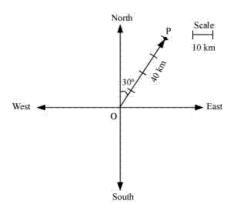


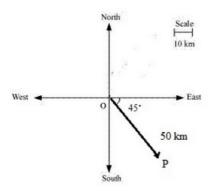
## Ex 23.1

### Algebra of Vectors Ex 23.1 Q1(i)



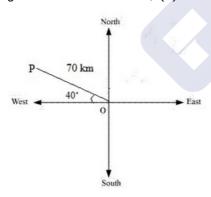
Here, vector  $\overrightarrow{OP}$  represents the displacement of 40 km, 30° East of North.

### Algebra of Vectors Ex 23.1 Q1(ii)



Here, vector  $\overrightarrow{OP} \, represents the displacement of 50 km, south-east$ 

### Algebra of Vectors Ex 23.1 Q1(iii)



Here, vector  $\overrightarrow{OP}$  represents the displacement of 70 km, 40° north of west

### Algebra of Vectors Ex 23.1 Q2

- (i) 15 kg is a scalar quantity because it involves only mass
- (ii)  $20\,kg\,weight\,$  is a vector quantity as it involves both magnitude and direction.
- (iii) 45° is a scalar quantity as it involves only magnitude.
- (iv) 10 meters south-east is a vector quantity as it involve direction.
- (v) 50 m/s2 is a scalar quantity as it involves magnitude of acceleration.

Million State & Practice
William Rearing Practice

Nondershare Robbeleinent



### Algebra of Vectors Ex 23.1 Q3

- Remove Watermark Wondershare PDFelement
- (i) Time period is a scalar quantity as it involves only magnitude.
- (ii) Distance is a scalar quantity as it involves only magnitude.
- (iii)Displacement is vector quantity as it involves both magnitude and direction.
- (iv) Force is a vector quantity as it involves both magnitude and direction.
- (v) Work done is a scalar quantity as it involves only magnitude.
- (vi) Velocity is a vector quantity as it involves both magnitude as well as direction.
- (vii) Acceleration is a vector quantity because it involves both magnitude as well as direction.

### Algebra of Vectors Ex 23.1 Q4

(i)

Collinear vectors are

 $\vec{x}$ , $\vec{z}$  and  $\vec{b}$ 

ÿ,ċ

ā,ā

(ii)

Equal vectors are

 $\vec{y}$  and  $\vec{c}$ 

 $\vec{x}$  and  $\vec{b}$ 

 $\vec{a}$  and  $\vec{d}$ 

(iii)

Coinitial vector are

 $\vec{a}$  ,  $\vec{y}$  and  $\vec{z}$ 

(iv)

Collinear but not equal

 $\vec{b}$  and  $\vec{z}$ 

 $\vec{x}$  and  $\vec{z}$ 

### Algebra of Vectors Ex 23.1 Q5

- (i) a and b are collinear, it is true.
- (ii) Two collinear vectors are may not be equal in magnitude, so it is false.
- (iii) Zero vector may not be unique, so it is false.
- (iv) Two vectors having same magnitude are may not be collinear so it is false.
- (v) Two collinear vectors having the same magnitude are may not be equal, so it is false.

Million Stars Practice
Williams And Stars Practice



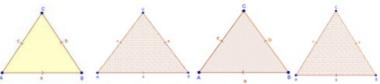
Given that, P, Q, R are collinear.

It also given that,  $\overrightarrow{PQ} = \overrightarrow{a}$  and  $\overrightarrow{QR} = \overrightarrow{b}$ 

$$\overrightarrow{PR} = \overrightarrow{PQ} + \overrightarrow{QR}$$
$$= \overrightarrow{a} + \overrightarrow{b}$$

 $\overrightarrow{PR} = \overrightarrow{a} + \overrightarrow{b}$ 

### Algebra of Vectors Ex 23.2 Q2



Given that,  $\bar{a}, \bar{b}$ , and  $\bar{c}$  are three sides of a triangle.

$$\vec{a} + \vec{b} + \vec{c}$$

$$= \vec{A}\vec{B} + \vec{B}\vec{C} + \vec{C}\vec{A}$$

$$= \vec{A}\vec{C} + \vec{C}\vec{A}$$

$$= \vec{A}\vec{C} - \vec{A}\vec{C}$$

$$[Since  $\vec{A}\vec{B} + \vec{B}\vec{C} = \vec{A}\vec{C}]$ 

$$= \vec{0}$$$$

So, 
$$\vec{a} + \vec{b} + \vec{c} = \vec{0}$$

Triangle law says that, if vectors are represented in magnitude and direction by the two sides of triangle taken is same order, then their sum is represented by the third side taken in reverse order.

Thus,  

$$\vec{a} + \vec{b} = \vec{c}$$
  
or  
 $\vec{a} + \vec{c} = \vec{b}$   
 $\vec{b} + \vec{c} = \vec{a}$ 

### Algebra of Vectors Ex 23.2 Q3

Here, it is given that  $\vec{a}$  and  $\vec{b}$  are two non-collinear vectors having the same initial point.

Let  $\vec{a} = \overrightarrow{AB}$  and  $\vec{b} = \overrightarrow{AD}$ , So we can draw a parallelogram ABCD as above.

By the properties of parallelogram  $\overrightarrow{BC} = \overrightarrow{b}$  and  $\overrightarrow{DC} = \overrightarrow{a}$ 

In  $\triangle ABC$ , Using triangle law,  $\overrightarrow{AB} + \overrightarrow{BC} = \overrightarrow{AC}$  $\vec{a} + \vec{b} = \overrightarrow{AC}$ --(i)In  $\triangle ABD$ ,

Using triangle law,  $\overrightarrow{AD} + \overrightarrow{DB} = \overrightarrow{AB}$  $\vec{b} + \vec{DB} = \vec{a}$  $\overrightarrow{DB} = \overrightarrow{a} - \overrightarrow{b}$ - -(ii)

From equation (i) and (ii), we get that

Willion Stars Practice  $\vec{a} + \vec{b}$  and  $\vec{a} - \vec{b}$  are diagonals of a parallelogram whose adjacent sides are  $\vec{a}$  and  $\vec{b}$ 

Given that m is a scalar and  $\vec{a}$  is a vector such that  $\vec{ma} = \vec{0}$ 

$$m(a_1\hat{i} + b_1\hat{j} + c_1\hat{k}) = 0 \times \hat{i} + 0 \times \hat{j} + 0 \times \hat{k}$$

$$ma_1\hat{i} + mb_1\hat{j} + mc_1\hat{k} = 0 \times \hat{i} + 0 \times \hat{j} + 0 \times \hat{k}$$

since let 
$$\vec{a} = a_1 \hat{i} + b_1 \hat{j} + c_1 \hat{k}$$

Comparing the coefficients of  $\hat{i}$ ,  $\hat{j}$ ,  $\hat{k}$  of LHS and RHS,

$$ma_1 = 0 \Rightarrow m = 0$$
 or  $a_1 = 0$  (i)

$$mb_1 = 0 \Rightarrow m = 0$$
 or  $b_1 = 0$  (ii)

$$mc_1 = 0 \Rightarrow m = 0$$
 or  $c_1 = 0$  (iii

From (i), (ii) and (iii)

$$m = 0$$
 or  $a_1 = b_1 = c_1 = 0$ 

$$\Rightarrow m = 0 \qquad \text{or} \quad \vec{a} = a_1 \hat{i} + b_1 \hat{j} + c_1 \hat{j} = 0$$

$$\Rightarrow m = 0$$
 or  $\vec{a} = 0$ 

### Algebra of Vectors Ex 23.2 Q5

Let 
$$\vec{a} = a_1 \hat{i} + b_1 \hat{j} + c_1 \hat{k}$$
  

$$\vec{b} = a_2 \hat{i} + b_2 \hat{j} + c_2 \hat{k}$$

Given that, a = -b

$$a_1\hat{i} + b_1\hat{j} + c_1\hat{k} = -a_2\hat{i} - b_2\hat{j} - c_2\hat{k}$$

Comparing the coefficients of i, j, k in LHS and RHS,

$$a_1 = -a_2$$

$$b_1 = -b_2 \tag{}$$

$$c_1 = -c_2$$
 (3)

$$|\vec{a}| = \sqrt{a_1^2 + b_1^2 + c_1^2}$$

Using (1), (2) and (3),

$$\left| \overrightarrow{\partial} \right| = \sqrt{\left( -\partial_2 \right)^2 + \left( -b_2 \right)^2 + \left( -c_2 \right)^2}$$

$$|\vec{a}| = \sqrt{a_2^2 + b_2^2 + c_2^2}$$

$$\therefore |\vec{a}| = |\vec{b}|$$

(ii)

Given a and b are two vectors such that  $|\vec{a}| = |\vec{b}|$ 

It means magnitude of vector  $\vec{a}$  is equal to the magnitude of vector  $\vec{b}$ , but we cannot conclude anything about the direction of the vector.

So, it is false that

$$|\vec{a}| = |\vec{b}| \Rightarrow \vec{a} = \pm \vec{b}$$

Given for any vector  $\vec{a}$  and  $\vec{b}$ 

$$\left| \vec{\hat{a}} \right| = \left| \vec{\hat{b}} \right|$$

Willion Stars & Practice
Williams Stars & Practice It means magnitude of the vector  $\vec{a}$  and  $\vec{b}$  are equal but we cannot say any thing about the direction of the vector  $\vec{a}$  and  $\vec{b}$ . And we know that  $\vec{a} = \vec{b}$  means magnitude and same direction. So, it is false.



In AADC, using triangle law, we get

 $\overrightarrow{CD} + \overrightarrow{DA} = \overrightarrow{CA}$ --(i)

In AABC, using triangle law, we get  $\overrightarrow{BC} + \overrightarrow{CA} = \overrightarrow{BA}$ --(ii)

Put value of  $\overrightarrow{CA}$  in equation (ii),  $\overrightarrow{BC} + \overrightarrow{CD} + \overrightarrow{DA} = \overrightarrow{BA}$ 

Adding  $\overrightarrow{BA}$  on both the sides,  $\overrightarrow{BA} + \overrightarrow{BC} + \overrightarrow{CD} + \overrightarrow{DA} = \overrightarrow{BA} + \overrightarrow{BA}$ 

 $\therefore \overrightarrow{BA} + \overrightarrow{BC} + \overrightarrow{CD} + \overrightarrow{DA} = 2\overrightarrow{BA}$ 

### Algebra of Vectors Ex 23.2 Q7

Given that ABCDE is a pentagon.

$$\overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{CD} + \overrightarrow{DE} + \overrightarrow{EA}$$

$$= (\overrightarrow{AB} + \overrightarrow{BC}) + \overrightarrow{CD} + \overrightarrow{DE} + \overrightarrow{EA}$$

$$= \overrightarrow{AC} + \overrightarrow{CD} + \overrightarrow{DE} + \overrightarrow{EA}$$
[Using triangle law in  $\triangle ABC$ ,  $\overrightarrow{AB} + \overrightarrow{BC} = \overrightarrow{AC}$ ]
$$= (\overrightarrow{AC} + \overrightarrow{CD}) + \overrightarrow{DE} + \overrightarrow{EA}$$

$$= (\overrightarrow{AD}) + \overrightarrow{DE} + \overrightarrow{EA}$$
[Using triangle law in  $\triangle ACD$ ,  $\overrightarrow{AC} + \overrightarrow{CD} = \overrightarrow{AD}$ ]

 $= \overrightarrow{AD} + \overrightarrow{DA}$ 

$$= \overrightarrow{AD} - (-\overrightarrow{AD})$$

 $= \vec{0}$ 

$$\therefore \overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{CD} + \overrightarrow{DE} + \overrightarrow{EA} = \vec{0}$$

It is given that ABCDE is a pentagon, So

$$\overrightarrow{AB} + \overrightarrow{AE} + \overrightarrow{BC} + \overrightarrow{DC} + \overrightarrow{ED} + \overrightarrow{AC}$$

$$= (\overrightarrow{AB} + \overrightarrow{BC}) + \overrightarrow{AE} + \overrightarrow{DC} + \overrightarrow{ED} + \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{DC} + (\overrightarrow{AE} + \overrightarrow{ED}) + \overrightarrow{AC}$$
[Using triangle law in  $\triangle ABC$ ,  $\overrightarrow{AB} + \overrightarrow{BC} = \overrightarrow{AC}$ ]
$$= \overrightarrow{AC} + \overrightarrow{DC} + (\overrightarrow{AD}) + \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{DC} + (\overrightarrow{AD}) + \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{DC} + \overrightarrow{DC} + \overrightarrow{AD} + \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{DC} + \overrightarrow{DC} + \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AD} + \overrightarrow{DC} + \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AD} + \overrightarrow{DC} + \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} = \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC}$$

$$= \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC} + \overrightarrow{AC}$$

So.

$$\overrightarrow{AB} + \overrightarrow{AE} + \overrightarrow{BC} + \overrightarrow{DC} + \overrightarrow{ED} + \overrightarrow{AC} = 3\overrightarrow{AC}$$

### Algebra of Vectors Ex 23.2 Q8

Let O be the centre of a regular octagon, we know that the centre of a regular octagon bisects all the diagonals passing through it.

Thus, 
$$\overrightarrow{OA} = -\overrightarrow{OE} \qquad (i)$$

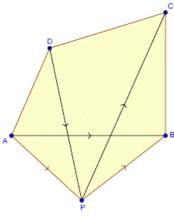
$$\overrightarrow{OB} = -\overrightarrow{OF} \qquad (ii)$$

$$\overrightarrow{OC} = -\overrightarrow{OG} \qquad (iii)$$

$$\overrightarrow{OD} = -\overrightarrow{OH} \qquad (iv)$$
Adding equation (i), (ii), and (iv),
$$\overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC} + \overrightarrow{OD} = -\overrightarrow{OE} - \overrightarrow{OF} - \overrightarrow{OG} - \overrightarrow{OH}$$

$$\overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC} + \overrightarrow{OD} + = -\left(\overrightarrow{OE} + \overrightarrow{OF} + \overrightarrow{OG} + \overrightarrow{OH}\right)$$

 $\overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC} + \overrightarrow{OD} + \overrightarrow{OE} + \overrightarrow{OF} + \overrightarrow{OG} + \overrightarrow{OH} = \vec{0}$ 



$$\overrightarrow{AP} + \overrightarrow{PB} + \overrightarrow{PD} = \overrightarrow{PC}$$
  
 $\overrightarrow{AP} + \overrightarrow{PB} = \overrightarrow{PC} - \overrightarrow{PD}$ 

$$\overrightarrow{AP} + \overrightarrow{PB} = \overrightarrow{PC} + \overrightarrow{DP}$$

$$\overrightarrow{AP} + \overrightarrow{PB} = \overrightarrow{DP} + \overrightarrow{PC}$$

$$\overrightarrow{AB} = \overrightarrow{DC}$$

Since 
$$\overrightarrow{DP} = -\overrightarrow{PD}$$

Using triangle law in 
$$\triangle APB$$
,  $\overrightarrow{AP} + \overrightarrow{PB} = \overrightarrow{AB}$   
Using triangle law in  $\triangle DPC$ ,  $\overrightarrow{DP} + \overrightarrow{PC} = \overrightarrow{DC}$ 

Therefore, AB is parallel to DC and equal is magnitude. Hence, ABCD is a parallelogram.

### Algebra of Vectors Ex 23.2 Q10

We need to show that

$$\overrightarrow{AB} + \overrightarrow{AC} + \overrightarrow{AD} + \overrightarrow{AE} + \overrightarrow{AF} = 6\overrightarrow{AO}$$

We know that centre  ${\cal O}$  of the hexagon bisects the diagonal  $\overrightarrow{\it AD}$ 

$$\overrightarrow{AO} = \frac{1}{2} \overrightarrow{AD}; \overrightarrow{BO} = -\overrightarrow{EO}; \overrightarrow{CO} = -\overrightarrow{FO}$$

### Now

$$\overrightarrow{AB} + \overrightarrow{BO} = \overrightarrow{AO}$$

$$\overrightarrow{AC} + \overrightarrow{CO} = \overrightarrow{AO}$$

$$\overrightarrow{AD} + \overrightarrow{DO} = \overrightarrow{AO}$$

$$\overrightarrow{AE} + \overrightarrow{EO} = \overrightarrow{AO}$$

$$\overrightarrow{AF} + \overrightarrow{FO} = \overrightarrow{AO}$$

Adding these equations we get

$$(\overrightarrow{AB} + \overrightarrow{AC} + \overrightarrow{AD} + \overrightarrow{AE} + \overrightarrow{AF}) + (\overrightarrow{BO} + \overrightarrow{CO} + \overrightarrow{DO} + \overrightarrow{EO} + \overrightarrow{FO})$$

$$\Rightarrow \qquad \left( \overrightarrow{AB} + \overrightarrow{AC} + \overrightarrow{AD} + \overrightarrow{AE} + \overrightarrow{AF} \right) + \overrightarrow{DO} = 5 \ \overrightarrow{AO}$$

But 
$$\overline{DO} = -\overline{AO}$$

$$\overrightarrow{AB} + \overrightarrow{AC} + \overrightarrow{AD} + \overrightarrow{AE} + \overrightarrow{AF} = 6 \overrightarrow{AO}.$$

Million Stars Practice
Anni Arink Learn



## Ex 23.3

### Algebra of Vectors Ex 23.3 Q1

Point R divides the line joining the two points P and Q in the ratio 1:2 internally.

Position vector of point R = 
$$\frac{1(\vec{a} - 2\vec{b}) + 2(2\vec{a} + \vec{b})}{1 + 2} = \frac{5\vec{a}}{3}$$

Point R divides the line joining the two points P and Q in the ratio 1:2 externally.

Position vector of point R = 
$$\frac{1(\vec{a} - 2\vec{b}) - 2(2\vec{a} + \vec{b})}{1 - 2} = \frac{-3\vec{a} - 4\vec{b}}{-1} = 3\vec{a} + 4\vec{b}$$

### Algebra of Vectors Ex 23.3 Q2

Here it is given that  $\vec{a}, \vec{b}, \vec{c}$  and  $\vec{d}$  be the position vectors of the four distinct points A,B,C,D such that

$$\vec{b} - \vec{a} = \vec{c} - \vec{d}$$

Given that,

$$\vec{b} - \vec{a} = \vec{c} - \vec{d}$$

$$\overrightarrow{AB} = \overrightarrow{DC}$$

So, AB is parallel and equal to DC (in magnitude).

