$a_n = n^2 - n + 1$ ---(i) is the given sequence

Then, first 5 terms are a_1 , a_2 , a_3 , a_4 and a_5

$$a_1 = (1)^2 - 1 + 1 = 1$$

$$a_2 = (2)^2 - 2 + 1 = 3$$

$$a_3 = (3)^2 - 3 + 1 = 7$$

$$a_4 = (4)^2 - 4 + 1 = 13$$

$$a_5 = (5)^2 - 5 + 1 = 21$$

First 5 terms 1, 3, 7, 13 and 21.

Q2

$$a_n = n^3 - 6n^2 + 11n - 6$$
 $n \in \mathbb{N}$.

The first three terms are a_1 , a_2 and a_3

$$a_1 = (1)^3 - 6(1)^2 + 11(1) - 6 = 0$$

$$a_2 = (2)^3 - 6(2)^2 + 11(2) - 6 = 0$$

$$a_3 = (3)^3 - 6(3)^2 + 11(3) - 6 = 0$$

.. The 1st 3 terms are zero.

and

$$a_n = n^3 - 6n^2 + 11n - 6$$

= $(n-2)^3 - (n-2)$ is positive as $n \ge 4$

∴ a, is always positive.

Q3

$$a_n = 3a_{n-1} + 2$$
 for $n > 1$

$$a_2 = 3a_{2-1} + 2 = 3a_1 + 2$$

$$= 3(3) + 2 = 11$$

$$\left[: a_1 = 3 \right]$$

$$a_3 = 3a_{3-1} + 2 = 3a_2 + 2$$

= (11) + 2 = 35

$$\begin{bmatrix} \therefore a_1 = 3 \end{bmatrix}$$

$$\begin{bmatrix} \therefore a_2 = 11 \end{bmatrix}$$

$$\begin{bmatrix} \because a_3 = 35 \end{bmatrix}$$

$$a_4 = 3a_{4-1} + 2 = 3a_2 + 2$$

= 3(35) + 2 = 107

$$[\because a_3 = 35]$$

∴ The first four terms of A.P are 3, 11, 35, 107.



(i)
$$a_1 = 1, \ a_n = a_{n-1} + 2, \ n \ge 2$$

 $a_2 = a_{2-1} + 2 = a_{1+2} = 3$ $[\because a_1 = 1]$
 $a_3 = a_{3-1} + 2 = a_2 + 2 = 5$ $[\because a_2 = 3]$
 $a_4 = a_{4-1} + 2 = a_3 + 2 = 7$ $[\because a_3 = 5]$
 $a_5 = a_{5-1} + 2 = a_4 + 2 = 9$ $[\because a_4 = 7]$

: The first 5 terms of series are 1, 3, 5, 7, 11.

(ii)
$$a_1 = a_2 = 1$$

 $a_n = a_{n-1} + a_{n-2}$ $n > 2$
 $\Rightarrow a_3 = a_{3-1} + a_{3-2}$
 $= a_2 + a_1 = 1 + 1 = 2$
 $\Rightarrow a_4 = a_{4-1} + a_{4-2}$
 $= a_3 + a_2 = 2 + 1 = 3$
 $\Rightarrow a_5 = a_{5-1} + a_{5-2}$
 $= a_4 + a_3 = 5$

... The given sequence is 1,1,3,5.

(iii)
$$a_1 = a_2 = 2$$

 $a_n = a_{n-1} - 1 \quad n > 2$
 $\Rightarrow a_3 = a_{3-1} - 1$
 $= a_2 - 1$
 $= 2 - 1 = 1$
 $\Rightarrow a_4 = a_{4-1} - 1$
 $= a_3 - 1 = 1 - 1 = 0$
 $\Rightarrow a_5 = a_{5-1} - 1$
 $= 0 - 1 = -1$

:. The first 5 terms of the sequence are 2,2,1,0,-1.





$$a_n = a_{n-1} + a_{n-2}$$
 for $n > 2$
 $\Rightarrow a_3 = a_{3-1} + a_{3-2} = a_2 + a_1 = 1 + 1 = 2$

$$\Rightarrow$$
 $a_4 = a_{4-1} + a_{4-2} = a_3 + a_2 = 2 + 1 = 3$

$$\Rightarrow$$
 $a_5 = a_{5-1} + a_{5-2} = a_4 + a_3 = 3 + 2 = 5$

$$\Rightarrow$$
 $a_6 = a_{6-1} + a_{6-2} = a_5 + a_4 = 5 + 31 = 8$

$$\therefore \qquad \text{For } n = 1$$

$$\frac{\partial_{n+1}}{\partial_n} = \frac{\partial_2}{\partial_1} = \frac{1}{1} = 1$$

$$\text{For } n = 2$$

$$\frac{\partial^3}{\partial_2} = \frac{2}{1} = 2$$

$$\text{For } n = 3$$

$$\frac{\partial^4}{\partial_3} = \frac{3}{2} = 1.5$$

$$\text{For } n = 4 \qquad \text{and} \qquad n$$

$$\therefore$$
 The required series is $1, 2, \frac{3}{2}, \frac{5}{3}, \frac{8}{5}, \dots$

For
$$n = 3$$

$$\frac{a_4}{a_3} = \frac{3}{2} = 1.5$$
For $n = 4$ and $n = 5$

$$\frac{a_5}{a_4} = \frac{5}{3}$$
 and $\frac{a_6}{a_5} = \frac{8}{5}$

$$\therefore \text{ The required series is } 1, 2, \frac{3}{2}, \frac{5}{3}, \frac{8}{5}, \dots$$

$$\mathbf{Q6(i)}$$

$$3, -1, -5, -9...$$

$$a_1 = 3, \ a_2 = -1, \ a_3 = -5, \ a_4 = -9$$

$$a_2 - a_1 = -1 - 3 = -4$$

$$a_3 - a_2 = -5 - (-1) = -4$$

$$a_4 - a_3 = -9(-5) = -4$$

 \therefore Common difirence is d = -4

$$a_4 - a_3 = a_3 - a_2 = a$$

:. The given sequence is a A.P.

$$a_5 = 3 + (5 - 1)(-4) = -13$$

$$a_6 = 3 + (6 - 1)(-4) = -17$$

$$a_7 = 3 + (7 - 1)(-4) = -21$$

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Q6(ii)

$$-1, \frac{1}{4}, \frac{3}{2}, \frac{11}{4} \dots$$

$$a_1 = -1, \ a_2 = \frac{1}{4}, \ a_3 = \frac{3}{2}, \ a_4 = \frac{11}{4}$$

$$a_4 - a_3 = a_3 - a_2 = a_2 - a_1 = \frac{5}{4}$$

- $\therefore \text{ Common difference is } d = \frac{5}{4}$
- : The given sequence is A.P.

$$a_5 = -1 + (5 - 1) \frac{5}{4} = 4$$

$$a_6 = -1 + (6 - 1) \frac{5}{4} = \frac{21}{4}$$

$$a_7 = -1 + (7 - 1) \frac{5}{4} = \frac{26}{4} = \frac{13}{2}$$

Q6(iii)

Q6(iii)

(iii)
$$\sqrt{2}$$
, $3\sqrt{2}$, $5\sqrt{2}$, $7\sqrt{2}$...

 $a_1 = \sqrt{2}$, $a_2 = 3\sqrt{2}$, $a_3 = 5\sqrt{2}$, $a_4 = 7\sqrt{2}$
 $a_4 - a_3 = a_3 - a_2 = a_2 - a_1 = 2\sqrt{2}$

The common difference is $2\sqrt{2}$ and the given sequence is A.P

 $a_5 = \sqrt{2} + 2\sqrt{2}(5-1) = 9\sqrt{2}$
 $a_6 = \sqrt{2} + 2\sqrt{2}(6-1) = 11\sqrt{2}$
 $a_7 = \sqrt{2} + 2\sqrt{2}(7-1) = 13\sqrt{2}$

 \therefore The common difference is $2\sqrt{2}$ and the given sequence is A.P

$$a_5 = \sqrt{2} + 2\sqrt{2}(5 - 1) = 9\sqrt{2}$$

$$a_6 = \sqrt{2} + 2\sqrt{2}(6 - 1) = 11\sqrt{2}$$

$$a_7 = \sqrt{2} + 2\sqrt{2}(7 - 1) = 13\sqrt{2}$$

Q6(iv)

$$a_4 - a_3 = a_3 - a_2 = a_2 - a_1 = -2$$

∴ The common difference is - 2 and the given sequence is A.P.

$$a_5 = 9 + (-2)(5 - 1) = 1$$

 $a_6 = 9 + (-2)(6 - 1) = -1$
 $a_7 = 9 + (-2)(7 - 1) = -3$



$$a_n = 2n + 7$$

 $a_1 = 2(1) + 7 = 9$
 $a_2 = 2(2) + 7 = 11$
 $a_3 = 2(3) + 7 = 13$

Here,
$$a_3 - a_2 = a_2 - a_1 = 2$$

: The given sequence is A.P
 $a_7 = 2(7) + 7 = 21$

7th term is 21.

Q8

$$a_{n} = 2n^{2} + n + 1$$

$$a_{1} = 2(1)^{2} + (1) + 1 = 4$$

$$a_{2} = 2(2)^{2} + (2) + 1 = 11$$

$$a_{3} = 2(3)^{2} + (3) + 1 = 21$$

$$a_{3} - a_{2} \neq a_{2} - a_{1}$$

.. The given sequence is not as A.P as consequtive terms do not have a common difference.

