

Ex - 30.1

Linear Programming Ex 30.1 Q1

The given data may be put in the following tabular form: -

Gadget	Foundry	Machine-shop	Profit
А	10	5	Rs 30
В	6	4	Rs 20
Firm's capacity per week	1000	600	

Let required weekly production of gadgets A and B be X and y respectively.

Given that, profit on each gadget A is Rs 30 So, profit on x gadget of type A = 30xProfit on each gadget of type B = Rs 20 So, profit on y gadget of type B = 20y

Let Z denote the total profit, so Z = 30x + 20y

Given, production of one gadget A requires 10 hours per week for foundry and gadget B requires 6 hours per week for foundry.

So, x units of gadget A requires 10x hours per week and y units of gadget B requires by hours per week, But the maximum capacity of foundry per week is 1000 hours, so

 $10x + 6y \le 1000$

This is first constraint.

Given, production of one unit gadget A requires 5 hours per week of machine shop and production of one unit of gadget B requires 4 hours per week of machine shop.

So, x units of gadget A requires 5x hours per week and y units of gadget B requires 4y hours per week, but the maximum capacity of machine shop is 600 hours per week

So, $5x + 4y \le 600$

This is second constraint. Hence, mathematical formulation of LPP is: Find x and y which Maximize Z = 30x + 2y

Subject to constraints, $10x + 6y \le 1000$ $5x + 4y \le 600$

And, $x, y \ge 0$

[Since production cannot be less than zero]



Programming Ex 30.1 Q2

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ven information can be written in tabular form as below:

roduct	Machine hours	Labour hours	Profit
А	1	1	Rs 60
В	-	1	Rs 80
Total capacity	400 for <i>A</i>	500	
Minimum supply of	product B is 200 units.		

Let production of product A be x units and production of product B be y units.

Given, profit on one unit of product A = Rs 60So, profit on x unit of product A = Rs 60xGiven, profit on one unit of product B = Rs 80So, profit on y units of product B = Rs 80y

Let Z denote the total profit, so Z = 60x + 80y

Given, minimum supply of product B is 200 So, $y \ge 200$ (First constraint)

Given that, production of one unit of product A requires 1 hour of machine hours, so x units of product A requires x hours but given total machine hours available for product A is 400 hours, so

 $x \le 400$ (Second constraint)

Given, each unit of product A and B requires one hour of labour hour, so x units of product A require x hours and y units of product B require y hours of labour hours but total labour hours available are 500, so

 $x + y \le 500$ (Third constraint)

Hence, mathematical formulation of LPP is, Find x and y which Minimize Z = 60x + 80y

Subject to constraints,

y ≥ 200

 $x \le 400$

 $x + y \le 500$

 $x,y \ge 0$ [Since production of product cannot be less than zero]

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MILLIONST Programming Ex 30.1 Q3

Product	Machine (M ₁)	Machine (M2)	Profit
А	4	2	3
В	3	2	2
С	5	4	4
Capacity maximum	2000	2500	

Let required production of product A, B and C be x, y and z units respectively.

Given, profit on one unit of product A, B and C are Rs 3, Rs 2, Rs 4, so Profit on x unit of A, y unit of B and z unit of C are given by Rs. A, Rs A, Rs

Let ${\cal U}$ be the total profit, so

$$U = 3x + 2y + 4z$$

Given, one unit of product A, B and C requires 4,3 and 5 minutes on machine M_1 . So, x units of product A, y units of B and z units of product C need Ax, Ax and Ax minutes on machine Ax is 2000 minutes, so

$$4x + 3y + 5z \le 200$$
 (First constraint)

Given, one unit of product A, B and C requires 2,2 and 4 minutes on machine M_2 . So, x units of A, y units of B and z units of C require 2x, 2y and 4z minutes on machine M_2 is 2500 minutes, so

$$2x + 2y + 4z \le 2500$$
 (Second constraint)

Also, given that firm must manufacture 100 A's, 200 B's and 50 C's but not more than 150 A's.

 $100 \le x \le 150$

y ≥ 200 (Other constraints)

z≥50

Hence, mathematical formulation of LPP is :-

Find x,y and z which

$$maximize U = 3x + 2y + 4z$$

Subject to constraints,

 $4x + 3y + 5z \le 2000$

 $2x + 2y + 4z \le 2500$

 $100 \le x \le 150$

 $y \ge 200$

 $z \ge 50$

And, $x,y,z \ge 0$ [Since, x,

[Since, x,y,z are non-negative]

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Given information can be written in tabular form as below:

Product	M_1	M ₂	Profit
А	1	2	2
В	1	1	3
Capacity	6 hours 40 min	10 hours	
	= 400 min.	= 600 min.	

Let required production of product A be x units and product B be y units.

Given, profit on one unit of product A and B are Rs 2 and Rs 3 respectively, so profits on X units of product A and Y units of product Y will be Rs Y and Rs Y respectively.

Let total profit be Z, so Z = 2x + 3y

Given, production of one unit of product A and B require 1 and 1 minute on machine M_1 respectively, so production of X units of product A and B units of product B require B minutes and B minutes on machine B but total time available on machine B is 600 minutes, so

 $x + y \le 400$ (First constraint)

Given, production of one unit of product A and B require 2 minutes and 1 minutes on machine M_2 respectively. So production of x units of product A and y units of product B require 2x minutes and y minutes respectively on machine M_2 but machine M_2 is available for 600 minutes, so

 $2x + y \le 600$ (Second constraint)

Hence, mathematical formulation of LPP is:-Find x and y which

maximize Z = 2x + 3y

Subject to constraints,

 $x + y \le 400$

 $2x + y \le 600$

and, $x, y \ge 0$ [Since production of product can not be less than zero]

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Plant	Α	В	С	Cost
I	50	100	100	2500
II	60	60	200	3500
Monthly demand	2500	3000	7000	

Let plant I requires x days and plant II requires y days per month to minimize cost.

Given, plant I and II costs Rs 2500 perday and Rs 3500 perday respectively, so cost to run plant I and II is Rs 2500x and Rs 3500y per month.

Let Z be the total cost per month, so Z = 2500x + 3500y

Given, production of tyre A from plant I and II is 50 and 60 respectively, so production of tyre A from plant I and II will be 50x and 60y respectively per month but the maximum demand of tyre A is 2500 per month so,

 $50x + 60y \ge 2500$ [First constraint]

Given, production of tyre B from plant I and II is 100 and 60 respectively, so production of tyre B from plant I and II will be 100x and 60y per month respectively but the maximum demand of tyre B is 3000 per month, so

100x +60y ≥ 3000 [Second constraint]

Given, production of tyre $\mathcal C$ from plant I and II is 100 and 200 respectively. So production of tyre $\mathcal B$ from plant I and II will be 100x and 200y per month respectively but the maximum demand of tyre $\mathcal C$ is 7000 per day, so

 $100x + 200y \ge 7000$ [Third constraint]

Hence, mathematical formulation of LPP is.. Find x and y which

Minimize Z = 2500x + 3500y

Subject to constraint,

 $50x + 60y \ge 2500$ $100x + 60y \ge 3000$

100x +200y ≥ 7000

And, $x,y \ge 0$ [Since number of days can not be less than zero]

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Product	Man hours	Maximum demand	Profit
Α	5	7000	60
В	3	10000	40
Total capacity	45000		

Let required production of product A be x units and production of product B be y units.

Given, profits on one unit of product A and B are Rs 60 and Rs 40 respectively, so profits on X units of product A and Y units of product B are Rs 60X and Rs 40Y.

Let ${\cal Z}$ be the total profit, so

Z = 60x + 40y

Given, production of one unit of product A and B require 5 hours and 3 hours respectively man hours, so X unit of product A and Y units of product B require X hours and X hours of man hours respectively but total man hours available are 45000 hours, so

 $5x + 3y \le 45000$ (First constraint)

Given, demand for product A is maximum 7000, so

 $x \le 7000$ (Second constraint)

Hence, mathematical formulation of LPP is,

Find x and y which

maximize Z = 60x + 40y

Subject to constraints,

 $5x + 3y \le 45000$

 $x \le 7000$

 $y \le 10000$

 $x,y \ge 0$ [Since production can not be less than zero]

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MILLIONST r Programming Ex 30.1 Q7

and y be the packets of 25 gm of Food I and Food II purchased. Let Z be the price paid. Obviously price has to be minimized.

Take a mass balance on the nutrients from Food I and II,

Calcium $10x + 4y \ge 20$

 $5x + 2y \ge 10$ (i)

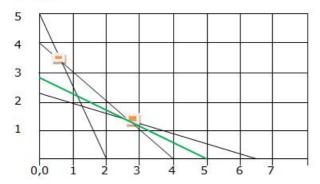
Protein $5x + 5y \ge 20$

 $x + y \ge 4$ (ii)

Calories $2x + 6y \ge 13$ (iii)

These become the constraints for the cost function, Z to be minimized i.e., 0.6x + y = Z, given cost of Food I is Rs 0.6/- and Rs 1/- per lb

From (i), (ii) & (iii) we get points on the X & Y-axis as [0, 5] & [2, 0]; [0, 4] & [4, 0]; [0, 13/6] & [6.5, 0] Plotting these



The smallest value of Z is 2.9 at the point (2.75, 1.25). We cannot say that the minimum value of Z is 2.9 as the feasible region is unbounded.

Therefore, we have to draw the graph of the inequality 0.6x + y < 2.9

Plotting this to see if the resulting line (in green) has any point common with the feasible region. Since there are no common points this is the minimum value of the function Z and the mix is

Food I = 2.75 lb; Food II = 1.25 lb; Price = Rs 2.9

When Z has an optimal value (maximum or minimum), where the variables x and y are subject to constraints described by linear inequalities, this optimal value must occur at a corner point (vertex) of the feasible region.

Here the feasible region is the unbounded region $\mbox{\sc A-B-C-D}$

Computing the value of ${\sf Z}$ at the corner points of the feasible region ABHG

Point	Corner point	Value of $Z = 0.6x + y$
Α	2, 5	6.2
В	0.67, 3.33	3.73
C	2.75, 1.25	2.9
D	6.5, 2.16	6.06

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r Programming Ex 30.1 Q8

information can be tabulated as:-

Product	Grinding	Turning	Assembling	Testing	Profit
Α	1	З	6	5	2
В	2	1	3	4	3
Maxim um	30 hours	60 hours	200 hours	200 hours	
capacity					

Let required production of product A and B be x and y respectively

Given, profits on one unit of product A and B are Rs 2 and Rs 3 respectively, so profits on x units of product A and y units of product B are given by 2x and 3y respectively. Let Z be total profit, so

$$Z = 2x + 3y$$

Given, production of 1 unit of product A and B require 1 hour and 2 hours of grinding respectively, so, production of X units of product A and Y units of of product B require X hours and 2Y hours of grinding respectively but maximum time available for grinding is 3 hours, so

$$x + 2y \le 30$$
 (First constraint)

Given, production of 1 unit of product A and B require 3 hours and 1 hours of turning respectively, so X units of product A and Y units of product B require A hours and Y hours of turning respectively but total time available for turning is 60 hours, so

$$3x + y \le 60$$
 (Second constraint)

Given, production of 1 unit of product A and B require 6 hour and 3 hours of assembling respectively, so productinon of x units of product A and y units of product B require A0 hours and A1 hours of assembling respectively but total time available for assembling is 200 hours, so

$$6x + 3y \le 200$$
 (Third constraint)

Given, production of 1 unit of product A and B require 5 hours and 4 hours of testing respectively, so production of x units of product A and y units of product B require Sx hours and Ay hours of testing respectively but total time available for testing is 200 hours, so

$$5x + 4y \le 200$$
 (Fourth constraint)

Hence, mathematical formulation of LPP is,

Find x and y which

maximize Z = 2x + 3y

Subject to constraints,

 $x + 2y \le 30$

 $3x + y \le 60$

 $6x+3y\leq 200$

 $5x + 4y \le 200$

and, $x,y \ge 0$

[Since production can not be negative]

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≥ 300

Z



30x

1.x lakh

T class

Cost

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	Model 314		Model 535	Limit
Variable	X		у	
F class	20x	+	20y	≥ 160

60y

+ 1.5y lakh

The above LPP can be presented in a table above.

The flight cost is to be minimized i.e., Min Z = x + 1.5y s.t. the constraints

x ≥ 2 at least 2 planes of model 314 must

be used

y ≥ 0 at least 1 plane of model 535 must be

used

 $20x + 20y \ge 160$ require at least 160 F class seats $30x + 60y \ge 300$ require at least 300 T class seats

Solving the above inequalities as equations we get, When x=0, y=8 and when y=0, x=8 When x=0, y=5 and when y=0, x=10

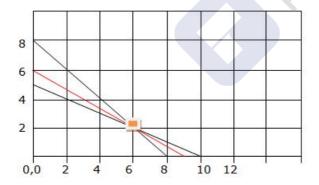
We get an unbounded region 8-E-10 as a feasible solution. Plotting the corner points and evaluating we have,

Corner point	Value of $Z = x + 1.5y$
10, 0	10
0,8	12
6, 2	9

Since we obtained an unbounded region as the feasible solution a plot of Z (x+1.5 < 9) is plotted.

Since there are no common points point E is the point that gives a minimum value.

Using 6 planes of model 314 & 2 of model 535 gives minimum cost of 9 lakh rupees.



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Programming Ex 30.1 Q13

MILLIONST nformation can be tabulated as below



Je 5	Time requirement	Points				
I	3	5				
II	2					
III	4	6				
Time for all th	Time for all three sets = $3\frac{1}{2}$ hours					
Time for Set I and Set II = $2\frac{1}{2}$ hours						
Number of qu	estions maximum 100					

Let he should x, y, z questions from set I, II and III respectively.

Given, each question from set I, II, III earn 5,4,6 points respectively, so x questions of set I, y questions of set II and z questions of set III earn 5x, 4y and 6z points, let total point credit be U

So,
$$U = 5x + 4y + 6z$$

Given, each question of set I, II and III require 3,2 and 4 minutes respectively, so x questions of set I, y questions of set II and z questions of set III require 3x, 2yand 4z mimutes respectively but given that total time to devote in all three sets is

$$3\frac{1}{2}$$
 hours = 210 minutes and first two sets is $2\frac{1}{2}$ hours = 150 minutes So,

$$3x + 2y + 4z \le 210$$
 (First constraint)
 $3x + 2y \le 150$ (Second constraint)

Given, total number of questions cannot exceed 100 So, $x + y + z \le 100$ (Third constraint)

Hence, mathematical formulation of LPP is Find x and y which maximize U = 5x + 4y + 6z

Subject to constraint,

$$3x + 2y + 4z \le 210$$

 $3x + 2y \le 150$

$$3x + 2y \le 150$$

$$x+y+z \le 100$$

$$x, y, z \ge 0$$

Since number of questions to solve from each set cannot be less than zero

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Programming Ex 30.1 Q14

information can be tabulated as below

Product	Yield	Cultivation	Priœ	Fertilizers
Tom atoes	2000 kg	5 days	1	100 kg
Lettuce	3000 kg	6 days	0.75	100 kg
Radishes	1000 kg	5 days	2	50 kg

Average 2000 kg/per acre

Total land = 100 Acre

Cost g fertilizers = Rs 0.50 per kg.

A total of 400 days of cultivation labour with Rs 20 per day

Let required quantity of field for tomatoes, lettuce and radishes be x,y and z Acre respectively.

Given, costs of cultivation and harveshing of tomatoes, lettuce and radishes are 5×20 = Rs 100, 6×20 = Rs 120, 5×20 = Rs 100 respectively per acre. Cost of fertilizers for tomatoes, lettuce and radishes 100×0.50 = Rs 50, 100×0.50 = Rs 50 and 50×0.50 = Rs 25 respectively per acre.

So, total costs of production of tomatoes, lettuce and radishes are Rs $100 + 50 = Rs \ 150x$, Rs $120 + 50 = Rs \ 170y$ and radishes are Rs $100 + 25 = Rs \ 125z$ respectively total selling price of tomatoes, lettuce and radishes, according to yield are $2000 \times 1 = Rs \ 2000x$, $3000 \times 0.75 = Rs \ 2250y$ and $100 \times 2 = Rs \ 2000z$ respectively.

Let U be the total profit,

So,

$$U = (2000x - 150x) + (2250y - 170y) + (2000z - 125z)$$

$$U = 1850x + 2080y + 1875z$$

Given, farmer has 100 acre form

So, $x + y + z \le 100$ (First constraint)

Number of cultivation and harvesting days are 400

So, $5x + 6y + 5z \le 400$

Hence, mathematical formulation of LPP is Find x,y,z which maximize U = 1850x + 2080y + 1875z

Subject to constraint,

 $x+y+z \leq 100$

 $5x + 6y + 5z \le 400$

 $x, y, z \ge 0$

[Since from used for cultivation cannot be less than zero.]