Hence,

ABCD is a parallelogram.

### Algebra of Vectors Ex 23.3 Q3

Here, it is given that  $\bar{a}, \bar{b}$  are position vector of A and B.

Let C be a point in AB produced such that AC = 3AB.

It is clear that point C divides the line AB in ratio 3:2 externally. So position vector point C is given by

So position vector point C is given by

$$\overline{C} = \frac{m\overline{b} - n\overline{a}}{m - n}$$

$$=\frac{3\bar{b}-2\bar{b}}{2\bar{b}}$$

$$\vec{C} = 3\vec{b} - 2\vec{a}$$

Again, let D be a point in BA produced such that BD = 2BA.

Let  $\overline{d}$  be the position vector of D. It is clear that point D divides the line AB in 1:2 externally. So position vector of D is given by

$$\overline{d} = \frac{m\overline{a} - n\overline{b}}{m - n}$$

$$=\frac{2\overline{a}-\overline{b}}{2-1}$$

$$\vec{d} = 2\vec{a} - \vec{b}$$

$$\hat{c} = 3\bar{b} - 2\bar{a}$$

Million Stars Practice
Williams Practice

$$3a + 5c = 2\vec{b} + 6\vec{d}$$

Sum of the coefficients on both the sides of the equation (i) is 8, so divide equation (i) by 8 on both the sides,

$$\frac{3\vec{a} + 5\vec{c}}{8} = \frac{2\vec{b} + 6\vec{d}}{8}$$
$$\frac{3\vec{a} + 5\vec{c}}{8} = \frac{2\vec{b} + 6\vec{d}}{8}$$

It shows that position vector of a point p dividing AC in the ratio 3:5, is same as that of a point dividing BD in the ratio of 2:6.

Hence, point P is common to AC and BD. Therefore, P is the point of intersection of AC and BD.

So, A,B,C and D are coplanar.

Position vector of point P is given by

$$\frac{3\vec{a} + 5\vec{c}}{8}$$

or 
$$\frac{2\vec{b} + 6\vec{d}}{9}$$

### Algebra of Vectors Ex 23.3 Q5

We have given that

$$5\vec{p} - 2\vec{q} + 6\vec{r} - 9\vec{s} = \vec{0}$$

Where  $\vec{p}, \vec{q}, \vec{r}$  and  $\vec{s}$  are the position vectors of point P, Q, R and S.

$$5\vec{p} + 6\vec{r} = 2\vec{q} + 9\vec{s}$$
 (i)

Sum of the coefficients on both the sides of the equation (i) is 11. So divide equation (i) by 11 on both the sides.

$$\frac{5\vec{p} + 6\vec{r}}{11} = \frac{2\vec{q} + 9\vec{s}}{11}$$

$$\frac{5\vec{p} + 6\vec{r}}{5 + 6} = \frac{2\vec{q} + 9\vec{s}}{2 + 9}$$

It shows that position vector of a point A dividing PR in the ratio of 6:5 and QS in the ratio of 9:2. Thus, A is the common point to PR and QS and it is also point of intersection of PQ and QS.

So,

P,Q,R and S are coplanar

Position vector of point A is given by

$$\frac{5p + 6q}{11}$$

or 
$$\frac{2\vec{q} + 9\vec{s}}{11}$$

### Algebra of Vectors Ex 23.3 Q6

Let ABC be a triangle.

Let the position vectors of A, B and C with respect to some origin, O be  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  respectively.

Let D be the point on BC where the bisector of  $\angle A$  meets.

Let d position vector of D which divides BC internally in the rai

where 
$$\beta = |\overrightarrow{AC}|$$
 and  $\gamma = |\overrightarrow{AB}|$   
Thus,  $\beta = |\overrightarrow{C} - \overrightarrow{C}|$  and  $\gamma = |\overrightarrow{D} - \overrightarrow{C}|$ 

Thus, by section formula, the position vector of D is given

$$\overrightarrow{OD} = \frac{\overrightarrow{\beta} \overrightarrow{b} + \overrightarrow{\gamma} \overrightarrow{c}}{\overrightarrow{\beta} + \overrightarrow{\gamma}}$$

Let 
$$\alpha = |\vec{b} - \vec{c}|$$

Incentre is the concurrent point of angle bisectors.

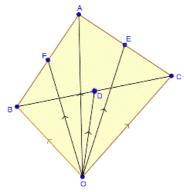
Thus, Incentre divides the line AD in the ratio  $\alpha:\beta+\gamma$ 

Thus, the position vector of incentre

equal to 
$$\frac{\alpha \vec{d} + \frac{\beta \vec{b} + \gamma \vec{c}}{(\beta + \gamma)} \times (\beta + \gamma)}{\alpha + \beta + \gamma} = \frac{\alpha \vec{d} + \beta \vec{b} + \gamma \vec{c}}{\alpha + \beta + \gamma}$$

## Ex 23.4

### Algebra of Vectors Ex 23.4 Q1



Here, in  $\triangle ABC$ , D, E, F are the mid points of the sides of BC, CA and ABrespectively. And O is any point in space.

Let  $\vec{a}, \vec{b}, \vec{c}, \vec{d}, \vec{e}, \vec{f}$  be the position vector of point A, B, C, D, E, F with respect to O.

So, 
$$\overrightarrow{OA} = \overrightarrow{a}$$
,  $\overrightarrow{OB} = \overrightarrow{b}$ ,  $\overrightarrow{OC} = \overrightarrow{c}$   
 $\overrightarrow{OD} = \overrightarrow{d}$ ,  $\overrightarrow{OE} = \overrightarrow{e}$ ,  $\overrightarrow{OF} = \overrightarrow{f}$ 

$$\vec{d} = \frac{\vec{b} + \vec{c}}{2}$$

$$\vec{e} = \frac{\vec{a} + \vec{c}}{2}$$

$$\vec{f} = \frac{\vec{a} + \vec{b}}{2}$$

$$\overrightarrow{OD} = \overrightarrow{d}, \overrightarrow{OE} = \overrightarrow{e}, \overrightarrow{OF} = \overrightarrow{f}$$

$$\overrightarrow{d} = \frac{\overrightarrow{b} + \overrightarrow{c}}{2}$$

$$\overrightarrow{e} = \frac{\overrightarrow{a} + \overrightarrow{c}}{2}$$
[Using mid point formula]
$$\overrightarrow{f} = \frac{\overrightarrow{a} + \overrightarrow{b}}{2}$$

$$\overrightarrow{OD} + \overrightarrow{OE} + \overrightarrow{OF} = \overrightarrow{d} + \overrightarrow{e} + \overrightarrow{f}$$

$$= \frac{\overrightarrow{b} + \overrightarrow{c}}{2} + \frac{\overrightarrow{a} + \overrightarrow{c}}{2} + \frac{\overrightarrow{a} + \overrightarrow{b}}{2}$$

$$= \frac{\overrightarrow{b} + \overrightarrow{c} + \overrightarrow{a} + \overrightarrow{c} + \overrightarrow{a} + \overrightarrow{b}}{2}$$

$$= \frac{2(\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c})}{2}$$

$$= \overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c}$$

$$= \overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC}$$

So, 
$$\overrightarrow{OD} + \overrightarrow{OE} + \overrightarrow{OF} = \overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC}$$

Million Stars Practice
Anima, Learn & Practice

**Remove Watermark** 

### Algebra of Vectors Ex 23.4 Q2

Here, we have to show that the sum of the three vectors ditermined by medians of a triangle directed from the vertices is zero.

Let ABC is triangle such that position vector of A,B and C are  $\vec{a}, \vec{b}$  and  $\vec{c}$  respectively.

As AD, BE, CF are medians, D, E and F are mid points.

Position vector of 
$$D = \frac{\vec{b} + \vec{c}}{2}$$

[Using mid point formula]

Position vector of 
$$E = \frac{\vec{c} + \vec{a}}{2}$$

[Using mid point formula]

Position vector of 
$$F = \frac{\vec{a} + \vec{b}}{2}$$

[Using mid point formula]

Now,  

$$\overrightarrow{AD} + \overrightarrow{BE} + \overrightarrow{CF}$$

$$= \left(\frac{\vec{b} + \vec{c}}{2} - \vec{a}\right) + \left(\frac{\vec{c} + \vec{a}}{2} - \vec{b}\right) + \left(\frac{\vec{a} + \vec{b}}{2} - \vec{c}\right)$$

$$= \frac{\vec{b} + \vec{c} - 2\vec{a}}{2} + \frac{\vec{c} + \vec{a} - 2\vec{b}}{2} + \frac{\vec{a} + \vec{b} - 2\vec{c}}{2}$$

$$= \frac{\vec{b} + \vec{c} - 2\vec{a} + \vec{c} + \vec{a} - 2\vec{b} + \vec{a} + \vec{b} - 2\vec{c}}{2}$$

$$= \frac{2\vec{b} + 2\vec{c} + 2\vec{a} - 2\vec{b} - 2\vec{a} - 2\vec{c}}{2}$$

$$= \frac{\vec{0}}{2}$$

$$= \vec{0}$$

$$\therefore \overrightarrow{AD} + \overrightarrow{BE} + \overrightarrow{CF} = \vec{0}$$

### Algebra of Vectors Ex 23.4 Q3

Here, it is given that ABCD is a parallelogram, P is the point of intersection of diagonals and O be the point of reference.

Using triangle law in AAOP,

$$\overrightarrow{OP} + \overrightarrow{PA} = \overrightarrow{OA}$$
 (i)

Using triangle law in AOBP,

$$\overrightarrow{OP} + \overrightarrow{PB} = \overrightarrow{OB}$$
 (ii)

Using triangle law in ΔΟΡC,

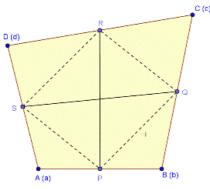
$$\overrightarrow{OP} + \overrightarrow{PC} = \overrightarrow{OC}$$
 (iii)

Using triangle law in  $\triangle OPD$ ,

$$\overrightarrow{OP} + \overrightarrow{PD} = \overrightarrow{OD}$$
 (iv)

Adding equation (i), (ii), (iii), and (iv), 
$$\overrightarrow{OP} + \overrightarrow{PA} + \overrightarrow{OP} + \overrightarrow{PB} + \overrightarrow{OP} + \overrightarrow{PC} + \overrightarrow{OP} + \overrightarrow{PD} = \overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC} + \overrightarrow{OD} + \overrightarrow{OD} + \overrightarrow{OD} + \overrightarrow{PA} + \overrightarrow{PB} + \overrightarrow{PC} + \overrightarrow{PD} = \overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC} + \overrightarrow{OD} + \overrightarrow{OD} + \overrightarrow{OD} + \overrightarrow{PA} + \overrightarrow{PB} + \overrightarrow{PB} + \overrightarrow{PC} + \overrightarrow{PD} = \overrightarrow{OA} + \overrightarrow{OB} + \overrightarrow{OC} + \overrightarrow{OD} +$$

Since 
$$\overrightarrow{PC} = -\overrightarrow{PA}$$
 and  $\overrightarrow{PD} = -\overrightarrow{PB}$  as  $P$  is mid point of  $AC,BD$ 



Let ABCD be a quadrilateral and P,Q,R,S be the mid points of sides AB,BC, CD and DA respectively.

Let position vector of A, B, C and D be  $\vec{a}, \vec{b}, \vec{c}$ , and  $\vec{d}$ .

So position vector of P,Q,R and S are  $\left(\frac{\vec{a}+\vec{b}}{2}\right), \left(\frac{\vec{b}+\vec{c}}{2}\right), \left(\frac{\vec{c}+\vec{d}}{2}\right)$  and  $\left(\frac{\vec{d}+\vec{a}}{2}\right)$  respectively.

Position vector of  $\overrightarrow{PQ}$ 

= Position vector of Q – Position vector of P

$$= \left(\frac{\vec{b} + \vec{c}}{2}\right) - \left(\frac{\vec{a} + \vec{b}}{2}\right)$$

$$= \frac{\vec{b} + \vec{c} - \vec{a} - \vec{b}}{2}$$

$$= \frac{\vec{c} - \vec{a}}{2} \qquad (i)$$

Position vector of  $\overrightarrow{SR}$ 

= Position vector of R - Position vector of S

(ii)

$$= \left(\frac{\vec{c} + \vec{d}}{2}\right) - \left(\frac{\vec{a} + \vec{d}}{2}\right)$$
$$= \frac{\vec{c} + \vec{d} - \vec{a} - \vec{d}}{2}$$
$$= \frac{\vec{c} - \vec{a}}{2}$$

2

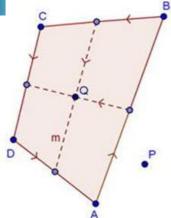
Using (i) and (ii) ,  $\overrightarrow{PQ} = \overrightarrow{SR}$ 

So, PQRS is a parallelogram.

Therefore, PR bisects QS

[as diagonals of parallelogram]

Line segment joining the mid point of opposite sides of a quadrilateral bisects each other.



Let  $\bar{a}, \bar{b}, \bar{c}, \bar{d}$  be the position vectors of the points A, B, C, and D respectively.

Then, position vector of

mid point of 
$$AB = \frac{\ddot{a} + \ddot{b}}{2}$$
  
mid point of  $BC = \frac{\ddot{b} + \ddot{c}}{2}$   
mid point of  $CD = \frac{\ddot{c} + \ddot{d}}{2}$   
mid point of  $DA = \frac{\ddot{a} + \ddot{d}}{2}$ 

Q is the mid point of the line joining the mid points of AB and CD

$$pr. \text{ or } Q = \frac{\frac{\vec{a} + \vec{a}}{2} + \frac{\vec{c} + \vec{d}}{2}}{2}$$
$$= \frac{\vec{a} + \vec{b} + \vec{c} + \vec{d}}{4}$$

Let  $\bar{p}$  be the position vector of P.

Then,

$$\overrightarrow{PA} + \overrightarrow{PB} + \overrightarrow{PC} + \overrightarrow{PD}$$

$$= \overrightarrow{a} - \overrightarrow{p} + \overrightarrow{b} - \overrightarrow{p} + \overrightarrow{c} - \overrightarrow{p} + \overrightarrow{d} - \overrightarrow{p}$$

$$= \left(\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c} + \overrightarrow{d}\right) - 4\overrightarrow{p}$$

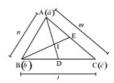
$$= 4\left(\frac{\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c} + \overrightarrow{d}}{4} - \overrightarrow{p}\right)$$

$$= 4\overrightarrow{PO}$$

## Algebra of Vectors Ex 23.4 Q6

Let  $A(\vec{a}), B(\vec{b})$  and  $C(\vec{c})$  be the position vectors of the vertices of the triangle  $\triangle ABC$  and the length of the sides BC, CA and AB be l, m and n respectively.

**Remove Watermark** 



The internal bisector of a triangle divides the opposite side in the ratio of the sides containing the angles.

Since AD is the internal bisector of the  $\angle ABC$ ,

$$\frac{BD}{DC} = \frac{AB}{AC} = \frac{n}{m}$$
 (1)
for e position vector of  $D = \frac{\vec{n}C + \vec{n}C}{\vec{n}C}$ 

Therefore position vector of  $D = \frac{\vec{nc} + m\vec{b}}{\vec{b}}$ 

Let the internal bisector intersect at I

Let the internal bisector intersect at 
$$I$$
.

$$\frac{ID}{AI} = \frac{BD}{AB} \qquad (2)$$

$$\frac{BD}{DC} = \frac{n}{m}$$
Therefore,
$$\frac{CD}{BD} = \frac{m}{n}$$

$$\frac{CD + BD}{BD} = \frac{m + n}{n}$$

$$\frac{BC}{BD} = \frac{m + n}{n}$$

$$BD = \frac{\ln m + n}{n}$$
From (2) and (3), we get  $ID$   $ID$   $ID$   $ID$ 

$$\frac{ID}{AI} = \frac{\ln m}{m+1}$$

Therefore,

(m+n)+lala + mb + ncPosition vector of I =l+m+n

Similarly, we can prove that I lie on the internal bisectors of angles B and C. Hence the three bisectors are concurrent.