- (i) 10th term of A.P 1, 4, 7, 10, ... Here, 1st term = $a_1 = 1$ and common difference d = 4 - 1 = 3We know $a_n = a_1 + (n-1)d$ $a_{10} = a_1 + (10 - 1)d$ $= 1 + (10 - 1)3 \Rightarrow 28$
- (ii) To find 18th term of A.P $\sqrt{2}$, $3\sqrt{2}$, $5\sqrt{2}$,... Here, 1st term $a_1 = \sqrt{2}$ $d = \text{common difference} = 2\sqrt{2}$ $a_n = a_1 + (n-1)d$ $a_{18} = \sqrt{2} + 2\sqrt{2} (17) = 35\sqrt{2}$
- (iii) Find nth term of A.P 13, 8, 3, -2 Here, $a_1 = 13$ d = -5 $a_n = a + (n-1)d$ = 13 + (n - 1)(-5)= -5n + 18

Q2

It is given that the sequence $\langle a_n \rangle$ is an A.P

$$\Rightarrow_n = a + (n-1)d \qquad ---(i)$$

Similarly from (i)

$$a_{m+n} = a + (m+n-1)d$$
 ---(ii)
 $a_{m-n} = a + (m-n-1)d$ ---(iii)

Adding (ii) and (iii)



(i) Let nth term of A.P = 248

$$a_n = 248 = a + (n-1)d$$

$$\Rightarrow$$
 248 = 3 + $(n-1)$ 5

$$\therefore$$
 $n = 50$

50th term of the given A.P is 248.

(ii) Which term of A.P 84,80,76 is 0?

Let nth term of A.P be 0

Then,
$$a_n = 0 = a + (n-1)d$$

 $0 = 84 + (n-1)(-4)$

$$\therefore \qquad n = 22$$

: 22nd term of the given A.P is 0.

(iii) Which term of A.P is 4, 9, 14,... is 254?

Let nth term of A.P be 254

$$a_n = a + (n - 1)d$$

$$254 = 4 + (n - 1)5$$

$$\therefore$$
 $n = 51$

: 51st term of the given A.P is 254.



Here,
$$a = 7$$

and
$$x = 10 - 7 = 3$$

$$\therefore a_n \text{ term is} = a + (n-1)d$$

$$= 7 + (n-1)3$$

Let 68 be nth temr of A.P

Then,

$$68 = 7 + 3(n - 1)$$

$$\Rightarrow$$
 68 = 7 + 3n - 3

$$\Rightarrow$$
 68 - 4 = 3n

$$\Rightarrow$$
 64 = 3n

$$\Rightarrow$$
 $n = \frac{64}{3}$

Which is not a natural number.

- : 68 is nota term of given A.P.
- (ii) Is 302 a term of A.P 3,8,13 Let 302 be nth ter, pf tje given A.P

Here,
$$302 = 3 + (n - 1)5$$

$$\frac{299}{5} = (n-1)$$

$$n = \frac{304}{5}$$

Which is not a natural number.

: 302 is not a term of given A.P.



(i) The given sequence is
$$24,23\frac{1}{4},22\frac{1}{2},21\frac{3}{4},...$$

Here,
$$a = 24$$

$$d = 23\frac{1}{4} - 24 = \frac{93 - 96}{4} = \frac{-3}{4}$$

Let nth term be the 1st negative term.

$$a_n < 0$$

 $a + (n - 1)d < 0$
 $24 - \frac{3}{4}(n - 1) < 0$
 $96 - 3n + 3 < 0$
 $99 < 3n$

or

34th term is 1st negative term.

(ii) The given sequence is
$$12+8i$$
, $11+6i$, $10+4i$,.

n > 33

$$d = -1 = 2$$

33 < n

: 34th term is 1st negative term.

(ii) The given sequence is
$$12 + 8i$$
, $11 + 6i$, $10 + 4i$,...

Here, $a = 12 + 8i$

$$d = -1 - 2i$$

Then, $a_n = a + (n - 1)d$

$$= 12 + 8i + (n - 1)(-1 - 2i)$$

$$= (13 - n) + i(10 - 2n)$$

Let nth term be purely real the (10-2n)=0 or n=5So, 5th term is purely real.

Let nth term be purely imaginary. Then, 13 - n = 0

So, 13th term is purely imaginary.

(i) The given A.P is 7, 10, 13, ... 43.

Let there be n terms,

then, n term = 43

or
$$43 = a_n = a + (n-1)d$$

$$\Rightarrow$$
 43 = 7 + (n - 1)3

$$\Rightarrow$$
 $n = 13$

Thus, there are 13 terms in the given sequence.

(ii) The given A.P is
$$-1, \frac{-5}{6}, \frac{-2}{3}, \frac{-1}{2}, \dots, \frac{10}{3}$$
?

Let there be n terms

then, *n*th term =
$$\frac{10}{3}$$

or
$$\frac{10}{3} = a_n = a + (n-1)a$$

or
$$\frac{10}{3} = a_n = a + (n-1)d$$

$$\Rightarrow \frac{10}{3} = -1 + (n-1)\left(\frac{-5}{6} + 1\right)$$

$$\Rightarrow n = 27$$
Thus, there are 27 terms in the given sequence.

Q7

Given: $a = 5$

$$d = 3$$

$$a_n = \text{last term} = 80$$

$$\Rightarrow$$
 $n = 27$

Given:
$$a = 5$$

$$d = 3$$

$$a_n = last term = 80$$

Let there be n terms

$$a_n = 80 = a + (n - 1)d$$

$$80 = 5 + (n - 1)3$$

∴ Thus, thre are 26 terms in the given sequence.

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Q8

Given that:

$$a_6 = 19 = a + (6 - 1)d$$
 --- (i)
 $a_{17} = 41 = a + (17 - 1)d$ --- (ii)

Solving (i) and (ii), we get
$$a = 9$$
 and $d = 2$

$$a_{40} = a + (40 - 1)d$$

$$= 9 + (40 - 1)2$$

$$= 9 + 39(2)$$

$$= 87$$

40th term of the given sequence is 87.

Q9

Given:

$$a_9 = 0$$

$$a + 8d = 0$$

$$a = -8d$$

$$a_{19} = a + (19 - 1)d$$

= $a + 18d$
= $-8d + 18d$
= $10d$

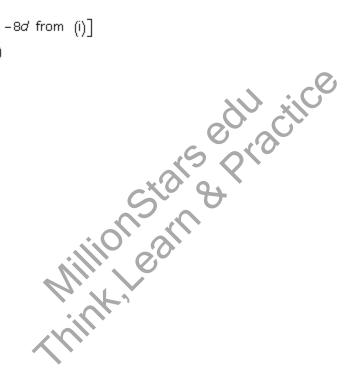
$$a_{29} = a + (29 - 1)d$$

= $-8d + 28d$
= $20d$

From (ii) and (iii)
$$a_{29} = 2a_{19}$$
 Hence proved.

$$[\because a = -8d \text{ from (i)}]$$
---(ii)

$$[\because a = -8d \text{ from (i)}]$$
---(iii)



Given:

$$10a_{10} = 15a_{15}$$

$$\Rightarrow 10(a + (10 - 1)d) = 15(a + (15 - 1)d)$$

$$\Rightarrow 10a + 90d = 15a + 210d$$

$$\Rightarrow 5a + 120d = 0$$

$$\Rightarrow a + 24d = 0 \qquad ---(i)$$

$$a_{25} = a + (25 - 1)d$$

$$= a + 24d$$

$$= 0 \qquad [: from (i) a + 24d = 0]$$

Hence proved.

Q11

Given:

$$a_{10} = 41 = a + 9d$$
 ---(i)
 $a_{18} = 73 = a + 17d$ ---(ii)
 $a_{19} = (i)$ and (ii)
 $a + 9d = 41$
 $a + 17d = 73$
 $a = 5$ and $d = 4$

We get
$$a = 5$$
 and $d = 4$

$$a_{26} = a + (26 - 1)d$$

$$= 5 + 25(4)$$

$$= 105$$

26th term of the given A.P is 105.

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Given:

$$a_{24} = 2a_{10}$$

$$\Rightarrow a + 23d = 2(a + 9d)$$

$$\Rightarrow a = 5d$$

$$a_{72} = a + (72 - 1)d$$

$$= a + 71d$$

$$\Rightarrow a_{72} = a + (34 - 1)d$$

$$a_{73} = a_{73} + (34 - 1)d$$

$$a_{74} = a_{75} + (34 - 1)d$$

$$a_{75} = a_{75} + (34 - 1)d$$

$$a_{75} = a_{75} + (34 - 1)d$$

$$a_{34} = a + (34 - 1)d$$

= $5d + 33d$ [: $a = 5d$ from (i)]
= $38d$ ---(iii)

From (ii) and (iii)
$$a_{72} = 2a_{34}$$
 Hence proved.

Q13

Given:

$$a_{m+1} = 2a_{n+1}$$

$$\Rightarrow a + (m+1-1)d = 2(a+(n+1-1)d)$$

$$\Rightarrow a + md = 2a + 2nd$$

$$\Rightarrow a = (m-2n)d \qquad ---(i)$$

Then,

$$a_{3m+1} = a + (3m+1-1)d$$

= $a + 3md$
= $3d - 2nd + 3md$
= $2(2m-n)d$ ----(ii)

$$a_{m+n+1} = a + (m+n+1-1)d$$

= $md - 2nd + md + nd$
= $(2m-n)d$ --- (iii)

From (ii) and (iii)
$$a_{2m+1} = 2a_{m+n+1} \qquad \qquad \text{Hence proved}.$$

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The given A.P is 9, 7, 5, ... and 15, 12, 9

$$A = 15$$

$$d = -2$$

$$D = 3$$

Let $a_n = A_n$ for same n.

$$a + (n - 1)d = A + (n - 1)d$$

$$\Rightarrow$$
 9 + $(n-1)(-2) = 15 + (n-1)3$

$$\Rightarrow$$
 $n = 7$

7th term of both the A.P is same.

Q15

(i) A.P is 3,5,7,9,...,201.

Here,
$$a = 3$$

$$d = 2$$

nth term from the end is l - (n-1)d

i.e.
$$201 - (n - 1)2$$
 or $203 - 2n$

12th term from end is

(ii) A.P is 3, 8, 13, ..., 253.

Then, 12th term from end is l - (n-1)d i.e.,

(iii) A.P is 1, 4, 7, 10, ..., 88

Then, 12th term from end is l - (n-1)d

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Given,

$$a_7 = 2a_3 + 1$$
 ---(ii)

Expanding (i) and (ii)

$$a + 3d = 2a$$

$$2a = 3d \text{ or } a = \frac{3d}{2} \qquad ---(iii)$$

$$a + 6d = 2a + 4d + 1$$

From (iii) and (iv)
$$a = 3$$
 and $d = 2$

: 1st term of the given A.P is 3, and common difference is 2.