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ar Programming Ex 30.1 Q15

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MILLIONST 2 en information can be tabulated as below:

Product	Department 1	Department 2	Selling price	Labour	Raw material
Product	Department 1	artment 1 Department 2 Sening price		cost	cost
А	3	4	25	16	4
В	2	6	30	20	4
Capacity					
, ,	130	260			

Let the required product of product A and B be x and y units respectively.

Given, labour cost and raw material cost of one unit of product A is Rs 16 and Rs 4, so total cost of product A is Rs 16 + Rs 4 = Rs 20 And given selling price of 1 unit of product A is Rs 25, So, profit on one unit of product

A = 25 - 20 = Rs 5

Again, given labour cost and raw material cost of one unit of product B is Rs 20 and Rs 4 So, that cost of product B is Rs 20 +Rs 4 = Rs 24 And given selling price of 1 unit of product B is Rs 30 So, profit on one unit of product B = 30 - 24 = Rs 6

Hence, profits on x unit of product A and y units of product B are Rs 5x and Rs 6y respectively.

Let Z be the total profit, so Z = 5x + 6y

Given, production of one unit of product A and B need to process for 3 and 4 hours respectively in department 1, so production of x units of product A and Y units of product B need to process for A and A hours respectively in Department 1. But total capacity of Department 1 is 130 hour ,

So, $3x + 2y \le 130$ (First constraint)

Given, production of one unit of product A and B need to process for 4 and 6 hours respectively in department 2, so production of x units of product A and A units of product A need to process for A and A hours respectively in Department 2 but total capacity of Department 2 is 260 hours

So, $4x + 6y \le 260$ (Second constraint)

Hence, mathematical formulation of LPP is, Find x and y which Maximize Z = 5x + 6y

Subject to constraint,

 $3x + 2y \le 130$

 $4x + 6y \le 260$

 $x, y \ge 0$ [Since production cannot be less than zero]

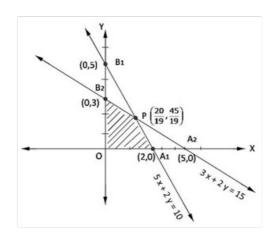
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Linear Programming Ex 30.2 Q1

Converting the given inequations into equations, we get 3x + 5y = 15, 5x + 2y = 10, x = 0, y = 0



Region represented by $5x + 2y \le 10$: The line meets coordinate axes at A_1 (2,0) and B_1 (0,5) respectively. Join these points to obtain the line 5x + 2y = 10, clearly, (0,0) satisfies the in equation $5x + 2y \le 10$, so, the region in xy-plane that contains the origin represents the solution set if the given in equation.

Region represented by $3x + 5y \le 10$: The line meets coordinate axes at A_2 (5,0) and B_2 (0,3) respectively. Join these points to obtain the line 3x + 5y = 15, clearly, (0,0) satisfies the in equation $3x + 5y \le 15$, so, the region in xy-plane contains the origin represents the solution set if the given in equation.

Region represented by $x \ge 0$, $y \ge 0$: It clearly represents first quadrant of xy-plane. Common region to regions represented by above in equalities.

The coordinates of the corner points of the shaded region are 0(0,0), A(2,0), $P(\frac{20}{19},\frac{45}{19})$, $B_2(0,3)$.

The value of Z = 5x + 3y at

$$0(0,0) = 5 \times +3 \times 0$$

$$A(2,0) = 5 \times 2 + 3 \times 0 = 10$$

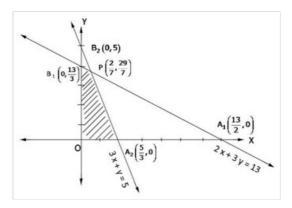
$$P\left(\frac{20}{19}, \frac{45}{19}\right) = 5\left(\frac{20}{19}\right) + 3\left(\frac{45}{19}\right) = \frac{235}{19}$$

$$B_2(0,3) = 5 \times 0 + 3 \times 3 = 9$$

Clearly, Z is maximum at $P\left(\frac{20}{19}, \frac{45}{19}\right)$

So,
$$x = \frac{20}{19}$$
, $y = \frac{45}{19}$, maximum $Z = \frac{235}{19}$

Converting the given inequations into equations, we get 2x + 3y = 13, 3x + y = 5, and x = 0, y = 0



Region represented by $2x+3y \le 13$: The line meets coordinate axes at $A_1\left(\frac{13}{2},0\right)$ and $B_1\left(0,\frac{13}{3}\right)$ respectively. Join these points to obtain the line 2x+3y=13, clearly, $\left(0,0\right)$ satisfies the in eqation $2x+3y \le 13$, so, the region in xy-plane that contains origin represents the solution set of $2x+3y \le 13$.

Region represented by $3x+y \le 5$: The line meets coordinate axes at $A_2\left(\frac{5}{3},0\right)$ and $B_2\left(0,5\right)$ respectively. Join these points to obtain the line 3x+y=5, clearly, $\left(0,0\right)$ satisfies the in eqation $3x+y\le 5$, so, the region in xy-plane that contains origin represents the solution set of $3x+y\le 5$.

Region represented by $x,y \ge 0$: It clearly represent first quadrant of xy-plane. The common region to regions represented by above in equalities.

The coordinates of the corner points of the shaded region are 0(0,0), $A\left(\frac{5}{3},0\right)$, $P\left(\frac{2}{7},\frac{29}{7}\right)$, $B_2\left(0,\frac{13}{3}\right)$.

The value of Z = 9x + 3y at 0(0,0) = 9(0) + 3(0) = 0 $A_1(\frac{5}{3},0) = 9(\frac{5}{3}) + 3(0) = 15$ $P(\frac{2}{7},\frac{29}{7}) = 9(\frac{2}{7}) + 3(\frac{29}{7}) = 15$

$$B_2\left(0, \frac{13}{3}\right) = 9\left(0\right) + 3\left(\frac{13}{3}\right) = 13$$

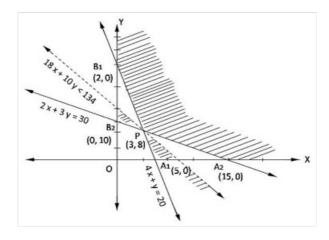
Clearly, Z is maximum at at every point on the line joining A_1 and P, so $X = \frac{5}{3}$ or $\frac{2}{7}$, Y = 0 or $\frac{29}{7}$

and maximum Z = 15.

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Converting given inequations into equations as

$$4x + y = 20$$
, $2x + 3y = 30$, $x = 0$, $y = 0$



Region represented by in equation $4x + y \ge 20$: The line 4x + y = 20 meets the coordinate axes at A_1 (5,0) and B_1 (0,20). Joining A_1B_1 we get 4x + y = 20. Clearly, (0,0), also does not satisfies the in equation, so the region does not containing the origin represents the in equality $4x + y \ge 20$ in the xy-plane.

Region represented by in equation $2x + 3y \ge 30$: The line 2x + 3y = 30 meets the coordinate axes at A_2 (15,0) and B_2 (0,20). Obtain line 2x + 3y = 30 by joining A_2 and B_2 . Clearly, (0,0), does not satisfies the in equation $2x + 3y \ge 30$, so the region does not containing the origin represents the in equality $2x + 3y \ge 30$ in the xy-plane.

Region represented by $x, y \ge 0$: $x, y \ge 0$ represents the first quadrant of xy-plane.

The shaded region is the feasible region with corner points A_2 (15,0), P (3,8), B_1 (0,20) where P is obtained by solving 2x + 3y = 30 and 4x + y = 20 simultaneously.

The value of Z = 18x + 10y at

 A_2 (15,0) = 18(15) + 10(8) = 270

P(3,8) = 18(3) + 10(8) = 134

 $B_1(0,20) = 18(0) + 10(20) = 200$

Clearly, Z is manimum at x = 3 and y = 8. The minimum value of Z is 134.

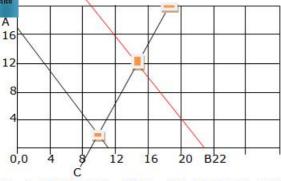
We observe that open half plane represented by 18x + 10y < 134 does not have points in common with the solution region. So Z has

Minimum value = 134 at x = 3, y = 8

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Programming Ex 30.2 Q4



2x-y \geq 18; when x = 12, y = 6 & when y=0, x=9 3x+2y \leq 34; when x = 0, y = 17 & when y=0, x=34/3

Plotting these points gives line AB and CD The feasible area is the unbounded area D-E-12

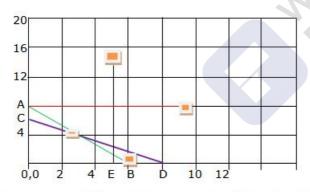
Corner point	Value of $Z = 50x + 30y$
10, 2	560
11.3, 17	1076.66

The maximize value of Z = 50x+30y, occurs at x = 34/3, y = 17

Since we have an unbounded region as the feasible area plot 50x + 30y > 1076.66

Since the region D-F-B has common points with region D-E-12 the problem has no optimal maximum value.

Linear Programming Ex 30.2 Q5



 $3x+4y \le 24$; when x = 0, y = 6 & when y=0, x=8, line

 $8x + 6y \leq 48$; when $x = 0, \, y = 8$ & when y=0, x=6, line $^{\rm CD}$

Plotting $x \le 5$ gives line EF; Plotting $y \le 6$ gives line AG The feasible area is 0,0-C-H-G-E

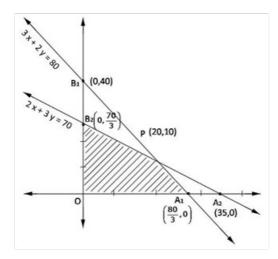
Corner point	Value of $Z = 4x + 3y$
0,0	0
0,6	18
3.4, 3.4	24
5, 1	23
5,0	20

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MILLIONST R Programming Ex 30.2 Q6

ng the inequations into equations as

$$3x + 2y = 80, 2x + 3y = 70, x = y = 0$$



Region represented by $3x+2y \le 80$: Line 3x+2y=80 meets coordinate axes at $A_1\left(\frac{80}{3},0\right)$ and $B_1\left(0,40\right)$, clearly, $\left(0,0\right)$ satisfies the $3x+2y \le 80$, so, region containing the origin represents by $3x+2y \le 80$ in xy-plane

Region represented by $2x + 3y \le 70$: Line 2x + 3y = 70 meets the coordinate axes at A_2 (35,0) and B_2 $\left(0,\frac{70}{3}\right)$, clearly, (0,0) satisfies the $2x + 3y \le 70$ so, the region containing the origin represents by $2x + 3y \le 70$ in xy-plane

Region represented by $x,y \ge 0$: It represent the first quadrant in xy-plane

So, shaded area OA_1PB_2 represents the feasible region.

Coordinate of P(20,10) can be obtained by solving 3x + 2y = 80 and 2x + 3y = 70

Now, the value of
$$Z = 15x + 10y$$
 at $O(0,0) = 15(0) + 10(0) = 0$
$$A_1\left(\frac{80}{3},0\right) = 15\left(\frac{80}{3}\right) + 10(0) = 400$$

$$P(20,10) = 15(20) + 10(10) = 400$$

$$B_2\left(0,\frac{70}{3}\right) = 15(0) + 10\left(\frac{70}{3}\right) = \frac{700}{3}$$

So, maximum Z=400 is on each and every point on the line joining A_1P , so we can have,

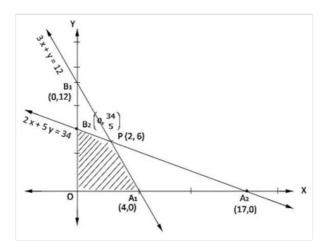
maximum
$$Z = 400$$
 at $x = \frac{80}{3}$ and $y = 0$
maximum $Z = 400$ at $x = 20$ and $y = 10$

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r Programming Ex 30.2 Q7

rting the given inequations into equations 3x + y = 12, 2x + 5y = 34, x = y = 0



Region represented by $3x+y \le 12$: Line 3x+y=12 meets the coordinate axes at A_1 (4,0) and B_1 (0,12), clearly, (0,0) satisfies $3x+y \le 12$, so, region containing origin is represented by $3x+y \le 12$ in xy-plane

Region represented by $2x + 5y \le 34$: Line 2x + y = 34 meets coordinate axes at A_2 (17,0) and B_2 (0, $\frac{34}{5}$), clearly, (0,0) satisfies the $2x + 5y \le 34$ so, region containing origin represents $2x + 5y \le 34$ in xy-plane

Region represented by $x,y \ge 0$: It represent the first quadrant in xy-plane

Therefore, shaded area OA_1PB_2 is the feasible region.

The coordinate of P(2,6) is obtained by solving 2x + 5y = 34 and 3x + y = 12

The value of Z = 10x + 6y at

$$O(0,0) = 10(0) + 6(0) = 0$$

$$A_1(4,0) = 10(4) + 6(0) = 40$$

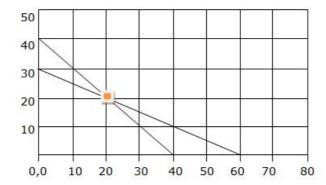
$$P(2,6) = 10(2) + 6(6) = 56$$

$$B_2(0,\frac{34}{5}) = 10(0) + 6(\frac{34}{5}) = \frac{204}{5} = 40\frac{4}{5}$$

Hence, maximum Z = 56 at x = 2, y = 6

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 $2x+2y \le 80$; when x=0, y=40 and when y=0, x=40 $2x+4y \le 120$; when x=0, y=30 and when y=0, x=60

The intersection of the two plotted lines gives (20, 20) Feasible area is 30-C-40

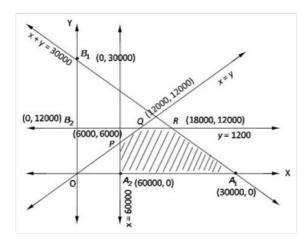
Corner point	Value of $Z = 3x + 4y$
0, 0	0
0, 30	120
20, 20	140
40,0	120

The maxima is obtained at x=20, y=20 and is 140



or Programming Ex 30.2 Q9

Converting the given inequations into equations, x + y = 30000, y = 12000, x = 6000, x = y, x = y = 0



Region represented by $x + y \le 30000$: Line x + y = 30000 meets the coordinate axes at A_1 (30000,0) and B_1 (0,30000), clearly (0,0) satisfies $x + y \le 30000$, so, region containing the origin represents $x + y \le 30000$ in xy-plane

Region represented by $y \le 12000$: Line y = 12000 is parallel to x -axis and meets y - axis at B_2 (0,12000). Clearly (0,0) satisfies $y \le 12000$, so, region containing origin represents $y \le 12000$ in xy -plane.

Region represented by $x \le 6000$: Line x = 6000 is parallel to y - axis and meets x - axisaxis at A_2 (6000,0). Clearly (0,0) satisfies $x \le 6000$, so, region containing origin represents $x \le 6000$ in xy -plane.

Region represented by $x \ge y$: Line x = y passes through origin and point Q (12000,12000). Clearly, A_2 (6000,0) satisfies $x \ge y$, so, region containing A_2 (6000,0) represents $x \ge y$ in xy -plane.

Region represented by $x, y \ge 0$: It represents the first quadrant in xy -plane.

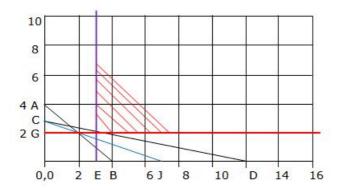
Shaded region A_2A_1QP represents the feasible region.

Coordinates of R (18000,12000) is obtained by solving x + y = 30000 and y = 12000, Q (12000, 12000) is obtained by solving x = y and y = 12000, P (6000,6000) is obtained by solving x = y and x = 6000.

The value of Z = 7x + 10y at

lue of
$$Z = 7x + 10y$$
 at A_2 (6000,0) = 7 (6000) + 10 (0) = 42000
 A_1 (30000,0) = 7 (30000) + 10 (0) = 210000
 R (18000,12000) = 7 (18000) + 10 (12000) = 246000
 Q (12000,12000) = 7 (12000) + 10 (12000) = 204000
 P (6000,6000) = 7 (6000) + 10 (6000) = 102000
eximum $Z = 246000$ at $x = 18000$, $y = 12000$

So, maximum Z = 246000 at x = 18000, y = 12000



 $2x+2y\ge 8$; When x=0, y=4 & when y=0, x=4 line AB $x+4y\ge 12$; When x=0, y=3 & when y=0, x=12 line CD $x\ge 3$, $y\ge 2$ are the lines parallel to Y-axis and X-axis resp.

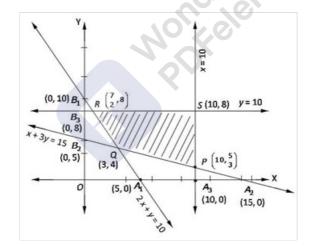
The diverging shaded area in red lines is the area of feasible solution. This area is unbounded. $Z = 2x+4y \otimes (3.2) = 14$.