Here 
$$\vec{\sigma} = -4\hat{i} - 3\hat{j}$$

$$|\vec{\sigma}| = \sqrt{(-4)^2 + (-3)^2}$$

$$= \sqrt{16 + 9}$$

$$= \sqrt{25}$$

$$= 5$$

### Algebra of Vectors Ex 23.5 Q2

Here 
$$\vec{a} = 12\hat{i} + n\hat{j}$$
  
 $|\vec{a}| = \sqrt{(12)^2 + (n)^2}$   
 $13 = \sqrt{144 + n^2}$ 

Since 
$$|\vec{a}| = 13$$

Squaring both sides,

$$(13)^2 = (\sqrt{144 + n^2})^2$$

$$169 = 144 + n^2$$

$$n^2 = 169 - 144$$

$$n^2 = 25$$

$$n = \pm \sqrt{25}$$

$$n = \pm 5$$

Here, 
$$\vec{a} = \sqrt{3}\hat{i} + \hat{j}$$

$$n^{2} = 169 - 144$$

$$n^{2} = 25$$

$$n = \pm\sqrt{25}$$

$$n = \pm 5$$
Algebra of Vectors Ex 23.5 Q3

Here,  $\vec{a} = \sqrt{3}\hat{i} + \hat{j}$ 

Let  $\vec{b}$  is any vector parallel to  $\vec{a}$ 

So,  $\vec{b} = \lambda \vec{a}$  (where  $\lambda$  is any scalar)
$$= \lambda \left(\sqrt{3}\hat{i} + \hat{j}\right)$$

$$\vec{b} = \lambda \sqrt{3}\hat{i} + \lambda \hat{j}$$

$$|\vec{b}| = \sqrt{(\lambda\sqrt{3})^{2} + (\lambda)^{2}}$$

$$= \sqrt{3\lambda^{2} + \lambda^{2}}$$

$$= \sqrt{4\lambda^{2}}$$

$$|\vec{b}| = 2\lambda$$

$$4 = 2\lambda$$

$$\lambda = \frac{4}{2}$$

$$\lambda = 2$$

(i) Here, 
$$A = (4, -1)$$

Position vector of  $A = 4\hat{i} - \hat{j}$ Position vector of  $B = \hat{i} + 3\hat{j}$ 

$$\overrightarrow{AB}$$
 = Position vector of  $B$  - Position vector of  $A$   
=  $(\hat{i} + 3\hat{j}) - (4\hat{i} - \hat{j})$   
=  $\hat{i} + 3\hat{j} - 4\hat{i} + \hat{j}$   
 $\overrightarrow{AB}$  =  $-3\hat{i} + 4\hat{j}$ 

$$\left| \overrightarrow{AB} \right| = \sqrt{(-3)^2 + (4)^2}$$
$$= \sqrt{9 + 16}$$
$$= \sqrt{25}$$

$$|\overrightarrow{AB}| = 5$$

$$\overrightarrow{AB} = -3\hat{i} + 4\hat{j}$$

(ii) Here, 
$$A = (-6, 3)$$
  
 $B = (-2, -5)$ 

Position vector of  $A = -6\hat{i} + 3\hat{j}$ Position vector of  $B = -2\hat{i} - 5\hat{j}$ 

$$\overrightarrow{AB}$$
 = Position vector of  $B$  - Position vector of  $A$   
=  $\left(-2\hat{i} - 5\hat{j}\right) - \left(-6\hat{i} + 3\hat{j}\right)$   
=  $-2\hat{i} - 5\hat{j} + 6\hat{i} - 3\hat{j}$   
 $\overrightarrow{AB} = 4\hat{i} - 8\hat{j}$ 

$$|\overrightarrow{AB}| = \sqrt{(4)^2 + (-8)^2}$$

$$= \sqrt{16 + 64}$$

$$= \sqrt{80}$$

$$= \sqrt{16 \times 5}$$

$$= 4\sqrt{5}$$

$$|\overrightarrow{AB}| = 4\sqrt{5}$$

$$\overrightarrow{AB} = 4\hat{i} - 8\hat{j}$$

### Algebra of Vectors Ex 23.5 Q5

Here, 
$$A = (-1,3)$$
  
 $B = (-2,1)$ 

Position vector of  $A = -\hat{i} + 3\hat{j}$ Position vector of  $B = -2\hat{i} + 1\hat{j}$ 

$$\overrightarrow{AB}$$
 = Position vector of  $B$  - Position vector of  $A$   
=  $\left(-2\hat{i}+\hat{j}\right)-\left(-\hat{i}+3\hat{j}\right)$   
=  $-2\hat{i}+\hat{j}+\hat{i}-3\hat{j}$   
=  $-\hat{i}-2\hat{i}$ 

So,

Coordinate of the position vector equivalent to  $\overrightarrow{AB} = (-1, -2)$ 

# Million Stars Practice Williams Practice

Here, 
$$A = (-2, -1)$$
  
 $B = (3, 0)$ 

$$C = (1, -2)$$

Let 
$$D = (x, y)$$

$$\overrightarrow{AB}$$
 = Position vector of  $B$  – Position vector of  $A$ 

$$= (3\hat{i} - 0 \times \hat{j}) - (-2\hat{i} - \hat{j})$$
$$= 3\hat{i} - 0 \times \hat{j} + 2\hat{i} + \hat{j}$$

$$\overrightarrow{AB} = 5\hat{i} + \hat{j}$$

 $\overrightarrow{DC}$  = Position vector of C – Position vector of D

$$= (\hat{i} - 2\hat{j}) - (x\hat{i} + y\hat{j})$$

$$=\hat{i}-2\hat{j}-x\hat{i}-y\hat{j}$$

$$\overrightarrow{DC} = (1-x)\hat{i} + (-2-y)\hat{j}$$

Since ABCD is a parallelogram, which have equal and parallel opposite sides.

So, 
$$\overrightarrow{AB} = \overrightarrow{DC}$$
  
 $5\hat{i} + \hat{j} = (1 - x)\hat{i} + (-2 - y)\hat{j}$ 

Comparing components of LHS and RHS

$$5 = 1 - x$$

$$x = 1 - 5$$

$$x = -4$$

$$1 = -2 - y$$

$$y = -2 - 1$$

$$y = -1$$

So, coordinate of D is (-4, -3)

### Algebra of Vectors Ex 23.5 Q7

Here, 
$$A(3,4), B(5,-6), C(4,-1)$$

$$\vec{a} = 3\hat{i} + 4\hat{j}$$

$$\vec{b} = 5\hat{i} - 6\hat{i}$$

$$\vec{c} = 4\hat{i} - \hat{j}$$

Now,

$$\vec{a} + 2\vec{b} - 3\vec{c} = (3\hat{i} + 4\hat{j}) + 2(5\hat{i} - 6\hat{j}) - 3(4\hat{i} - \hat{j})$$
$$= 3\hat{i} + 4\hat{j} + 10\hat{i} - 12\hat{j} - 12\hat{i} + 3\hat{j}$$
$$= \hat{i} - 5\hat{j}$$

$$\vec{a} + 2\vec{b} - 3\vec{c} = \hat{i} - 5\hat{i}$$

### Algebra of Vectors Ex 23.5 Q9

$$|\overrightarrow{AB}| = 5 \text{ units}$$

$$\left| \overrightarrow{BC} \right| = \sqrt{(8)^2}$$

$$\left| \overrightarrow{BC} \right| = 8 \text{ units}$$

$$\left| \overline{AC} \right| = \sqrt{\left(-3\right)^2 + \left(8\right)^2}$$
$$= \sqrt{9 + 16}$$

= 
$$\sqrt{25}$$

$$|\overline{AC}| = 5 \text{ units}$$

Here, 
$$\left| \overrightarrow{AB} \right| = \left| \overrightarrow{AC} \right|$$

So, there are two sides AB, and BC of  $\triangle ABC$  have same length.

∆ABC is an isosceles triangle.

Million Stars Practice

Williams Practice

Let  $\vec{a} = \hat{i} + \sqrt{3}\hat{j}$ 

Suppose  $\vec{b}$  is any vector parallel to  $\vec{a}$ 

$$\vec{b} = \lambda \vec{a} \quad \text{where } \lambda \text{ is a scalar}$$

$$= \lambda \left( \hat{i} + \sqrt{3} \hat{j} \right)$$

$$\vec{b} = \lambda \hat{i} + \sqrt{3} \lambda \hat{j}$$

$$|\vec{b}| = \sqrt{(\lambda)^2 + (\sqrt{3}\lambda)^2}$$

$$= \sqrt{\lambda^2 + 3\lambda^2}$$

$$= \sqrt{4\lambda^2}$$

$$= 2\lambda$$

Unit vector of 
$$\vec{b} = \frac{\vec{b}}{|\vec{b}|}$$

$$\hat{b} = \frac{\lambda \hat{i} + \sqrt{3}\lambda \hat{j}}{2\lambda}$$

$$\hat{b} = \frac{\sqrt{\hat{i} + \sqrt{3}} \hat{j}}{2}$$

$$\hat{b} = \frac{1}{2} (\hat{i} + \sqrt{3} \hat{j})$$

### Algebra of Vectors Ex 23.5 Q11

(i) Here, P = (3, 2)

Position vector of  $P = 3\hat{i} + 2\hat{j}$ 

Component of P along x-axis =  $3\hat{i}$ Component of P along y-axis =  $2\hat{j}$ 

(ii) Here, 
$$Q = (-5,1)$$
  
Position vector of  $Q = -5\hat{i} + \hat{j}$ 

Component of Q along x-axis =  $-5\hat{i}$ Component of Q along y-axis =  $\hat{j}$ 

(ii) Here, 
$$R = (-11, -9)$$
  
Position vector of  $R = -11\hat{i} - 9\hat{j}$ 

Component of R along x-axis =  $-11\hat{i}$ Component of R along y-axis =  $-9\hat{j}$ 

(iv) Here, 
$$S = (4, -3)$$
  
Position vector of  $S = 4\hat{i} - 3\hat{j}$ 

Component of S along x-axis =  $4\hat{i}$ Component of S along y-axis =  $-3\hat{j}$ 

Magnitude of a vector  $x\hat{i} + y\hat{j} + z\hat{k}$  is given by  $\sqrt{(x)^2 + y^2 + z^2}$ .

So,  $|\vec{a}| = \sqrt{(2)^2 + (3)^2 + (-6)^2}$  $=\sqrt{4+9+36}$  $=\sqrt{49}$ = 7

### Algebra of Vectors Ex 23.6 Q2

Unit vector of  $\vec{a} = \frac{\vec{a}}{|\vec{a}|}$ 

Unit vector of  $3\hat{i} + 4\hat{j} - 12\hat{k} = \frac{3\hat{i} + 4\hat{j} - 12\hat{k}}{\sqrt{(3)^2 + (4)^2 + (-12)^2}}$  $= \frac{3\hat{i} + 4\hat{j} - 12\hat{k}}{\sqrt{9 + 16 + 144}}$  $= \frac{3\hat{i} + 4\hat{j} - 12\hat{k}}{\sqrt{169}}$ Mondershare

Unit vector of 
$$(3\hat{i} + 4\hat{j} - 12\hat{k}) = \frac{1}{13}(3\hat{i} + 4\hat{j} - 12\hat{k})$$

### Algebra of Vectors Ex 23.6 Q3

Let 
$$\vec{a} = \hat{i} - \hat{j} + 3\hat{k}$$
  
 $\vec{b} = 2\hat{i} + \hat{j} - 2\hat{k}$   
 $\vec{b} = \hat{i} + 2\hat{i} - 2\hat{k}$ 

Let d be the resultant of  $\vec{a}$ ,  $\vec{b}$ , and  $\vec{c}$ ,

$$\vec{d} = \vec{a} + \vec{b} + \vec{c}$$

$$= (\hat{i} - \hat{j} + 3\hat{k}) + (2\hat{i} + \hat{j} - 2\hat{k}) + (\hat{i} + 2\hat{j} - 2\hat{k})$$

$$\vec{d} = 4\hat{i} + 2\hat{j} - \hat{k}$$

Unit vector 
$$\vec{d} = \frac{\vec{d}}{|\vec{d}|}$$

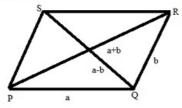
$$= \frac{4\hat{i} + 2\hat{j} - \hat{k}}{\sqrt{(4)^2 + (2)^2 + (-1)^2}}$$

$$\vec{d} = \frac{4\hat{i} + 2\hat{j} - \hat{k}}{\sqrt{16 + 4 + 1}}$$

**Remove Watermark** 

### Algebra of Vectors Ex 23.6 Q4

Let PQRS be a parallelogram such that  $PQ = \vec{a} = \hat{i} + \hat{j} - \hat{k}$  and  $QR = \vec{b} = -2\hat{i} + \hat{j} + 2\hat{k}$ 



$$\overrightarrow{PQ} + \overrightarrow{QR} = \overrightarrow{PR}$$

$$\overrightarrow{PR} = \vec{\alpha} + \vec{b} = \hat{i} + \hat{j} - \hat{k} + \left(-2\hat{i} + \hat{j} + 2\hat{k}\right)$$

$$\overrightarrow{PR} = -\hat{i} + 2\hat{j} + \hat{k}$$

In △PSQ

$$\overrightarrow{PS} + \overrightarrow{SQ} = \overrightarrow{PQ}$$

$$\overrightarrow{SQ} = \overrightarrow{a} - \overrightarrow{b} = \widehat{i} + \widehat{j} - \widehat{k} - \left(-2\widehat{i} + \widehat{j} + 2\widehat{k}\right)$$

$$\overrightarrow{SQ} = 3\hat{i} + 0\hat{j} - 3\hat{k}$$

The unit vector along 
$$\overrightarrow{PR} = \frac{\overrightarrow{PR}}{|\overrightarrow{PR}|} = \frac{-\hat{i} + 2\hat{j} + \hat{k}}{\sqrt{1 + 4 + 1}} = \frac{1}{\sqrt{6}} \left( -\hat{i} + 2\hat{j} + \hat{k} \right)$$
The unit vector along  $\overrightarrow{SQ} = \frac{\overrightarrow{SQ}}{|\overrightarrow{SQ}|} = \frac{3\hat{i} + 0\hat{j} - 3\hat{k}}{\sqrt{9 + 0 + 9}} = \frac{1}{\sqrt{2}} \left( \hat{i} - \hat{k} \right)$ 

The unit vector along 
$$\overrightarrow{SQ} = \frac{\overrightarrow{SQ}}{|\overrightarrow{SQ}|} = \frac{3\hat{i} + 0\hat{j} - 3\hat{k}}{\sqrt{9 + 0 + 9}} = \frac{1}{\sqrt{2}} (\hat{i} - \hat{k})$$

### Algebra of Vectors Ex 23.6 Q5

Algebra of Vectors Ex 23.6 Q5
$$3\vec{a} - 2\vec{b} + 4\vec{c} = 3\left(3\hat{i} - \hat{j} - 4\hat{k}\right) - 2\left(-2\hat{i} + 4\hat{j} - 3\hat{k}\right) + 4\left(\hat{i} + 2\hat{j} - \hat{k}\right)$$

$$= 9\hat{i} - 3\hat{j} - 12\hat{k} + 4\hat{i} - 8\hat{j} + 6\hat{k} + 4\hat{i} + 8\hat{j} - 4\hat{k}$$

$$= 17\hat{i} - 3\hat{j} - 10\hat{k}$$

$$\begin{vmatrix}3\vec{a} - 2\vec{b} + 4\vec{c}\end{vmatrix} = \sqrt{(17)^2 + (-3)^2 + (10)^2}$$

$$= \sqrt{289 + 9 + 100}$$

$$= \sqrt{398}$$

$$\begin{vmatrix} 3\vec{a} - 2\vec{b} + 4\vec{c} \end{vmatrix} = \sqrt{(17)^2 + (-3)^2 + (10)^2}$$
$$= \sqrt{289 + 9 + 100}$$
$$= \sqrt{398}$$

$$|3\vec{a} - 2\vec{b} + 4\vec{c}| = \sqrt{398}$$

### Algebra of Vectors Ex 23.6 Q6

Here, 
$$\overrightarrow{PQ} = 3\hat{i} + 2\hat{j} - \hat{k}$$

Position vector of  $P = \hat{i} - \hat{j} + 2\hat{k}$ 

$$\overrightarrow{PQ} = \text{Position vector of } Q - \text{Position vector of } P$$
 
$$3\hat{i} + 2\hat{j} - \hat{k} = \text{Position vector of } Q - \left(\hat{i} - \hat{j} + 2\hat{k}\right)$$

Position vector of Q = 
$$(3\hat{i} + 2\hat{j} - \hat{k}) + (\hat{i} - \hat{j} + 2\hat{k})$$
  
=  $4\hat{i} + \hat{j} + \hat{k}$ 

Coordinates of Q = (4, 1, 1)

# Million Stars Practice Anima Arina Practice

**Remove Watermark** 

### Igebra of Vectors Ex 23.6 Q7

et 
$$\vec{A} = \hat{i} - \hat{j}$$
  
 $\vec{B} = 4\hat{i} + 3\hat{j} + \hat{k}$   
 $\vec{C} = 2\hat{i} - 4\hat{i} + 5\hat{k}$ 

$$\overline{AB} = \overline{B} - \overline{A}$$

$$= (4\hat{i} + 3\hat{j} + R) - (\hat{i} - \hat{j})$$

$$= 4\hat{i} + 3\hat{j} + R - \hat{i} + \hat{j}$$

$$= 3\hat{i} + 4\hat{i} + R$$

$$|\overline{AB}| = \sqrt{(3)^2 + (4)^2 + (1)^2} = \sqrt{9 + 16 + 1} = \sqrt{26}$$

$$\overline{BC} = \overline{C} - \overline{B} 
= (2\hat{i} - 4\hat{j} + 5R) - (4\hat{i} + 3\hat{j} + R) 
= 2\hat{i} - 4\hat{j} + 5R - 4\hat{i} - 3\hat{j} - R 
= -2\hat{i} - 7\hat{j} + 4R$$

$$\left| \overline{BC} \right| = \sqrt{(2)^2 + (-7)^2 + (4)^2} = \sqrt{4 + 49 + 16} = \sqrt{69}$$

$$\overline{CA} = \overline{A} - \overline{C} 
= \hat{i} - \hat{j} - (2\hat{i} - 4\hat{j} + 5\hat{k}) 
= \hat{i} - \hat{j} - 2\hat{i} + 4\hat{j} - 5\hat{k} 
= -\hat{i} + 3\hat{j} - 5\hat{k}$$

$$|\overline{CA}| = \sqrt{(-1)^2 + (3)^2 + (-5)^2} = \sqrt{1 + 9 + 25} = \sqrt{35}$$

Here, 
$$|AB|^2 + |\overline{CA}|^2 = |\overline{BC}|^2$$
  
 $26 + 35 = 69$   
 $61 \neq 69$   
LHS  $\neq RHS$ 

Since sum of square of two sides is not equal to the square of third sides. So,  $\triangle ABC$  is not a right triangle

### Algebra of Vectors Ex 23.6 Q8

Here,

Let vertex 
$$\vec{A} = a_1 \hat{i} + a_2 \hat{j} + a_3 \hat{k}$$
  
vertex  $\vec{B} = b_1 \hat{i} + b_2 \hat{j} + b_3 \hat{k}$   
vertex  $\vec{C} = c_1 \hat{i} + c_2 \hat{j} + c_3 \hat{k}$ 