Q17

$$a_6 = a + 5d = 12$$

$$a_8 = a + 7d = 22$$

Solving (i) and (ii)

$$a = -13$$
 and $d = 5$

Then,

$$a_n = a + (n - 1)d$$

= -13 + (n - 1)5
= 5n - 18

and

$$a_2 = a + (2 - 1) d$$

= -13 + 5
= -8

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The first two digit number divisible by 3 is 12. and last two digit number divisible by 3 is 99.

So, the required series is 12,15,18,...99. Let there be n terms then nth term = 99

$$\Rightarrow$$
 99 = $a + (n-1)d$

$$\Rightarrow$$
 99 = 12 + $(n-1)$ 3

$$\Rightarrow$$
 $n = 30$

30 two digit numbers are divisible by 3.

Q19

Given,

$$n = 60$$

$$a = 7$$

$$/ = 125$$

:
$$a + (n - 1)d = 125$$

$$7 + (59)d = 125$$

$$d = 2$$

$$\begin{array}{rcl} \therefore & a_{32} = a + (32 - 1)d \\ & = 7 + (31)2 \\ & = 69 \end{array}$$

32nd term is 69.

$$a_4 + a_8 = 24$$
 [Given]

$$\Rightarrow (a+3d)+(a+7d)=24$$

$$\Rightarrow \quad a + 5d = 12 \qquad \qquad ---(i)$$

$$a_6 + a_{10} = 34$$

$$\Rightarrow$$
 $(a + 5d) + (a + 9d) = 34$

$$a = \frac{-1}{2}$$
 and $d = \frac{5}{2}$

 \therefore 1st term is $\frac{-1}{2}$ and common difference is $\frac{5}{2}$.

Q21

The nth term from starting

$$=a_n=aa+(n-1)d$$

The nth term from end

$$= l - (n - 1)d$$

Adding (i) and (ii), we get

Sum of nth term from begining and nth term from the end

$$= a + (n-1)d + l - (n-1)d$$

$$= a + l$$
 Hence proved.



$$\frac{a_4}{a_7} = \frac{2}{3}$$

$$\frac{a+3d}{a+6d} = \frac{2}{3}$$

$$\Rightarrow$$
 $a = 3d$

$$\frac{a_6}{a_8} = \frac{a + 5d}{a + 7d}$$

$$\Rightarrow = \frac{3d + 5d}{3d + 7d}$$

$$\Rightarrow = \frac{8d}{10d}$$

$$\Rightarrow = \frac{4}{5}$$

$$\frac{a_6}{a_8} = \frac{4}{5}$$

[: 3d from (i)]

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Q23

$$\begin{split} &\sec \theta_1 \sec \theta_2 + \sec \theta_2 \sec \theta_3 + \dots + \sec \theta_{n-1} \sec \theta_n = \frac{\tan \theta_n - \tan \theta_1}{\sin d} \\ &\theta_2 - \theta_1 = \theta_3 - \theta_2 = \dots = d \\ &\sec \theta_1 \sec \theta_2 = \frac{1}{\cos \theta_1 \cos \theta_2} = \frac{\sin d}{\sin d (\cos \theta_1 \cos \theta_2)} \\ &= \frac{\sin (\theta_2 - \theta_1)}{\sin d (\cos \theta_1 \cos \theta_2)} \\ &= \frac{\sin \theta_2 \cos \theta_1 - \cos \theta_2 \sin \theta_1}{\sin d (\cos \theta_1 \cos \theta_2)} \\ &= \frac{1}{\sin d} \left[\frac{\sin \theta_2 \cos \theta_1}{(\cos \theta_1 \cos \theta_2)} - \frac{\cos \theta_2 \sin \theta_1}{(\cos \theta_1 \cos \theta_2)} \right] \\ &= \frac{1}{\sin d} [Tan\theta_2 - Tan\theta_1] \\ &\text{Similarly, } \sec \theta_2 \sec \theta_3 = \frac{1}{\sin d} [Tan\theta_3 - Tan\theta_2] \\ &\text{If we add up all terms, we get} \\ &= \frac{1}{\sin d} [Tan\theta_2 - Tan\theta_1 + Tan\theta_3 - Tan\theta_2 + \dots + Tan\theta_n - Tan\theta_{n-1}] \\ &= \frac{1}{\sin d} [Tan\theta_n - Tan\theta_1] \\ &\text{Hence Proved} \end{split}$$

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Ex 19.3

Q1

Let the 3rd term of A.P be a-d, a, a+dThen, a-d+a+a+d=21 3a=21 a=7and (a-d)(a+d)=a+6 $a^2-d^2=a+6$ $7^2-d^2=7+6$ $d^2=36$ $d=\pm6$

Since d can't be negative, therefore

:. The A.P is 1, 7, 13.

Q2

Let the 3 numbers in A.P are

$$a-d$$
, a , $a+d$

Then,

$$a - d + a + a + d = 27$$

$$3a = 27$$

and

$$(a-d)(a)(a+d) = 648$$

$$(9-d)9(9-d)=648$$

$$9^2 - d^2 = 72$$

$$d = 3$$

---(ii)

∴ The given sequence is 6, 9, 12.

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Let the four numbers in A.P be

$$a - 3d$$
, $a - d$, $a + d$, $a + 3d$
 $(a - 3d) + (a - d) + (a + d) + (a + 3d) = 50$
 $4a = 50$
 $a = \frac{25}{2}$ ----(i)

and

$$(a+3d) = 4(a-3d)$$

$$\frac{25+6d}{2} = 50-12d$$

$$30d = 75$$

$$d = \frac{25}{10} = \frac{5}{2}$$
 --- (ii)

: The required sequence is 5,10,15,20.

Q4

Let three numbers be a-d, a, a+d

$$3a = 12$$

$$a = 4$$

and

$$(a-d)^3 + a^3 + (a+d)^3 = \pm 288$$

$$a^{3} + d^{3} + 3ad(a+d) + a^{3} + a^{3} - a^{3} - 3ad(a-d) - 288$$

$$\Rightarrow$$
 $2a^3 + 3a^2d + 3ad^2 - 3a^2d + 3ad^2 = 288$

$$\Rightarrow$$
 $2a^3 + 3a^2d^2 = 288$

$$\Rightarrow$$
 128 + 48 d^2 = 288

∴ The required sequence is 2, 4, 6 or 6, 4, 2.

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Let 3 numbers in A.P be
$$a - d$$
, a and $a + d$

$$\Rightarrow (a - d) + (a) + (a + d) = 24$$
 $3a = 24$
 $a = 8$
and
$$(a - d)(a)(a + d) = 440$$
 $8^2 - d^2 = 55$
 $d = 3$

: The required sequence is 5, 8, 11.

Q6

Let the four angle be
$$a - 3d, a - d, a + d, a + 3d$$

Then,

sum of all angles = 360°
 $a - 3d + a - d + a + d + a + 3d = 360^{\circ}$
 $4a = 360^{\circ}$
 $a = 90^{\circ}$

and

 $(a - d) - (a - 3d) = 10$
 $2d = 10$
 $d = 5$

.. The angle of the given quadrilateral are 75°, 85°, 95° and 105°.

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Ex 19.4

Q1

(i) 50, 46, 42, ..., 10 terms
$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{10} = \frac{10}{2} [2 \times 50 + (10-1)(-4)]$$
= 320

(ii) 13,5,...,12 terms
$$S_{12} = \frac{12}{2} [2 \times 1 + (12 - 1)2]$$

$$= 6 \times 24 = 144$$

(iii)
$$3, \frac{9}{2}, 6, \frac{15}{2}, ..., 25 \text{ terms}$$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{25} = \frac{25}{2} (2 \times 3 + 24 \times \frac{3}{2})$$

$$= 525$$

(iv) 41,36,31,...,12 terms
$$S_n = \frac{n}{2} [2a + (n-1)d]$$
$$S_{25} = \frac{25}{2} [2 \times 41 + (11)(-5)]$$
$$= 162$$

(v)
$$a+b, a-b, a-3b, ...$$
 to 22 terms
$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{22} = \frac{22}{2} [2a + 2b + 21(-2b)]$$

$$= 22a - 440b$$

(vi)
$$(x-y)^2$$
, (x^2+y^2) , $(x+y)^2$, ..., x terms

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$= \frac{n}{2} [2(x^2+y^2-2xy) + (x-1)(-2xy)]$$

$$= n[(x-y)^2 + (n-1)xy]$$



$$\frac{x-y}{x+y}$$
, $\frac{3x-2y}{x+y}$, $\frac{5x-3y}{x+y}$,....to n terms

nth term in above sequence is $\frac{(2n-1)x-ny}{x+y}$

Sum of n terms is given by

$$\frac{1}{x+y} \Big[x+3x+5x+....+(2n-1)x-(y+2y+3y...+ny) \Big]$$

$$= \frac{1}{x+y} \Big[\frac{n}{2} (2x+(n-1)2x) - \frac{n(n+1)y}{2} \Big]$$

$$= \frac{1}{2(x+y)} \Big[2n^2x - 2n^2y - ny \Big]$$



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(i)
$$2+5+8+...+182$$
.
 a_n term of given A.P is 182
 $a_n = a + (n-1)d = 182$
 $\Rightarrow 182 = 2 + (n-1)3$
or $n = 61$
Then,
 $S_n = \frac{n}{2}[a+l]$
 $= \frac{61}{2}[2+182]$
 $= 61 \times 92$

= 5612

(ii)
$$101+99+97+...+47$$

 a_n term of A.P of n terms is 47.
 $\therefore 47 = a + (n-1)d$
 $47 = 101 + (n-1)(-2)$
or $n = 28$
Then,
 $S_n = \frac{n}{2}[a+l]$

$$S_n = \frac{n}{2} [a+l]$$

$$= \frac{28}{2} [101+47]$$

$$= 14 \times 148$$

$$= 2072$$

(iii)
$$(a-b)^2 + (a^2 + b^2) + (a+b)^2 + ... + [(a+b)^2 + 6ab]$$

Let number of terms be n

Then,

$$a_{n} = (a+b)^{2} + 6ab$$

$$\Rightarrow (a-b)^{2} + (n-1)(2ab) = (a+b)^{2} + 6ab$$

$$\Rightarrow a^{2} + b^{2} - 2ab + 2abn - 2ab = a^{2} + b^{2} + 2ab + 6ab$$

$$\Rightarrow n = 6$$
Then,
$$S_{n} = \frac{n}{2}[a+l]$$

$$S_{6} = \frac{6}{2}[a^{2} + b^{2} - 2ab + a^{2} + b^{2} + 2ab + 6ab]$$

$$= 6[a^{2} + b^{2} + 3ab]$$

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Q3

A.P formed is 1, 2, 3, 4, ..., n.