Plot 2x+4y > 14 line CJ to see if there is any common region. There is no common region so there is no optimal solution.

Linear Programming Ex 30.2 Q11

Converting the given inequations into equations,

$$2x + y = 10$$
, $x + 3y = 15$, $x = 10$, $y = 8$, $x = y = 0$



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Region represented by $2x + y \ge 10$: Line 2x + y = 10 meets coordinate and $B_1(0,10)$. Clearly, (0,0) does not satisfy $2x + y \ge 10$, so, region not containing origin represents $2x + y \ge 10$ in xy -plane.

Region represented by $x + 3y \ge 15$: Line x + 3y = 15 meets coordinate axes at $A_2(15,0)$ and $B_2(0,5)$. Clearly, (0,0) does not satisfy $x + 3y \ge 15$, so, region not containing origin represents $x + 3y \ge 15$ in xy - plane.

Region represented by $x \le 10$: Line x = 10 is parallel to y-axis and meet x-axis at $A_3(10,0)$. Clearly (0,0) satisfies $x \le 10$, so region containing origin represent $x \le 10$ in xy-plane.

Region represented by $y \le 8$: Line y = 8 is parallel to x-axis and meet y-axis at $B_3(0,8)$, clearly (0,0) satisfies $y \le 8$, so region containing origin represent $y \le 8$ in xy-plane.

Region represented by $x,y \ge 0$: It represent the first quadrant in xy-plane.

Shaded region QPSR is the feasible region. Q (3, 4) is obtained by solving 2x + y = 10and x + 3y = 15, $P\left(10, \frac{5}{3}\right)$ is obtained by solving x + 3y = 15 and x = 10, $R\left(\frac{7}{2}, 8\right)$ is obtained by 2x + y = 10 and y = 8.

The value of Z = 5x + 3y at

$$P\left(10, \frac{5}{3}\right) = 5\left(10\right) + 3\left(\frac{5}{3}\right) = 55$$

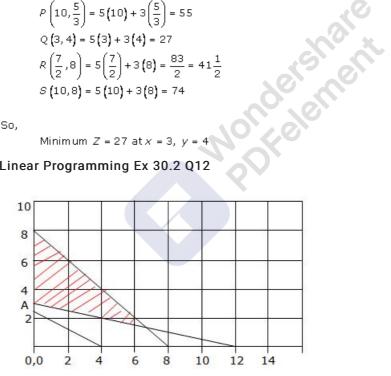
$$Q\left(3, 4\right) = 5\left(3\right) + 3\left(4\right) = 27$$

$$R\left(\frac{7}{2}, 8\right) = 5\left(\frac{7}{2}\right) + 3\left(8\right) = \frac{83}{2} = 41\frac{1}{2}$$

$$S\left(10, 8\right) = 5\left(10\right) + 3\left(8\right) = 74$$

So,

Linear Programming Ex 30.2 Q12



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Williams and Stars of the Children of $x + y \le 8$; when x=0, y=8 & when y=0, x=8, line 8-8 x + 4y≥12; when x=0, y=3 & when y=0, x=12 line A-12 5x+8y=20; when x=0, y=5/2 & when y=0, x=4

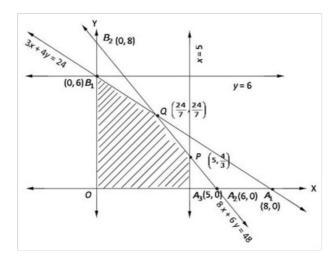
The shaded area in red is the area of feasible solution.

Corner point	Value of $Z = 30x + 20y$
0, 3	60
0,8	160
6.66, 1.33	226.66

The maxima is obtained at x=6.66, y=1.33 and is 226.66

Converting the given inequations into equations,

$$3x + 4y = 24$$
, $8x + 6y = 48$, $x = 5$, $y = 6$, $x = y = 0$



Region represented by $3x + 4y \le 24$: Line 3x + 4y = 24 meets coordinate axes at A_1 (8,0) and $B_1(0,6)$, clearly (0,0) satisfies $3x + 4y \le 24$, so region containing origin represents $3x + 4y \le 24$ in xy -plane.

Region represented by $8x + 6y \le 48$: Line 8x + 6y = 48 meets coordinate axes at A_2 (6,0) and $B_2(0,8)$. Clearly, (0,0) satisfies $8x + 6y \le 48$, so region containing origin represents $8x + 6y \le 48 \text{ in } xy - \text{plane.}$

Region represented $x \le 5$: Line x = 5 is parallel to y-axis and meets x-axis at A_3 (5,0). Clearly (0,0) satisfies $x \le 5$, so region containing origin represent $x \le 5$ in xy-plane.

Region represented by $y \le 6$: Line y = 6 is parallel to x-axis and meets y-axis at $B_1(0,6)$. Clearly (0,0) satisfies $y \le 6$, so, region containing origin represents $y \le 6$ in xy-plane.

Region represented by $x,y \ge 0$: It represents the first quadrant in xy-plane.

So, shaded region QA3PQB represents feasible region.

Coordinate of $P\left(5, \frac{4}{3}\right)$ is obtained by solving 8x + 6y = 48 and x = 5, coordinate of $Q\left(\frac{24}{7}, \frac{24}{7}\right)$ is obtained by solving 3x + 4y = 24 and 8x + 6y = 48.

The value of Z = 4x + 3y at

$$0 (0,0) = 4(0) + 3(0) = 0$$

$$A_3 (5,0) = 4(5) + 3(0) = 20$$

$$P \left(5, \frac{4}{3}\right) = 4(5) + 3\left(\frac{4}{3}\right) = 24$$

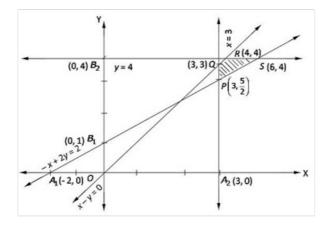
$$Q \left(\frac{24}{7}, \frac{24}{7}\right) = 4\left(\frac{24}{7}\right) + 3\left(\frac{24}{7}\right) = 24$$

$$B_1 (0,6) = 4(0) + 3(6) = 18$$

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Converting the given inequations into equations,

$$x - y = 0$$
, $-x + 2y = 2$, $x = 3$, $y = 4$, $x = y = 0$



Region represented by $x - y \ge 0$: x - y = 0 is a line passing through origin and R(4,4). Clearly, (3,0) satisfies $x - y \ge 0$, so, region containing (3,0) represents $x - y \ge 0$ in xy-plane.

Region represented by $-x + 2y \ge 2$: Line -x + 2y = 2 meets coordinate axes at $A_1(-2,0)$ and $B_1(0,1)$. Clearly, (0,0) does not satisfy $-x+2y \ge 2$, so, region not containing origin represents $-x + 2y \ge 2$ in xy -plane.

Region represented $x \ge 3$: Line x = 3 is parallel to y-axis and meets x-axis at $A_2(3,0)$. Clearly, (0,0) does not satisfy $x \ge 3$, so region not containing origin represent $x \ge 3$ in xy-plane.

Region represented by $y \le 4$: Line y = 4 is parallel to x-axis and meets y-axis at \mathcal{B}_2 (0,4). Clearly (0,0) satisfies $y \leq 4$, so region containing origin represents $y \leq 4$ in xy-plane.

Region represented by $x,y \ge 0$: It represent the first quadrant in xy-plane.

So, shaded region PQRS represents feasible region.

The coordinate of $P\left(3, \frac{5}{2}\right)$ is obtained by solving x = 3 and -x + 2y = 2, $Q\left(3, 3\right)$ by solving x = 3 and x - y = 0, R(4, 4) by solving x = 4 and x - y = 0, S(6, 4) by solving y = 4 and -x + 2y = 2Million Stars & Practice

The value of Z = x - 5y + 20 at

$$P\left(3, \frac{5}{2}\right) = 3 - 5\left(\frac{5}{2}\right) + 20 = \frac{21}{2} = 11\frac{1}{2}$$

$$Q\left(3, 3\right) = 3 - 5\left(3\right) + 20 = 8$$

$$R\left(4, 4\right) = 4 - 5\left(4\right) + 20 = 4$$

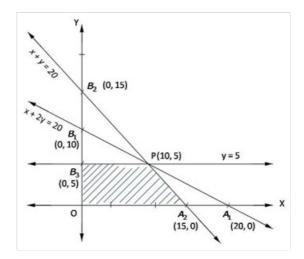
$$S(6,4) = 6 - 5(4) + 20 = 6$$

Hence,

Minimum
$$Z = 4$$
 at $x = 4$ and $y = 4$

Converting the given inequations into equations:-

$$x + 2y = 20$$
, $x + y = 15$, $y = 5$, $x = y = 0$



Region represented by $x+2y \le 20$: Line x+2y=20 meets coordinate axes at $A_1(20,0)$ and $B_1(0,10)$, clearly, (0,0) satisfies $x+2y \le 20$, so region containing origin represents $x+2y \le 20$ in xy-plane.

Region represented by $x+y \le 15$: Line x+y=15 meets coordinate axes at A_2 (15,0) and B_2 (0,15), clearly, (0,0) satisfies $x+y \le 15$, so region containing origin represents $x+y \le 15$ in xy-plane.

Region represented by $y \le 5$: Line y = 5 is parallel to x-axis and meets at $B_3(0,5)$ on y-axis. Clearly (0,0) satisfies $y \le 5$, so region containing origin represents $y \le 5$ in xy-plane.

Region represented by $x, y \ge 0$: It represent the first quadrant in xy-plane.

So, shaded region OA_2PB_3 represents the feasible region.

Coordinate of P(10,5) is obtained by solving x + 2y = 20 and y = 5.

The value of
$$Z = 3x + 5y$$
 at
$$O(0,0) = 3(0) + 5(0) = 0$$

$$A_2(15,0) = 3(15) + 5(0) = 45$$

$$P(10,5) = 3(10) + 5(5) = 55$$

$$B_3(0,5) = 3(0) + 5(5) = 25$$

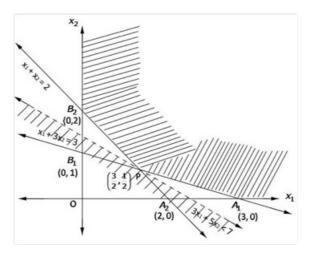
Hence, maximum Z = 55 at x = 10 and y = 5

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Linear Programming Ex 30.2 Q16

Converting the given inequations into equations,

$$X_1 + 3X_2 = 3$$
, $X_1 + X_2 = 2$, $X_1 = X_2 = 0$



Region represented by $x_1 + 3x_2 \ge 3$: Line $x_1 + 3x_2 = 3$ meets the coordinate axes at A_1 (3,0) and B_1 (0,1), clearly, (0,0) does not satisfy $x_1 + 3x_2 \ge 3$, so, region not containing (3,0) represents $x_1 + 3x_2 \ge 3$ in x_1x_2 -plane.

Region represented by $x_1+x_2\geq 2$: Line $x_1+x_2=2$ meets the coordinate axes at A_2 (2,0) and B_2 (0,2), clearly, (0,0) does not satisfy $x_1+x_2\geq 2$, so, region not containing origin represents $x_1+x_2\geq 2$ in x_1x_2 -plane.

Region represented $x_1, x_2 \ge 0$: It represents the first quadrant in x_1x_2 -plane.

The unbounded shaded region with corner points $A_1(3,0)$, $B_2(0,2)$, and $P\left(\frac{3}{2},\frac{1}{2}\right)$.

$$P\left(\frac{3}{2},\frac{1}{2}\right)$$
 is obtained by $x_1+x_2=2$ and $x_1+3x_2=3$.

The value of $Z = 3x_1 + 5x_2$ at

$$A_1(3,0) = 3(3) + 5(0) = 9$$

$$P\left(\frac{3}{2}, \frac{1}{2}\right) = 3\left(\frac{3}{2}\right) + 5\left(\frac{1}{2}\right) = 7$$

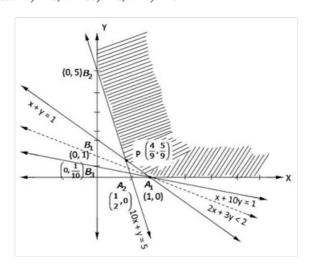
$$B_2(0,2) = 3(0) + 5(2) = 10$$

The smallest value of Z = 7,

region has no point in common, so smallest value is the minimum value.

Hence, minimum
$$Z = 7$$
 at $x = \frac{3}{2}$ and $y = \frac{1}{2}$

Converting the given inequations into equations x + y = 1, 10x + y = 5, x + 10y = 1, x = y = 0



Region represented by $x + y \ge 1$: Line x + y = 1 meets coordinate axes at $A_1(1,0)$ and $B_1(0,1)$, dearly, (0,0) does not satisfy $x + y \ge 1$, so region not containing origin represents $x + y \ge 1$ in xy -plane.

Region represented by $10x + y \ge 5$: Line 10x + y = 5 meets coordinate axes at $A_2\left(\frac{1}{2}, 0\right)$ and $B_2(0,5)$. Clearly, (0,0) does not satisfy $10x + y \ge 5$, so region not containing origin represents $10x + y \ge 5$ in xy -plane.

Region represented by $x + 10y \ge 1$: Line x + 10y = 1 meets coordinate axes $A_i(1,0)$ and $B_3\left(0,\frac{1}{10}\right)$. Clearly, $\left(0,0\right)$ does not satisfy $x+10y\geq 1$, so, region not containing origin represents $x + 10y \ge 1$ in xy-plane.

Region represented by $x,y \ge 0$: It represents first quadrant in xy-plane.

So, unbounded shaded represents feasible region. Its corner points are $A_1(1,0)$, $P\left(\frac{4}{0},\frac{5}{0}\right)$ and $B_2(0,5)$.

The coordinate of $P\left(\frac{4}{9}, \frac{5}{9}\right)$ is obtained by solving 10x + y = 5 and x + y = 1.

The value of Z = 2x + 3y at

$$A_1(1,0) = 2(1) + 3(0) = 2$$

$$P\left(\frac{4}{9}, \frac{5}{9}\right) = 2\left(\frac{4}{8}\right) + 3\left(\frac{5}{9}\right) = \frac{23}{9} = 2\frac{5}{9}$$

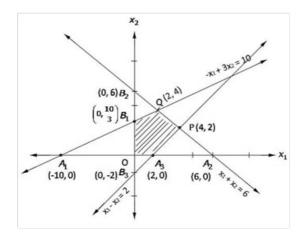
$$B_2(0,5) = 2(0) + 3(5) = 15$$

Willion earn a practice with the property of t The smallest value of Z is 2. Now, open half plane 2x + 3y < 2 has no point in common with feasible region so, smallest value of ${\it Z}$ is the minimum value.

Hence, maximum Z = 2 at x = 1 and y = 0

Converting the given inequations into equations,

$$-X_1 + 3X_2 = 10$$
, $X_1 + X_2 = 6$, $X_1 = X_2 = 2$, $X_1 = X_2 = 0$



Region represented by $-x_1+3x_2 \le 10$: Line $-x_1+3x_2=10$ meets coordinate axes at $A_1\left(-10,0\right)$ and $B_1\left(0,\frac{10}{3}\right)$, clearly, $\left(0,0\right)$ satisfies $-x_1+3x_2 \le 10$, so region containing origin represents $-x_1+3x_2 \le 10$ in x_1x_2 -plane.

Region represented by $x_1 + x_2 \le 6$: Line $x_1 + x_2 = 6$ meets coordinate axes at A_2 (6,0) and B_2 (0,6). Clearly, (0,0) satisfies $x_1 + x_2 \le 6$, so region containing origin represents $x_1 + x_2 \le 6$ in $x_1 x_2$ -plane.

Region represented by $x_1 - x_2 \le 2$: Line $x_1 - x_2 = 2$ meets coordinate axes at A_3 (2, 0) and B_3 (0, -2). Clearly, (0,0) satisfies $x_1 - x_2 \le 2$, so, region containing origin represents $x_1 - x_2 \le 2$ in x_1x_2 -plane.

Region represented $x_1, x_2 \ge 0$: It represents first quadrant in x_1x_2 -plane.

So, shaded region OA3PQB, represents feasible region.

