3, 5+3 > 4$$

That is, the sum of any two of the given numbers is greater than the third number.

So, 3cm, 4cm & 5cm can be the lengths of the sides of a triangle.

(iv) we have

$$2+5 \neq 7$$

so, the given numbers cannot be the lengths of the sides of a triangle.

(v) we have

$$5+8 \neq 20$$

so, the given numbers cannot be the lengths of the sides of a triangle.

Solution-02:-

(i) <

(ii) <

(iii) <

Solution-03:-

(i) False

(ii) True

(iii) False.

Solution-04:-

$$OA + OB > AB \quad \text{--- (1)}$$

$$\text{Similarly } OB + OC > BC \quad \text{--- (2)}$$

$$OC + OA > CA \quad \text{--- (3)}$$

Add (1), (2) & (3)

$$(OA + OB) + (OB + OC) + (OC + OA) > AB + BC + CA$$

$$\Rightarrow 2(OA + OB + OC) > AB + BC + CA$$

$$\Rightarrow OA + OB + OC > \frac{1}{2}(AB + BC + CA)$$



Solution :-

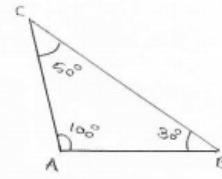
Given ,

In $\triangle ABC$

$$\angle A = 100^\circ, \angle B = 30^\circ, \angle C = 50^\circ.$$

$\rightarrow AC$ is the smallest side which is opposite to the smallest angle $\angle B$.

$\rightarrow BC$ is the largest side which is opposite to the largest angle $\angle A$.



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Exercise-15.5

Exercise -15.5.

Solution -01:-

Pythagoras theorem:-

In a right triangle, the square of the hypotenuse equal to the sum of the squares of its remaining two sides.

Converse of Pythagoras theorem:-

If the square of one side of triangle is equal to the sum of the squares of the other two sides, then the triangle is a right triangle with the angle opposite the first side as right angle

In $\triangle ABC$, we have

$$AB^2 = CA^2 + BC^2.$$

Solution -2:-

(i) $a = 6\text{cm}$, $b = 8\text{cm}$, $c = ?$.

wkt, by Pythagoras theorem

$$a^2 + b^2 = c^2$$

$$c^2 = 6^2 + 8^2$$

$$c^2 = 36 + 64$$

$$c = \sqrt{100} = 10\text{cm}.$$

Given,
(ii) $a = 8\text{cm}$, $b = 15\text{cm}$, $c = ?$.

$$a^2 + b^2 = c^2 \quad [\text{by Pythagoras theorem}]$$

$$8^2 + 15^2 = c^2$$

$$c^2 = 64 + 225$$

$$c^2 = 289$$

$$c = \sqrt{289} = 17\text{cm}$$

$$c = 17\text{cm}$$

(iii) Given,
 $a = 3\text{cm}$, $b = 4\text{cm}$ and $c = ?$

wkt, By Pythagoras theorem

$$a^2 + b^2 = c^2$$

$$3^2 + 4^2 = c^2$$

$$c^2 = 25$$

$$c = \sqrt{25} = 5\text{cm}$$

$$c = 5\text{cm}$$

(iv) Given,
 $a = 2\text{cm}$, $b = 1.5\text{cm}$ and $c = ?$

wkt, By Pythagoras theorem

$$a^2 + b^2 = c^2$$

$$2^2 + 1.5^2 = c^2$$

$$c = \sqrt{4 + 1.5 \times 1.5}$$

$$c = \sqrt{2.5 \times 2.5}$$

$$c = 2.5$$



Solution - 03:-

Given,

$$\text{Hypotenuse} = 2.5 \text{ cm}$$

$$\text{side} = 1.5 \text{ cm}$$

$$\text{side}_2 = ?$$

$$\text{side}^2 + \text{side}^2 = \text{hyp}^2$$

$$2.5^2 - 1.5^2 = \text{side}^2$$

$$\text{side}^2 = 4$$

$$\text{side} = \sqrt{4} = 2 \text{ cm.}$$

Solution - 04:-

Given Ladder Length = 3.7 m

Ladder Base = 1.2 m

∴ By using Pythagoras theorem

$$3.7^2 = 1.2^2 + \text{side}^2$$

$$13.69 - 1.44 = \text{side}^2$$

$$\text{side} = \sqrt{12.25}$$

$$\text{side} = 3.5 \text{ m.}$$

∴ required height = 3.5 m

Solution - 05:-

Given,

$$a = 3 \text{ cm}, b = 4 \text{ cm} \text{ and } c = 6 \text{ cm}$$

Here the Largest side is $c = 6 \text{ cm}$.

$$\text{we have } a^2 + b^2 = c^2$$

$$\text{clearly, } 3^2 + 4^2 \neq 6^2$$

$$9 + 16 \neq 36$$

So, the triangle with the given sides is not a right angle.