Here,

$$d = 1$$

$$I = n$$

So sum of
$$n$$
 terms = $S_n = \frac{n}{2} [2a + (n-1)d]$
= $\frac{n}{2} [2 + (n-1)1]$
= $\frac{n(n+1)}{2}$ is the sum of first n natural numbers.

Q4

The natural numbers which are divisible by 2 or 5 are:

$$2+4+5+6+8+10+\cdots+100 = (2+4+6+\cdots+100)+(5+15+25+\cdots+95)$$
 Now $(2+4+6+\cdots+100)$ and $(5+15+25+\cdots+95)$ are AP with common difference 2 and 10 respectively.

Therefore

ectively.
efore
$$2+4+6+\cdots+100=2\frac{50}{2}(1+50)$$

$$=2550$$
n
$$5+15+25+\cdots+95=5(1+3+5+\cdots+19)$$

Again

$$5+15+25+\dots+95 = 5(1+3+5+\dots+19)$$
$$= 5\left(\frac{10}{2}\right)(1+19)$$
$$= 500$$

Therefore the sum of the numbers divisible by 2 or 5 is:

$$2+4+5+6+8+10+\cdots+100 = 2550+500$$

= 3050

Q5

The series of n odd natural numbers are 1, 3, 5, ..., n

Where n is odd natural number Then, sum of n terms is

$$S_n = \frac{n}{2} [2a + (n-1)d]$$
$$= \frac{n}{2} [2(1) + (n-1)(2)]$$

$$= n^2$$

The sum of n odd natural numbers is n^2 .

The series so formed is 101, 103, 105, ..., 199

Let number of terms be n

Then,

$$a_n = a + (n - 1)d = 199$$

$$\Rightarrow$$
 199 = 101 + $(n-1)$ 2

The sum of
$$n$$
 terms = $S_n = \frac{n}{2} [a+l]$
$$S_{50} = \frac{50}{2} [101+199]$$

$$= 7500$$

The sum of odd numbers between 100 and 200 is 7500.

Q7

The odd numbers between 1 and 100 divisible by 3 are 3, 9, 15, ..., 999

Let the number of terms be n then, nth term is 999.

$$a_n = a(n-1)d$$

$$999 = 3 + (n - 1)6$$

$$\Rightarrow$$
 $n = 167$

The sum of n terms

$$S_n = \frac{n}{2} [a+l]$$

$$\Rightarrow S_{167} = \frac{167}{2} [3 + 999]$$
$$= 83667$$

Hence proved.

The required series is 85, 90, 95, ..., 715

Let there be n terms in the A.P

Then,

$$n \text{ th term} = 715$$

 $715 = 85 + (n - 1)5$

$$n = 127$$

Then,

$$S_n = \frac{n}{2} [a+l]$$

$$S_{127} = \frac{127}{2} [85+715]$$

Q9

The series of integers divisble by 7 between 50 and 500 are 56, 63, 70, ..., 497

Let the number of terms be n then, nth term = 497

$$a_n = a + (n-1)d$$

$$\Rightarrow$$
 497 = 56 + (n - 1)7

$$\Rightarrow$$
 $n = 64$

The sum
$$S_n = \frac{n}{2}[a+l]$$

$$\Rightarrow S_{64} = \frac{64}{2} [56 + 497]$$
$$= 32 \times 553$$
$$= 17696$$

Willions are a practice with the property of t



Q10

All even integers will have common difference = 2

$$\begin{array}{ll} \therefore & \text{A.P is } 102, 104, 106, ..., 998 \\ t_n = a + (n-1)d \\ t_n = 998, a = 102, d = 2 \\ 998 = 102 + (n-1)(2) \\ 998 = 102 + 2n - 2 \\ 998 - 100 = 2n \\ 2n = 898 \\ n = 449 \end{array}$$

S449 can be calculated by

$$S_n = \frac{n}{2} [a + l]$$

$$= \frac{449}{2} [102 + 998]$$

$$= \frac{449}{2} \times 1100$$

$$= 449 \times 550$$

$$= 246950$$

Q11

The series formed by all the integers between 100 and 550 which are divisible by 9 is 108,117,123,...,549

Let there be n terms in the A.P then, the nth term is 549

She have be note in the second terms in the
$$549 = a + (n - 1)d$$

$$549 = 108 + (n - 1)9$$

$$\Rightarrow n = 50$$
Then,
$$S_n = \frac{n}{2}[a + l]$$

$$S_n = \frac{n}{2} [a+l]$$

$$S_{50} = \frac{50}{2} [108 + 549]$$

$$= 16425$$

In the given series 3+5+7+9+... to 3n

Here,

$$a = 3$$

$$d = 2$$

Number of terms = 3n

The sum of n term is

$$S_n = \frac{n}{2} \Big[2a + (n-1)d \Big]$$

$$\Rightarrow S_{3n} = \frac{3n}{2} \left[6 + (3n - 1)2 \right]$$
$$= 3n (2n + 3)$$

Q13

The first number between 100 and 800 which on division by 16 leaves the remainder 7 is 112 and last number is 791.

Thus, the series so formed is 103,119,...,791

Let number of terms be n, then

Then,

$$a_n = a + (n-1)d$$

$$\Rightarrow$$
 791 = 103 + $(n-1)$ 16

Then, sum of all terms of the given series is

$$S_{43} = \frac{44}{2} [103 + 791]$$
$$= \frac{44 \times 894}{2}$$
$$= 19668$$



Here, sum of the given series of say n terms is 115 So, the nth term = x

Here,
$$a = 25$$
 and $d = 22 - 25 = -3$

$$\therefore a_n = a + (n-1)d$$

$$\Rightarrow \qquad x = 25 - 3(n - 1)$$

$$\Rightarrow x = 28 - 3n$$

The sum of n terms

$$S_n = \frac{n}{2} [a+l]$$

$$\Rightarrow 115 = \frac{n}{2} [25 + 28 - 3n]$$

$$\Rightarrow 230 = 53n - 3n^2$$

$$\Rightarrow$$
 $3n^2 - 53n - 230 = 0$

$$\Rightarrow 3n^2 - 30n - 23n - 230 = 0$$

$$\Rightarrow n = 10 \text{ or } \frac{23}{3}$$

But n can't be function

$$\therefore n = 10$$

$$x = 28 - 3n$$

$$= 28 - 3(10)$$

$$x = -2$$

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Sum first n terms of the given AP is

$$S_n = 3n^2 + 2n$$

$$S_{n-1} = 3(n-1)^2 + 2(n-1)$$

$$a_n = S_n - S_{n-1}$$

$$a_n = 3n^2 + 2n - 3(n-1)^2 - 2(n-1)$$

$$a_n = 6n - 1$$

$$a_r = 6r - 1$$

rth term is 6r - 1.

Q16

Given,

$$a_1 = -14 = a + 0d$$

$$a_5 = 2 = a + 4d$$

Solving (i) and (ii)

$$a_1 = a = -14$$
 and $d = 4$

Let ther be n terms then sum of there n terms = 40

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$\Rightarrow 40 = \frac{n}{2} \left[-28 + (n-1) 4 \right]$$

$$\Rightarrow$$
 $4n^2 - 32n - 80 = 0$

or
$$n = 10$$
 or -2

But n can't be negative

$$\therefore$$
 $n = 10$

The given A.P has 10 terms.

Given,

$$a_7 = 10$$

$$S_{14} - S_7 = 17$$

$$S_{14} = 17 + S_7 = 17 + 10 = 27$$

From (i) and (ii)

$$S_7 = \frac{7}{2} [2a + (7-1)d]$$

Using
$$S_n = \frac{n}{2} [2a + (n-1)d]$$

and

$$S_{14} = \frac{14}{2} [2a + 13d]$$

Solving (iii) and (iv)

$$a = 1$$
 and $d = \frac{1}{7}$

:. The required A.P is

$$1, 1 + \frac{1}{7}, 1 + \frac{2}{7}, 1 + \frac{3}{7}, \dots, +\infty$$

$$1, \frac{8}{7}, \frac{9}{7}, \frac{10}{7}, \frac{11}{7}, \dots, \infty$$

Q18

Given,

$$a_3 = 7 = a + 2d$$

$$a_7 = 3a_3 + 2$$

$$a_7 = 3(7) + 2$$

$$a = -1$$
, $d = 4$

= 23 = a + 6d

$$\Rightarrow S_{20} = \frac{20}{2} [2 + (20 - 1) 4]$$

Using
$$S_n = \frac{n}{2} \left[2a + (n-1) \right]$$

 $[U \operatorname{sing} S_n = \frac{n}{2}[2a + (n-1)d]]$ $= 10 \times 74$ = 740First term is -1 common defference = 4, sum of 20 terms = 740

Given,

$$a = 2$$
 $l = 50$

$$\therefore l = a + (n - 1)d$$

$$50 = 2 + (n - 1)d$$

$$(n - 1)d = 48$$

--- (i)

 S_n of all n terms is given 442

$$S_n = \frac{n}{2} [a+l]$$

$$442 = \frac{n}{2} [2+50]$$
or $n = 17$ ---- (ii)

From (i) and (ii)
$$d = \frac{48}{n-1} = \frac{48}{16} = 3$$

The common difference is 3.