Coordinate of P (4,2) is obtained by solving $x_1 + x_2 = 6$ and $x_1 - x_2 = 2$, Q (2,4) by solving $x_1 + x_2 = 6$ and $-x_1 + 3x_2 = 10$

The value of $Z = -x_1 + 2x_2$ at

$$O(0,0) = -(0) + 2(0) = 0$$

$$A_3(2,0) = -(2) + 2(0) = -2$$

$$P(4,2) = -(4) + 2(2) = 0$$

$$Q(2,4) = -(2) + 2(4) = 6$$

$$B_1\left(0, \frac{10}{3}\right) = -\left(0\right) + 2\left(\frac{10}{3}\right) = \frac{20}{3} = 6\frac{2}{3}$$

Hence, maximum $Z = \frac{20}{3}$ at x = 0 and $y = \frac{10}{3}$

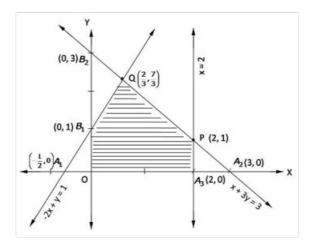
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Linear Programming Ex 30.2 Q19

Converting the given inequations into equations,

$$-2x + y = 1$$
, $x = 2$, $x + y = 3$, $x = y = 0$



Region represented by $-2x+y \le 1$: Line -2x+y=1 meets coordinate axes at $A_1\left(\frac{-1}{2},0\right)$ and $B_1\left(0,1\right)$, clearly, $\left(0,0\right)$ satisfies $-2x+y \le 1$, so region containing origin represents $-2x+y \le 1$ in xy-plane.

Region represented by $x \le 2$: Line x = 2 is parallel to y-axis and meets x-axis at $A_3(2,0)$. Clearly, (0,0) satisfies $x \le 2$, so region containing origin represents $x \le 2$ in xy-plane.

Region represented by $x+y \le 3$: Line x+y=3 meets coordinate axes at A_2 (3,0) and B_2 (0,3). Clearly, (0,0) satisfies $x+y \le 3$, so region containing origin represents $x+y \le 3$ in xy -plane.

Region represented by $x, y \ge 0$: It represents first quadrant in xy-plane.

So, shaded region OA_3PQB , represents the feasible region.

Coordinates of P (2,1) is obtained by solving x + y = 3 and x = 2, $Q\left(\frac{2}{3}, \frac{7}{3}\right)$ by solving -2x + y = 1 and x + y = 3.

The value of Z = x + y at

$$O(0,0) = 0+0=0$$

$$A_3(2,0) = 2 + 0 = 2$$

$$P(2.1) = 2 + 1 = 2$$

$$Q\left(\frac{2}{3}, \frac{7}{3}\right) = \frac{2}{3} + \frac{7}{3} = 3$$

$$B_1(0,1) = 0+1=1$$

So, maximum Z = 3 is at every point on the line joining PQ.

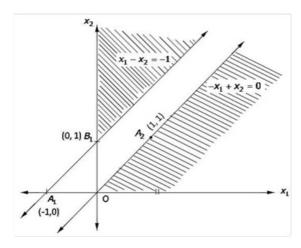
Hence, maximum
$$Z = 3$$
 at $x = 2$ and $y = 1$ Or $x = \frac{2}{3}$ and $y = \frac{7}{3}$

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Linear Programming Ex 30.2 Q20

Converting the given inequations into equations,

$$X_1 - X_2 = -1$$
, $-X_1 + X_2 = 0$, $X_1 = X_2 = 0$



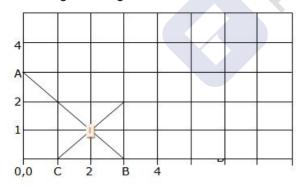
Region represented by $x_1 - x_2 \le -1$: Line $x_1 - x_2 = -1$ meets coordinate axes at A_1 (-1,0) and B_1 (0,1), clearly, (0,0) does not satisfy $x_1 - x_2 \le -1$, so region not containing origin represents $x_1 - x_2 \le -1$ in x_1x_2 -plane.

Region represented by $-x_1+x_2 \le 0$: Line $-x_1+x_2 = 0$ passes through origin and A_2 (1,1). Clearly, (0,0) does not satisfy $-x_1+x_2 \le 0$, so, region not containing (0,1) represents $-x_1+x_2 \le 0$ in x_1x_2 -plane.

Since, there is not common shaded region represented by $x_1 - x_2 \le -1$ and $-x_1 + x_2 \le 0$ which can form feasible region.

Hence, maximum $Z = 3x_1 + 4x_2$ does not exists.

Linear Programming Ex 30.2 Q21



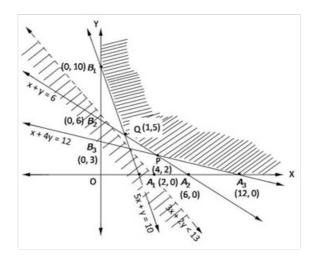
 $x-y \le 1$; when x=0, y=1 & when y=0, x=2 $x+y \ge 3$; when x=0, y=3 & when y=0, x=3, line AB a unbounded region A-C-D is obtained using the constraints.

Corner point	Value of $Z = 3x + 3y$
0, 3	9
2, 1	9

So an optimal solution does not exist.

Converting the given inequations into equations

$$5x + y = 10$$
, $x + y = 6$, $x + 4y = 12$, $x = y = 0$



Region represented by $5x + y \ge 10$: Line 5x + y = 10 meets coordinate axes at $A_1(2,0)$ and $B_1(0,10)$. Clearly, (0,0) does not satisfy $5x + y \ge 10$, so region not containing origin represents $5x + y \ge 10$ in xy -plane.

Region represented by $x + y \ge 6$: Line x + y = 6 meets coordinate axes at A_2 (6,0) and $B_2(0,6)$. Clearly, (0,0) does not satisfy $x+y \ge 6$, so region not containing origin represents $x + y \ge 6$ in xy -plane.

Region represented by $x + 4y \ge 12$: Line x + 4y = 12 meets coordinate axes at $A_3(12,0)$ and $B_3(0,3)$. Clearly, (0,0) does not satisfy $x + 4y \ge 12$, so, region not containing origin $x + 4y \ge 12$ in xy -plane.

Region represented by $x, y \ge 0$: It represents first quadrant in xy-plane.

The unbounded shaded region with corner points $A_3(12,0)$, P(4,2), Q(1,5), $B_1(0,10)$ represents feasible region. Point P is obtained by solving x + 4y = 12 and x + y = 6, Q by solving x + y = 6 and 5x + y = 10.

The value of Z = 3x + 2y at

$$A_3(12,0) = 3(12) + 2(0) = 36$$

$$P(4,2) = 3(4) + 2(2) = 16$$

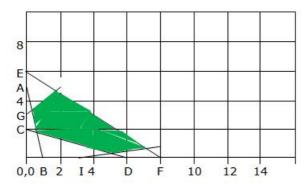
$$Q(1,5) = 3(1) + 2(5) = 13$$

$$B(0,10) = 3(0) + 2(10) = 20$$

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Williams Range of the Control of the Cont Smallest value of Z = 13, Now open half plane 3x + 2y < 13 has no point in common with feasible region, so, smallest value is the minimum value of Z, Hence

Minimum
$$Z = 13$$
 at $x = 1$, $y = 5$





 $x+3y \ge 6$; or y=-0.333x+2; when x=0, y=2 & when y=0, x=6; line CD

 $x-3y \le 3$; or y=0.333x-1; when x=0, y=-1 & when y=0, x=3; line IJ

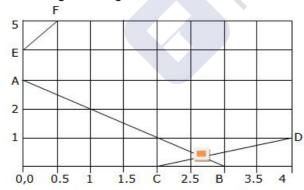
 $3x+4y \le 24$; or y=-0.75x+6; when x=0, y=6 & when y=0, x=8; line EF

 $-3x+2y \le 6$; or y= 1.5x+3; when x=0, y=3 & when y=0, x=-2;line GH

 $5x+y \ge 5$; or y=-5x+5; when x=0, y=5 & when y=0, x=1; line AB

The feasible area is shaded in green

4.5, 0.5 9.5 0.64, 1.78 3.07 6.46, 1.15 Maximum 14.07 1.33, 5 7.6667 0.30, 3.46 4.0769 num value is 14.07 at the point (6.46, 1.15) num value is 3.07 at the point (0.64, 1.78) Programming Ex 30.2 Q24 F	Corner point	Value of Z =	2x + y	
1.33, 5 7.6667 0.30, 3.46 4.0769 1.33 the point (6.46, 1.15) representation of the point (0.64, 1.78) representation o	4.5, 0.5		9.5	
1.33, 5 7.6667 0.30, 3.46 4.0769 num value is 14.07 at the point (6.46, 1.15) num value is 3.07 at the point (0.64, 1.78) Programming Ex 30.2 Q24	0.64, 1.78		3.07	
0.30, 3.46 4.0769 from value is 14.07 at the point (6.46, 1.15) um value is 3.07 at the point (0.64, 1.78) Programming Ex 30.2 Q24	6.46, 1.15	Maximum	14.07	$1 \cdot a$
num value is 14.07 at the point (6.46, 1.15) um value is 3.07 at the point (0.64, 1.78) Programming Ex 30.2 Q24	1.33, 5		7.6667	
um value is 3.07 at the point (0.64, 1.78) Programming Ex 30.2 Q24	0.30, 3.46		4 0769	
		1 07 at the noi		1 15)
	num value is 14 um value is 3.0 Programmin	07 at the point	nt (6.46, : (0.64, 1	
	um value is 14 um value is 3.0 Programmin	07 at the point	nt (6.46, : (0.64, 1	



 $-2x+y \le 4$; or y=2x+4; when x=0, y=4 & when y=0, x=-2 line EF

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 $x+y\geq 3$; or y=-x+3; when x=0, y=3 & when y=0, x=3; line AB

 $x-2y \le 2$; or y=0.5x-1; when x=0, y=-1 & when y=0,

x=2 line CD

The feasible solution is the unbounded area with F-E-A-G-D

Corner point	Value of $Z = 3x + 5y$		
(2.67, 0.33)	Minimum	9.66	
(0, 3)		15	
(0, 4)		20	

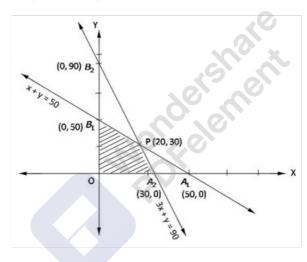
To check whether it is the minimal value plot the objective function with a value less than 9.66 or y = -0.6x - 1.932

it can be seen that the values of x and y are always negative. So there is no optimal solution.

Linear Programming Ex 30.2 Q25

Converting the given inequations into equations,

$$x + y = 50$$
, $3x + y = 90$, $x = y = 0$



Region represented by $x + y \le 50$: Line x + y = 50 meets coordinate axes at A_1 (50, 0) and B_1 (0,50). Clearly, (0,0) satisfies $x + y \le 50$, so, region containing origin represents $x + y \le 50$ in xy -plane.

Region represented by $3x + y \le 90$: Line 3x + y = 90 meets coordinate axes at A_2 (30,0) Million Stars & Practice
Williams and Stars of the Children of and $B_2(0,90)$. Clearly, $\{0,0\}$ satisfies $3x + y \le 90$, so, region containing origin represents $3x + y \le 90$ in xy -plane.

Region represented by $x, y \ge 0$: It represents first quadrant in xy-plane.

Shaded region OA_2PB_1 represents the feasible region. P (20,30) can be obtained by solving x + y = 50 and 3x + y = 90.

The value of
$$Z = 60x + 15y$$
 at

$$O(0,0) = 60(0) + 15(0) = 0$$

$$A_2(30,0) = 60(30) + 15(0) = 1800$$

$$P(20,30) = 60(20) + 15(30) = 1650$$

$$B_1(0,50) = 60(0) + 15(50) = 750$$

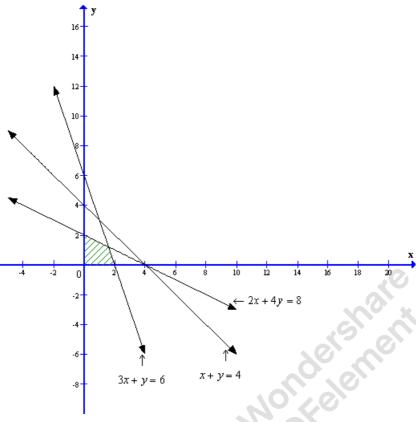
Hence,

maximum Z is 1800 at x = 30 and y = 0.

Converting the inequations into equations, we obtain the lines

$$2x + 4y = 8$$
, $3x + y = 6$, $x + y = 4$, $x = 0$, $y = 0$.

These lines are drawn on a suitable scale and the feasible region of the LPP is shaded in the graph.



From the graph we can see the corner points as (0, 2) and (2, 0).

Now solving the equations 3x + y = 6 and 2x + 4y = 8 we get the values of x and y as $x = \frac{8}{5}$ and $y = \frac{6}{5}$.

Substituting
$$x = \frac{8}{5}$$
 and $y = \frac{6}{5}$ in $Z = 2x + 5y$ we get,
$$Z = 2\left(\frac{8}{5}\right) + 5\left(\frac{6}{5}\right)$$

$$Z = \frac{46}{5}$$

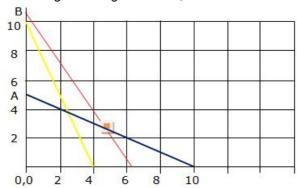
Hence maximum value of Z is $\frac{46}{5}$ at $x = \frac{8}{5}$ and $y = \frac{6}{5}$.

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Ex 30.3

Linear Programming Ex 30.3 Q1



Let x and y be the No. of 25 gm packets of foods F_1 and F_2

Minimum cost of diet Z = 0.20x + 0.15y

The constraints are

 $0.25x + 0.1y \ge 1$; when x=0, y=10 & y=0, x=4 10-4 $0.75x + 1.5y \ge 7.5$; when x=0, y=5 & y=0, x=10 A-10 $1.6x + 0.8y \ge 10$; when x=0, y=25/2 & y=0, x=25/4

The feasible region is the open region B-E-10

The minimum cost of the diet can be checked by finding the value of Z at corner points B, E & 10

Corner point	Value of Z = 20x + 15y
0, 12.5	187.5
10, 0	200
5, 2.5	137.5

Since the feasible region is an open region so we plot 20x + 15y < 137.5, to check whether the resulting open half plane has any point common with the feasible region. Since it has common points Z = 20x + 15y

There is no optimal minimum value subject to the given constraints.

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Linear Programming Ex 30.3 Q2

Let required quantity of food A and B be x and y units respectively.

Costs of one unit of food A and B are Rs 4 and Rs 3 per unit respectively, so, costs of x unit of food A and y unit of food B are 4x and 3y respectively. Let Z be minimum total cost, so

$$Z = 4x + 3y$$

Since one unit of food A and B contain 200 and 100 units of vitamin respectively. So, X units of food A and Y units of food B contain 200X and 100Y units of vitamin but minimum requirement of vitamin is 4000 units, so

$$200x + 100y \ge 4000$$

 $\Rightarrow 2x + y \ge 40$ (first constraint)

Since one unit of food A and B contain 1 unit and 2 unit of minerals, so X units of food A and Y units of food Y units of minerals respectively but minimum requirement of minerals is 50 units, so

```
x + 2y \ge 50 (second constraint)
```

Since one unit of food A and B contain 40 calories each, so x units of food A and y units of food B contain 40x and 40y calories respectively but minimum requirement of calories is 1400, so

```
40x + 40y \ge 1400
```

```
⇒ 2x + 2y \ge 70

⇒ x + y \ge 35 (third constraint)
```

So, mathematical formulation of LPP is find x and y which minimize Z = 4x + 3y

Subject to constraint,

```
2x + y \ge 40
x + 2y \ge 50
x + y \ge 35
x, y \ge 0
```

[Since quantity of food can not be less than zero]

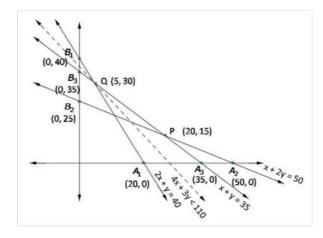
Region $2x + y \ge 40$: Line 2x + y = 40 meets axes at $A_1(20, 0)$, $B_1(0, 40)$ region not containing origin represents $2x + y \ge 40$ as (0,0) does not satisfy $2x + y \ge 40$.

Region $x + 2y \ge 50$: Line x + 2y = 50 meets axes at A_2 (50,0), B_2 (0,25). Region not containing origin represents $x + 2y \ge 50$ as (0,0) does not satisfy $x + 2y \ge 50$.

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Region $x + y \ge 35$: Line x + y = 35 meets axes at $A_3(35,0)$, $B_3(0,35)$. Region containing origin represents $x + y \ge 35$ as (0,0) does not satisfy $x + y \ge 35$.

Region $x, y \ge 0$: It represent first quadrant in xy-plane.



Unbounded shaded region A_2PQB_1 represents feasible region with corner points A_2 (50,0), P (20,15), Q (5,30), B_1 (0,40)

The value of Z = 4x + 3y at

$$A_2(50,0) = 4(50) + 3(0) = 2000$$

$$P(20,15) = 4(20) + 3(15) = 125$$

$$Q(5,30) = 4(5) + 3(30) = 110$$

$$B_1(0,40) = 4(0) + 3(40) = 110$$

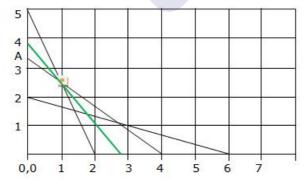
Smallest value of Z = 110

Open half plane 4x + 3y < 110 has no point in common with feasible region, so, smallest value is the minimum value.