Solution - 06:-

(i) Given

$$a = 7 \text{ cm}, b = 24 \text{ cm} \text{ and } c = 25 \text{ cm}$$

Here the Larger side is $c = 25 \text{ cm}^2$

$$\text{we have: } a^2 + b^2 = c^2$$

$$7^2 + 24^2 = 25^2$$

$$49 + 576 = 625$$

$$625 = 625$$

So, the triangle with the given sides is a right triangle.

(ii) Here the Largest side $c = 18 \text{ cm}$.

$$\text{we have: } a^2 + b^2 = c^2$$

$$18^2 \neq 9^2 + 16^2$$

$$81 + 256 \neq 324$$

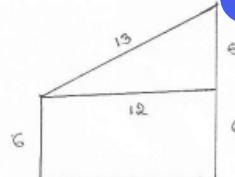
$$337 \neq 324$$

So, the triangle with the given sides is not a right triangle



Solution-07:-

Two poles of heights 6m and 11m
distance between their tops
 $= \sqrt{12} \text{ m.}$



$$\text{Side} = 11 \text{ m} - 6 \text{ m} \\ = 5 \text{ m}$$

∴ By using pythagoras theorem

$$5^2 + 12^2 = \text{Hyp}^2$$

$$\text{Hyp}^2 = 25 + 144$$

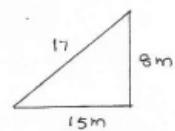
$$\text{Hyp} = \sqrt{169}$$

$$\text{Hyp} = 13 \text{ m.}$$

Solution-08:-

Given -

distances of sides are
15m and 8m.



How far is he from the starting point's hypotenuse

By using Pythagoras theorem

$$\text{Hyp}^2 = \text{side}^2 + \text{side}^2$$

$$\text{Hyp}^2 = 15^2 + 8^2 = 225 + 64 = 289$$

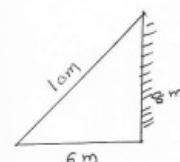
$$\text{Hyp} = \sqrt{289}$$

$$\text{Hyp} = 17.$$

Solution-09:-

Given,

In initial position
foot of a ladder = 6 m
height = 8 m.



By Applying Pythagoras theorem, we get

$$6^2 + 8^2 = \text{hyp}^2$$

$$36 + 64 = \text{hyp}^2$$

$$\text{hyp} = \sqrt{100}$$

$$= 10 \text{ m}$$

In Final position

foot of a ladder = 8 m

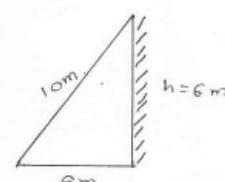
$$l = \text{hyp} = 10 \text{ m.}$$

$$10^2 = 8^2 + \text{height}^2$$

$$\text{height}^2 = 100 - 64$$

$$h = \sqrt{36}$$

$$\text{height} = 6 \text{ m.}$$





Solution -10:-

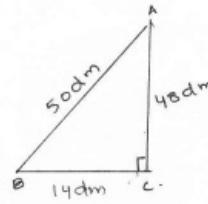
Given

$$\text{Ladder Length} = 50 \text{dm}$$

$$\text{height} = 48 \text{dm}$$

$$\text{base of the wall} = ?$$

$$\text{Ladder Length} = 50 \text{dm}$$



By Applying Pythagoras theorem we get

$$50^2 = 48^2 + \text{base}^2$$

$$\text{base}^2 = 2500 - 2304$$

$$\text{base}^2 = 196$$

$$\text{base} = \sqrt{196}$$

$$\text{base} = 14 \text{dm}$$

$$\therefore \text{base of the wall} = 14 \text{dm}.$$

Solution -11:-

The two legs of a right triangle are equal
and $\text{Hyp}^2 = 50$

$$\text{side}_1 = \text{side}_2 = \text{side}$$

$$\text{side}_1^2 + \text{side}_2^2 = \text{Hyp}^2 \quad [\because \text{Pythagoras theorem}]$$