Let no. of terms be 2n

Odd terms sum= $24=T_1+T_3+...+T_{2n-1}$

Even terms sum= $30=T_2+T_4+...+T_{2n}$

Subtract above two equations

nd=6

$$T_{2n} = T_1 + \frac{21}{2}$$

$$T_{2n} - a = \frac{21}{2}$$

$$(2n-1)d = \frac{21}{2}$$

$$12 - \frac{21}{2} = d = \frac{3}{2}$$

$$\Rightarrow n = 6 \times \frac{2}{3} = 4$$

Subtitute above values in equation of sum of even terms or odd terms, we get $a = \frac{3}{2}$ So series is $\frac{3}{2}$, 3, $\frac{9}{2}$

$$a=\frac{3}{2}$$

So series is
$$\frac{3}{2}$$
, 3, $\frac{9}{2}$

Remove Watermark

Q21

Let a be the first term of the AP and d is the common difference. Then

$$S_n = \frac{n}{2} (2a + (n-1)d)$$

$$n^2 p = \frac{n}{2} (2a + (n-1)d)$$

$$np = \frac{1}{2} [2a + (n-1)d]$$

$$2np = 2a + (n-1)d \qquad(1)$$

Again

$$S_{m} = \frac{m}{2} (2a + (m-1)d)$$

$$m^{2} p = \frac{m}{2} (2a + (m-1)d)$$

$$mp = \frac{1}{2} [2a + (m-1)d]$$

$$2mp = 2a + (m-1)d \qquad(2)$$

Now subtract (1) from (2)

$$2p(m-n) = (m-n)d$$

$$d = 2p$$

Therefore

$$2mp = 2a + (m-1) \cdot 2p$$
$$2a = 2p$$
$$a = p$$

The sum up to p terms will be:

$$S_{p} = \frac{p}{2} (2a + (p-1)d)$$

$$= \frac{p}{2} (2p + (p-1) \cdot 2p)$$

$$= \frac{p}{2} (2p + 2p^{2} - 2p)$$

$$= p^{3}$$

Hence it is shown.

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$$a_{12} = a + 11d = -13$$

 $s_4 = \frac{4}{2}(2a + 3d) = 24$

From (i) and (ii)
$$d = -2 \text{ and } a = 0$$

d = -2 and a = 9

Then,

Sum of irst 10 terms is

$$S_{10} = \frac{10}{2} [2 \times 9 + (9)(-2)]$$
$$= 0$$

$$\left[\text{Using } S_n = \frac{n}{2} \left[2a + (n-1)d \right] \right]$$

Sum of first 10 terms is zero.

Q23

$$a_5 = a + 4d = 30$$

 $a_{12} = a + 11d = 65$

From (i) and (ii)
$$d = 5$$
 and $a = 10$

Then,

Sum of irst 20 terms is

$$S_n = \frac{n}{2} \Big[2a + \left(n - 1 \right) d \Big]$$

$$\Rightarrow S_{20} = \frac{20}{2} [2 \times 10 + (20 - 1)5]$$
= 1150

Sum of first 20 terms is 1150.

Willions are a practice

Here,
$$a_k = 5k + 1$$

$$a_1 = 5 + 1 = 6$$

$$a_2 = 5(2) + 1 = 11$$

$$a_3 = 5(3) + 1 = 16$$

$$d = 11 - 6 = 16 - 11 = 5$$

$$S_n = \frac{n}{2}[2a + (n - 1)d]$$

$$= \frac{n}{2}[2(6) + (n - 1)(5)]$$

$$= \frac{n}{2}[12 + 5n - 5]$$

$$S_n = \frac{n}{2}(5n + 7)$$

sum of all two digit numbers which when divided by 4, yields 1 as remainder, \Rightarrow all 4n+1 terms with n \ge 3 13,17,21,..............97 n = 22, a = 13, d = 4 sum of terms $= \frac{22}{2} [26 + 21 \times 4] = 11 \times 110 - 10^{-10}$

Sum of terms 25, 22, 19,...., is 116

$$\frac{n}{2}[50 + (n-1)(-3)] = 116$$

$$\frac{n}{2}[53-3n]=116$$

$$53n - 3n^2 = 232$$

$$3n^2 - 53n + 232 = 0$$

$$3n^2 - 29n - 24n + 232 = 0$$

$$n(3n-29)-8(3n-29)=0$$

$$(3n-29)(n-8)=0$$

$$\Rightarrow n = 8or \frac{29}{3}$$

n cannot be in fraction, so n=8

last term=25-7 × 3=4

Q27

Let the number of terms is n.

Now the sum of the series is:

$$1+3+5+\cdots+2001$$

Here
$$l = 2001$$
 and $d = 2$.

Therefore

$$l=a+(n-1)d$$

$$2001 = 1 + (n-1) \cdot 2$$

$$2(n-1) = 2000$$

$$n-1=1000$$

$$n = 1001$$

Therefore the sum of the series is:

$$S = \frac{1001}{2} \left[2 + (1001 - 1)2 \right]$$

$$=1001^{2}$$

$$=1002001$$

Let the number of terms to be added to the series is n. Now a = -6 and d = 0.5.

Therefore

$$-25 = \frac{n}{2} \Big[2(-6) + (n-1)(0.5) \Big]$$

$$-50 = n \Big[-12 + 0.5n - 0.5 \Big]$$

$$-12.5n + 0.5n^2 + 50 = 0$$

$$n^2 - 25n + 100 = 0$$

$$n = 20.5$$

Therefore the value of n will be either 20 or 5.

Q29

Here the first term a = 2. Let the common difference is d. Now

the first term
$$a = 2$$
. Let the common difference is d .

$$\frac{5}{2} [2a + (5-1)d] = \frac{1}{4} [\frac{5}{2} [2(a+5d) + (5-1)d]]$$

$$\frac{5}{2} [2 \cdot 2 + 4d] = \frac{5}{8} [2 \cdot 2 + 14d]$$

$$10 + 10d = \frac{5}{2} + \frac{35}{4}d$$

$$\frac{5}{4}d = -7.5$$

$$d = -6$$

$$20^{th} \text{ term will be:}$$

$$a + (n-1)d = 2 + (20-1)(-6)$$

The 20th term will be:

$$a+(n-1)d=2+(20-1)(-6)$$

$$=-112$$

Hence it is shown.



$$S_{(2n+1)} = S_1 = \frac{(2n+1)}{2} [2a + (2n+1-1)d]$$

$$S_1 = \frac{(2n+1)}{2} [2a + 2nd]$$

$$= (2n+1)(a+nd) \qquad ---(i)$$

Sum of odd terms = S_2

$$S_{2} = \frac{(n+1)}{2} [2a + (n+1-1)(2d)]$$

$$= \frac{(n+1)}{2} [2a + 2nd]$$

$$S_{2} = (n+1)(a+nd) \qquad --- (ii)$$

From equation (i) and (ii),

$$S_1: S_2 = (2n+1)(a+nd): (n+1)(a+nd)$$

 $S_1: S_2 = (2n+1); (n+1)$

Q31

Here,

$$S_n = 3n^2$$

[Given]

Where n is number of term

$$S_n = \frac{n}{2} [2a + (n-1)d]$$
 --- (ii)

$$3n^2 = \frac{n}{2} [2a + (n-1)d]$$

 $6n = 2a + nd - d$

Equating both sides

$$6n = nd$$

$$d = 6$$

---(iii)

and

$$0 = 2a - d$$

or
$$d = 2a$$

---(iv)

From (iii) and (iv)
$$a = 3$$
 and $d = 6$

Millions are edulaciice Chink, earn



$$S_n = nP + \frac{1}{2}n(n-1)Q$$
 [Given]

$$S_n = \frac{n}{2}[2P + (n-1)Q]$$
 ---(i)

We know

$$S_n = \frac{n}{2} \left[2a + (n-1)d \right] \qquad ---(ii)$$

Where a =first term and d =common difference comparing (i) and (ii) d = Q

: The common difference is Q.

Q33

Let sum of n terms of two A.P be S_n and S'n.

Then, $S_n = 5n + 4$ and $S'_n = 9n + 16$ respectively.

Then, if ratio of sum of n terms of 2A.P is giben, then the ratio of there nth ther is obtained by replacing n by (2n-1).

$$\frac{a_n}{a_n'} = \frac{5(2n-1)+4}{9(2n-1)+16}$$

: Ratio of there 18th term is

$$\frac{a_{18}}{a'_{18}} = \frac{5(2 \times 18 - 1) + 4}{9(2 \times 18 - 1) + 16}$$
$$= \frac{5 \times 35 + 4}{9 \times 35 + 16}$$
$$= \frac{179}{321}$$

Millions are edulaciice Chink, earn

Let sum of n term of 1 A.P series be S_n are other S_n

The,
$$S_n = 7n + 2$$

$$S_n = n + 4$$

If the ratio of sum of n terms of 2 A.P is given, then the ratio of there nth term is obtained by replacing n by (2n-1).

$$\frac{a_n}{a_{n'}} = \frac{7(2n-1)+2}{(2n-1)+4}$$

Putting n = 5 to get the ratio of 5th term, we get

$$\frac{a_5}{a'5} = \frac{7(2 \times 5 - 1) + 2}{(2 \times 5 - 1) + 4} = \frac{65}{13} = \frac{5}{1}$$
tio is 5: 1.

The ratio is 5:1.





Ex 19.5

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Q1(i)

$$\frac{b+c}{a}, \frac{c+a}{b}, \frac{a+b}{c} \text{ will be in A.P if } \frac{c+a}{b} - \frac{b+c}{a} = \frac{a+b}{c} - \frac{c+a}{b}$$
if
$$\frac{ca+a^2-b^2-cb}{ab} = \frac{ab+b^2-c^2-ac}{bc}$$

LHS
$$\Rightarrow \frac{ca + a^2 - b^2 - cb}{ab}$$

 $\Rightarrow \frac{c^2a + a^2c - b^2c - c^2b}{abc}$
 $\Rightarrow \frac{c(a-b)[a+b+c]}{abc}$ ---(i)

RHS
$$\Rightarrow \frac{ab+b^2-c^2-ac}{bc}$$

 $\Rightarrow \frac{a^2b+ab^2-ac^2-a^2c}{abc}$
 $\Rightarrow \frac{a(b-c)[a+b+c]}{abc}$ ---(ii)
and since $\frac{1}{a}$, $\frac{1}{b}$, $\frac{1}{c}$ are in A.P

and since
$$\frac{1}{a}$$
, $\frac{1}{b}$, $\frac{1}{c}$ are in A.P
$$\frac{1}{b} - \frac{1}{a} = \frac{1}{c} - \frac{1}{b}$$

$$c(b-a) = a(b-c)$$

: LHS = RHS and the given terms are in A.P.