Hence,

quantity of food A = x = 5 unit quantity of food B = y = 30 unit minimum cost = Rs 110

Linear Programming Ex 30.3 Q3



Let x & y be the units of Food I and Food II resptly.

The objective function is to minimize the function Z = 0.6x + y such that $10x + 4y \ge 20$ requirement of calcium, line 5-2 $5x + 6y \ge 20$ requirement of protein, line A-4 $2x + 6y \ge 12$ requirement of calories, line 2-6

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These when plotted give 5-F-E-6 an open unbounded region.

The function 20x + 15y < 57.5 needs to be plotted to check if there are any common points. The green line shows that there are no common points. So

Corner point	Value of $Z = 0.6x + y$
0,5	5
F(1, 2.5)	3.1
E(2.67, 1.11)	2.71
6, 0	3.6

The minimum cost occurs when Food I is 1 unit and Food II is 2.5 units. Since it is an unbounded region plotting Z<3.1 gives the green line which has no common points, so (1, 2.5) can be said to be a minimum point.

Linear Programming Ex 30.3 Q4

Let required quantity of food A and food B be x and y units.

Given, costs of one unit of food A and B are 10 paise per unit each, so costs of xunit of food A and y unit of food B are 10x and 10y respectively, let Z be total cost of foods, so

$$Z = 10x + 10y$$

Since one unit of food A and B contain 0.12 mg and 0.10 mg of Thiamin respectively, so, x units of food A and y units of food B contain 0.12x mg and 0.10y mg of Thiamin respectively but minimum requirement of Thiamin is 0.4 mg, so

$$0.12x + 0.10y \ge 0.5$$

$$\Rightarrow 12x + 10y \ge 50$$

$$\Rightarrow$$
 6x + 5y \geq 25 (first constraint)

Since one unit of food A and B contain 100 and 150 Calories respectively, so x units of food A and y units of food B contain 100x and 150y units of Calories but minimum requirement of Calories is 600, so

$$100x + 150y \ge 600$$

$$\Rightarrow$$
 2x + 3y \ge 12

(second constraint)

Hence, mathematical formulation of LPP is find x and y which minimize Z = 10x + 10y

Subject to constraint,

$$6x + 5y \ge 25$$

$$2x + 3y \ge 12$$

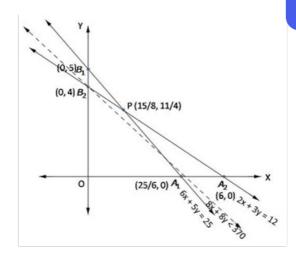
$$x, y \ge 0$$

[Since quantity of food A and B can not be less than zero]

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William Rearing Representations of the second s Region $6x + 5y \ge 25$: 6x + 5y = 25 meets axes at $A_1\left(\frac{25}{6}, 0\right)$, $B_1\left(0, 5\right)$. Region not containing origin represents $6x + 5y \ge 25$ as (0,0) does not satisfy $6x + 5y \ge 25$.

Region $2x + 3y \ge 12$: Line 2x + 3y = 12 meets axes at $A_2(6,0)$, $B_2(0,4)$. Region not containing origin represents $2x + 3y \ge 12$ as (0,0) does not satisfy $2x + 3y \ge 12$.

Region $x, y \ge 0$ represent first quadrant in xy-plane.



Unbounded shaded region $A_2 P B_1$ represents feasible region with corner points $A_2 (6,0)$,

$$P\left(\frac{15}{8}, \frac{11}{4}\right), B_1(0,5)$$

The value of Z = 10x + 10y at

$$A_2(6,0)$$

$$P\left(\frac{15}{8}, \frac{11}{4}\right) = 10\left(\frac{15}{8}\right) + 10\left(\frac{11}{4}\right) = \frac{370}{8} = 46\frac{1}{4}$$

$$B_1(0,5) = 10(0) + 10(5) = 50$$

Smallest value of Z is $46\frac{1}{4}$.

Now open half plane $10x + 10y < \frac{370}{8}$

8x + 8y < 370 has no point in common with feasible region, so smallest value is the minimum value.

Hence,

Required quantity of food
$$A = \frac{15}{8}$$
 units, food $B = \frac{11}{4}$ units



Linear Programming Ex 30.3 Q5

Let required quantity of food X and food Y be x kg and y kg.

Since costs of food X and Y are Rs 5 and Rs 8 per kg., So, costs of food X and food Y are Rs. 5x and Rs. 8y respectively. Let Z be the total cost of food, then

$$Z = 5x + 8y$$

Since one kg of food X and Y contain 1 and 2 unit of vitamin A, so, X kg of food X and Y kg of food Y contain X and Y units of vitamin Y respectively but minimum requirement of vitamin Y is 6 units, so

```
x + 2y \ge 6 (first constraint)
```

Since one kg of food X and Y contain 1 unit of vitamin B each, so X kg of food X and Y kg of food Y contain X and Y units of vitamin Y but minimum requirement of vitamin Y is 7 units, so

```
x + y \ge 7 (second constraint)
```

Since one kg of food X and food Y contain 1 unit and 3 units of vitamin C respectively, so X kg of food X and Y kg of food Y contain X and 3Y units of vitamin Y respectively but minimum requirement of vitamin Y is 11 units, so

```
x + 3y \ge 11 (third constraint)
```

Since 1 kg of food X and food Y contain 2 units and 1 unit of vitamin D respectively, so, X kg of food X and Y kg of food Y contain D and Y units of vitamin D respectively but minimum requirement of vitamin D is 9 units, so

```
2x + y \ge 9 (fourth constraint)
```

Hence, mathematical formulation of LPP is find x and y which minimize Z = 5x + 8y

Subject to constraints,

 $x + 2y \ge 6$ $x + y \ge 7$ $x + 3y \ge 11$ $2x + y \ge 9$

 $x, y \ge 0$

[Since quantity of food X and Y can not be less than zero]

Region $x + 2y \ge 6$: Line x + 2y = 6 meets axes at $A_1(6,0)$, $B_1(0,3)$. Region not containing origin represents $x + 2y \ge 6$ as (0,0) does not satisfy $x + 2y \ge 6$.

Region $x + y \ge 7$: Line x + y = 7 meets axes at $A_2(7,0)$, $B_2(0,7)$ respectively. Region not containing origin represents $x + y \ge 7$ as (0,0) does not satisfy $x + y \ge 7$.

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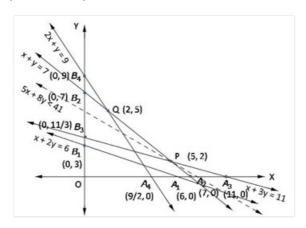


Region $x + 3y \ge 11$: Line x + 3y = 11 meets axes at $A_3\left(11,0\right)$, $B_3\left(0,\frac{11}{3}\right)$ respectively

Region not containing origin represents $x+3y\geq 11$ as (0,0) does not satisfy $x+3y\geq 11$.

Region $2x + y \ge 9$: Line 2x + y = 9 meets axes at $A_4\left(\frac{9}{2}, 0\right)$, $B_4\left(0, 9\right)$ respectively. Region not containing origin represents $2x + y \ge 9$ as $\left(0, 0\right)$ does not satisfy $2x + y \ge 9$.

Region $x, y \ge 0$ it represent first quadrant.



Unbounded shaded region A_2 PQ B_4 is the feasible region with corner points A_3 (11,0), P (5,2), Q(2,5), B_4 (0,9)

The value of Z = 5x + 8y at

$$A_3(11,0) = 5(11) + 8(0) = 55$$

$$P(5,2) = 5(5) + 8(2) = 41$$

$$Q(2,5) = 5(2) + 8(5) = 50$$

$$B_4(0,9) = 5(0) + 8(9) = 72$$

Smallest value of Z is 41.

Now open half plane 5x + 8y < 41 has no point is common with feasible region, os, smallest value of is the minimum value. hence

last cost of mixture= Rs 41

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Linear Programming Ex 30.3 Q6

Let quantity of food F_1 and F_2 be x and y units.

respectively.

Given, costs of one unit of food F_1 and F_2 be Rs 4 and Rs 6 per unit, So, costs of X unit of food F_1 and Y units of food F_2 be 4x and 6y respectively,

Let ${\cal Z}$ be the total cost , so

$$Z = 4x + 8y$$

Since one unit of food F_1 and F_2 contain 3 and 6 unit of vitamin A respectively, so, x units of food F_1 and y units of food F_2 contain 3x and 6y units of vitamin A respectively, but minimum requirement

of vitamin A is 80 units, so

 $3x + 6y \ge 80$

(first constraint)

Since one unit of food F_1 and F_2 contain 4 unit and 3 unit of mineral, so x unit of food F_1 and y unit of food F_2 contain 4x and 3y units of mineral respectively but minimum requirement of minerals be 100 units, so

$$4x + 3y \ge 100$$

 \Rightarrow $4x + 3y \ge 100$

(second constraint)

mathematical formulation of LPP is, Find x and y which minimum

$$Z = 4x + 6y$$

Subject to constraints,

$$3x + 6y \ge 80$$

$$4x + 3y \ge 100$$

 $x, y \ge 0$

since quantity of food can not be less than zero

Region $3x + 6y \ge 80$: line 3x + 6y = 80 meets axes at $A_1\left(\frac{80}{3}, 0\right), B_1\left(0, \frac{40}{3}\right)$ respectively. Region not containing origin represents $3x + 6y \ge 80$ as $\{0,0\}$ does not satisfy $3x + 6y \ge 80$.

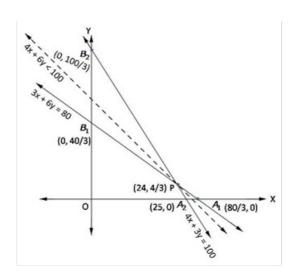
Region $4x + 3y \ge 100$ line 3x + 6y = 100 meets axes at $A_2(25, 0)$, $B_2(0, \frac{100}{3})$ respectively. Region not containing origin represents $4x + 3y \ge 100$ as (0,0) does not satisfy $4x + 3y \ge 100$.

Region $x, y \ge 0$ represents first quadrant

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Unbounded shaded region A_1P B_2 represents feasible region with corner points $A_1\left(\frac{80}{3},0\right)$, $P\left(24,\frac{4}{3}\right)$, $B_2\left(0,\frac{100}{3}\right)$.

The value of Z = 4x + 6y at

$$A_{1}\left(\frac{80}{3},0\right) = 4\left(\frac{80}{3}\right) + 6\left(0\right) = \frac{320}{3}$$

$$P\left(24,\frac{4}{3}\right) = 4\left(24\right) + 6\left(\frac{4}{3}\right) = 104$$

$$B_{2}\left(0,\frac{100}{3}\right) = 4\left(0\right) + 6\left(\frac{100}{3}\right) = 200$$

Smallest value of Z is 104 .Now open half plane 4x + 6y < 104 has no point in common with feasible region so, smallest value is minimum value. Hence,

Minimum cost of mixture = Rs 104



Linear Programming Ex 30.3 Q7

Let required quantity of bran and rice be x kg and y kg. Given, costs of one kg of bran and rice are Rs 5 and Rs 4 per kg, So, costs of X unit of bran and Y kg of rice are 5x and Rs 4y respectively, Let total cost of bran and rice be Z, so,

$$Z = 5x + 4y$$

Since one kg of bran and rice contain 80 and 100 mg of protien, so, x kg of bran and y kg of rice contain 80x and 100y grms of protien respectively, but minimum requirement of protien for kelloggs is 88 gms, so

$$80x + 100y \ge 88$$

$$\Rightarrow$$
 20x + 25y \geq 22

(first constraint)

Since one kg of bran and rice contain 40 mg and 30 mg of iron, so, x kg of bran and y kg of rice contain 40x and 30y mg of iron respectively, but minimum requirement of iron is 36 mg for kelloggs, so

$$40x + 30y \ge 36$$

(second constraint)

Hence, mathematical formulation of LPP is, Find x and y which minimize

$$Z = 5x + 4y$$

subject to constraints,

 $20x + 25y \ge 22$

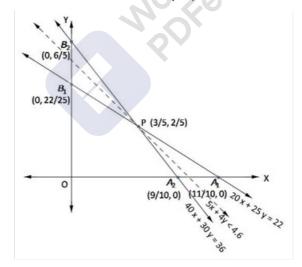
 $40x + 30y \ge 36$

 $x, y \ge 0$

[Since quantity of bran and rice can not be less than zero]

Region $20x + 25y \ge 22$: line 20x + 25y = 22 meets axes at $A_1\left(\frac{11}{10}, 0\right)$, $B_1\left(0, \frac{22}{25}\right)$ respectively. Region not containing origin represents $20x + 25y \ge 22$ as (0,0) does not satisfy $20x + 25y \ge 22$.

Region $40x + 30y \ge 36$ line 40x + 30y = 36 meets axes at $A_2\left(\frac{9}{10}, 0\right), B_2\left(0, \frac{6}{5}\right)$. Region not containing origin represents $40x + 30y \ge 36$ as (0,0) does not satisfy $40x + 30y \ge 36$.



$$A_1\left(\frac{11}{10},0\right) = 5\left(\frac{11}{10}\right) + 4(0) = 5.5$$

$$P\left(\frac{3}{5}, \frac{2}{5}\right) = 5\left(\frac{3}{5}\right) + 4\left(\frac{2}{5}\right) = 4.0$$

$$B_2\left(0, \frac{6}{5}\right) = 5\left(0\right) + 4\left(\frac{6}{5}\right) = 4.8$$

 $(5)^{-4.0}$ $-2\left(0,\frac{7}{5}\right) = 5\left(0\right) + 4\left(\frac{6}{5}\right) = 4.8$ Smallest value of Z is 4.6. Now open half plane 5x + 4y < 4.6 has no point in common with feasible region so, smallest value z is the minimum value.

Hence

Minimum cost of mixture = Rs 4.6

Remove Watermark



Linear Programming Ex 30.3 Q8

Let required number of bag A and bag B be x and y respectively.

Since, costs of each bag A and bag B are Rs 8 and Rs 12 per kg., So, cost of x number of bag A and y number of bag B are Rs 8x and Rs 12y respectively, Let B be total cost of bags, so,

$$Z = 8x + 12y$$

Since, each bag A and B contain 60 and 30 gms. of almonds respectively. so, X bags of A and Y bags of Y contain 60X and 30Y gms. of almonds respectively but, mixtures should contain at least 240 gms almonds, so,

$$60x + 30y \ge 240$$

 $2x + y \ge 8$ (first constraint)

Since, each bag A and B contain 30 and 60 gms. of cashew nuts respectively. so, X bags of A and Y bags of Y contain 30X and 60Y gms. of cashew nuts respectively but, mixtures should contain at least 300 gms of cashew nuts, so,

$$30x + 60y \ge 300$$

⇒ $x + 2y \ge 10$ (second constraint)

Since, each bag A and B contain 30 and 180 gms. of hazel nuts respectively. so, X bags of A and Y bags of Y contain Y contain 30X and 180Y gms. of hazel nuts respectively but, mixtures should contain at least 540 gms of hazel nuts, so,

$$30x + 180y \ge 540$$

 $\Rightarrow x + 6y \ge 18$ (third constraint)

Hence, mathematical formulation of LPP is, Find x and y which maximize

$$Z = 8x + 12y$$
subject to constraints,
$$2x + y \ge 8$$

$$x + 2y \ge 10$$

$$x + 6y \ge 18$$

 $x, y \ge 0$

Since quantity of bags can not be less than zero

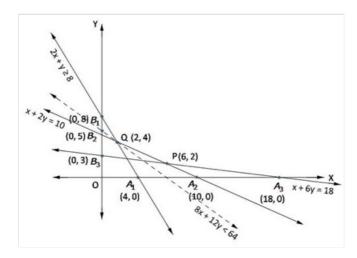
Region $2x + y \ge 8$: line 2x + y = 8 meets axes at $A_1(4,0), B_1(0,8)$ respectively. Region not containing origin represents $2x + y \ge 8$ as (0,0) does not satisfy $2x + y \ge 8$.

Region $x + 2y \ge 10$: line x + 2y = 10 meets axes at $A_2(10,0)$, $B_2(0,5)$ respectively. Region not containing origin represents $2x + y \ge 10$ as (0,0) does not satisfy $x + 2y \ge 10$

t satisfy x + 2y ≥ 10

Region $x + 6y \ge 18$: line x + 6y = 18 meets axes at A_3 (18,0), B_3 (0,3) renot containing origin represents $x + 6y \ge 8$ as (0,0) does not satisfy $x + 6y \ge 8$

Region $x,y \ge 0$: it represents first quadrant.