Side 
$$\overrightarrow{AB} = \overrightarrow{B} - \overrightarrow{A}$$
  

$$= (b_1 \hat{i} + b_2 \hat{j} + b_3 \hat{k}) - (a_1 \hat{i} + a_2 \hat{j} + a_3 \hat{k})$$

$$\overrightarrow{AB} = (b_1 - a_1) \hat{i} + (b_2 - a_2) \hat{j} + (b_3 - a_3) \hat{k}$$

$$\begin{split} \overrightarrow{BC} &= \overrightarrow{C} - \overrightarrow{B} \\ &= \left( c_1 \hat{i} + c_2 \hat{j} + c_3 \hat{k} \right) - \left( b_1 \hat{i} + b_2 \hat{j} + b_3 \hat{k} \right) \\ &= c_1 \hat{i} + c_2 \hat{j} + c_3 \hat{k} - b_1 \hat{i} - b_2 \hat{j} - b_3 \hat{k} \\ \overrightarrow{BC} &= \left( c_1 - b_1 \right) \hat{i} + \left( c_2 - b_2 \right) \hat{j} + \left( c_3 - b_3 \right) \hat{k} \end{split}$$

$$\begin{split} \overrightarrow{AC} &= \left(c_1 \hat{i} + c_2 \hat{j} + c_3 \hat{k}\right) - \left(a_1 \hat{i} + a_2 \hat{j} + a_3 \hat{k}\right) \\ &= c_1 \hat{i} + c_2 \hat{j} + c_3 \hat{k} - a_1 \hat{i} - a_2 \hat{j} - a_3 \hat{k} \\ \overrightarrow{AC} &= \left(c_1 - a_1\right) \hat{i} + \left(c_2 - a_2\right) \hat{j} + \left(c_3 - a_3\right) \hat{k} \end{split}$$

$$|\overrightarrow{AB}| = \sqrt{(b_1 - a_1)^2 + (b_2 - a_2)^2 + (b_3 - a_3)^2}$$

$$|\overrightarrow{BC}| = \sqrt{(c_1 - b_1)^2 + (c_2 - b_2)^2 + (c_3 - b_3)^2}$$

$$|\overrightarrow{AC}| = \sqrt{(c_1 - a_1)^2 + (c_2 - a_2)^2 + (c_3 - a_3)^2}$$

Willion Stars & Practice

$$\vec{A} = \hat{i} - \hat{j} + 2\hat{k}$$
vertex  $B = (2,1,3)$ 

$$\vec{B} = 2\hat{i} + \hat{j} + 3\hat{k}$$

vertex 
$$C = (-1, 2, -1)$$

$$\vec{C} = -\hat{i} + 2\hat{j} - \hat{k}$$

Centroid 
$$\vec{O} = \frac{\vec{A} + \vec{B} + \vec{C}}{3}$$

$$= \frac{(\hat{i} - \hat{j} + 2\hat{k}) + (2\hat{i} + \hat{j} + 3\hat{k}) + (-\hat{i} + 2\hat{j} - \hat{k})}{3}$$

$$= \frac{2\hat{i} + 2\hat{j} + 4\hat{k}}{3}$$

Centroid 
$$\vec{O} = \frac{2\hat{i}}{3} + \frac{2\hat{j}}{3} + \frac{4\hat{k}}{3}$$

### Algebra of Vectors Ex 23.6 Q10

The position vector of point R dividing the line segment joining two points

P and Q in the ratio m: n is given by:

i. Internally:

$$\frac{m\vec{b} + n\vec{a}}{m+n}$$

ii. Externally:

$$\frac{m\vec{b} - n\vec{a}}{m - n}$$

Position vectors of P and Q are given as:

$$\overrightarrow{OP} = \hat{i} + 2\hat{j} - \hat{k}$$
 and  $\overrightarrow{OQ} = -\hat{i} + \hat{j} + \hat{k}$ 

(i) The position vector of point R which divides the line joining two points P and Q internally in the ratio 2:1 is given by,

$$\begin{aligned} \overrightarrow{OR} &= \frac{2\left(-\hat{i} + \hat{j} + \hat{k}\right) + 1\left(\hat{i} + 2\hat{j} - \hat{k}\right)}{2 + 1} = \frac{\left(-2\hat{i} + 2\hat{j} + 2\hat{k}\right) + \left(\hat{i} + 2\hat{j} - \hat{k}\right)}{3} \\ &= \frac{-\hat{i} + 4\hat{j} + \hat{k}}{3} = -\frac{1}{3}\hat{i} + \frac{4}{3}\hat{j} + \frac{1}{3}\hat{k} \end{aligned}$$

### Algebra of Vectors Ex 23.6 Q11

Here, 
$$P\left(2\hat{i}-3\hat{j}+4\hat{k}\right)$$
 and 
$$Q\left(4\hat{i}+\hat{j}-2\hat{k}\right)$$

We know that,

If A and B are two points with position vector  $\vec{a}$  and  $\vec{b}$  then the position vector of mid point C is given by

$$\frac{\vec{a} + \vec{b}}{2}$$

Let R is the mid point of PQ.

Position vector of 
$$R = \frac{\vec{P} + \vec{Q}}{2}$$

$$\vec{R} = \frac{2\hat{i} - 3\hat{j} + 4\hat{k} + 4\hat{i} + \hat{j} - 2\hat{k}}{2}$$

$$= \frac{6\hat{i} - 2\hat{j} + 2\hat{k}}{2}$$

$$= \frac{2\left(3\hat{i} - \hat{j} + \hat{k}\right)}{2}$$

Position vector of mid point =  $3\hat{i} - \hat{j} + \hat{k}$ 

Willion Stars & Practice

e, point 
$$P = (1, 2, 3)$$

$$\vec{P} = \hat{i} + 2\hat{j} + 3\hat{k}$$
Point  $Q = (4, 5, 6)$ 

$$\vec{Q} = 4\hat{i} + 5\hat{j} + 6\hat{k}$$

$$\overrightarrow{PQ} = \text{ Position vector of } Q - \text{ Position vector of } P$$

$$= \left(4\hat{i} + 5\hat{j} + 6\hat{k}\right) - \left(\hat{i} + 2\hat{j} + 3\hat{k}\right)$$

$$= 4\hat{i} + 5\hat{j} + 6\hat{k} - \hat{i} - 2\hat{j} - 3\hat{k}$$

$$= 3\hat{i} + 3\hat{j} + 3\hat{k}$$

$$= 3\left(\hat{i} + \hat{j} + k\right)$$

$$\begin{aligned} \left| \overrightarrow{PQ} \right| &= 3\sqrt{\left(1\right)^2 + \left(1\right)^2 + \left(1\right)^2} \\ &= 3\sqrt{1 + 1 + 1} \\ \left| \overrightarrow{PQ} \right| &= 3\sqrt{3} \end{aligned}$$

Unit vector in the direction of 
$$\overrightarrow{PQ} = \frac{\overrightarrow{PQ}}{\left|\overrightarrow{PQ}\right|}$$
$$= \frac{3\left(\widehat{i} + \widehat{j} + \widehat{k}\right)}{3\sqrt{3}}$$

Unit vector is the direction of  $\overrightarrow{PQ} = \frac{1}{f_2} (\hat{i} + \hat{j} + \hat{k})$ 

The position vectors  $\mathbf{E}\mathbf{x}$  23.6 Q13

The position vectors of AB and C are  $2\hat{i}-\hat{j}+\hat{k},\hat{i}-3\hat{j}-5\hat{k}$  and  $3\hat{i}-4\hat{j}-4\hat{k}$  respectively.

Therefore,  $\overrightarrow{AB} = -\hat{i}-2\hat{j}-6\hat{k}, \overrightarrow{BC} = 2\hat{i}-\hat{j}+\hat{k} \text{ and } \overrightarrow{CA} = -\hat{i}+3\hat{j}+5\hat{k}$ Clearly,  $\overrightarrow{AB}+\overrightarrow{BC}+\overrightarrow{CA}=0$ .

So,  $\overrightarrow{AB}, \overrightarrow{BC}, \overrightarrow{CA}$  form a triangle.

Now  $|\overrightarrow{AB}| = \sqrt{1+4+36} = \sqrt{41}$   $|\overrightarrow{BC}| = \sqrt{4+1+1} = \sqrt{6}$   $|\overrightarrow{CA}| = \sqrt{1+9+25} = \sqrt{35}$ 

$$\overrightarrow{AB} = -\hat{i} - 2\hat{j} - 6\hat{k}, \overrightarrow{BC} = 2\hat{i} - \hat{j} + \hat{k} \text{ and } \overrightarrow{CA} = -\hat{i} + 3\hat{j} + 5\hat{k}$$

Clearly, 
$$\overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{CA} = 0$$

$$\overrightarrow{AB} = \sqrt{1 + 4 + 36} = \sqrt{4}$$

$$|\overrightarrow{BC}| = \sqrt{4+1+1} = \sqrt{6}$$

$$\overrightarrow{CA} = \sqrt{1+9+25} = \sqrt{35}$$

Clearly,

$$\left| \overrightarrow{AB} \right|^2 = \left| \overrightarrow{BC} \right|^2 + \left| \overrightarrow{CA} \right|^2$$

$$AB^2 = BC^2 + CA^2$$

Hence  $\triangle ABC$  is a right triangle right angle at C.

### Algebra of Vectors Ex 23.6 Q14

Find the position vector of the mid point of the vector joining the points P (2, 3, 4) and Q (4, 1, - 2).

Solution 16:

Million Stars Practice

Williams Stars Practice The position vector of mid-point R of the vector joining points P (2, 3, 4) and Q (4, 1,

$$\overrightarrow{OR} = \frac{\left(2\hat{i} + 3\hat{j} + 4\hat{k}\right) + \left(4\hat{i} + \hat{j} - 2\hat{k}\right)}{2} = \frac{\left(2 + 4\right)\hat{i} + \left(3 + 1\right)\hat{j} + \left(4 - 2\right)\hat{k}}{2}$$

$$= \frac{6\hat{i} + 4\hat{j} + 2\hat{k}}{2} = 3\hat{i} + 2\hat{j} + \hat{k}$$

### Algebra of Vectors Ex 23.6 Q15



 $x\Big(\hat{i}+\hat{j}+\hat{k}\Big) \text{is a unit vector if} \bigg|x\Big(\hat{i}+\hat{j}+\hat{k}\Big)\bigg| = 1 \; .$ 

$$\left| x \left( \hat{i} + \hat{j} + \hat{k} \right) \right| = 1$$

$$\Rightarrow \sqrt{x^2 + x^2 + x^2} = 1$$

$$\Rightarrow \sqrt{3x^2} = 1$$

$$\Rightarrow \sqrt{3} x = 1$$

$$\Rightarrow x = \pm \frac{1}{\sqrt{3}}$$

Hence, the required value of x is  $\pm \frac{1}{\sqrt{3}}$ .

### Algebra of Vectors Ex 23.6 Q16

We have,

$$\vec{a} = \hat{i} + \hat{j} + \hat{k}, \ \vec{b} = 2\hat{i} - \hat{j} + 3\hat{k} \text{ and } \vec{c} = \hat{i} - 2\hat{j} + \hat{k}$$

$$2\vec{a} - \vec{b} + 3\vec{c} = 2(\hat{i} + \hat{j} + \hat{k}) - (2\hat{i} - \hat{j} + 3\hat{k}) + 3(\hat{i} - 2\hat{j} + \hat{k})$$

$$= 2\hat{i} + 2\hat{j} + 2\hat{k} - 2\hat{i} + \hat{j} - 3\hat{k} + 3\hat{i} - 6\hat{j} + 3\hat{k}$$

$$= 3\hat{i} - 3\hat{j} + 2\hat{k}$$

$$|2\vec{a} - \vec{b} + 3\vec{c}| = \sqrt{3^2 + (-3)^2 + 2^2} = \sqrt{9 + 9 + 4} = \sqrt{22}$$

$$\begin{aligned} \left| 2\vec{a} - \vec{b} + 3\vec{c} \right| &= \sqrt{3^2 + \left( -3 \right)^2 + 2^2} = \sqrt{9 + 9 + 4} = \sqrt{22} \\ \text{Hence, the unit vector along } 2\vec{a} - \vec{b} + 3\vec{c} \text{ is} \\ \frac{2\vec{a} - \vec{b} + 3\vec{c}}{\left| 2\vec{a} - \vec{b} + 3\vec{c} \right|} &= \frac{3\hat{i} - 3\hat{j} + 2\hat{k}}{\sqrt{22}} = \frac{3}{\sqrt{22}}\hat{i} - \frac{3}{\sqrt{22}}\hat{j} + \frac{2}{\sqrt{22}}\hat{k}. \end{aligned}$$





Here, 
$$\vec{a} = \hat{i} + \hat{j} + \hat{k}$$
  
 $\vec{b} = 4\hat{i} - 2\hat{j} + 3\hat{k}$   
 $\vec{c} = \hat{i} - 2\hat{j} + \hat{k}$ 

$$\begin{aligned} 2\vec{a} - \vec{b} + 3\vec{c} \\ &= 2\left(\hat{i} + \hat{j} + \hat{k}\right) - \left(4\hat{i} - 2\hat{j} + 3\hat{k}\right) + 3\left(\hat{i} - 2\hat{j} + \hat{k}\right) \\ &= 2\hat{i} + 2\hat{j} + 2\hat{k} - 4\hat{i} + 2\hat{j} - 3\hat{k} + 3\hat{i} - 6\hat{j} + 3\hat{k} \\ &= \hat{i} - 2\hat{j} + 2\hat{k} \end{aligned}$$

Let  $\vec{d}$  is a vector parallel to  $2\vec{a} - \vec{b} + 3\vec{c}$ 

So, 
$$\vec{d} = \lambda \left( 2\vec{a} - \vec{b} + 3\vec{c} \right)$$
  
Where  $\lambda$  is any scalar
$$= \lambda \left( \hat{i} - 2\hat{j} + 2\hat{k} \right)$$

$$\vec{d} = \lambda \hat{i} - \lambda 2\hat{j} + \lambda 2\hat{k}$$
(i)

Given that 
$$|\vec{\sigma}| = 6$$

$$\sqrt{(\lambda)^2 + (-2\lambda)^2 + (2\lambda)^2} = 6$$

$$\sqrt{\lambda^2 + 4\lambda^2 + 4\lambda^2} = 6$$

$$\sqrt{9\lambda^2} = 6$$

$$3\lambda = 6$$

$$\lambda = \frac{6}{3}$$

$$\lambda = 2$$

Put the value of  $\lambda$  in equation (i)

$$\vec{d} = 2\hat{i} - 2(2)\hat{j} + 2(2)\hat{k}$$
$$= 2\hat{i} - 4\hat{j} + 4\hat{k}$$

A vector of magnitude 6 which is parallel to  $2\vec{a} - \vec{b} + 3\vec{c}$  is given by  $2\hat{i} - 4\hat{j} + 4\hat{k}$ 

### Algebra of Vectors Ex 23.6 Q18

Given that

$$\vec{a} = 2\hat{i} + 3\hat{j} - \hat{k}$$

ana

$$\vec{b} = \hat{i} - 2\hat{i} + \hat{k}$$

Thus, Find a vector of magnitude of 5 units parallel to the resultant of the vectors

$$\vec{a} + \vec{b} = 2\hat{i} + 3\hat{j} - \hat{k} + \hat{i} - 2\hat{j} + \hat{k}$$
  
$$\Rightarrow \vec{a} + \vec{b} = 3\hat{i} + \hat{j}$$

 $\Rightarrow |\vec{a} + \vec{b}| = \sqrt{9 + 1} = \sqrt{10}$ 

Thus, the unit vector along the resultant vector  $\vec{a} + \vec{b}$  is

$$\frac{3\hat{i} + \hat{j}}{\sqrt{10}}$$

The vector of magnitude of 5 units parallel to the resultant

$$vector = \frac{3\hat{i} + \hat{j}}{\sqrt{10}} \times 5 = \sqrt{\frac{5}{2}} (3\hat{i} + \hat{j})$$

ultant

William Start Practice

William Start Practice



Let D be the point at which median drawn from A touches side B Let ā, Ď and č be the position vectors of the vertices A, B and C.

Position vector of D = 
$$\frac{\vec{b} + \vec{c}}{2}$$
.......[Since D is midpoint of B and C]
$$\vec{A}\vec{D} = \frac{\vec{b} + \vec{c}}{2} - \vec{a} = \frac{\vec{b} + \vec{c} - 2\vec{a}}{2} = \frac{\vec{b} - \vec{a} + \vec{c} - \vec{a}}{2} = \frac{\vec{A}\vec{B} + \vec{A}\vec{C}}{2} = \frac{\vec{j} + \vec{i} + 3\vec{i} - \vec{j} + 4\vec{k}}{2}$$

$$\vec{A}\vec{D} = 2 \vec{i} + 2\vec{k}$$

$$|\overrightarrow{AD}| = \sqrt{4+4} = 4\sqrt{2} \text{ units}$$

Note: Answer given in the book is incorrect.



Million Stars Practice
Anni Arink Learn

Here, position vector of A = Position vector of  $A = \vec{a} - 2\vec{b} + 3\vec{c}$ position vector of B = Position vector of C = Position vector of

 $\overrightarrow{AB}$  = position vector of B - position vector of A=  $(2\vec{a} + 3\vec{b} - 4\vec{c}) - (\vec{a} - 2\vec{b} + 3\vec{c})$ =  $2\vec{a} + 3\vec{b} - 4\vec{c} - \vec{a} + 2\vec{b} - 3\vec{c}$  $\overrightarrow{AB} = \vec{a} + 5\vec{b} - 7\vec{c}$ 

 $\overrightarrow{BC} = \text{position vector of } C - \text{position vector of } B$   $= \left( -7\vec{b} + 10\vec{c} \right) - \left( 2\vec{a} + 3\vec{b} - 4\vec{c} \right)$   $= -7\vec{b} + 10\vec{c} - 2\vec{a} - 3\vec{b} + 4\vec{c}$   $\overrightarrow{BC} = -2\vec{a} - 10\vec{b} + 14\vec{c}$ 

From  $\overrightarrow{AB}$  and  $\overrightarrow{BC}$ , we get  $\overrightarrow{BC} = -2(\overrightarrow{AB})$ 

So,  $\overrightarrow{AB}$  and  $\overrightarrow{BC}$  are parallel but  $\overrightarrow{B}$  is a common vector. Hence, A,B,C are collinear.