Q1(ii)

$$a(b+c)$$
, $b(c+a)$, $c(a+b)$ are in A.P if $b(c+a) - a(b+c) = c(a+b) - b(c+a)$

LHS =
$$b(c+a) - a(b+c)$$

= $bc + ab - ab - ac$
= $c(b-a)$ ---(i)

RHS =
$$c(a+b) - b(c+a)$$

= $ca + cb - bc - ba$
= $a(c-b)$ ---(ii)

and
$$\frac{1}{a}, \frac{1}{b}, \frac{1}{c}$$
 are in A.P

$$\frac{1}{a} - \frac{1}{b} = \frac{1}{b} - \frac{1}{c}$$
or $c(b-a) = a(c-b)$ ---(iii)

From (i),(ii) and (iii)
$$a(b+c),b(c+a),c(a+b) \text{ are in A.P}$$





$$\frac{a}{b+c}$$
, $\frac{b}{a+c}$, $\frac{c}{a+b}$ are in A.P if $\frac{b}{a+c}$ - $\frac{a}{b+c}$ = $\frac{c}{a+b}$ - $\frac{b}{a+c}$

LHS
$$= \frac{b}{a+c} - \frac{a}{b+c}$$

$$\Rightarrow \frac{b^2 + bc - a^2 - ac}{(a+c)(b+c)}$$

$$\Rightarrow \frac{(b-a)(a+b+c)}{(a+c)(b+c)}$$
---(i)

RHS =
$$\frac{a}{a+b} - \frac{b}{a+c}$$

$$\Rightarrow \frac{ca+c^2-b^2-ab}{(a+b)(b+c)}$$

$$\Rightarrow \frac{(c-b)(a+b+c)}{(a+b)(b+c)}$$
---(ii)

and
$$a^2, b^2, c^2$$
 are in A.P

$$b^2 - a^2 = c^2 - b^2$$
 --- (iii)

Substituting
$$b^2 - a^2$$
 with $c^2 - b^2$
(i) = (ii)

$$\therefore \frac{a}{b+c}, \frac{b}{a+c}, \frac{c}{a+b} \text{ are in A.P.}$$

Q3(i)

$$a^{2}(b+c), b^{2}(c+a), c^{2}(a+b)$$
 are in A.P.

If
$$b^2(c+a) - a^2(b+c) = c^2(a+b) - b^2(a+c)$$

$$\Rightarrow b^2c + b^2a - a^2b - a^2c = c^2a + c^2b - b^2a - b^2c$$

If
$$b^2(c+a) - a^2(b+c) = c^2(a+b) - b^2(a+c)$$

 $\Rightarrow b^2c + b^2a - a^2b - a^2c = c^2a + c^2b - b^2a - b^2c$
Given, $b - a = c - b$ [a, b, c are in A.P.]
 $c(b^2 - a^2) + ab(b - a) = a(c^2 - b^2) + bc(c - b)$
 $(b - a)(ab + bc + ca) = (c - b)(ab + bc + ca)$
Cancelling $ab + bc + ca$ from both sides
 $b - a = c - b$
 $2b = c + a$ which is true
Hence, $a^2(b+c)$, $(c+a)b^2$ and $c^2(a+b)$ are also in A.P.

Cancelling ab + bc + ca from both sides

$$b-a=c-b$$

 $2b=c+a$ which is true

Hence,
$$a^2(b+c)$$
, $(c+a)b^2$ and $c^2(a+b)$ are also in A.P.



Q3(ii)

(ii) T.P.b+c-a,c+a-b,a+b-c are in A.P.

b+c-a,c+a-b,a+b-c are in A.P only if (c+a-b)-(b+c-a)=(a+b-c)-(c+a-b)

LHS
$$\Rightarrow$$
 $(c+a-b)-(b+c-a)$

RHS
$$\Rightarrow$$
 $(a+b-c)-(c+a-b)$

Since,

$$b-a=c-b$$

or
$$a-b=b-c$$

Thus, given numbers

$$b+c-a,c+a-b,a+b-c$$
 are in A.F.

Q3(iii)

To prove
$$bc - a^2$$
, $ca - b^2$, $ab - c^2$ are in A.P

$$b-a=c-b$$

 $a-b=b-c$ ---(iii)
(i),(ii) and (iii)
LHS = RHS
given numbers
 $b+c-a,c+a-b,a+b-c$ are in A.P
)
ove $bc-a^2,ca-b^2,ab-c^2$ are in A.P
 $(ca-b^2)-(bc-a^2)=(ab-c^2)-(ca-b^2)$

$$LHS = \left(a - b^2 - bc + a^2\right)$$

$$= (a-b)[a+b+c]$$

RHS =
$$ab - c^2 - ca + b^2$$

$$= (b-c)[a+b+c]$$

and since a, b, c are in ab

$$b-c=a-b$$

and

...

Thus,
$$bc - a^2$$
, $ca - b^2$, $ab - c^2$ are in A.P.

Millions are edulaciice Williams Practice

(i) If
$$\frac{1}{a}$$
, $\frac{1}{b}$, $\frac{1}{c}$ are in A.P
$$\frac{1}{b} - \frac{1}{a} = \frac{1}{c} - \frac{1}{b}$$
LHS
$$= \frac{1}{b} - \frac{1}{a}$$

$$= \frac{a - b}{ab} = \frac{c(a - b)}{abc}$$
---(i)

RHS =
$$\frac{1}{c} - \frac{1}{b}$$

= $\frac{a(b-c)}{abc}$ ---(ii)

Since,
$$\frac{b+c}{a}$$
, $\frac{c+a}{b}$, $\frac{a+b}{c}$ are in A.P

$$\frac{b+c}{a} - \frac{c+a}{b} = \frac{c+a}{b} - \frac{a+b}{c}$$

$$\frac{b^2 + cb - ac - a^2}{ab} = \frac{c^2 + ac - ab - b^2}{bc}$$

$$\Rightarrow \frac{(b-a)(a+b+c)}{ab} = \frac{(c-b)(a+b+c)}{bc}$$
or
$$\frac{a(b-c)}{abc} = \frac{c(a-b)}{abc}$$
---(iii)

From (i), (ii) and (iii)
$$LHS = RHS$$

Hence,
$$\frac{1}{2}$$
, $\frac{1}{5}$, $\frac{1}{6}$ are in A.P

$$ca - bc = ab - ca$$

 $c(a - b) = a(b - c)$ ---(i)

If
$$\frac{1}{a}$$
, $\frac{1}{b}$, $\frac{1}{c}$ are in A.P
$$\frac{1}{b} - \frac{1}{a} = \frac{1}{c} - \frac{1}{b}$$

$$\Rightarrow c(a-b) = a(b-c) \qquad ---(ii)$$

Millions are edulaciice Chink, learn Thus, the condition necessary to prove bc, ca, ab in A.P is fullfilled.

Thus, bc, ca, ab, are in A.P.



(i) If
$$(a-c)^2 = 4(a-b)(b-c)$$

Then

$$a^2 + c^2 - 2ac = 4(ab - b^2 - ac + bc)$$

$$\Rightarrow$$
 $a^2 + c^2 4b^2 + 2ac - 4ab - 4bc = 0$

$$\Rightarrow (a+c-2b)^2=0$$

Using
$$(a+b+c)^2 = a^2+b^2+c^2+2ab+2ac+2bc$$

$$\therefore \quad a+c-2b=0$$

or
$$a+c=2b$$

and since.

$$a+c=2b$$

Hence proved.

$$(a-c)^2 = 4(a-b)(b-c)$$

[Given]

(ii) If
$$a^2 + c^2 + 4ac = 2(ab + bc + ca)$$

Then,

$$a^2 + c^2 + 2ac - 2ab - 2bc = 0$$

or
$$(a+c-b)^2-b^2=0$$

or
$$b = a + c - b$$

or
$$2b = a + c$$

$$b = \frac{a+c}{2}$$

and since,

$$b = \frac{a+c}{2}$$

Thus, $a^2 + c^2 + 4ac = 2(ab + bc + ca)$ Hence proved.

(iii) If
$$a^3 + c^3 + 6abc = 8b^3$$

or
$$a^3 + c^3 - (2b)^3 + 6abc = 0$$

or
$$a^3 + (-2b)^3 + c^3 + 3 \times a \times (-2b) \times c = 0$$

$$(a-2b+c)=0$$

or
$$a+c=2b$$

$$a-b=c-b$$

and since, a, b, c are in A.P

Thus,
$$a-b=c-b$$

Hence proved.
$$a^3 + c^3 + 6abc = 8b^3$$

$$\because (a+b+c)^2 = a^2 + b^2 + c^2 + 2ab + 2ac + 2bc$$

 $\begin{cases} \because x^3 + y^3 + z^3 + 3xyz = 0 \\ \text{or if } x + y + z = 0 \end{cases}$

Remove Watermark



Q6

Here,

$$a\left(\frac{1}{b} + \frac{1}{c}\right), \ b\left(\frac{1}{c} + \frac{1}{a}\right), \ c\left(\frac{1}{a} + \frac{1}{b}\right) \text{ are in A.P.}$$

$$\Rightarrow \quad a\left(\frac{1}{b} + \frac{1}{c}\right) + 1, \ b\left(\frac{1}{c} + \frac{1}{a}\right) + 1, \ c\left(\frac{1}{a} + \frac{1}{b}\right) + 1 \text{ are in A.P.}$$

$$\Rightarrow \quad \left(\frac{ac + ab + bc}{bc}\right), \ \left(\frac{ab + bc + ac}{ac}\right), \ \left(\frac{cb + ac + ab}{ab}\right) \text{ are in A.P.}$$

$$\Rightarrow \quad \frac{1}{bc}, \ \frac{1}{ac}, \ \frac{1}{ab} \text{ are in A.P.}$$

$$\Rightarrow \quad \frac{abc}{bc}, \ \frac{abc}{ac}, \ \frac{abc}{ab} \text{ are in A.P.}$$

Q7

 \times , y and z are in AP. Let d be the common difference then, v = x+d and z = x+2d

a, b, c are in A.P.