Unbouded shaded region A_3PQB_1 is feasible region with corner point A_3 (18,0),P (6,2) Q (2,4), B_1 (0,8).P is obtained by solving X+6y=18 and X+2y=10, Q is obtained by solving QX+Y=10

The value of z = 8x + 12y at

$$A_3(18,0) = 8(18) + 12(0) = 144$$

 $P(6,2) = 8(6) + 12(2) = 72$

$$Q(2,4)$$
 = 8(2) + 12(4) = 64
 $B_1(0,8)$ = 8(0) + 12(8) = 96

Smallest value of
$$Z$$
 is 64, open half plane $8x + 12y \ge 64$ has no point is common with feasible region, so, smallest value is the minimum value

Minimum cost = Rs64 quantity of mixture A = 2 kg. quantity of mixture B = 4 kg



Let required number of cakes of type A and B are x and y respectively.

Let Z be total number of cakes ,so,

$$Z = x + y$$

Since one unit of cake of type A and B contain 300 gm and 150 gm flour respectively, so, x unit of cake of type A and y units of cake of type B require 300x and 150y gms of flour respectivley, but maximum flour available is $7.5 \times 1000 = 7500$ qm,so

$$300x + 150y \le 7500$$

$$\Rightarrow$$
 2x + y \le 50

(first constraint)

Since one unit of cake of type A and B contain 15 and 30 gm fat respectively, so, x unit of cake of type A and y units of cake of type B contain 15x and 30y gms of fat respectivley, but maximum fat available is 600 gm, so

$$15x + 30y \le 600$$

$$\Rightarrow x + 2y \le 40$$

(second constraint)

Hence, mathematical formulation of LPP is find x and y which maximize Z = x + y

Subject to constriants,

$$2x+y \le 50$$

$$x + 2y \le 40$$

$$x, y \ge 0$$

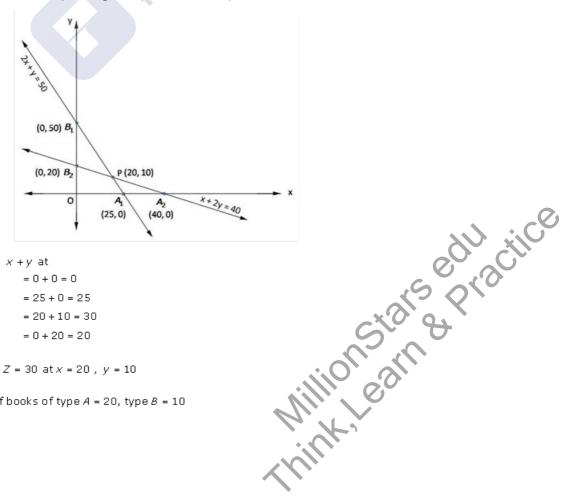
[Since number of cakes can not be less than zero]

Region $2x + y \le 50$: line 2x + y = 50 meets axes at A_1 (25,0), B_1 (0,50) respectively. Region containing origin represents $2x + y \le 50$ as $\{0,0\}$ satisfies $2x + y \le 50$.

Region $x + 2y \le 40$: line x + 2y = 40 meets axes at $A_2(40,0)$, $B_2(0,20)$ respectively. Region containing origin represents $x + 2y \le 40$ as (0,0) satisfies $x + 2y \le 40$.

Region $x, y \ge 0$: it represent first quandrant

Shaded region OA_1PB_2 represents feasible region. Point P(20,10) is obtained by solving x + 2y = 40 and 2x + y = 50



The value of Z = x + y at

$$= 0 + 0 = 0$$

$$A_1$$
 (25,0)

$$= 25 + 0 = 25$$

$$B_2(0,20)$$

maximum Z = 30 at x = 20, y = 10

Number of books of type A = 20, type B = 10

Remove Watermark

Linear Programming Ex 30.3 Q10

Let x kg of food P and y kg of food Q are mixed together to make the mixture.

Then the mathematical model of the LPP is as follows:

Minimize Z = 60x + 80y

Subject to $3x + 4y \ge 8$,

5x + 2y ≥ 11

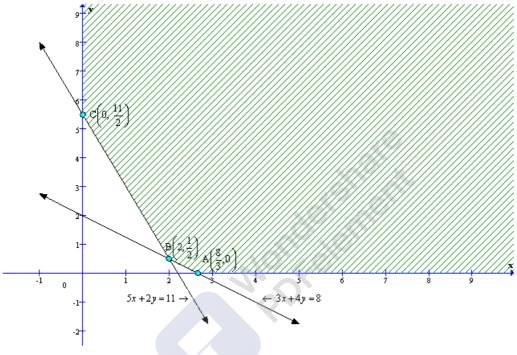
and $x \ge 0$, $y \ge 0$

To solve the LPP we draw the lines,

3x + 4y = 8,

5x + 2y = 11

The feasible region of the LPP is shaded in graph.



The coordinates of the vertices (Corner - points) of shaded feasible region ABC are $A\left(\frac{8}{3}, 0\right), B\left(2, \frac{1}{2}\right)$ and $C\left(0, \frac{11}{2}\right)$

The values of the objective of function at these points are given in the following table:

Point (x_1, x_2)	Value of objective function $Z = 60x + 80 y$
$A\left(\frac{8}{3}, 0\right)$	Z = 160
$B\left(2, \frac{1}{2}\right)$	Z = 160
$C\left(0, \frac{11}{2}\right)$	Z = 440

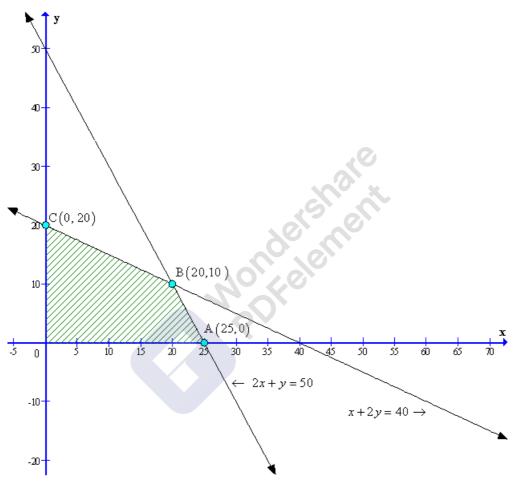
Million Stars & Practice
Anny Property of the Children of the The minimum value of the mixture is Rs. 160 at all points on the line segment joining points $\left(\frac{8}{3}, 0\right)$ and $\left(2, \frac{1}{2}\right)$

Let x be the number of one kind of cake and y be the number of second kind of cakes that are made.

Then the mathematical model of the LPP is as follows: Maximize Z = x + ySubject to 200x + 100y ≤ 5000, 25x + 50y ≤1000 and $x \ge 0$, $y \ge 0$

To solve the LPP we draw the lines, 2x + y = 50,x + 2y = 40

The feasible region of the LPP is shaded in graph.



Million Stars & Practice
Anny Property of the Control of the Contr The coordinates of the vertices (Corner - points) of shaded feasible region ABC are A(25, 0), B(20, 10) and C(0, 20).

The values of the objective of function at these points are given in the following table:

Paint (x_1, x_2)	Value of objective function $Z = x + y$
A (25, 0)	Z = 25
B(20, 10)	Z = 30
C(0, 20)	Z = 20

The maximum of 30 cakes can be made.

Linear Programming Ex 30.3 Q12

Let x be the number of packets of food P y be the number of packets of food Q used to minimize vitamin A.

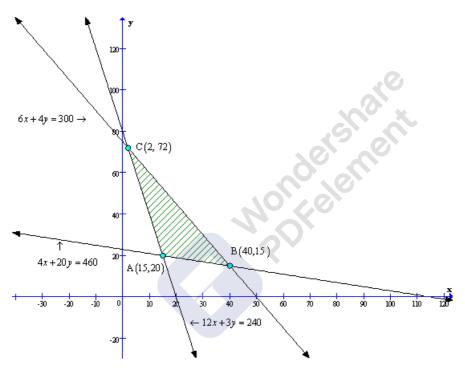
Then the mathematical model of the LPP is as follows:

Minimize Z = 6x + 3ySubject to $12x + 3y \ge 240$, $4x + 20y \ge 460$ $6x + 4y \le 300$ and $x \ge 0$, $y \ge 0$

To solve the LPP we draw the lines,

12x + 3y = 240, 4x + 20y = 460, 6x + 4y = 300

The feasible region of the LPP is shaded in graph.



The coordinates of the vertices (Corner - points) of shaded feasible region ABC are A(15, 20),B(40,15) and C(2, 72).

The values of the objective of function at these points are given in the following table:

Point (x_1, x_2)	Value of objective function $Z = 6x + 3y$
A(15, 20) B(40, 15)	Z = 150
B(40, 15)	Z = 285
C(2, 72)	Z = 228

Million Star & Practice 15 packets of food P and 20 packets of food Q should be used to minimise the amount of vitamin A. The minimum amount of vitamin A is 150 units.

Wondershare **PDFelement**

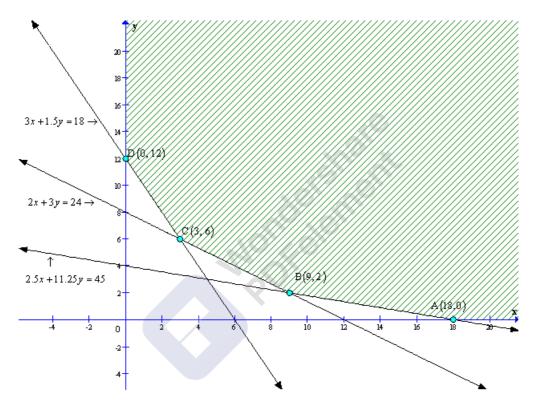
Let x be the number of bags of brand P y be the number of bags of brand Q.

Then the mathematical model of the LPP is as follows: Minimize Z = 250x + 200ySubject to $3x + 1.5y \ge 18$, $2.5x + 11.25y \ge 45$ $2x + 3y \ge 24$

To solve the LPP we draw the lines, 3x + 1.5y = 182.5x + 11.25y = 452x + 3y = 24

and $x \ge 0$, $y \ge 0$

The feasible region of the LPP is shaded in graph.



The coordinates of the vertices (Corner - points) of shaded feasible region ABCD are A(18, 0),B(9,2), C(3, 6) and D(0, 12).

The values of the objective of function at these points are given in the following table:

THE TURBLES OF	are objective or faircaon at arese points are gr	voir iii die followiiig cable.
Point (x_1, x_2)	Value of objective function $Z = 250x + 200y$	1
A(18, 0)	Z = 4500	
B(9, 2)	Z = 2650	O.: (
C(3, 6)	Z = 1950	
D(0,12)	Z = 2400	
having a minu Mimum cost o	id P and 6 bags of brand Q should be mixed in umum cost per bag. f the mixture per bag is = $\frac{1950}{9}$ = Rs. 216.67. en in the book is incorrect.	order to prepare the mixture

Let x be the amount of food X and y be the amount of food Y than to be mixed which will produce the required diet.

Then the mathematical model of the LPP is as follows:

Minimize Z = 16x + 20ySubject to $x + 2y \ge 10$, $2x + 2y \ge 12$ 3x + y ≥8 and $x \ge 0$, $y \ge 0$

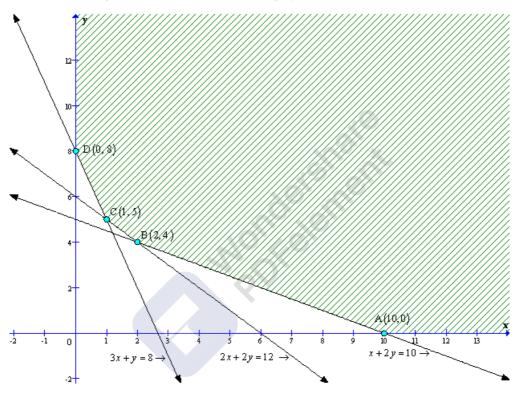
To solve the LPP we draw the lines,

$$x + 2y = 10,$$

$$2x + 2y = 12$$

$$3x + y = 8$$

The feasible region of the LPP is shaded in graph.



The coordinates of the vertices (Corner - points) of shaded feasible region ABCD are A(10, 0),B(2,4), C(1, 5) and D(0, 8).

The values of the objective of function at these points are given in the following table:

Paint (x_1, x_2)	Value of objective function $Z = 16x + 20y$	
A (10, 0)	Z = 160	
B(2, 4)	Z = 112	
C(1, 5)	Z = 116	
D(0, 8)	Z = 160	8) 00
	and 4 kg of food y will be required to mimir of the mixture is Rs. 112.	nize the cost of the diet.

Linear Programming Ex 30.3 Q15

 $Let \times bags \ of \ fertilizer \ P \ and \ y \ bags \ of \ fertilizer \ Q \ used \ in \ the \ garden \ to \ minimize \ the \ usage \ of \ nitrogen.$

Then the mathematical model of the LPP is as follows:

Minimize Z = 3x + 3.5y

Subject to $x + 2y \ge 240$,

 $3x + 1.5y \ge 270$

 $1.5x + 2y \le 310$

and $x \ge 0$, $y \ge 0$

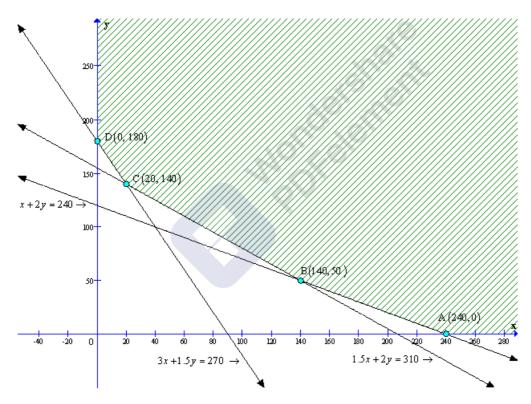
To solve the LPP we draw the lines,

x + 2y = 240

3x + 1.5y = 270

1.5x + 2y = 310

The feasible region of the LPP is shaded in graph.



	•	_
The coordinate	s of the vertices (Corner - points) of shade	d feasible region ABC are
A(40, 100),B(1	140,50) and C(20, 140).	
		70, 410
The values of t	he objective of function at these points are	given in the following table:
Point (x_1, x_2)	Value of objective function $Z = 3x + 3.5y$	5000
A(40, 100)	Z = 470	
B(140, 50)	Z = 595	~x'0, 01,
C(20, 140)	Z = 550	500
40 bags of brar	nd P and 100 bags of brand Q should be use	ed to minimize
	nitrogen added to the garden.	
The minimum	amount of nitrogen added in the garden is	170kg.
	•	
		•



Ex 30.4

Linear Programming Ex 30.4 Q1

Let he drives x km at a speed f 25 km/hr and y km at a speed of 40 km/hr. Let Z be total distance travelled by him, so,

$$Z = x + y$$

Since he spend Rs 2 per km on petrol when speed is 25 km/hr and Rs 5 per km on petrol when speed is 40 km/hr, so, expence on x km and y km are Rs 2x and Rs 5y respectivley, but he has only Rs 100.,so

$$2x + 5y \le 100$$
 (first constraint)

Time taken to travel x km =
$$\frac{\text{Distance}}{\text{speed}}$$
$$= \frac{x}{25} \text{ hr}$$

Time taken to travel $y \text{ km} = \frac{y}{40} \text{ hr}$ Given he has 1 hr to travel, so

$$\frac{x}{25} + \frac{y}{40} \le 1$$

$$\Rightarrow$$
 $40x + 25y \le 1000$

⇒
$$8x + 5y \le 200$$
 (second constraint)

Hence, mathematical formulation of LPP is find x and y which

maximize
$$Z = x + y$$

Subject to constriants,

$$2x + 5y \le 100$$

$$x, y \ge 0$$

[Since distances can not be less than zero]

Region $2x + 5y \le 100$: line 2x + 5y = 100 meets axes at A_1 (50,0), B_1 (0,20) respectively. Region containing origin represents $2x + 5y \le 100$ as (0,0) satisfies $2x + 5y \le 100$.

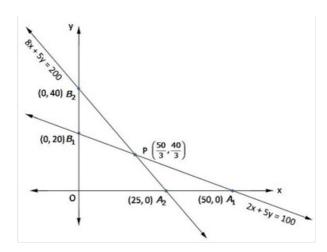
Region $8x + 5y \le 200$: line 8x + 5y = 200 meets axes at A_2 (25,0), B_2 (0,40) respectively. Region containing origin represents $8x + 5y \le 200$ as (0,0) satisfies $8x + 5y \le 200$.

Region $x, y \ge 0$: it represent first quandrant

Shaded region OA2PB1 represents feasible region.