### Algebra of Vectors Ex 23.7 Q2(i)

Let the points be A,B,C

Position vector of  $A = \vec{a}$ Position vector of  $B = \vec{b}$ Position vector of  $C = 3\vec{a} - 2\vec{b}$ 

 $\overrightarrow{AB}$  = Position vector of B - Position vector of A=  $\overrightarrow{b}$  -  $\overrightarrow{a}$ 

 $\overrightarrow{BC}$  = Position vector of C - Position vector of B=  $3\vec{a} - 2\vec{b} - \vec{b}$ =  $3\vec{a} - 3\vec{b}$ 

Using  $\overrightarrow{AB}$  and  $\overrightarrow{BC}$ 

Let  $\overrightarrow{BC} = \lambda \left( \overrightarrow{AB} \right)$  [where  $\lambda$  is and scalar]  $3\vec{a} - 3\vec{b} = \lambda \left( \vec{b} - \vec{a} \right)$   $3\vec{a} - 3\vec{b} = \lambda \vec{b} - \lambda \vec{a}$  $3\vec{a} - 3\vec{b} = \lambda \vec{a} + \lambda \vec{b}$ 

Comparing the coefficients of LHS and RHS, we get

 $-\lambda = 3$  $\lambda = 3$  $\lambda = -3$ 

Since the value of  $\lambda$  are different. Therefore, A,B,C are not collinear.

Million Stars & Practice
William Barractice

### Algebra of Vectors Ex 23.7 Q2(ii)

Let the points be A,B,C

Position vector of  $A = \vec{a} + \vec{b} + \vec{c}$ Position vector of  $B = 4\vec{a} + 3\vec{b}$ Position vector of  $C = 10\vec{a} + 7\vec{b} - 2\vec{c}$ 

 $\overrightarrow{AB}$  = Position vector of B - Position vector of A  $= \left(4\vec{a} + 3\vec{b}\right) - \left(\vec{a} + \vec{b} + \vec{c}\right)$  $= 4\vec{a} + 3\vec{b} - \vec{a} - \vec{b} - \vec{c}$  $\overrightarrow{AB} = 3\overrightarrow{a} + 2\overrightarrow{b} - \overrightarrow{c}$ 

 $\overrightarrow{BC}$  = Position vector of C - Position vector of B $= (10\vec{a} + 7\vec{b} - 2\vec{c}) - (4\vec{a} + 3\vec{b})$  $= 10\vec{a} + 7\vec{b} - 2\vec{c} - 4\vec{a} - 3\vec{b}$  $\overrightarrow{BC} = 6\vec{a} + 4\vec{b} - 2\vec{c}$ 

Using  $\overrightarrow{AB}$  and  $\overrightarrow{BC}$  $\overrightarrow{BC} = 2(\overrightarrow{AB})$ 

So,  $\overrightarrow{AB}$  is parallel to  $\overrightarrow{BC}$  but  $\overrightarrow{B}$  is a common vector. Hence, A,B,C are collinear.

### Algebra of Vectors Ex 23.7 Q3

 $(2) + 3\hat{k}$   $\therefore \text{ of } B = 3\hat{i} + 4\hat{j} + 7\hat{k}$   $\therefore \text{ an vector of } C = -3\hat{i} - 2\hat{j} - 5\hat{k}$   $\overrightarrow{AB} = \text{Position vector of } B - \text{Position vector of } A$   $= (3\hat{i} + 4\hat{j} + 7\hat{k}) - (\hat{i} + 2\hat{j} + 3\hat{k})$   $= 3\hat{i} + 4\hat{j} + 7\hat{k} - \hat{i} - 2\hat{j} - 3\hat{k}$   $\overrightarrow{AB} = 2\hat{i} + 2\hat{j} + 4\hat{k}$   $\overrightarrow{C} = \text{Position}$ 

 $= \left(-3\hat{i} - 2\hat{j} - 5\hat{k}\right) - \left(3\hat{i} + 4\hat{j} + 7\hat{k}\right)$  $=-3\hat{i}-2\hat{j}-5\hat{k}-3\hat{i}-4\hat{j}-7\hat{k}$  $\overrightarrow{BC} = -6\hat{i} - 6\hat{j} - 12\hat{k}$ 

Using  $\overrightarrow{AB}$  and  $\overrightarrow{BC}$  we get  $\overrightarrow{BC} = -3(\overrightarrow{AB})$ 

So,  $\overrightarrow{AB}$  is parallel to  $\overrightarrow{BC}$  but  $\overrightarrow{B}$  is a common vector. Hence, A,B,C are collinear.

# Million Stars Practice

**Remove Watermark** 

### Algebra of Vectors Ex 23.7 Q4

Let the points be A,B,C

Position vector of  $A = 10\hat{i} + 3\hat{j}$ Position vector of  $B = 12\hat{i} - 5\hat{j}$ Position vector of  $C = a\hat{i} + 11\hat{j}$ 

Given that, A,B,C are collinear  $\Rightarrow \overrightarrow{AB}$  and  $\overrightarrow{BC}$  are collinear

 $\Rightarrow \overrightarrow{AB} = \lambda \left( \overrightarrow{BC} \right) \qquad \text{(Where } \lambda \text{ is same scalar)}$ 

 $\Rightarrow$  Position vector of B - Position vector of A =  $\lambda$  - (Position vector of C - Position vector of B)

$$\Rightarrow \qquad \left(12\hat{i}-5\hat{j}\right)-\left(10\hat{i}+3\hat{j}\right)=\lambda\left[\left(\hat{a}\hat{i}+11\hat{j}\right)-\left(12\hat{i}-5\hat{j}\right)\right]$$

$$\Rightarrow 12\hat{i} - 5\hat{j} - 10\hat{i} - 3\hat{j} = \lambda \left( a\hat{i} + 11\hat{j} - 12\hat{i} + 5\hat{j} \right)$$

$$\Rightarrow \qquad 2\hat{i} - 8\hat{j} = (\lambda a - 12\lambda)\hat{i} = (11\lambda + 5\lambda)\hat{j}$$

Comparing the coefficients of LHS and RHS, we get

$$\lambda a - 12\lambda = 2$$
 (i)

$$-8 = 11\lambda + 5\lambda \qquad \text{(ii)}$$

$$-8 = 11\lambda + 5\lambda$$
$$-8 = 16\lambda$$

$$\lambda = \frac{-8}{16}$$

$$\lambda = -\frac{1}{2}$$

Put the value of & in equation (i),

$$\left(-\frac{1}{2}\right)a - 12\left(-\frac{1}{2}\right) = 2$$

$$-\frac{1}{2}a + \frac{12}{2} = 2$$

$$-\frac{1}{2}a + 6 = 2$$

$$-\frac{1}{2}a = 2 - 6$$

$$-\frac{1}{2}a = -4$$

$$a = (-4) \times (-2)$$

Million Stars Practice
Anillion Stars Practice

Let A, B, C be the points then

Position vector of  $A = \vec{a} + \vec{b}$ Position vector of  $B = \vec{a} - \vec{b}$ Position vector of  $C = \vec{a} + \lambda \vec{b}$ 

 $\overrightarrow{AB}$  = Position vector of B - Position vector of A  $= (\vec{a} - \vec{b}) - (\vec{a} + \vec{b})$  $=\vec{a}-\vec{b}-\vec{a}-\vec{b}$  $\overrightarrow{AB} = -2\overrightarrow{b}$ 

 $\overrightarrow{BC}$  = Position vector of C - Position vector of B $= \left( \vec{a} + \lambda \vec{b} \right) - \left( \vec{a} - \vec{b} \right)$  $= \vec{a} + \lambda \vec{b} - \vec{a} + \vec{b}$  $=\lambda \vec{b} + \vec{b}$ 

Using  $\overrightarrow{AB}$  and  $\overrightarrow{BC}$ , we get  $\overrightarrow{AB} = \left[\frac{(\lambda + 1)}{-2}\right] \left(\overrightarrow{BC}\right)$ 

Let  $\left(\frac{\lambda+1}{-2}\right) = \mu$ 

 $\overrightarrow{BC} = (\lambda + 1)\overrightarrow{b}$ 

Since & is a real number. So,  $\mu$  is also a real no.

So,  $\overrightarrow{AB}$  is parallel to  $\overrightarrow{BC}$ , but  $\overrightarrow{B}$  is a common vector. Hence, A, B, C are collinear.

### Algebra of Vectors Ex 23.7 Q6

Here, 
$$\overrightarrow{OA} + \overrightarrow{OB} = \overrightarrow{OB} + \overrightarrow{OC}$$
  
 $\overrightarrow{OA} - \overrightarrow{BO} = \overrightarrow{BO} - \overrightarrow{CO}$   
 $\overrightarrow{AB} = \overrightarrow{BC}$ 

So,  $\overrightarrow{AB}$  is parallel to  $\overrightarrow{BC}$  but  $\overrightarrow{B}$  is a common vector. Hence, A, B, C are collinear.

### Algebra of Vectors Ex 23.7 Q7

Let the given points be A and B

Position vector of  $A = 2\hat{i} - 3\hat{j} + 4\hat{k}$ Position vector of  $B = -4\hat{i} + 6\hat{j} - 8\hat{k}$ 

Let O be the initial point having postion vector  $0 \times \hat{i} + 0 \times \hat{i} + 0 \times \hat{k}$ 

Therefore,  $\overrightarrow{OA}$  is parallel to  $\overrightarrow{OB}$  but O is the common point to them. Hence, 4 and B are collinear.

**Remove Watermark** 

Here, 
$$A = (m, -1)$$
  
 $B = (2, 1)$ 

$$C=\left(4,5\right)$$

$$\overrightarrow{AB}$$
 = Position vector of  $B$  - Position vector of  $A$   
=  $(2\hat{i} + \hat{j}) - (m\hat{i} - \hat{j})$   
=  $2\hat{i} + \hat{j} - m\hat{i} + \hat{j}$   
=  $(2 - m)\hat{i} + 2\hat{j}$ 

$$\overrightarrow{BC} = \text{Position vector of } C - \text{Position vector of } B$$

$$= \left(4\hat{i} + 5\hat{j}\right) - \left(2\hat{i} + \hat{j}\right)$$

$$= 4\hat{i} + 5\hat{j} - 2\hat{i} - \hat{j}$$

$$\overrightarrow{BC} = 2\hat{i} + 4\hat{j}$$

A,B,C are collinear. So,  $\overrightarrow{AB}$  and  $\overrightarrow{BC}$  are collinear.

So, 
$$\overrightarrow{AB} = \lambda \left( \overrightarrow{BC} \right)$$
  
 $(2-m)\hat{i} + 2\hat{j} = \lambda \left( 2\hat{i} + 4\hat{j} \right)$ , for  $\lambda$  scalar  $(2-m)\hat{i} + 2\hat{j} = 2\lambda \hat{i} + 4\lambda \hat{j}$ 

Mondershare Comparing the coefficient of LHS and RHS.

$$2 - m = 2\lambda$$

$$\frac{2 - m}{2} = \lambda$$

$$2 = 4\lambda$$

$$\frac{2}{4} = \lambda$$

$$\frac{1}{2} = \lambda$$
(ii)

Using (i) and (ii)

$$\frac{2-m}{2} = \frac{1}{2}$$

$$4-2m = 2$$

$$-2m = 2$$

$$-2m = 2-4$$

$$-2m = -2$$

$$m = \frac{-2}{-2}$$

$$m = 1$$

$$\therefore m = 1$$





Here, let 
$$A = (3, 4)$$
  
 $B = (-5, 16)$   
 $C = (5, 1)$ 

$$\overrightarrow{AB}$$
 = Position vector of  $B$  - Position vector of  $A$   
=  $\left(-5\hat{i} + 16\hat{j}\right) - \left(3\hat{i} + 4\hat{j}\right)$   
=  $-5\hat{i} + 16\hat{j} - 3\hat{i} - 4\hat{j}$   
 $\overrightarrow{AB}$  =  $-8\hat{i} + 12\hat{j}$ 

$$\overrightarrow{BC} = \text{Position vector of } C - \text{Position vector of } B$$

$$= \left(5\hat{i} + \hat{j}\right) - \left(-5\hat{i} + 16\hat{j}\right)$$

$$= 5\hat{i} + \hat{j} + 5\hat{i} - 16\hat{j}$$

$$\overrightarrow{BC} = 10\hat{i} - 15\hat{j}$$

So, 
$$4(\overrightarrow{AB}) = -5(\overrightarrow{BC})$$

 $\overrightarrow{AB}$  is parallel to  $\overrightarrow{BC}$  but B is a common point.

Hence, A,B,C are collinear.

### Algebra of Vectors Ex 23.7 Q10

Here, it is given that vectors  $a=2\hat{i}-3\hat{j}$  and  $b=-6\hat{i}+m\hat{j}$  are collinear.

$$a=2\hat{i}-3\hat{j}$$
 and  $b=-6\hat{i}+m\hat{j}$  are collinear.  
So,  $a=\lambda b$ , for a scalar  $\lambda$   
 $2\hat{i}-3\hat{j}=\lambda\left(-6\hat{i}+m\hat{j}\right)$   
 $2\hat{i}-3\hat{j}=-6\lambda\hat{i}+\lambda m\hat{j}$   
Comparing the coefficients of LHS and RHS,  
 $2=-6\lambda$   
 $\lambda=\frac{2}{-6}$   
 $\lambda=\frac{-1}{3}$  (i)  
 $-3=\lambda m$   
 $\lambda=\frac{-3}{m}$  (ii)

$$\lambda = \frac{2}{-6}$$

$$! = \frac{-1}{3}$$

$$\lambda = \frac{-3}{3}$$

$$\lambda = \frac{-3}{m}$$
 (ii)

From (i) and (ii),

$$\frac{-1}{3} = \frac{-3}{m}$$
$$m = 3 \times 3$$

$$m = 3 \times 3$$

$$hlored{h} m = 9$$

Million Stars & Practice
Annihit Learn



The given points are A (1, -2, -8), B (5, 0, -2), and C (11, 3, 7).

Thus, the given points A, B, and C are collinear.

Now, let point B divide AC in the ratio  $\lambda:1$ . Then, we have:

$$\begin{aligned} \overrightarrow{OB} &= \frac{\lambda \overrightarrow{OC} + \overrightarrow{OA}}{(\lambda + 1)} \\ \Rightarrow 5\hat{i} - 2\hat{k} &= \frac{\lambda \left(11\hat{i} + 3\hat{j} + 7\hat{k}\right) + \left(\hat{i} - 2\hat{j} - 8\hat{k}\right)}{\lambda + 1} \\ \Rightarrow (\lambda + 1)\left(5\hat{i} - 2\hat{k}\right) &= 11\lambda\hat{i} + 3\lambda\hat{j} + 7\lambda\hat{k} + \hat{i} - 2\hat{j} - 8\hat{k} \\ \Rightarrow 5(\lambda + 1)\hat{i} - 2(\lambda + 1)\hat{k} &= (11\lambda + 1)\hat{i} + (3\lambda - 2)\hat{j} + (7\lambda - 8)\hat{k} \end{aligned}$$

On equating the corresponding components, we get:

$$5(\lambda+1) = 11\lambda+1$$

$$\Rightarrow 5\lambda+5 = 11\lambda+1$$

$$\Rightarrow 6\lambda = 4$$

$$\Rightarrow \lambda = \frac{4}{6} = \frac{2}{3}$$

Hence, point B divides AC in the ratio 2:3

### Algebra of Vectors Ex 23.7 Q12

We have

we have  $\overrightarrow{AP} = Position \ vector \ of \ P - Position \ vector \ of \ A$   $\Rightarrow \overrightarrow{AP} = \hat{i} + 2\hat{j} + 3\hat{k} - (-2\hat{i} + 3\hat{j} + 5\hat{k}) = 3\hat{i} - \hat{j} - 2\hat{k}$   $\overrightarrow{PB} = Position \ vector \ of \ B - Position \ vector \ of \ P$   $\Rightarrow \overrightarrow{PB} = 7\hat{i} - \hat{k} - (\hat{i} + 2\hat{j} + 3\hat{k}) = 6\hat{i} - 2\hat{j} - 4\hat{k}$   $Clearly, \overrightarrow{PB} = 2\overrightarrow{AP}$ so vectors  $\overrightarrow{AP}$  and  $\overrightarrow{PB}$  are collinear.

But P is a point common to  $\overrightarrow{AP}$  and  $\overrightarrow{PB}$ .

Hence P. A. B are collinear points.

Similarly,  $\overrightarrow{CP} = \hat{i} + 2\hat{j} + 3\hat{k} - (-3\hat{i} - 2\hat{j} - 5\hat{k}) = 4\hat{i} + 4\hat{j} + 8\hat{k}$ and  $\overrightarrow{PD} = 3\hat{i} + 4\hat{j} + 7\hat{k} - (\hat{i} + 2\hat{j} + 3\hat{k}) = 2\hat{i} + 2\hat{j} + 4\hat{k}$ 

So vectors  $\overrightarrow{CP}$  and  $\overrightarrow{PD}$  are collinear.

But P is a common point to  $\overrightarrow{CP}$  and  $\overrightarrow{CD}$ .

Hence, C, P, D are collinear points.

Thus, A, B, C, D and P are points such that A, P, B and C, P, D are two sets of collinear points. Hence AB and CD intersect at the point P

Sk

T., P, D

Sect at the

Points (  $\lambda$ , - 10, 3), (1-1, 3) and (3, 5, 3) are collinear.

:. ( 
$$\lambda$$
, - 10, 3) = x(1 -1, 3) + y(3, 5, 3) for some scalars x and y.   
  $\Rightarrow \lambda = x + 3y$ , -10 = -x + 5y and 3 = 3x + 3y

Solving -10 = -x + 5y and 3 = 3x + 3y for x and y we get, 
$$x = \frac{5}{2}$$
 and  $y = -\frac{3}{2}$ 

Now,

$$\lambda = x + 3y$$

$$\Rightarrow \lambda = \frac{5}{2} + 3\left(-\frac{3}{2}\right) = -2$$



Millionstars edulaciice
Millionstars edulaciice
Anink Learn

(i) Let P, Q, R be the points whose position vectors are  $2\hat{i} + \hat{j} - \hat{k}$ ,  $3\hat{i} - 2\hat{j} + \hat{k}$  and  $\hat{i} + 4\hat{j} - 3\hat{k}$  respectively.

$$\overrightarrow{PQ} = \text{Position vector of } Q - \text{Position vector of } P$$

$$= \left(3\hat{i} - 2\hat{j} + \hat{k}\right) - \left(2\hat{i} + \hat{j} - \hat{k}\right)$$

$$= 3\hat{i} - 2\hat{j} + \hat{k} - 2\hat{i} - \hat{j} + \hat{k}$$

$$\overrightarrow{PQ} = \hat{i} - 3\hat{j} + 2\hat{k}$$

$$\begin{split} \overrightarrow{QR} &= \text{Position vector of } R - \text{Position vector of } Q \\ &= \left(\hat{i} + 4\hat{j} - 3\hat{k}\right) - \left(3\hat{i} - 2\hat{j} + \hat{k}\right) \\ &= \hat{i} + 4\hat{j} - 3\hat{k} - 3\hat{i} + 2\hat{j} - \hat{k} \\ &= -2\hat{i} + 6\hat{j} - 4\hat{k} \\ \overrightarrow{QR} &= -2\overrightarrow{PQ} \end{split}$$

Therefore,  $\overrightarrow{QR}$  is parallel to  $\overrightarrow{PQ}$  but there is a common point Q. So, P,Q,R are collinear.