$$2 \text{side}^2 = \text{Hyp}^2$$

$$\text{Side}^2 = \frac{50}{2}$$

$$\text{Side} = \sqrt{25}$$

$$\text{Side} = 5 \text{units.}$$

$$\therefore \text{length of each leg} = 5 \text{units.}$$

SOLUTION -12:-

(i) Given numbers are 12, 35 & 37

$$12^2 + 35^2 = 37^2$$

$$144 + 1225 = 1369.$$

(12, 35, 37) is a triplet

→ Yes.

(ii) Given numbers are 7, 24 and 25

By Pythagoras theorem

$$7^2 + 24^2 = 25^2$$

$$49 + 576 = 625$$

$$625 = 625$$

(7, 24, 25) is a triplet

→ Yes.



(iii) Given numbers are, 27, 36 and 45

By using Pythagoras theorem

$$27^2 + 36^2 \neq 45^2$$

$$729 + 1296 = 2025$$

$$2025 = 2025$$

(27, 36 & 45) is a triplet

→ Yes.

(iv) Given numbers are 15, 36 and 39

By using Pythagoras theorem

$$15^2 + 36^2 = 39^2$$

$$225 + 1296 = 1521$$

$$1521 = 1521$$

(15, 36, 39) is a triplet

→ Yes.

Solution -13 :-

Given,

$$\angle A = 85^\circ$$

$$\angle ABC = 105^\circ, \angle BAC = 35^\circ$$

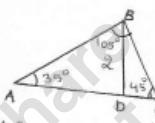
By using Angle sum property of a triangle, we have

$$105^\circ + 35^\circ + \angle C = 180^\circ$$

$$\angle C = 180^\circ - 140^\circ = 40^\circ$$

$$BD = 8 \text{ cm}$$

$$DC = 8 \text{ cm}$$



Solution -14 :-

Given,

In $\triangle ABC$, AD is the altitude from A

$$AD = 12 \text{ cm}$$

$$DC = 16 \text{ cm}$$

$$DB = 9 \text{ cm}$$

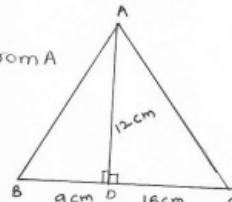
By using Pythagoras $\triangle ABD$, we have

$$9^2 + 12^2 = hyp^2$$

$$hyp^2 = 144 + 81$$

$$hyp^2 = 225$$

$$hyp = AB = 15 \text{ cm}$$



In $\triangle ADC$, we have

$$12^2 + 16^2 = hyp^2 = AC^2$$

$$144 + 256 = AC^2$$

$$AC = \sqrt{400}$$

$$AC = 20 \text{ cm}$$

No, $\triangle ABC$ is right angled at A.



Solution -15:-

Given that

$$AC = 4 \text{ cm}$$

$$BC = 3 \text{ cm}$$

$$\angle C = 105^\circ$$

By construction

$$AB = 4\sqrt{5} \text{ cm}$$

$$(AB)^2 = AC^2 + BC^2$$

$$(4\sqrt{5})^2 \neq 4^2 + 3^2$$

$$20 \cdot 25 \neq 25$$

$$20 \cdot 25 < 25$$

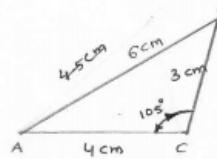
$$(6)^2 \neq 3^2 + 4^2$$

$$36 \neq 9 + 16$$

$$36 > 25$$

$$\text{No, } AB^2 \neq AC^2 + BC^2$$

$$(AB)^2 > AC^2 + BC^2$$



Solution-16:-

Given

$$AC = 4 \text{ cm},$$

$$BC = 3 \text{ cm} \text{ and } \angle C = 80^\circ$$

By construction, we get

$$AB = 4\sqrt{6}$$

By Pythagoras theorem

$$(AB)^2 = AC^2 + BC^2$$

$$(4\sqrt{6})^2 \neq 4^2 + 3^2$$

→ No,

$$(4\sqrt{6})^2 < 4^2 + 3^2 = 16 + 9 = 25$$

$$\therefore (AB)^2 < AC^2 + BC^2.$$