Point
$$P\left(\frac{50}{3}, \frac{40}{3}\right)$$
 is obtained by solving $8x + 5y = 200$, $2x + 5y = 100$

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The value of Z = x + y at

$$O(0,0) = 0 + 0 = 0$$

$$A_2(25,0) = 25 + 0 = 25$$

$$P(\frac{50}{3}, \frac{40}{3}) = \frac{50}{3} + \frac{40}{3} = 30$$

maximum
$$Z = 30 \text{ at } x = \frac{50}{3} \text{ , } y = \frac{40}{3}$$

Mondelshale Distance travelled at speed of 25 km/hr = $\frac{50}{3}$ km and at speed of 40 km/hr = $\frac{40}{3}$ km maximum distance = 30 km.

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Programming Ex 30.4 Q2

Let required quantity of items A and B.

Given, profits on one item A and B are Rs 6 and Rs 4 respectively So, profits on X items of type A and Y items of type B are 6x and Rs 4y respectively, Let total profit be z, so,

$$Z = 6x + 4y$$

Given, machine I works 1 hour and 2 hours on item A and B respectively, so, x number of item A and y number of item B need x hour and 2y hours on machine I respectively, but machine I works at most 12 hours, so

$$x + 2y \ge 12$$
 (first constraint)

Given, machine II works 2 hours and 1 hours on item A and B respectively, so, x number of item A and y number of item B need 2x hours and y hour on machine II , but machine II works maximum 12 hours, so

$$2x + y \ge 12$$
 (second constraint)

Given, machine III works 1 hour and $\frac{5}{4}$ hour on one item A and B respectively, so,

x number of item A and y number of item B need x hour and $\frac{5}{4}y$ hours respectively on machine III , but machine III works at least 5 hours, so

$$x + \frac{5}{4}y \ge 5$$

 $4x + 5y \ge 20$ (third constraint)

Hence, mathematical formulation of LPP is, $\operatorname{Find} x$ and y which miximize

$$z = 6x + 4y$$
subject to constraints,
$$x + 2y \ge 12$$

$$2x + y \ge 12$$

$$4x + 5y \ge 20$$

4x + 5y ≥ 2l

 $x, y \ge 0$

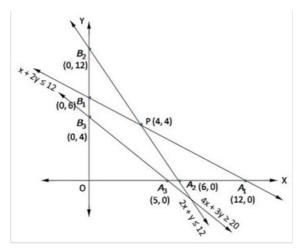
[Since number of item A and B not be less than zero]

Region $x + 2y \ge 12$: line x + 2y = 12 meets axes at $A_1(12,0)$, $B_1(0,6)$ respectively. Region containing origin represents $x + 2y \ge 12$ as (0,0) satisfies $2x + y \ge 12$.

Region $4x + 5y \ge 20$: line 4x + 5y = 20 meets axes at $A_3(5,0)$, $B_3(0,4)$ respectively. Region not containing origin represents $4x + 5y \ge 20$ as (0,0) does not satisfy $4x + 5y \ge 20$.

Region $x,y \ge 0$: it represent first quadrant.

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Shaded region $A_2A_3PB_3B_1$ represents feasible region.

The value of Z = 6x + 4y at

 $A_2(6,0) = 6(6) + 4(0) = 36$

 $A_3(5,0) = 6(5) + 4(0) = 30$

 $B_3(0,4) = 6(0) + 4(4) = 16$

 $B_2(0,6)$ = 6(0) + 4(6) = 24 P(4,4) = 6(4) + 4(4) = 40

Hence, Z is maximum at x = 4, Y = 4

Required number of product A = 4, product B = 4Miximum profit = Rs 40





Linear Programming Ex 30.4 Q3

Suppose tailor A and B work for x and y days respectively.

Since, tailor A and B earn Rs 15 and Rs 20 respectively So, tailor A and B earn is X and Y days Rs 15x and 20y respectively, let Z denote maximum profit that gives minimum labour cost, so,

Z = 15x + 20y

Since, Tailor A and B stitch 6 and 10 shirts respectively in a day, so, tailor A can stitch 6x and B can stitch 10y shirts in x and y days respectively, but it is desired to produce 60 shirts at least, so

 $6x + 10y \ge 60$

 $3x + 5y \ge 30$ (first constraint)

Since, Tailor A and B stitch 4 pants per day each, so, tailor A can stitch 4x and B can stitch 4y pants in x and y days respectively, but it is desired to produce at least 32 pants, so

 $4x + 4y \ge 32$

 $x + y \ge 8$ (second constraint)

Hence, mathematical formulation of LPP is, Find x and y which minimize

Z = 15x + 20y

subject to constraints,

 $3x + 5y \ge 30$

x + y ≥ 8

 $x, y \ge 0$

[Since x and y not be less than zero]

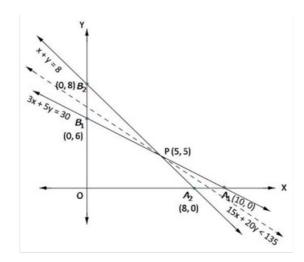
Region $3x + 5y \ge 30$: line 3x + 5y = 30 meets axes at $A_1(10, 0)$, $B_1(0, 6)$ respectively. Region not containing origin represents $3x + 5y \ge 30$ as (0,0) does not satisfy $3x + 5y \ge 30$.

Region $x + y \ge 8$: line x + y = 8 meets axes at $A_2(8,0)$, $B_2(0,8)$ respectively. Region not containing origin represents $x + y \ge 8$ as (0,0) does not satisfy $x + y \ge 8$.

Region $x, y \ge 8$: it represent first quadrant.

Unbounded shaded region A_1PB_2 represents feasible region with corner points $A_1(10,0),P(5,3),B_2(0,8)$.

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The value of Z = 15x + 20y at

$$A_1 (10, 0)$$

$$= 15(5) + 20(3) = 135$$

$$B_2(0,8)$$

$$= 15(0) + 20(8) = 160$$

Smallest value of Z is 135 ,Now open half plane 15x + 20y < 135 has no point in common with feasible region, so smallest value is the minimum value. So,

$$Z = 135$$
, at $x = 5$, $y = 3$

Tailor A should work for 5 days and B should work for 3 days

Linear Programming Ex 30.4 Q4

Let the factory manufacture \boldsymbol{x} screws of type A and \boldsymbol{y} screws of type B on each day. Therefore,

 $x \ge 0$ and $y \ge 0$

The given information can be compiled in a table as follows.

	Screw A	Screw B	Availability
Automatic Machine (min)	4	6	4 × 60 =120
Hand Operated Machine (min)	6	3	4 × 60 =120

The profit on a package of screws A is Rs 7 and on the package of screws B is Rs 10. Therefore, the constraints are

$$4x + 6y \le 240$$

$$6x + 3y \le 240$$

Total profit,
$$Z = 7x + 10y$$

The mathematical formulation of the given problem is

Maximize Z = 7x + 10y ... (1)

subject to the constraints,

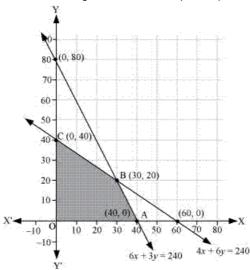
$$4x + 6y \le 240 \dots (2)$$

$$6x + 3y \le 240 \dots (3)$$

$$x, y \ge 0 \dots (4)$$

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The feasible region determined by the system of constraints is



The corner points are A (40, 0), B (30, 20), and C (0, 40).

The values of Z at these corner points are as follows.

Corner point	Z = 7x + 10y	
A(40, 0)	280	
B(30, 20)	410	→ Maximum
C(0, 40)	400	

The maximum value of Z is 410 at (30, 20).

Thus, the factory should produce 30 packages of screws A and 20 packages of screws B to get the maximum profit of Rs 410.





Linear Programming Ex 30.4 Q5

Let required number of belt A and B be x and y. Given, profit on belt A and B be Rs 2 and Rs 1.50 per belt, So, profit on x belt of type A and B belt fo type B be 2x and 1.5y respectively, Let B be total profit, so,

Z = 2x + 1.5y

Since, each belt of type A requires twice as much time as belt B. Let each belt B require 1 hour to make, so, A requires 2 hours. For X and Y belts of type A and Y and Y and Y hours to make but total time available is equal to procduction 1000 belt Y that is 1000 hours, so,

 $2x + y \le 1000$ (first constraint)

Given supply of leather only for 800 belts per day (both A and B combined), so

 $x + y \le 800$ (second constraint)

Buckels available for A is only 400 and for B only 700, so,

 $x \le 400$ (third constraint)

 $y \le 700$ (fourth constraint)

Hence, mathematical formulation of LPP is, $\operatorname{Find} x$ and y which $\operatorname{miximize}$

Z = 2x + 1.5y

subject to constraints,

 $2x + y \le 1000$

 $x + y \le 800$

 $x \le 400$

 $y \le 700$

 $x, y \ge 0$

[Since number of belt can not be less than zero]

Region $2x + y \le 1000$: line 2x + y = 1000 meets axes at A_1 (500,0), B_1 (0,1000) respectively. Region containing origin represents $2x + y \le 1000$ as (0,0) satisfies $2x + y \le 1000$.

Region $x + y \le 800$: line x + y = 800 meets axes at A_2 (800,0), B_2 (0,800) respectively. Region containing origin represents $x + y \le 800$ as (0,0) satisfies $x + y \le 800$.

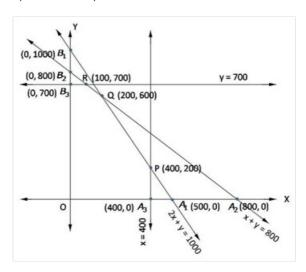
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Region Region $x \le 400$: line x = 400 meets axes is parallel to y axis an $A_3(400,0)$. Region containing origin represents $x \le 400$ as (0,0) satisfies $x \le 400$.

Region Region y \leq 400: line y = 700 is parallel to x- axis and meet y - axis at $B_3(0,700)$. Region containing origin represents y \leq 700 as (0,0) satisfies y \leq 700.

Region $x,y \ge 0$: it represent first quadrant.



Shaded region OA_3PQRB_3 is feasible region, P is points of intersections of 2x + y = 1000 and x = 400, Q is the point of intersection of x + y = 800 and 2x + y = 1000, R is not point of intersection of y = 700, x + y = 800.

The value of Z = 2x + 1.5y at

$$\begin{array}{lll} O\left(0,0\right) & = 2\left(0\right) + 1.5\left(0\right) = 0 \\ A_3\left(400,0\right) & = 2\left(400\right) + 1.5\left(0\right) = 800 \\ P\left(400,200\right) & = 2\left(400\right) + 1.5\left(200\right) = 1100 \\ Q\left(200,600\right) & = 2\left(200\right) + 1.5\left(600\right) = 1300 \\ R\left(100,700\right) & = 2\left(100\right) + 1.5\left(700\right) = 1250 \\ B_3\left(0,700\right) & = 2\left(0\right) + 1.5\left(700\right) = 1050 \end{array}$$

Therefore, maximum Z = 1300, at x = 200, y = 600

Required number belt A = 200 , belt B = 600 maximum profit = Rs 1300





Let required number of deluxe model and ordinary model be x and y respec

Since, profits on each model of deluxe and ordinary type model are Rs 15 and Rs 10 respectively. So, profits on x deluxe models and y ordinary models are 15x and 10y

Let ${\it Z}$ be total profit, then,

$$Z = 15x + 10y$$

Since, each deluxe and ordinary model require 2 and 1 hour of skilled men, so, x deluxe and y ordinary models required 2x and y hours of skilled men but time available by skilled men is $5 \times 8 = 40$ hours, So,

$$2x + y \le 40$$
 (first constraint)

Since, each deluxe and ordinary model require 2 and 3 hours of semi-skilled men, so, x deluxe and y ordinary models require 2x and 3y hours of semi-skilled men respectively but total time available by semi-skilled men is $10 \times 8 = 80$ hours, So,

$$2x + 3y \le 80$$
 (second constraint)

Hence, mathematical formulation of LPP is, Find x and y which maximize Z = 15x + 10y subject to constraints,

$$2x+y \le 40$$

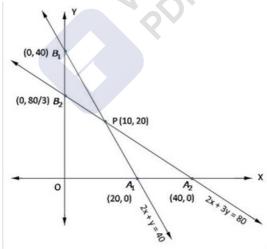
$$2x + 3y \le 80$$

$$x,y \ge 0$$

[Since number of deluxe and ordinary models can not be less than zero]

Region $2x + y \le 40$: line 2x + y = 40 meets axes at $A_1(20,0), B_1(0,40)$ respectively. Region containing origin represents $2x + y \le 40$ as (0,0) satisfies $2x + y \le 40$.

Region $2x + 3y \le 80$: line 2x + 3y = 80 meets axes at $A_2(40, 0)$, $B_2(0, \frac{80}{3})$ respectively. Region containing origin represents $2x + 3y \le 80$.



The value of Z = 15x + 10y at

$$(0,0) = 15(0) + 10(0) = 0$$

$$A_1(20,0) = 15(20) + 10(0) = 300$$

$$P(10,20) = 15(10) + 10(20) = 350$$

$$B_2\left(0, \frac{80}{3}\right) = 15\left(0\right) + 10\left(\frac{80}{3}\right) = \frac{800}{3}$$

Therefore, maximum Z = 350, at x = 10, y = 20

Required number deluxe model = 10 number of ordinary model = 600 maximum profit =Rs 350





Linear Programming Ex 30.4 Q7

Let required number of tea-cups of type A and B are x and y respectively.

Since, profits on each tea-cups of type A and B are 75 paise and 50 paise So, profits on X tea-cups of type A and Y tea-cups of type B are 75X and 50Y respectively, Let total profit on tea-cups be Z, so, Z = 75X + 50Y

Since, each tea-cup of type A and B require to work machine I for 12 and 6 minutes respectively so, x tea cups of type B require to work on machine I for 12x and 6y minutes respectively . Total time available on machine I is $6 \times 60 = 360$ minutes. so,

 $12x + 6y \ge 360$ (first constraint)

Since, each tea-cup of type A and B require to work machine II for 18 and 0 minutes respectively so, x tea cups of type A and y tea cups of B require to work on machine II for 18x and 0y minutes respectively but Total time available on machine II is $6 \times 60 = 360$ minutes. so,

 $18x + 0y \ge 360$ (second constraint) $x \le 20$

Since, each tea-cup of type A and B require to work machine III for 6 and 9 minutes respectively so, x tea cups of type A and y tea cups of B require to work on machine III for 6x and 9x minutes respectively. Total time available on machine III is $6 \times 60 = 360$ minutes. so,

 $6x + 9y \ge 360$ (third constraint)

Hence, mathematical formulation of LPP is, Find x and y which maximize Z = 75x + 50y subject to constraints,

subject to constraints, $12x + 6y \le 360$ $x \le 20$ $6x + 9y \le 360$ $x, y \ge 0$

[Since production of tea cups can not be less than zero]

Region $12x + 6y \le 360$: line 12x + 6y = 360 meets axes at $A_1(30,0)$, $B_1(0,60)$ respectively. Region containing origin represents $12x + 6y \le 360$ as (0,0) satisfies $12x + 6y \ge 360$.

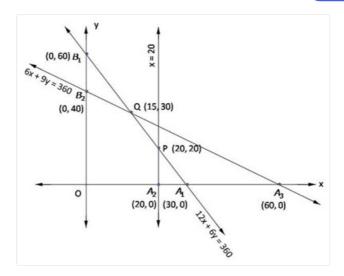
Region $x \le 20$: line x = 20 is parallel to y – axes and meets x – axes at A_2 (20,0). Region containing origin represents $x \le 20$ as (0,0) satisfies $x \le 20$.

Region $6x + 9y \le 360$: line 8x + 9y = 360 meets axes at $A_3(60,0)$, $B_2(0,40)$ respectively. Region containing origin represents $6x + 9y \le 360$ as (0,0) satisfies $6x + 9y \ge 360$.

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Region $x, y \ge 0$: it represents first quadrant.



Shaded region OA_2PQB_2 is the feasible region P is point obtained by solving X = 20 and 12X + 6y = 360 and Q is point obtained by solving 12X + 6y = 360 and 6X + 9y = 360.

The value of Z = 75x + 50y at

O(0,0) = 75(0) +50(0) = 0 $A_2(20,0)$ = 75(20) +50(0) = 1500 P(20,20) = 75(20) +50(20) = 2500 Q(15,30) = 75(15) +50(30) = 2624 $B_2(0,40)$ = 75(0) +50(40) = 2000

Hence, Z is maximum at x = 15, Y = 30

Therefore,

15 teacups of type A and 30 tea-cups f type B are needed to maximize profit



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MILLIONSTAR near Programming Ex 30.4 Q8

t required number of machine A and B are x and y respectively.