(ii) Let P, Q, R be the points represented be the vectors are  $3\hat{i} - 2\hat{j} + 4\hat{k}$ ,  $\hat{i} + \hat{j} + \hat{k}$  and  $-\hat{i} + 4\hat{j} - 2\hat{k}$  respectively.

$$\overrightarrow{PQ} = \text{Position vector of } Q - \text{Position vector of } P$$

$$= \left(-\hat{i} + 4\hat{j} - 2\hat{k}\right) - \left(3\hat{i} - 2\hat{j} + 4\hat{k}\right)$$

$$= \hat{i} + \hat{j} + \hat{k} - 3\hat{i} + 2\hat{j} - 4\hat{k}$$

$$= -2\hat{i} - 3\hat{j} - 3\hat{k}$$

$$\overrightarrow{QR} = \text{Position vector of } R - \text{Position vector of } Q$$

$$= \left( -\hat{i} + 4\hat{j} - 2\hat{k} \right) - \left( \hat{i} + \hat{j} + \hat{k} \right)$$

$$= -\hat{i} + 4\hat{j} - 2\hat{k} - \hat{i} - \hat{j} - \hat{k}$$

$$= -2\hat{i} + 3\hat{j} - 3\hat{k}$$

$$\overrightarrow{PQ} = \overrightarrow{QR}$$

So,  $\overrightarrow{PQ}$  is parallel to  $\overrightarrow{QR}$  but Q is the common point Q. So, P, Q, R are collinear.

### Algebra of Vectors Ex 23.8 Q2(i)

Here, 
$$\overrightarrow{A} = 6\hat{i} - 7\hat{j} - \hat{k}$$
  
 $\overrightarrow{B} = 2\hat{i} - 3\hat{j} + \hat{k}$   
 $\overrightarrow{C} = 4\hat{i} - 5\hat{j} - 0 \times \hat{k}$ 

$$\overrightarrow{AB} = \overrightarrow{B} - \overrightarrow{A}$$

$$= (2\hat{i} - 3\hat{j} + \widehat{k}) - (6\hat{i} - 7\hat{j} - \widehat{k})$$

$$= 2\hat{i} - 3\hat{j} + \widehat{k} - 6\hat{i} + 7\hat{j} + \widehat{k}$$

$$\overrightarrow{AB} = -4\hat{i} + 4\hat{i} + 2\hat{k}$$

$$\begin{aligned} \overrightarrow{BC} &= \overrightarrow{C} - \overrightarrow{B} \\ &= \left( 4\hat{i} - 5\hat{j} - 0 \times \widehat{k} \right) - \left( 2\hat{i} - 3\hat{j} + \widehat{k} \right) \\ &= 4\hat{i} - 5\hat{j} - 0 \times \widehat{k} - 2\hat{i} + 3\hat{j} - \widehat{k} \\ \overrightarrow{BC} &= 2\hat{i} - 2\hat{j} - \widehat{k} \end{aligned}$$

$$\overrightarrow{AB} = -2 \left( \overrightarrow{BC} \right)$$

So,  $\overrightarrow{AB}$  is parallel to  $\overrightarrow{BC}$  but B is the common point. So, A,B,C are collinear.

Million Stars Practice

Williams Stars Practice

### Algebra of Vectors Ex 23.8 Q2(ii)

Here, 
$$\overrightarrow{A} = 2\hat{i} - \hat{j} + 3\hat{k}$$
  
 $\overrightarrow{B} = 4\hat{i} + 3\hat{j} + \hat{k}$   
 $\overrightarrow{C} = 3\hat{i} + \hat{j} + 2\hat{k}$ 

$$\begin{aligned} \overrightarrow{AB} &= \overrightarrow{B} - \overrightarrow{A} \\ &= \left( 4\widehat{i} + 3\widehat{j} + \widehat{k} \right) - \left( 2\widehat{i} - \widehat{j} + 3\widehat{k} \right) \\ &= 4\widehat{i} + 3\widehat{j} + \widehat{k} - 2\widehat{i} + \widehat{j} - 3\widehat{k} \\ \overrightarrow{AB} &= 2\widehat{i} + 4\widehat{j} - 2\widehat{k} \end{aligned}$$

$$\begin{aligned} \overrightarrow{BC} &= \overrightarrow{C} - \overrightarrow{B} \\ &= \left( 3\hat{i} + \hat{j} + 2\widehat{k} \right) - \left( 4\hat{i} + 3\hat{j} + \widehat{k} \right) \\ &= 3\hat{i} + \hat{j} + 2\widehat{k} - 4\hat{i} - 3\hat{j} - \widehat{k} \\ \overrightarrow{BC} &= -\hat{i} - 2\hat{j} + \widehat{k} \end{aligned}$$

So, 
$$\overrightarrow{AB} = -2 \left( \overrightarrow{BC} \right)$$

 $\overrightarrow{AB}$  is parallel to  $\overrightarrow{BC}$  but  $\overrightarrow{B}$  is a common vector. Therefore, A,B,C are collinear.

### Algebra of Vectors Ex 23.8 Q2(iii)

Here, 
$$\vec{A} = \hat{i} + 2\hat{j} + 7\hat{k}$$
  
 $\vec{B} = 2\hat{i} + 6\hat{j} + 3\hat{k}$   
 $\vec{C} = 3\hat{i} + 10\hat{j} - \hat{k}$ 

$$\overrightarrow{AB} = \overrightarrow{B} - \overrightarrow{A}$$

$$= \left(2\widehat{i} + 6\widehat{j} + 3\widehat{k}\right) - \left(\widehat{i} + 2\widehat{j} + 7\widehat{k}\right)$$

$$= 2\widehat{i} + 6\widehat{j} + 3\widehat{k} - \widehat{i} - 2\widehat{j} - 7\widehat{k}$$

$$\overrightarrow{AB} = \widehat{i} + 4\widehat{j} - 4\widehat{k}$$

$$\begin{aligned} \overrightarrow{BC} &= \overrightarrow{C} - \overrightarrow{B} \\ &= \left( 3\hat{i} + 10\hat{j} - \widehat{k} \right) - \left( 2\hat{i} + 6\hat{j} + 3\widehat{k} \right) \\ &= 3\hat{i} + \hat{j} + 2\widehat{k} - 2\hat{i} - 6\hat{j} - 3\widehat{k} \\ \overrightarrow{BC} &= \hat{i} + 4\hat{j} - 4\widehat{k} \end{aligned}$$

$$\overrightarrow{AB} = \overrightarrow{BC}$$

So,  $\overrightarrow{AB}$  is parallel to  $\overrightarrow{BC}$  but  $\overrightarrow{B}$  is a common vector. So, A,B,C are collinear.

### Algebra of Vectors Ex 23.8 Q2(iv)

Here, 
$$\overrightarrow{A} = -3\hat{i} - 2\hat{j} - 5\hat{k}$$
  

$$\overrightarrow{B} = \hat{i} + 2\hat{j} + 3\hat{k}$$

$$\overrightarrow{C} = 3\hat{i} + 4\hat{j} + 7\hat{k}$$

$$\overrightarrow{AB} = \overrightarrow{B} - \overrightarrow{A}$$

$$= (\widehat{i} + 2\widehat{j} + 3\widehat{k}) - (-3\widehat{i} - 2\widehat{j} - 5\widehat{k})$$

$$= \widehat{i} + 2\widehat{j} + 3\widehat{k} + 3\widehat{i} + 2\widehat{j} + 5\widehat{k}$$

$$\overrightarrow{AB} = 4\widehat{i} + 4\widehat{j} + 8\widehat{k}$$

$$\overrightarrow{BC} = \overrightarrow{C} - \overrightarrow{B}$$

$$= (3\hat{i} + 4\hat{j} + 7\hat{k}) - (\hat{i} + 2\hat{j} + 3\hat{k})$$

$$= 3\hat{i} + 4\hat{j} + 7\hat{k} - \hat{i} - 2\hat{j} - 3\hat{k}$$

$$\overrightarrow{BC} = 2\hat{i} + 2\hat{j} + 4\hat{k}$$

So, 
$$\overrightarrow{AB} = 2\overrightarrow{BC}$$

Hence,  $\overrightarrow{AB}$  is parallel to  $\overrightarrow{BC}$  but  $\overrightarrow{B}$  is a common vector. Therefore, A,B,C are collinear.

# Million Stars Practice Anillion Stars Practice

Here, 
$$\vec{A} = 2\hat{i} - \hat{j} + 3\hat{k}$$
  
 $\vec{B} = 3\hat{i} - 5\hat{j} + \hat{k}$   
 $\vec{C} = -\hat{i} + 11\hat{j} + 9\hat{k}$ 

$$\begin{aligned} \overrightarrow{AB} &= \overrightarrow{B} - \overrightarrow{A} \\ &= \left( 3\widehat{i} - 5\widehat{j} + \widehat{k} \right) - \left( 2\widehat{i} - \widehat{j} + 3\widehat{k} \right) \\ &= 3\widehat{i} - 5\widehat{j} + \widehat{k} - 2\widehat{i} + \widehat{j} - 3\widehat{k} \\ \overrightarrow{AB} &= \widehat{i} - 4\widehat{j} - 2\widehat{k} \end{aligned}$$

$$\begin{split} \overrightarrow{BC} &= \overrightarrow{C} - \overrightarrow{B} \\ &= \left( -\hat{i} + 11\hat{j} + 9\widehat{k} \right) - \left( 3\hat{i} - 5\hat{j} + \widehat{k} \right) \\ &= -\hat{i} + 11\hat{j} + 9\widehat{k} - 3\hat{i} + 5\hat{j} - \widehat{k} \\ &= -4\hat{i} + 16\hat{j} + 8\widehat{k} \end{split}$$

So, 
$$\overrightarrow{AB} = -4 \left( \overrightarrow{BC} \right)$$

 $\overrightarrow{AB}$  is parallel to vector  $\overrightarrow{BC}$  but  $\overrightarrow{B}$  is a common vector.

So, A, B, C are collinear

### Algebra of Vectors Ex 23.8 Q3(i)

We know that,

Three vectors are coplanar if one of the vector can be expressed as the linear combination of other two.

Let,  

$$5\vec{a} + 6\vec{b} + 7\vec{c} = x (7\vec{a} - 8\vec{b} + 9\vec{c}) + y (3\vec{a} + 20\vec{b} + 5\vec{c})$$
  
 $5\vec{a} + 6\vec{b} + 7\vec{c} = 7\vec{a}x - 8\vec{b}x + 9\vec{c}x + 3\vec{a}y + 20\vec{b}y + 5\vec{c}y$   
 $5\vec{a} + 6\vec{b} + 7\vec{c} = (7x + 3y)\vec{a} + (-8x + 20y)\vec{b} + (9x + 5y)\vec{c}$   
Comparing the LHS and RHS,  
 $7x + 3y = 5$  (i)  
 $-8x + 20y = 6$  (ii)  
 $9x + 5y = 7$  (iii)

$$x + 3y = 5$$

$$-8x + 20y = 6$$
 (i

$$9x + 5y = 7$$
 fiii

Subtract  $-8 \times (i)$  from  $7 \times (ii)$ ,

$$-56x + 140y = 42$$

$$\frac{-56x - 24y = -40}{(+)(+)(+)}$$

$$164y = 82$$

$$y = \frac{82}{164}$$

$$y=\frac{1}{2}$$

$$+3y = 5$$

$$7x + 3\left(\frac{1}{2}\right) = 5$$

$$7x + \frac{3}{2} = 5$$

$$7x = \frac{5}{1} - \frac{3}{2}$$

$$7x = \frac{10 - 3}{2}$$

$$7x = \frac{7}{2}$$

$$X = \frac{7}{14}$$

$$x = \frac{1}{2}$$

Now, put  $x = \frac{1}{2}$  and  $y = \frac{1}{2}$  in equation (iii),

$$9x + 5y = 7$$

$$9\left(\frac{1}{2}\right) + 5\left(\frac{1}{2}\right) = 7$$

$$\frac{9}{2} + \frac{5}{2} = 7$$

$$\frac{14}{2} = 7$$

LHS = RHS

.. The value of x,y satisfy equation (iii).

$$5\vec{a} + 6\vec{b} + 7\vec{c}$$
,  $7\vec{a} - 8\vec{b} + 9\vec{c}$ ,  $3\vec{a} + 20\vec{b} + 5\vec{c}$  are coplanar.

### Algebra of Vectors Ex 23.8 Q3(ii)

We know that,

Three vectors are coplanar if one of them can be expressed as the linear combination of other two.

**Remove Watermark** 

Let

$$\vec{a}-2\vec{b}+3\vec{c}=x\left(-3\vec{b}+5\vec{c}\right)+y\left(-2\vec{a}+3\vec{b}-4\vec{c}\right)$$

$$\vec{a} - 2\vec{b} + 3\vec{c} = -3\vec{b}x + 5\vec{c}x + 2\vec{a}y + 3\vec{b}y - 4\vec{c}y$$

$$\vec{a} - 2\vec{b} + 3\vec{c} = -3\vec{b}x + 5\vec{c}x + 2\vec{a}y + 3\vec{b}y - 4\vec{c}y$$
  
$$\vec{a} - 2\vec{b} + 3\vec{c} = (-2y)\vec{a} + (-3x + 3y)\vec{b} + (5x - 4y)\vec{c}$$

Comparing the LHS and RHS,

$$2y = 1$$

$$-3x + 3y = -2$$

$$4v = 3$$
 fiii

From solving (i) and  $y = -\frac{1}{2}$ 

Put value of y in equation (ii),

$$-3x + 3y = -2$$

$$-3x + 3\left(-\frac{1}{2}\right) = -2$$

$$-3x - \frac{3}{2} = -2$$

$$-3x = \frac{-2}{1} + \frac{3}{2}$$

$$-3x = \frac{-4+3}{2}$$

$$-3x = \frac{-1}{2}$$

$$X = \frac{-1}{-6}$$

$$X = \frac{1}{6}$$

Put value of x and y in equation (iii)

$$5x - 4y = 3$$

$$5\left(\frac{1}{6}\right) - 4\left(-\frac{1}{2}\right) = 3$$

$$\frac{5}{6} + \frac{4}{2} = 3$$

$$\frac{5+12}{6} = 3$$

$$\frac{17}{6} = 3$$

ioneath & Practice So, value of x and y do not satisfy the equation (iii).

vectors  $\vec{a} - 2\vec{b} + 3\vec{c}$ ,  $-3\vec{b} + 5\vec{c}$ , and  $-2\vec{a} + 3\vec{b} - 4\vec{c}$  are not coplanar.

Here,

Position vector of  $P = 6\hat{i} - 7\hat{j}$ 

Position vector of  $Q = 16\hat{i} - 19\hat{j} - 4\hat{k}$ 

Position vector of  $R = 3\hat{i} - 6\hat{k}$ 

Position vector of  $S = 2\hat{i} - 5\hat{j} + 10\hat{k}$ 

 $\overrightarrow{PQ}$  = Position vector of Q - Position vector of P

$$= \left(16\hat{i} - 19\hat{j} - 4\hat{k}\right) - \left(6\hat{i} - 7\hat{j}\right)$$

$$= 16\hat{i} - 19\hat{j} - 4\hat{k} - 6\hat{i} + 7\hat{j}$$

$$= 10\hat{i} - 12\hat{j} - 4\hat{k}$$

 $\overrightarrow{PR}$  = Position vector of R - Position vector of P

$$= \left(3\hat{j} - 6\hat{k}\right) - \left(6\hat{i} - 7\hat{j}\right)$$

$$=3\hat{j}-6\hat{k}-6\hat{i}+7\hat{j}$$

$$= -6\hat{i} + 10\hat{j} - 6\hat{k}$$

 $\overrightarrow{PS}$  = Position vector of S - Position vector of P

$$= \left(2\hat{i} - 5\hat{j} + 10\hat{k}\right) - \left(6\hat{i} - 7\hat{j}\right)$$

$$=2\hat{i}-5\hat{j}+10\hat{k}-6\hat{i}+7\hat{j}$$

$$= -4\hat{i} + 2\hat{j} + 10\hat{k}$$

Let  $\overrightarrow{PQ} = x\overrightarrow{PR} + y\overrightarrow{PS}$ 

$$10\hat{i}-12\hat{j}-4\hat{k}=\times\left(-6\hat{i}+10\hat{j}-6\hat{k}\right)+\left(-4\hat{i}+2\hat{j}+10\hat{k}\right)$$

$$= -6x\hat{i} + x10\hat{j} - 6x\hat{k} - 4y\hat{i} + 2y\hat{j} + 10y\hat{k}$$
$$10\hat{i} - 12\hat{j} - 4\hat{k} = \left(-6x - 4y\right)\hat{i} + \left(10x + 2y\right)\hat{j} + \left(-6x + 10y\right)\hat{k}$$

$$10\hat{i} - 12\hat{j} - 4\hat{k} = x \left( -6\hat{i} + 10\hat{j} - 6\hat{k} \right) + \left( -4\hat{i} + 2\hat{j} + 10\hat{k} \right)$$

$$= -6x\hat{i} + x10\hat{j} - 6x\hat{k} - 4y\hat{i} + 2y\hat{j} + 10y\hat{k}$$

$$10\hat{i} - 12\hat{j} - 4\hat{k} = \left( -6x - 4y \right)\hat{i} + \left( 10x + 2y \right)\hat{j} + \left( -6x + 10y \right)\hat{k}$$
Comparing the coefficients of  $\hat{i}$ ,  $\hat{j}$  and  $\hat{k}$  of LHS and RHS,
$$-6x - 4y = 10$$

$$3x + 2y = -5$$
(i)
$$10x + 2y = -12$$
(ii)
$$-6x + 10y = -4$$
(iii)
Substracting (i) from (ii),

Comparing the coefficients of  $\hat{i},\hat{j}$  and  $\hat{k}$  of LHS and RHS,

$$-6x - 4y = 10$$

$$3x + 2y = -5$$

$$10x + 2y = -12$$
 (ii)

$$-6x + 10y = -4$$
 (iii

Substracting (i) from (ii),

$$10x + 2y = -12$$

$$3x + 2y = -5$$
  
 $(-)$   $(-)$   $(+)$ 

$$x = \frac{-7}{7}$$

Put x = -1 in equation (i)

$$3x + 2y = -5$$

$$3\left(-1\right)+2y=-5$$

$$-3 + 2y = -5$$

$$2y = -5 + 3$$

$$y = \frac{-2}{2}$$

$$y = -1$$

Put x = -1 and y = -1 in equation (iii),

$$-6x + 10y = -4$$

Therefore,

P,Q,R,S are coplanar.