To show $x^2 + xy + y^2$, $z^2 + zx + x^2$ and $y^2 + yz + z^2$ are consecutive terms of an A.P., it is enough to show that,

$$(z^2 + zx + x^2) - (x^2 + xy + y^2) = (y^2 + yz + z^2) - (z^2 + zx + x^2)$$

LHS =
$$(z^2 + zx + x^2) - (x^2 + xy + y^2)$$

= $z^2 + zx - xy - y^2$
= $(x + 2d)^2 + (x + 2d)x - x(x + d) - (x + d)^2$
= $x^2 + 4xd + 4d^2 + x^2 + 2xd - x^2 - xd - x^2 - 2xd - d^2$
= $3xd + 3d^2$

RHS =
$$(y^2 + yz + z^2) - (z^2 + zx + x^2)$$

= $y^2 + yz - zx - x^2$
= $(x + d)^2 + (x + d)(x + 2d) - (x + 2d)x - x^2$
= $x^2 + 2dx + d^2 + x^2 + 2dx + xd + 2d^2 - x^2 - 2dx - x^2$
= $3xd + 3d^2$
: LHS = RHS
: $x^2 + xy + y^2$, $z^2 + zx + x^2$ and $y^2 + yz + z^2$ are consecutive terms of an A.P.

(i) 7 and 13

Let A be the arithematic mean of 7 and 13.

Then,

$$\Rightarrow$$
 $A-7=13-A$

$$\Rightarrow A = \frac{13+7}{2} = 10$$

A.M is 10.

(ii) 12 and -8

Let A be the arithematic mean of 12 and -8 Then.

$$\Rightarrow$$
 $A-12=-8-A$

$$\Rightarrow A = \frac{12 + (-8)}{2} = 2$$

.. A.M is 2.

(iii)
$$(x-y)$$
 and $(x+y)$

Let A be the arithematic mean of (x - y) and (x + y)

Then,

$$(x-y)$$
, A , $(x+y)$ are in A.P

$$\Rightarrow$$
 $A - (x - y) = (x + y) - A$

$$\Rightarrow A = \frac{(x-y)+(x+y)}{2} = \frac{2x}{2} = x$$

... A.M is x.



Let
$$A_1$$
, A_2 , A_3 , A_4 be the 4 A.M.s between 4 and 19 Then,
4, A_1 , A_2 , A_3 , A_4 , 19 are in A.P of 6 terms
$$A_n = a + (n-1)d$$

$$a_6 = 19 = 4 + (6-1)d$$
or $d = 3$ ----(i)
Now,
$$A_1 = a + d = 4 + 3 = 7$$

$$A_2 = A_1 + d = 7 + 3 = 10$$

$$A_3 = A_2 + d = 10 + 3 = 13$$

The 4 A.M.s between 4 and 19 are 7, 10, 13, 16.

 $A_4 = A_3 + d = 13 + 3 = 16$

Q3

$$2, a_1, a_2, a_3, a_4, a_5, a_6, a_7, 17$$

$$17 = a + 8d$$

$$a = 2 \Rightarrow d = \frac{15}{8}$$

$$a_1 = 2 + \frac{15}{8} = \frac{31}{8}$$

$$a_2 = \frac{31}{8} + \frac{15}{8} = \frac{46}{8}$$

so we get our final series as

$$2, \frac{31}{8}, \frac{46}{8}, \frac{61}{8}, \frac{76}{8}, \frac{91}{8}, \frac{106}{8}, \frac{121}{8}, \frac{136}{8} = 17$$

Let A_1 , A_2 , A_3 , A_4 , A_5 , A_6 be the 6 AM's between 15 and - 13

Here,
$$-13 = a_8 = a + 7d$$

$$\Rightarrow$$
 -13 = 15 + 7 d

or
$$d = -4$$

$$A_1 = a + d = 15 - 4 = 11$$

$$A_2 = a + 2d = 15 - 2(4) = 7$$

$$A_3 = a + 3d = 15 - 4(3) = 3$$

$$A_4 = a + 4d = 15 - 4(4) = -1$$

$$A_5 = a + 5d = 15 - 4(5) = -5$$

$$A_6 = a + 6d = 15 - 4(6) = -9$$

The 6 A.M.s between 15 and -13 are 11,7,3,-1,-5 and -9

Q5

Let the n A.M's between 3 and 17 be $A_1, A_2, A_3, ..., A_n$ Then,

$$AT\zeta$$

$$\frac{A_n}{A_1} = \frac{3}{1}$$

We know that

3,
$$A_1$$
, A_2 , A_3 , ..., A_n , 17 are in A.P of $n+2$ terms

So, 17 is the (n+2) th terms.

i.e.
$$17 = 3 + (n + 2 - 1)d$$

[Using
$$a_n = a + (n-1)d$$
]

or
$$d = \frac{1}{\sqrt{r}}$$

$$d = \frac{14}{(n+1)}$$

$$A_n = 3 + (n+1-1)d$$

$$=3+\frac{14n}{n+1}=\frac{17n+3}{n+1}$$

$$A_1 = 3 + d = \frac{3n + 17}{n + 1}$$

From (i), (iii) and iv

$$\frac{A_n}{A_1} = \frac{17n + 3}{3n + 17} = \frac{3}{1}$$

There are 6 A'M between 3 and 17.

Remove Watermark

---(i)



Q6

Let there be n A.M between 7 and 71 and let the A.M's be $A_1, A_2, A_3, ..., A_n$. So,

[∵a=7]

7,
$$A_1$$
, A_2 , A_3 , ..., A_n , 71 are in A.P of $(n+2)$ terms

$$A_5 = a_6 = a + 5d = 27$$
 [Given]

The
$$(n+2)$$
 th term of A.P is 71

$$a_{n+2} = 7 = a + (n+2-1)d$$

or
$$n = 15$$

There are 15 AM's between 7 and 71.

Q7

Let $A_1, A_2, A_3, A_4, \ldots, A_n$ be the n AMs inserted between two number a and b. Then,

$$A_1, A_2, A_3, A_4, ..., A_n, b$$
 are in A.P

So, the mean of a and b

$$A.M = \frac{a+b}{2}$$

The mean of A_1 and A_n

$$A.M = \frac{a+d+b-d}{2} = \frac{a+b}{2}$$

Similarly mean of A_2 and A_{n-1}

A.M =
$$\frac{a + 2d + b - 2d}{2} = \frac{a + b}{2}$$

Similarly we observe the means is equidistant from begining and the end is constant $\frac{a+b}{2}$.

The AM is
$$\frac{a+b}{2}$$
.



Q8

Here,

 A_1 is the A.M of x and y,

 A_2 is the A.M of y and z. and

Then,

$$A_1 = \frac{X + Y}{2}$$

$$A_2 = \frac{y+z}{2} \qquad ---(ii)$$

Let A.M be the arithematic mean of A_1 and A_2 Then,

$$A.M = \frac{A_1 + A_2}{4}$$

$$= \frac{x + y + y + z}{4}$$

$$= \frac{x + 2y + z}{4} \qquad ----(iii)$$

Since, 4, y, z are in A.P

$$y = \frac{x + a}{2} \qquad ---(iv)$$

From (iii) and (iv)

$$= \frac{x + 2y + z}{4} \qquad ---(iii)$$

$$4, y, z \text{ are in A.P} \qquad [Given]$$

$$y = \frac{x + a}{2} \qquad ---(iv)$$

$$(iii) \text{ and (iv)}$$

$$A.M = \frac{\left(\frac{x + a}{2}\right) + \left(\frac{2y}{2}\right)}{2} = \frac{y + y}{2} = y$$

$$e, \text{ proved A.M between } A_1 \text{ and } A_2 \text{ is } y.$$

Hence, proved A.M between A_1 and A_2 is y.

Q9

$$8, a_1, a_2, a_3, a_4, a_5, 26$$

$$a = 8$$

$$a + 6d = 26$$

$$\Rightarrow d = \frac{18}{6} = 3$$

So series is 8, 11, 14, 17, 20, 23, 26

Ex 19.7

Q1

Let the amount saved by the man in first year be x.

$$x + (x + 100) + (x + 200) + ... + (x + 900) = 16500$$

As his saving increased by Rs 100 every year.

$$\therefore$$
 10x + 100 + 200 + ... + 900 = 16500

--- (i)

Here,

100 + 200 + 300 + ... + 900 form a seried of

$$a = 100$$
, $d = 100$ and $n = 9$

So,

$$S_n = \frac{n}{2} [a+l]$$

$$S_9 = \frac{9}{2} [100 + 900] = 4500$$

--- (ii)

$$10x + (4500) = 16500$$

$$10x = 12000$$

or
$$x = 1200$$

The man saved Rs 1200 in the first year.

Q2

Let the man save Rs 200 in n number then,

A70

It rorms a series of n terms, with a = 32 and d = 4

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$\Rightarrow$$
 200 = $\frac{n}{2}[2(32) + (n-1)4]$

$$\Rightarrow 400 = 60n + 4n^2$$

$$\Rightarrow n^2 + 15n - 100 = 0$$

$$\Rightarrow$$
 $n = 5 \text{ or } -20$

But,
$$n \neq -20$$

$$\therefore n = 5$$

The man will save Rs 200 in 5 years.

Alillion earn a link. Learn a link.

Let the 40 annual instalments form an alithmetic series of common diference d and first instalment a. Then, series so firmed is

$$a + (a + d) + (a + 2d) + ... = 3600$$

or
$$s_n = \frac{n}{2} [2a + (n-1)d]$$

or
$$3600 = 20[2a + 39d]$$

and sum of first 30 terms is $\frac{2}{3}$ of 3600

$$\Rightarrow 2400 = \frac{30}{2} [2a + (29)d]$$

$$a = 51$$

The first installment paid by this man is Rs 51.