Million Stars Practice

Williams Stars Practice

## Algebra of Vectors Ex 23.8 Q5(i)

We know that, three vectors are coplanar if one of the vector can be expanded as linear combination of other two.

Let,

$$2\hat{i} - \hat{j} + \hat{k} = x \left( \hat{i} - 3\hat{j} - 5\hat{k} \right) + y \left( 3\hat{i} - 4\hat{j} - 4\hat{k} \right)$$

$$2\hat{i} - \hat{j} + \hat{k} = x\hat{i} - 3x\hat{j} - 5x\hat{k} + 3y\hat{i} - 4y\hat{j} - 4y\hat{k}$$

$$2\hat{i} - \hat{j} + \hat{k} = (x + 3y)\hat{i} + (-3x - 4y)\hat{j} + (-5x - 4y)\hat{k}$$

Comparing the coefficients of LHS and RHS,

$$x + 3y = 2$$
 (i)

$$-3x - 4y = -1$$
 (ii)

$$-5x - 4y = 1$$
 (iii)

For solving equation (i) and (ii),

Add 3 x (i) with equation (ii),

$$3x + 9y = 6$$

$$-3x - 4y = -3$$

$$5y = -3$$

$$y = \frac{5}{5}$$

$$y = 1$$

Put y in equation (i),

$$x + 3y = 2$$

$$x + 3(1) = 2$$

$$x + 3 = 2$$

$$x = 2 - 3$$

$$x = -1$$

Put the value of x and y in equation (iii),

$$-5x-4y=1$$

$$-5(-1)-4(1)=1$$

LHS = RHS

So, the value of x and y satisfy equation (iii).

Hence, vectors are coplanar.

$$\begin{split} \hat{i} + \hat{j} + \hat{k} &= x \left( 2\hat{i} + 3\hat{j} - \hat{k} \right) + y \left( -\hat{i} - 2\hat{j} + 2\hat{k} \right) \\ \hat{i} + \hat{j} + \hat{k} &= 2x\hat{i} + 3x\hat{j} - x\hat{k} + -y\hat{i} - 2y\hat{j} + 2y\hat{k} \\ \hat{i} + \hat{j} + \hat{k} &= \left( 2x - y \right)\hat{i} + \left( 3x - 2y \right)\hat{j} + \left( -x + 2y \right)\hat{k} \end{split}$$

Comparing the coefficients of LHS and RHS,

$$2x - y = 1$$

$$3x - 2y = 1$$

$$-x + 2y = 1$$
 (iii)

For solving (i) and (ii),

Subtracting 2 × (i) from (ii),

$$3x - 2y = 1$$

$$4x - 2y = (-)^2$$

$$x = 1$$

Put the value of x in equation (i),

$$2x - y = 1$$

$$2(1) - y = 1$$

$$2-y=1$$

$$-y = 1 - 2$$

$$-y = -1$$

$$y = 1$$

Put the value of x and y in equation (iii),

$$-x + 2y = 1$$

$$-(1)+2(1)=1$$

$$-1 + 2 = 1$$

The value of x and y satisfy equation (iii).

Hence, vectors are coplanar.

Wondershare **Remove Watermark PDFelement** 

## Algebra of Vectors Ex 23.8 Q6(i)

We know that,

Three vectors are coplanar if one of them vector can be expressed as the linear combination of the other two.

Let,

$$\begin{split} \left(3\hat{i} + \hat{j} - \hat{k}\right) &= x\left(2\hat{i} - \hat{j} + 7\hat{k}\right) + y\left(7\hat{i} - \hat{j} + 23\hat{k}\right) \\ &= 2x\hat{i} - x\hat{j} + 7x\hat{k} + 7y\hat{i} - y\hat{j} + 23y\hat{k} \\ \left(3\hat{i} + \hat{j} - \hat{k}\right) &= \left(2x + 7y\right)\hat{i} + \left(-x - y\right)\hat{j} + \left(7x + 23y\right)\hat{k} \end{split}$$

Equating the coefficients of LHS and RHS,

$$2x + 7y = 3$$

$$-x-y=1$$

$$7x + 23y = -1$$
 (iii)

For solving (i) and (ii),

Add (i) and 
$$2 \times (ii)$$
,

$$2x + 7y = 3$$

$$\frac{-2x - 2y = 2}{5y = 5}$$

$$y = \frac{5}{5}$$

Put the value of y in equation (i),

$$2x + 7y = 3$$

$$2x + 7(1) = 3$$

$$2x + 7 = 3$$

$$2x = 3 - 7$$

$$2x = -4$$

$$x = \frac{1}{2}$$

$$x = -2$$

Put the value of x and y in equation (iii)

$$7x + 23y = -1$$

$$7(2) + 23(1) = -1$$

The value of x and y do not satisfy the equation (iii).

Hence, vectors are non-coplanar.

# Wondershare PDFelement

## Algebra of Vectors Ex 23.8 Q6(ii)

We know that,

Three vectors are coplanar if any one of the vector can be expressed as the linear combination of other two vectors.

Let,

$$\hat{i} + 2\hat{j} + 3\hat{k} = x(2\hat{i} + \hat{j} + 3\hat{k}) + y(\hat{i} + \hat{j} + \hat{k}) = 2x\hat{i} + x\hat{j} + 3x\hat{k} + y\hat{i} + y\hat{j} + y\hat{k}$$
  

$$\hat{i} + 2\hat{j} + 3\hat{k} = (2x + y)\hat{i} + (x + 2y)\hat{j} + (3x + y)\hat{k}$$

Comparing the coefficients of LHS and RHS,

$$2x + y = 1 (i)$$

$$x + 2y = 2$$

$$3x + y = 3$$
 (iii)

Subtracting  $2 \times (ii)$  from equation (i),

(ii)

$$2x + 4y = 4$$

$$2x + y = 1$$
  
 $(-)$   $(-)$   $(-)$   $(-)$   $3y = 3$ 

$$y = \frac{3}{3}$$

$$y = 1$$

Put the value of y in equation (i),

$$2x + y = 1$$

$$2x + 1 = 1$$

$$2x = 1 - 1$$

$$2x = 0$$

$$x = \frac{0}{2}$$

Put the value of x and y in equation (iii),

$$3x + y = 3$$

$$3(0) + 1 = 3$$

$$0 + 1 = 3$$

The value of x and y do not satisfy the equation (iii).

Hence, vectors are non-coplanar.

We know that,

Three vectors are coplanar if any one of them can be expressed as the linear combination of other two vectors.

Let,

$$(2\vec{a} - \vec{b} + 3\vec{c}) = x (\vec{a} + \vec{b} - 2\vec{c}) + y (\vec{a} + \vec{b} - 3\vec{c})$$

$$= \vec{a}x + \vec{b}x - 2\vec{c}x + \vec{a}y + \vec{b}y - 3\vec{c}y$$

$$(2\vec{a} - \vec{b} + 3\vec{c}) = (x + y)\vec{a} + (x + y)\vec{b} + (-2x - 3y)\vec{c}$$

Comparing the coefficients of LHS and RHS,

$$x + y = 2$$

$$x + y = -1$$

$$-2x - 3y = 3$$
 (iii)

For solving the equation (i) and (ii),

Subtracting (ii) from (i),

$$x + y = 2$$

$$\frac{x + y = -1}{(-)(-)}$$
0 = 3

There is no value of x and y that can satisfy the equation (iii).

Hence, vectors are non-coplanar.

## Algebra of Vectors Ex 23.8 Q7(ii)

We know that,

Three vectors are coplanar if any one of them can be expressed as the linear combination of other two vectors.

Let

$$\vec{a} + 2\vec{b} + 3\vec{c} = x (2\vec{a} + \vec{b} + 3\vec{c}) + y (\vec{a} + \vec{b} + \vec{c})$$

$$= 2\vec{a}x + \vec{b}x + 3\vec{c}x + \vec{a}y + \vec{b}y + \vec{c}y$$

$$\vec{a} + 2\vec{b} + 3\vec{c} = (2x + y)\vec{a} + (x + y)\vec{b} + (3x + y)\vec{c}$$

Comparing the coefficients of LHS and RHS,

$$2x + y = 1$$

$$x + y = 2$$

$$3x + y = 3$$

For solving the equation (i) and (ii),

Subtracting equation (i) from equation (ii),

$$x + y = 2$$

$$2x + y = 1$$
  
 $(-)$   $(-)$   $(-)$ 

Willion Stars & Practice
Williams Stars & Practice

Million Stars Practice
Anillion Stars Practice

Put the value of x in equation (i)

$$x + y = 2$$

$$-1 + y = 2$$

$$y = 2 + 1$$

$$y = 3$$

Put the x and y in equation (iii),

$$3x + y = 3$$
  
 $3(-1) + 3 = 3$   
 $-3 + 3 = 3$   
 $0 = 3$   
LHS  $\neq$  RHS

The value of x and y do not satisfy the equation (iii). Hence, vectors are non-coplanar.

## Algebra of Vectors Ex 23.8 Q8

We know that,

Three vectors are coplanar if any one of them can be expressed as the linear combination of other two vectors.

Let  

$$\vec{a} = x\vec{b} + y\vec{c}$$

$$= x\left(2\hat{i} + \hat{j} + 3\hat{k}\right) + y\left(\hat{i} + \hat{j} + \hat{k}\right)$$

$$= 2\hat{i}x + \hat{j}x + 3\hat{k}x + \hat{i}y + \hat{j}y + \hat{k}y$$

$$\hat{i} + 2\hat{j} + 3\hat{k} = (2x + y)\hat{i} + (x + y)\hat{j} + (3x + y)\hat{k}$$

Comparing the coefficient of LHS and RHS,

$$2x + y = 1$$
 (i)  
 $x + y = 2$  (ii)  
 $3x + y = 3$  (iii)

For solving (i) and (ii), Subtracting (i) from (ii), x + y = 2

$$2 \times + y = 1$$

$$(-) \quad (-) \quad (-)$$

$$- \times = 1$$

$$\times = -1$$

Put the value of x in equation (i),

$$x + y = 2$$

$$-1 + y = 2$$

$$y = 2 + 1$$

$$y = 3$$

Put the values of x and y in equation (iii)

$$3x + y = 3$$
  
 $3(-1) + 3 = 3$   
 $-3 + 3 = 3$   
 $0 = 3$   
LHS  $\neq$  RHS

The values of x and y do not satisfy equation (iii). Hence,

 $\vec{a}, \vec{b}, \vec{c}$  are non coplanar.



Let.

$$\begin{split} \vec{d} &= x\vec{b} + y\hat{j} + z\hat{k} \\ &= x\left(\hat{i} + 2\hat{j} + 3\hat{k}\right) + y\left(2\hat{i} + \hat{j} + 3\hat{k}\right) + z\left(\hat{i} + \hat{j} + \hat{k}\right) \\ &= x\hat{i} + 2x\hat{j} + 3x\hat{k} + 2y\hat{i} + \hat{j}y + 3y\hat{k} + z\hat{i} + z\hat{j} + z\hat{k} \end{split}$$

$$2\hat{i}-\hat{j}-3\hat{k}=\left(x+2y+z\right)\hat{i}+\left(2x+y+z\right)\hat{j}+\left(3x+3y+z\right)\hat{k}$$

Comparing the coefficient of LHS and RHS,

$$x + 2y + z = 2$$

$$2x + y + z = -1$$

$$3x + 3y + z = -3$$
 (iii)

Subtracting equation (i) from (ii),

$$2x + y + z = -1$$

$$x + 2y + z = 2$$
  
 $(-)(-)$   $(-)$   $(-)$   $(-)$ 

(v)

Mondershare

Subtracting equation (ii) from (iii),

$$3x + 3y + z = -3$$

Subtracting (iv) from (v),

$$x + 2y = -2$$

$$(-)(+)$$
  $(+)$ 

$$y = \frac{1}{3}$$

Put y in equation (v),

$$x + 2y = -2$$

$$x + 2\left(\frac{1}{3}\right) = -2$$

$$2 + \frac{2}{3} = -2$$

$$x = \frac{-2}{1} - \frac{2}{3}$$
$$= \frac{-6 - 2}{3}$$

$$x = \frac{-8}{2}$$

Put value of x and y in equation (i),

$$x + 2y + z = 2$$

$$\frac{-8}{3} + 2\left(\frac{1}{3}\right) + z = 2$$

$$\frac{-8}{3} + \frac{2}{3} + z = 2$$

$$z = \frac{2}{1} + \frac{8}{3} - \frac{2}{3}$$
$$z = \frac{6 + 8 - 2}{3}$$

$$z = \frac{6+8-}{3}$$

$$Z=\frac{14-2}{3}$$

$$z = \frac{12}{3}$$

$$z = 4$$

So,

$$\vec{d} = x\vec{a} + y\vec{b} + z\vec{c}$$

$$\vec{d} = \left(\frac{-8}{3}\right)\vec{a} + \left(\frac{1}{3}\right)\vec{b} + (4)\vec{c}$$

Million Stars edulaciice Williams edulaciice

Necessary Condition: Let  $\vec{a}, \vec{b}, \vec{c}$  are three coplanar vectors. Then one of can be expressed as the linear combination of other two vectors.

Let, 
$$\vec{c} = x\vec{a} + y\vec{b}$$
  
 $x\vec{a} + y\vec{b} - \vec{c} = 0$ 

Put 
$$x = l$$
,  $y = m$ ,  $(-1) = n$ 

$$\vec{la} + \vec{mb} + \vec{nc} = 0$$

Thus, if  $\vec{a}, \vec{b}, \vec{c}$  are coplanar vectors, then there exist scalars l, m, n $I\vec{a} + m\vec{b} + n\vec{c} = 0$ 

Such that I,m,n are not all zero simultaneously.

Sufficient Condition: Let  $\vec{a}, \vec{b}, \vec{c}$  be three vectors such that there exist scalars l, m, n not all zero simultaneously satisfying  $l\vec{a} + m\vec{b} + n\vec{c} = 0$ 

$$|\vec{a} + m\vec{b} + n\vec{c}| = 0$$
$$|\vec{n} = -|\vec{a} - m\vec{b}|$$

Dividing by n, both the sides

$$\frac{\overrightarrow{nc}}{n} = \frac{-\overrightarrow{la}}{n} - \frac{\overrightarrow{mb}}{n}$$

$$\overrightarrow{c} = \left(-\frac{l}{n}\right)\overrightarrow{a} + \left(-\frac{m}{n}\right)\overrightarrow{b}$$

Mondershare  $\vec{c}$  is a linear combination of  $\vec{a}$  and  $\vec{b}$ 

Hence,  $\vec{a}, \vec{b}, \vec{c}$  are coplanar vectors.

## Algebra of Vectors Ex 23.8 Q10

Given that, A,B,C and D are four points with position vector  $\vec{a},\vec{b},\vec{c}$  and  $\vec{c}$  respectively.

Let A, B, C, D are coplanar.

If so, there exists x, y, z, u not all zero such that

$$\vec{xa} + y\vec{b} + z\vec{c} + u\vec{d} = 0$$

$$x + y + z + u = 0$$

Let, 
$$x = 3$$
,  $y = -2$ ,  $z = 1$ ,  $u = -2$ 

$$3\vec{a} - 2\vec{b} + \vec{c} - 2\vec{d} = 0$$

and, 
$$x + y + z + u = 3 + (-2) + 1 + (-2)$$

Thus, A,B,C,D are coplanar.

if 
$$3\vec{a} - 2\vec{b} + \vec{c} - 2\vec{d} = 0$$

Let 
$$3\vec{a} - 2\vec{b} + \vec{c} - 2\vec{d} = 0$$

$$3\vec{a} + \vec{c} = 2\vec{b} + 2\vec{d}$$

Divide by sum of the coefficients that is by 4 on both sides,

$$\frac{3\vec{a}+\vec{c}}{4}=\frac{2\vec{b}+2\vec{d}}{4}$$

$$\frac{3\vec{a} + \vec{c}}{3 + 1} = \frac{2\vec{b} + 2\vec{d}}{2 + 2}$$

It shows that P is the point which divides AC in ratio 1:3 internally as well as BD in ratio 2:2 internally.

Thus, P is the point of intersection of AC and BD.

Hence,

A, B, C, D are coplanar.

We can say that,

A,B,C,D are coplanar if and only if Let  $3\vec{a}-2\vec{b}+\vec{c}-2\vec{d}=\vec{0}$ 

# Ex 23.9

## Algebra of Vectors Ex 23.9 Q1

We know that, If l,m,n are the direction cosine of a vector and  $\alpha,\beta,\gamma$  can the

$$l = \cos \alpha$$
,  $m = \cos \beta$   $n = \cos \gamma$ 

and, 
$$l^2 + m^2 + n^2 = 1$$
 (i)  

$$\therefore l = \cos 45^\circ, m = \cos 60^\circ, n = \cos 120^\circ$$

$$l = \frac{1}{\sqrt{D}}, m = \frac{1}{2}, n = -\frac{1}{2}$$

Put 
$$l, m, n$$
 in equation (i)

$$I^{2} + m^{2} + n^{2} = 1$$

$$\left(\frac{1}{\sqrt{2}}\right)^{2} + \left(\frac{1}{2}\right)^{2} + \left(\frac{-1}{2}\right)^{2} = 1$$

$$\frac{1}{2} + \frac{1}{4} + \frac{1}{4} = 1$$

$$\frac{2+1+1}{4} = 1$$

$$\frac{4}{4} = 1$$

$$1 = 1$$
LHS = RHS

Therefore, a vector can have direction angle 45°, 60°, 120°.