Q4

Let the number of Radio manufactured increase by x each year and number of radio manufacture in first year be a. So, A.P formed ATQ is

$$a, a + x, a + 2x, ...$$

Here,

$$a_3 = a + 2x = 600$$

$$a_7 = a + 6x = 700$$

---(i)

---(ii)

$$a = 550, x = 25$$

- (i) 550 Radio's were manufactured in the first year.
- (ii) The total produce in 7 years is sum of produce in the first 7 years.

$$S_7 = \frac{7}{2} [550 + 700]$$
$$= 4375$$

e first 7 years.
$$\left[\because S_n = \frac{n}{2} [a+l] \right]$$

= 4373

4375 Radio's were manufactured in first 7 years.

(iii) The product in 10th year

$$a_{10} = a + 9d$$

= 550 + 9 (25) = 775

775 Radio's were manufactured in the 10th year.



There are 25 trees at equal distance of 5 m in a line with a well(w), and the distance of the well from the nearesst tree = 10 m.

Thus.

The total distance travelled by gardener to tree 1 and back is $2 \times 10 \text{ m} = 20 \text{ m}$ Similarly for all the 25 trees.

The distance covered by gardener is

$$= 2[10 + (10 + 5) + (10 + 2 \times 5) + (10 + 3 \times 5) + ... + (10 + 23 \times 5)]$$
 --- (i)

This forms a series of 1st term a = 10, common difference d = 5 and n = 25

$$\Rightarrow S_{25} = \frac{25}{2} [2 \times 10 + (24)5] = 25 [10 + 60] = 1750 \text{ m} \qquad --- (ii)$$

From (i) and (ii)

Total distance = $2 \times 1750 \text{ m} = 3500 \text{ m}$.

Q6

The man counts at the rate of Rs 180 per minute for half an hour. After this he counts at the rate of Rs 3 less every minute than preceding minute.

Then, the amount counted in first 30 minute

The amount left to be counted after 30 minute

ATQ

A.P formed is
$$(180 - 3) + (180 - 2 \times 3) + ... = 5310$$

Let time taken to count 5310 be t

Then.

$$S_t = \frac{t}{2} [(180 - 3) + (t - 1)(-3)]$$

$$5310 = \frac{t}{2} [200 - 3t]$$

Thus, the total time taken by the man to count Rs 10710 is (59+30) = 89 minutes.



The piece of equipment deprecites 15% in first year i.e., $\frac{15}{100} \times 600,000 = \text{Rs } 90,000$

The equipment deprecites at the rate 135% in 2nd year i.e., $\frac{135}{1000} \times 600,000 = 81000$

Value after 2nd year = 81000

The value after 3rd year = $\frac{12}{100} \times 600000 = 72000$

The total depreciation in 10 years

$$S_{10} = \frac{10}{2} [2 \times 81000 + (9)(-9000)]$$

$$= 5[81000]$$

$$= 405000$$

$$\left[\text{Using } S_n = \frac{n}{2} [2a + (n-1)d] \right]$$

: The cost of machine after 10 years = Rs 600000 - 405000 = 105000.

Q8

Total cost of tractor

$$= 6000 + \left[(500 + 12\% \text{ of } 6000 \text{ for } 1 \text{ year}) + (500 + 12\% \text{ of } 5500 \text{ 1 year}) + \dots + 12 \text{ times} \right]$$

$$= 6000 + 6000 + \frac{12}{100} (6000 + 5500 + \dots + 12 \text{ times})$$

$$= 12000 + \frac{12}{100} \left[\frac{12}{2} (6000 + 5000) \right]$$

$$= 12000 + \frac{12}{100} \times \frac{12}{2} \times 6500$$

$$= 12000 + (72 \times 65)$$

$$= 12000 + 4680$$

$$= 16680$$
tal cost of tractor = Rs. 16680

Total cost of tractor = Rs. 16680

Remove Watermark

Q9

Total cost of Scooter

= Rs4000 +
$$\left\{ \text{Rs } 1000 + \text{S.I. on Rs Rs } 18000 \text{ for 1 year} \right\} + \left\{ \text{Rs } 1000 + \text{S.I. on Rs Rs } 17000 \text{ for 1 year} \right\} + \dots + 18 \text{ times}$$
= $\left(4000 + 18000 \right) + \text{S.I. for 1 year on } \left(18000 + 17000 + \dots \text{ to } 18 \text{ times} \right)$
= $22000 + \text{S.I. for 1 year on } \left\{ \frac{18}{18000 + 1000} \right\}$

= 22000 + S.I. for 1 year on
$$\left\{ \frac{18}{2} (18000 + 1000) \right\}$$

$$= 22000 + 9 (19000) \times \frac{10}{100}$$

- = 22000 + 17100
- = Rs 39100

Total cost of Scooter = Rs. 39100

Q10

First year the person income is: 300,000

Second year his income will be: 300,000 + 10,000 = 310,000

This way he receives the amount after 20 years will be:

$$300,000 + 310,000 + \cdots + 490,000$$

This is an AP with first term a = 300000 and common difference d = 10,000.

Therefore

$$S = \frac{20}{2} [2.300000 + (20 - 1)10000]$$
$$= 10[600000 + 190000]$$
$$= 7900000$$

Q11

In 1st installment the man paid 100 rupees.

In 2^{nd} installment the man paid (100+5)=105 rupees.

Likewise he pays up to the 30th installment as follows:

 $100+105+\cdots+(100+5\times29)$

This is an AP with a = 100 and common difference d = 5. Therefore at the 30th installment the amount he will pay

$$T_{30} = 100 + (30 - 1)(5)$$

= 100 + 145
= 245

Millions are appractice.

White are a practice.

Suppose carpenter took n days to finish his job.

First day carpenter made five frames $a_1 = 5$

Each day after first day he made two more frames d=2

∴ On nⁱⁿ day frames made by carpenter are,

$$a_n = a_1 + (n-1)d$$

$$\Rightarrow a_n = 5 + (n-1)2$$

Sum of all the frames till n[™] day is

$$S = \frac{n}{2} [a_i + a_n]$$

$$192 = \frac{n}{2} [5 + 5 + (n - 1)2]$$

$$192 = 5n + n^2 - n$$

$$n^2 + 4n - 192 = 0$$

$$(n+16)(n-12)=0$$

$$n = -16$$
 or $n = 12$

But number of days cannot be negative hence n = 12.

The carpenter took 12 days to finish his job.

We know that sum of interior angles of a polygon with n sides is given by,

$$a_n = 180^{\circ} (n - 2)$$

Sum of interior angles of a polygon with 3 sides is given by,

$$a_1 = 180^{\circ} (3 - 2) = 180^{\circ} \dots (i)$$

Sum of interior angles of a polygon with 7 sides is given by,

$$a_4 = 180^{\circ}(4-2) = 360^{\circ}....(ii)$$

Sum of interior angles of a polygon with 5 sides is given by,

$$a_s = 180^{\circ}(5 - 2) = 540^{\circ}....(iii)$$

From eq" (i), eq" (ii) and eq" (iii) we get,

$$a_4 = 360^\circ = 180^\circ + 180^\circ = a_1 + 180^\circ = a_1 + d$$

$$a_x = 540^\circ = 180^\circ + 360^\circ = a_1 + 2d$$

Hence the sums of the interior angles of polygons with 3, 4, 5, 6,. sides form an arithmetic progression.

Sum of interior angles of 21 sided polygon

$$= 180^{\circ}(21 - 2)$$

Q14

20 potatoes are placed in a line at intervals of 4 meters.

The first potato 24 meters from the starting point.

$$a_1 = 24$$

$$a_2 = a_1 + d = 24 + 8 = 32$$

$$a_n = a_1 + (n-1)d$$

$$a_{2n} = 24 + 19 \times 4 = 24 + 76 = 100$$

$$S = \frac{20}{2} [a_1 + a_{2b}] = 10[24 + 100] = 1240$$

Millions are edulaciice
Chink, Learn As contestant is required to bring the potatos back to the starting point.

The distanced contestant would run

- = 1240 + 1240
- = 2480 m.

Q15(i)

A man accepts a position with an initial salary of Rs.5200 per month.

$$a_1 = 5200$$

Man will receive an automatic increase of Rs.320.

$$d = 320$$

We need to find his salary for the n™ month is given by,

$$a_n = a_1 + (n-1)d$$

$$a_{10} = 5200 + 9 \times 320 = 8080$$

The salary of that man for tenth month is Rs.8080.

Q15(ii)

A man accepts a position with an initial salary of Rs.5200 per month.

$$a_1 = 5200$$

Man will receive an automatic increase of Rs.320.

$$d = 320$$

Man's salary for the n™ month is given by,

$$a_n = a_1 + (n-1)d$$

Total earnig of the man for the first year

$$= \frac{12}{2} [a_1 + a_{12}]$$

Total earnig of the man for the first year is Rs. 83,520.

Millions are a practice

Millions are a practice.

Williams are a practice.

Q16

Suppose the man saved Rs. x in the first year

$$a_i = x$$

In each succeeding year after the first year man saved Rs 200 more then what he saved in the previous year.

$$d = 200$$

Man saved Rs. 66000 in 20 years.

$$S = 66000$$

$$\frac{20}{2}[a_i + a_i + (20 - 1)200] = 66000$$

$$a_1 = 1400$$

Man saved Rs 1400 in the first year.

Q17

Suppose the award increases by Rs. \times .

$$d = x$$

In cricket team tournament 16 teams participated.

$$n = 16$$

The last place team is awarded Rs. 275 in prize money

Sum of Rs. 8000 is to be awarded as prize money

$$S = 8000$$

$$\frac{16}{2}$$
[$a_i + a_i + (16 - 1) \times$] = 8000

$$2a_1 + 15 \times = 1000$$

$$15 \times = 450$$

$$x = 30$$

The amount received by first place team

$$= a_{16}$$

$$= a_i + (16 - 1) d$$

$$= 275 + 15 \times 30$$

$$= 275 + 450$$

$$= 725$$

The amount received by first place team is Rs. 725.