## Algebra of Vectors Ex 23.9 Q2

Here, 
$$l = 1, m = 1, n = 1$$

Put it in

$$l^{2} + m^{2} + n^{2} = 1$$
 $(1)^{2} + (1)^{2} + (1)^{2} = 1$ 
 $1 + 1 + 1 = 1$ 
 $3 = 1$ 
LHS  $\neq$  RHS

Therefore,

1,1,1 can not be direction cosines of a straight line.

# Mondershare Algebra of Vectors Ex 23.9 Q3

Here, 
$$\alpha = \frac{\pi}{4}$$
,  $\beta = \frac{\pi}{4}$ ,  $\gamma = ?$ 

$$I = \cos \alpha = \cos \frac{\pi}{4}$$

$$I = \frac{1}{\sqrt{2}}$$

$$m = \cos \beta = \cos \frac{\pi}{4}$$

$$m = \frac{1}{\sqrt{2}}$$

$$n = \cos y$$

Put value of l, m, and n in

$$n = \cos y$$
  
ue of  $l, m,$  and  $n$  in  $l^2 + m^2 + n^2 = 1$   
 $\left(\frac{1}{\sqrt{2}}\right)^2 + \left(\frac{1}{\sqrt{2}}\right)^2 + \cos^2 y = 1$   
 $\frac{1}{2} + \frac{1}{2} + \cos^2 y = 1$   
 $1 + \cos^2 y = 1$   
 $\cos^2 y = 0$   
 $\cos y = 0$ 

$$\frac{1}{2} + \frac{1}{2} + \cos^2 r = 1$$

$$1 + \cos^2 y = 1$$

$$\cos^2 y = 1 - 1$$

$$\cos^2 y = 0$$

## ra of Vectors Ex 23.9 Q4

$$\alpha = \beta = \gamma$$
 $\cos \alpha = \cos \beta = \cos \gamma$ 

$$\Rightarrow$$
  $I = m = n = x \text{ (say)}$ 

We know that,  $I^{2} + m^{2} + n^{2} = 1$   $X^{2} + X^{2} + X^{2} = 1$   $3X^{2} = 1$   $X^{2} = \frac{1}{3}$   $X = \pm \frac{1}{\sqrt{3}}$ 

$$I = \pm \frac{1}{\sqrt{3}}, \ m = \pm \frac{1}{\sqrt{3}}, \ n = \pm \frac{1}{\sqrt{3}}$$

Hence, direction cosiner of  $\vec{r}$  are,

$$\pm \frac{1}{\sqrt{3}}$$
,  $\pm \frac{1}{\sqrt{3}}$ ,  $\pm \frac{1}{\sqrt{3}}$ 

$$\begin{aligned} \text{Vector } \vec{r} &= \left| \vec{r} \right| \left( l \hat{i} + m \hat{j} + n \hat{k} \right) \\ &= 6 \left( \pm \frac{1}{\sqrt{3}} \hat{i} + \pm \frac{1}{\sqrt{3}} \hat{j} + \pm \frac{1}{\sqrt{3}} \hat{k} \right) \\ &= \frac{\pm 6 \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}} \left( \hat{i} + \hat{j} + \hat{k} \right) \end{aligned}$$

[Rationalizing the denominator]

$$=\frac{\pm 6\sqrt{3}}{3}\left(\hat{i}+\hat{j}+\hat{k}\right)$$

$$\vec{r} = \pm 2\sqrt{3} \left( \hat{i} + \hat{j} + \hat{k} \right)$$

## Algebra of Vectors Ex 23.9 Q5

Here, 
$$\alpha = 45^{\circ}$$
,  $\beta = 60^{\circ}$ ,  $\gamma = \theta$  (say)

$$I = \frac{1}{\sqrt{2}}$$

$$m = \cos \beta$$
$$= \cos 60^{\circ}$$
$$m = \frac{1}{2}$$

$$n = \cos\theta$$

Put I, m, and n in

$$l^2 + m^2 + n^2 = 1$$

$$\left(\frac{1}{\sqrt{2}}\right)^2 + \left(\frac{1}{2}\right)^2 + \cos^2 \theta = 1$$

$$\frac{2+1}{4} + \cos^2 \theta = 1$$

$$\frac{3}{4} + \cos^2 \theta = 1$$

$$\cos^2 \theta = \frac{1}{1} - \frac{4}{4}$$

$$\cos^2 \theta = \frac{1}{4}$$

So, 
$$l = \frac{1}{2}$$
,  $m = \frac{1}{2}$ ,  $n = \pm \frac{1}{2}$ 

The required,

vector 
$$\hat{r} = |\vec{r}|(l\hat{i} + m\hat{j} + n\hat{k})$$

$$= 8\left(\frac{1}{\sqrt{2}}\hat{i} + \frac{1}{2}\hat{j} \pm \frac{1}{2}\hat{k}\right)$$
$$= 8\frac{\sqrt{2}\hat{i} + \hat{j} \pm \hat{k}}{2}$$

$$\vec{r} = 4\left(\sqrt{2}\hat{i} + \hat{j} \pm \hat{k}\right)$$

Here, the direction ratios of the vector

$$2\hat{i} + 2\hat{j} - \hat{k} = 2, 2, -1$$

The direction cosines of the vector

$$= \frac{2}{|\vec{r}|}, \frac{2}{|\vec{r}|}, \frac{-1}{|\vec{r}|}$$

$$= \frac{2}{\sqrt{(2)^2 + (2)^2 + (-1)^2}}, \frac{2}{\sqrt{(2)^2 + (2)^2 + (-1)^2}}, \frac{-1}{\sqrt{(2)^2 + (2)^2 + (-1)^2}}$$

$$= \frac{2}{\sqrt{4 + 4 + 1}}, \frac{2}{\sqrt{4 + 4 + 1}}, \frac{-1}{\sqrt{4 + 4 + 1}}$$

$$= \frac{2}{\sqrt{9}}, \frac{2}{\sqrt{9}}, \frac{-1}{\sqrt{9}}$$

$$= \frac{2}{3}, \frac{2}{3}, \frac{-1}{3}$$

Here, let 
$$\vec{r} = 6\hat{i} - 2\hat{j} - 3\hat{k}$$
  
and,  $|\vec{r}| = \sqrt{(6)^2 + (-2)^2 + (-3)^2}$   
 $= \sqrt{36 + 4 + 9}$   
 $= \sqrt{49}$   
 $|\vec{r}| = 7$ 

$$= \frac{6}{|\vec{r}|}, \frac{-2}{|\vec{r}|}, \frac{-3}{|\vec{r}|}$$

$$= \frac{6}{7}, \frac{-2}{7}, \frac{-3}{7}$$

Let, 
$$\vec{r} = \hat{i} - \hat{j} + \hat{k}$$

The direction cosines of 
$$\vec{r}$$
 are given by 
$$= \frac{6}{|\vec{r}|}, \frac{-2}{|\vec{r}|}, \frac{-3}{|\vec{r}|}$$

$$= \frac{6}{7}, \frac{-2}{7}, \frac{-3}{7}$$
Algebra of Vectors Ex 23.9 Q7(i)
Let,  $\vec{r} = \hat{i} - \hat{j} + \hat{k}$ 
The direction ratios of the vector  $\vec{r} = 1, -1, 1$ 
And,  $|\vec{r}| = \sqrt{(1)^2 + (-1)^2 + (1)^2}$ 

$$= \sqrt{1 + 1 + 1}$$

$$= \sqrt{3}$$
The direction cosines of the vector  $\vec{r} = \frac{1}{|\vec{r}|}, \frac{-1}{|\vec{r}|}, \frac{1}{|\vec{r}|}$ 

$$= \frac{1}{|\vec{r}|}, \frac{-1}{|\vec{r}|}, \frac{1}{|\vec{r}|}$$

$$= \frac{1}{\sqrt{3}}, \frac{-1}{\sqrt{3}}, \frac{1}{\sqrt{3}}$$

So, 
$$I = \cos \alpha = \frac{1}{\sqrt{3}}$$
  
 $\alpha = \cos^{-1} \left(\frac{1}{\sqrt{3}}\right)$ 

$$m = \cos \beta = \frac{-1}{\sqrt{3}}$$
$$\beta = \cos^{-1} \left( \frac{-1}{\sqrt{3}} \right)$$

$$n = \cos \gamma = \frac{1}{\sqrt{3}}$$
$$\gamma = \cos^{-1}\left(\frac{1}{\sqrt{3}}\right)$$

Thus, angles made by  $\vec{r}$  with the coordinate axes are given by  $\cos^{-1}\left(\frac{1}{\sqrt{3}}\right)$ ,  $\cos^{-1}\left(-\frac{1}{\sqrt{3}}\right)$ ,  $\cos^{-1}\left(\frac{1}{\sqrt{3}}\right)$ 

Million Stars Practice
Annihit Rearns Practice

The direction ratios of  $\vec{r} = 0, 1, -1$ 

and, 
$$|\vec{r}| = \sqrt{(0)^2 + (1)^2 + (-1)^2}$$
  
=  $\sqrt{0 + 1 + 1}$   
 $|\vec{r}| = \sqrt{2}$ 

The direction cosines of the  $\vec{r}$  are given by

$$= \frac{0}{\left| \overrightarrow{r} \right|}, \quad \frac{1}{\left| \overrightarrow{r} \right|}, \quad \frac{-1}{\left| \overrightarrow{r} \right|}$$
$$= \frac{0}{\sqrt{2}}, \quad \frac{1}{\sqrt{2}}, \quad \frac{-1}{\sqrt{2}}$$

So, 
$$l = \cos \alpha = 0$$
  
 $\alpha = \cos^{-1}(0)$   
 $\alpha = \frac{\pi}{2}$ 

$$m = \cos \beta = \frac{1}{\sqrt{2}}$$
$$\beta = \cos^{-1} \left(\frac{1}{\sqrt{2}}\right)$$

$$\beta = \frac{\pi}{4}$$

$$n = \cos \gamma = -\frac{1}{\sqrt{2}}$$
$$\gamma = \cos^{-1}\left(-\frac{1}{\sqrt{2}}\right)$$

$$\lambda = \pi - \frac{\pi}{7}$$

$$\gamma = \frac{3\pi}{4}$$

So, angles made by the vector  $\vec{r}$  with coordinate axes are given by

$$\frac{\pi}{2}$$
,  $\frac{\pi}{4}$ ,  $\frac{3\pi}{4}$ 

## Algebra of Vectors Ex 23.9 Q7(iii)

Let, 
$$4\hat{i} + 8\hat{j} + \hat{k} = \vec{r}$$

The direction ratios of  $\vec{r}$  = 4, 8, 1

And, 
$$|\vec{r}| = \sqrt{(4)^2 + (8)^2 + (1)^2}$$
  
=  $\sqrt{16 + 64 + 1}$   
=  $\sqrt{81}$   
 $|\vec{r}| = 9$ 

The direction cosines of the  $\vec{r}$  are given by

$$= \frac{4}{|\vec{r}|}, \frac{8}{|\vec{r}|}, \frac{1}{|\vec{r}|}$$

$$= \frac{4}{9}, \frac{8}{9}, \frac{1}{9}$$

Now, 
$$I = \cos \alpha = \frac{4}{9}$$
  
 $\alpha = \cos^{-1}\left(\frac{4}{9}\right)$ 

$$m = \cos \beta = \frac{8}{9}$$

$$n = \cos \gamma = \frac{1}{9}$$

$$\gamma = \cos^{-1} \left( \frac{1}{4} \right)^{\frac{1}{2}}$$

 $n = \cos y = \frac{1}{9}$   $y = \cos^{-1}\left(\frac{1}{9}\right)$ The smade by the verification  $y = \cos^{-1}\left(\frac{4}{9}\right)$ . The smade by the verification  $y = \cos^{-1}\left(\frac{4}{9}\right)$ . The angles made by the vector  $\vec{r}$  with the coordinate axes are given by

$$\cos^{-1}\left(\frac{4}{9}\right), \cos^{-1}\left(\frac{8}{9}\right), \cos^{-1}\left(\frac{1}{9}\right)$$

## Algebra of Vectors Ex 23.9 Q8

Let  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ .

$$|\vec{a}| = \sqrt{1^2 + 1^2 + 1^2} = \sqrt{3}$$

Therefore, the direction cosines of  $\vec{a}$  are  $\left(\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}\right)$ .

Now, let  $\alpha$ ,  $\beta$ , and the angles formed by  $\vec{a}$  with the positive directions of x, y, and

Then, we have 
$$\cos \alpha = \frac{1}{\sqrt{3}}, \cos \beta = \frac{1}{\sqrt{3}}, \cos \gamma = \frac{1}{\sqrt{3}}$$
.

Hence, the given vector is equally inclined to axes OX, OY, and OZ.

## Algebra of Vectors Ex 23.9 Q9

Let a vector be equally inclined to axes OX, OY, and OZ at angle  $\alpha$ .

Then, the direction cosines of the vector are  $\cos \alpha$ ,  $\cos \alpha$ , and  $\cos \alpha$ .

Now,

$$\cos^2 \alpha + \cos^2 \alpha + \cos^2 \alpha = 1$$

$$\Rightarrow 3\cos^2 \alpha = 1$$

$$\Rightarrow \cos \alpha = \frac{1}{\sqrt{3}}$$

Hence, the direction cosines of the vector which are equally inclined to the axes

are 
$$\frac{1}{\sqrt{3}}$$
,  $\frac{1}{\sqrt{3}}$ ,  $\frac{1}{\sqrt{3}}$ 

## Algebra of Vectors Ex 23.9 Q10

Let unit vector  $\overset{
ightarrow}{a}$  have  $(a_1, a_2, a_3)$  components.

$$\Rightarrow \vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$$

Since  $\vec{a}$  is a unit vector,  $|\vec{a}| = 1$ .

Also, it is given that  $\vec{a}$  makes angles  $\frac{\pi}{3}$  with  $\hat{j}$ ,  $\frac{\pi}{4}$  with  $\hat{j}$ , and an acute angle  $\theta$  with  $\hat{k}$ .

Then, we have:

$$\cos\frac{\pi}{3} = \frac{a_1}{|\vec{a}|}$$

$$\Rightarrow \frac{1}{2} = a_1$$

$$[|\vec{a}|=1]$$

$$\cos\frac{\pi}{4} = \frac{a_2}{|\vec{a}|}$$

$$\Rightarrow \frac{1}{\sqrt{2}} = a_2$$
  $\left[ \left| \vec{a} \right| = 1 \right]$ 

$$[|\vec{a}| = 1$$

Also, 
$$\cos \theta = \frac{a_3}{|\vec{a}|}$$
.

$$\Rightarrow a_3 = \cos \theta$$

Now,

$$|a| = 1$$

$$\Rightarrow \sqrt{a_1^2 + a_2^2 + a_3^2} = 1$$

Willion Stars Practice
Williams Practice



$$\Rightarrow \left(\frac{1}{2}\right)^2 + \left(\frac{1}{\sqrt{2}}\right)^2 + \cos^2 \theta = 1$$

$$\Rightarrow \frac{1}{4} + \frac{1}{2} + \cos^2 \theta = 1$$

$$\Rightarrow \frac{3}{4} + \cos^2 \theta = 1$$

$$\Rightarrow \cos^2 \theta = 1 - \frac{3}{4} = \frac{1}{4}$$

$$\Rightarrow \cos \theta = \frac{1}{2} \Rightarrow \theta = \frac{\pi}{3}$$

$$\therefore a_3 = \cos \frac{\pi}{3} = \frac{1}{2}$$

Hence,  $\theta = \frac{\pi}{3}$  and the components of  $\vec{a}$  are  $\left(\frac{1}{2}, \frac{1}{\sqrt{2}}, \frac{1}{2}\right)$ .

## The Plane Ex 23.9 Q11

Let I, m, n be the direction cosines of the vector  $\vec{r}$ .

$$I = \cos \alpha$$
,  $m = \cos \left(\frac{\pi}{4}\right) = \frac{1}{\sqrt{2}}$  and  $n = \cos \left(\frac{\pi}{2}\right) = 0$ 

$$l^2 + m^2 + n^2 = 1$$

$$|^2 + \frac{1}{2} + 0 = 1$$

$$I = \pm \frac{1}{\sqrt{2}}$$

$$\vec{r} = |\vec{r}|(\hat{l}\hat{i} + m\hat{j} + n\hat{k})$$

$$\vec{r} = 3\sqrt{2} \left( \pm \frac{1}{\sqrt{2}} \hat{i} + \frac{1}{\sqrt{2}} \hat{j} + 0 \right)$$

$$\vec{r} = \pm 3\hat{i} + 3\hat{j}$$

## The Plane Ex 23.9 Q12

Let I, m, n be the direction cosines of the vector  $\vec{r}$ .

Vector  $\vec{r}$  is indined at equal angles to the three axes.

$$I = \cos \alpha$$
,  $m = \cos \alpha$  and  $n = \cos \alpha$ 

$$\Rightarrow$$
 I = m = n

$$l^2 + m^2 + n^2 = 1$$

$$\Rightarrow$$
I = m = n =  $\pm \frac{1}{\sqrt{3}}$ 

$$\vec{r} = |\vec{r}|(\hat{l}\hat{i} + \hat{m}\hat{j} + \hat{n}\hat{k})$$

$$\vec{r} = 2\sqrt{3} \left( \pm \frac{1}{\sqrt{3}} \hat{\mathbf{i}} \pm \frac{1}{\sqrt{3}} \hat{\mathbf{j}} \pm \frac{1}{\sqrt{3}} \hat{\mathbf{k}} \right)$$

$$\vec{r} = \pm 2\hat{i} \pm 2\hat{i} \pm 2\hat{k}$$