Since, production of each machine A and B are 60 and 40 units daily respectively,So, productions by x number of machine A and y number of machine B are 60x and 40y respectively, Let Z denote total output daily, so,

$$Z = 60x + 40y$$

Since, each machine of type A and B require 1000 sq.m and 1200 sq.m area so, x machine of type A and y machine of type B require 100x and 1200y sq.m area but, Total area available for machine is 7600 sq.m. so,

$$1000x + 1200y \le 7600$$

5x + 6y \le 38 (first constraint)

Since, each machine of type A and B require 12 men and 8 men to work respectively so, x machine of type A and y machine of type B require 12x and 8y men to work respectively but, Total 72 men available for work so,

$$12x + 8y \le 72$$

 $3x + 2y \le 18$ (second constraint)

Hence, mathematical formulation of LPP is, Find \boldsymbol{x} and \boldsymbol{y} which maximize

$$Z = 60x + 40y$$
subject to constraints,
$$5x + 6y \le 38$$

$$3x + 2y \le 18$$

$$x, y \ge 0$$

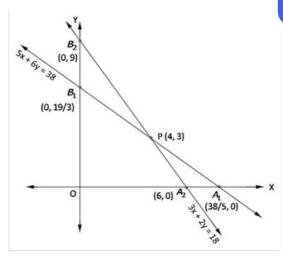
[Number of machines can not be less than zero]

Region $5x + 6y \le 38$: line 5x + 6y = 38 meets axes at $A_1\left(\frac{38}{5}, 0\right), B_1\left(0, \frac{19}{3}\right)$ respectively. Region containing origin represents $5x + 6y \le 38$ as origin satisfies $5x + 6y \ge 38$.

Region $3x + 2y \le 18$: line 3x + 2y = 18 meets axes at $A_2(6,0)$, $B_2(0,9)$ respectively. Region containing origin represents $3x + 2y \le 18$ as (0,0) satisfies $3x + 2y \le 18$.

Region $x,y \ge 0$: it represents first quadrant.

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Shaded region OA_2PB_1 is the feasible region P(4,3) is obtained by solving 3x + 2y = 18 and 5x + 6y = 38

The value of Z = 60x + 40y at

$$O(0,0) = 60(0) + 40(0) = 0$$

$$A_{3}(6,0) = 60(6) + 40(0) = 360$$

$$P(4,3) = 60(4) + 40(3) = 360$$

$$B_1\left(0, \frac{19}{3}\right) = 60(0) + 40\left(\frac{19}{3}\right) = \frac{760}{3}$$

Therefore maximum Z = 360 at x = 4, Y = 3 or x = 6, y = 0

Wondershare Wondershare Output is maximum when 4 machines of type A and 3 machine of type B or 6 machines of type A and no machine of type B.



Linear Programming Ex 30.4 Q9

Let number of goods A and B are x and y respectively.

Since, profits on each A and B are Rs 40 and Rs 50 respectively. So, profits on x of type A and y of type B are 40x and 50y respectively, Let Z be total profit on A and B, so,

$$Z = 40x + 50y$$

Since, each A and B require 3 gm and 1 gm of silver respectively. so, x of type A and y type B require 3x and y gm silver respectively but, Total silver available is 9 gm. so,

```
3x + y \le 9 (first constraint)
```

Since, each A and B require 1 gm and 2 gm of gold respectively. so, x of type A and y type B require x and 2y gm of gold respectively but, Total gold available is 8 gm, so,

```
x + 2y \le 8 (second constraint)
```

Hence, mathematical formulation of LPP is, Find \boldsymbol{x} and \boldsymbol{y} which maximize

$$Z = 40x + 50y$$

Subject to constraints,

 $3x + y \le 9$

 $x + 2y \le 8$

 $x, y \ge 0$

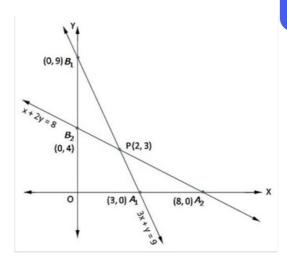
[Since production of A and B can not be less than zero]

Region $3x + y \le 9$: line 3x + y = 9 meets axes at $A_1(3,0), B_1(0,9)$ respectively. Region containing origin represents $3x + y \le 9$ as (0,0) satisfies $3x + y \ge 9$.

Region $x + 2y \le 8$: line x + 2y = 8 meets axes at $A_2(8,0)$, $B_2(0,4)$ respectively. Region containing origin represents $x + 2y \le 8$ as (0,0) satisfies $x + 2y \le 8$.

Region $x,y \ge 0$: it represents first quadrant.

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Shaded region OA_2PB_2 is the feasible region.Point P (2, 3) is obtained by solving 3x + y = 9 and x + 2y = 8

The value of Z = 40x + 50y at

$$O(0,0) = 40(0) + 50(0) = 0$$

$$= 40 (3) + 50 (0) = 120$$

$$=40(2)+50(3)=230$$

$$B_2(0,4)$$

$$= 40(0) + 50(4) = 200$$

Therefore maximum Z = 230 at x = 2, Y = 3

Hence,

Maximum profit = Rs 230 number of goods of type A = 2, type B = 3



Linear Programming Ex 30.4 Q10

Let daily production of chairs and tables be x and y respectively.

Since, profits on each chair and table are Rs 3 and Rs 5. So, profits on x number of chairs and y number of tables are Rs 3x and Rs 5y respectively, Let Z be total profit on table and chair, so,

$$Z = 3x + 5y$$

Since, each chair and table require 2 hrs and 4 hrs on machine A respectively. so, x number of chair and y number of table require 2x and 4y hrs on machine A respectively but, maximum time available on machine A be 16 hrs, so,

$$2x + 4y \le 16$$

 $x + 2y \le 8$ (first constraint)

Since, each chair and table require 6 hrs and 2 hrs on machine B. so, x number of chair and y number of table require 6x and 2y hrs on machine B respectively but, maximum time available on machine B be 30 hrs, so,

$$6x + 2y \le 30$$

 $3x + y \le 15$ (second constraint)

Hence, mathematical formulation of LPP is, Find x and y which maximize

$$Z = 3x + 5y$$
subject to constraints,
$$x + 2y \le 8$$

$$3x + y \le 15$$

$$x, y \ge 0$$

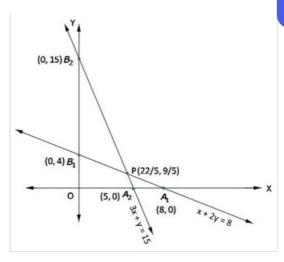
[Since production of chair and table can not be less than zero]

Region $x+2y \le 8$: line x+2y=8 meets axes at A_1 (8,0), B_1 (0,4) respectively. Region containing origin represents $x+2y \le 8$ as (0,0) satisfies $x+2y \le 8$.

Region $3x + y \le 15$: line 3x + y = 15 meets axes at $A_2(5,0)$, $B_2(0,15)$ respectively. Region containing origin represents $3x + y \le 15$ as $\{0,0\}$ satisfies $3x + y \le 15$.

Region $x, y \ge 0$: it represents first quadrant.

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Shaded region $O(A_2PB_1)$ representa feasible region.Point $P\left(\frac{22}{5}, \frac{9}{5}\right)$ is obtained by solving x + 2y = 8and 3x + y = 15

The value of Z = 3x + 5y at

$$A_{2}$$
 (5,

$$P\left(\frac{22}{5}, \frac{9}{5}\right)$$

$$P\left(\frac{22}{5}, \frac{9}{5}\right) = 3\left(\frac{22}{5}\right) + 5\left(\frac{9}{5}\right) = \frac{111}{5} = 22.2$$

$$B_1(0, 4) = 3(0) + 5(4) = 20$$

$$B_1(0,4)$$

$$=3(0)+5(4)=20$$

Maximum Z = 22.2 at $x = \frac{22}{5}$, $y = \frac{9}{5}$

$$P\left(\frac{22}{5}, \frac{9}{5}\right) = 3\left(\frac{22}{5}\right) + 5\left(\frac{9}{5}\right) = \frac{111}{5} = 22.2$$

$$B_1(0, 4) = 3(0) + 5(4) = 20$$

$$\text{mum } Z = 22.2 \text{ at } x = \frac{22}{5}, y = \frac{9}{5}$$

$$\text{Daily production of chair} = \frac{22}{5}, \text{ table} = \frac{9}{5}$$

$$\text{maximum profit} = \text{Rs } 22.2$$



Let required production of chairs and tables be x and y.

Since, profits on each chair and table are Rs 45 and Rs 80, So, profits on x number of chairs and y number of tables are Rs 45x and Rs 80y, Let Z be total profit on tables and chairs, so,

$$Z = 45x + 80y$$

Since, each chair and table require 5 sq.ft. and 20 sq.ft. of wood respectively. so, x number of chair and y number of table require 5x and 20y sq.ft. of wood respectively but, 400 sq.ft. of wood is available, so,

$$5x + 20y \le 400$$

 $\Rightarrow x + 4y \le 80$

(first constraint)

Since, each chair and table require 10 and 25 men-hrs respectively. so, x number of chairs and y number of tables require 10x and 25y men-hrs respectively but, only 450 men-hrs are available, so,

$$10x + 25y \le 450$$

 $\Rightarrow 2x + 5y \le 90$

(second constraint)

Hence, mathematical formulation of LPP is, Find x and y which maximize Z = 45x + 80y

2 - 10/ 1 00/

Subject to constraints, $x + 4y \le 80$

 $2x + 5y \le 90$

 $x, y \ge 0$

[Since production of tabel and chair can not be less than zero]

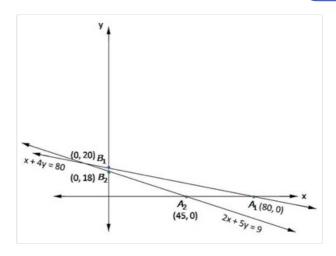
Region $x + 4y \le 80$: line x + 4y = 80 meets axes at $A_1 (80,0)$, $B_1 (0,20)$ respectively. Region containing origin represents $x + 4y \le 80$ as (0,0) satisfies $x + 4y \le 80$.

Region $2x + 5y \le 90$: line 2x + 5y = 90 meets axes at A_2 (45,0), B_2 (0,18) respectively. Region containing origin represents $2x + 5y \le 90$ as (0,0) satisfies $2x + 5y \le 90$.

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Region $x, y \ge 0$: it represents first quadrant.



Shaded region OA_2B_2 is the feasible region.

The value of
$$Z = 45x + 80y$$
 at

$$O(0,0) = 45(0) + 80(0) = 0$$

$$A_2$$
 (45, 0) = 45 (45) + 80 (0) = 2025

$$B_2(0,18) = 45(0) + 80(18) = 1440$$

Therefore,

Maximum
$$Z = 2025$$
 at $x = 45, y = 0$

a, tables = 0 Profit is maximum when number of chairs = 45, tables = 0 profit = Rs 2025



Let required production of product A and B be x and y respectively.

Since, profit on each product A and B are Rs 3 and Rs 4 respectively, So, profit on x product A and y product B are Rs 3x and Rs 4y respectively, Let Z be the total profit on product, so,

$$Z = 3x + 4y$$

Since, each product A and B requires 4 minutes each on machine M_1 , so, X product A and Y product Y and Y minutes on machine Y respectively but maximum available time on machine Y is 8 hrs 20 min.=500 min.so,

Since, each product A and B requires 8 minutes and 4 min. on machine M_2 respectively. so, x product A and B require 8B and 4B min. respectively on machine B0 but, maximum available time on machine B1 is 10 hrs = 600 min. so,

$$8x + 4y \le 600$$

 $2x + y \le 150$ (second constraint)

Hence, mathematical formulation of LPP is, Find x and y which maximize Z=3x+4y subject to constraints,

$$x + y \le 125$$
$$2x + y \le 150$$
$$x, y \ge 0$$

[Since number of product can not be less than zero]

Region $x+y \le 125$: line x+y=125 meets axis at A_1 (125,0), B_1 (0,125) respectively. Region $x+y \le 125$ contains origin represents as (0,0) satisfies $x+y \le 125$.

Region $2x + y \le 150$: line 2x + y = 150 meets axis at A_2 (75,0), B_2 (0,150) respectively. Region containing origin represents $2x + y \le 150$ as (0,0) satisfies $2x + y \le 150$

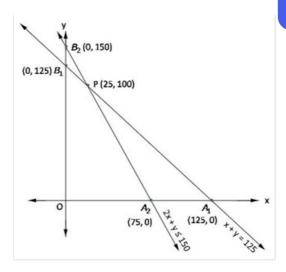
Region $x,y \ge 0$: it represents first quadrant.

Shaded region OA_2PB_1 is feasible region P (25,100) is obtained by solving x + y = 125 and 2x + y = 150

ring x + y = 125

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The value of Z = 3x + 4y at

$$= 3(0) + 4(0) = 0$$

$$A_2$$
 (75, 0)

$$= 3(75) + 4(0) = 225$$

$$= 3(25) + 4(100) = 475$$

$$B_1(0,125)$$

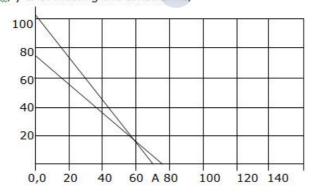
$$= 3(0) + 4(125) = 500$$

Maximum profit = Rs 500, product A = 0 product B = 125

Linear Programming Ex 30.4 Q13

	Item A	Item B	
	X	У	
Motors	3x	2y	≤ 210
Transformer	4x	4y	≤ 300
Profit Rs.	20x	30y	Maximize

The above LPP can be presented in a table above. Aim is to find the values of x & y that maximize the function Z = 20x + 30y, subject to the conditions $3x + 2y \le 210$; gives x=0, y=105 & y=0, x=70 $4x + 4y \le 300$; gives x=0, y=75 & y=0, x=75 &, $y \ge 0$. Plotting the constraints,



The feasible region is 80-B-A-0,0 Tabulating the value of Z at the corner points

Corner point	Value of $Z = 20x + 30y$
0, 0	0
0, 75	2250
70, 0	1400
60, 15	1650

The maximum occur with the production of 0 units of Item A and 75 units of Item B, with a value of Rs. 2250/-



Let number of I product and II product produced are x and y respectively.

Since, profits on each unit of product I and product II are 2 and 3 monetary unit, So, profits on x units of product I and y units of product II are 2x and 3y monetary units respectively, Let Z be total profit, so,

$$Z = 2x + 3y$$

Since, each product I and II require 2 and 4 units of resources A, so, x units of product I and y units of product II require 2x and 4y units of resource A respectively, but maximum available quantity of resource A is 20 units. so,

$$2x + 4y \le 20$$

 $\Rightarrow x + 2y \le 10$ (first constraint)

Since, each product I and II require 2 and 4 units of resource B each, so, x units of product I and y units of product II require 2x and 2y units of resource B respectively, but maximum available quantity of resource B is 12 units. so,

$$2x + 2y \le 12$$

 $\Rightarrow x + y \le 6$ (second constraint)

Since, each units of product I require 4 units of resource C. It is not required by product II, so, x units of product I require 4x units of resource C, but maximum available quantity of resource C is 16 units. so,

$$4x \le 16$$

 $\Rightarrow x \le 6$ (Third constraint)

Hence, mathematical formulation of LPP is, Find ${\it x}$ and ${\it y}$ which maximize

$$Z = 2x + 3y$$

Subject to constraints,

 $x + 2y \le 10$ $x + y \le 6$ $x \le 4$ $x, y \ge 0$

[Since production fo I and II can not be less than zero]

Region $x + 2y \le 10$: line x + 2y = 10 meets axes at $A_1(10, 0)$, $B_1(0, 5)$ respectively. Region containing origin represents $x + 2y \le 10$ as (0,0) satisfies $x + 2y \le 10$.

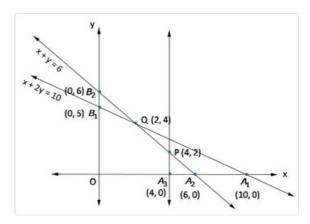
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Region $x + y \le 6$: line x + y = 6 meets axes at $A_2(6,0)$, $B_2(0,6)$ respect containing origin represents $x + y \le 6$ as (0,0) satisfies $x + y \le 6$.

Region $x \le 4$: line x = 4 is parallel to y - axis and meets y-axis at A_3 (4,0). Region containing origin represents $x \le 4$ as (0,0) satisfies $x \le 4$

Region $x,y \ge 0$: it represents first quadrant.



Shaded region OA_3PQB_1 represents feasible region P(4,2) is obtained by solving x = 4 and x + y = 6, Q(2,4) is obtained by solving x + y = 6 and x + 2y = 10.

The value of Z = 2x + 3y at

$$O(0,0) = 2(0) + 3(0) = 0$$

$$A_3(4,0) = 2(4) + 3(0) = 8$$

$$P(4,2) = 2(4) + 3(2) = 14$$

$$Q(12,4) = 2(12) + 3(4) = 16$$

$$B_1(0,5) = 2(0) + 3(5) = 15$$

Maximum Z = 16 at x = 2, y = 4

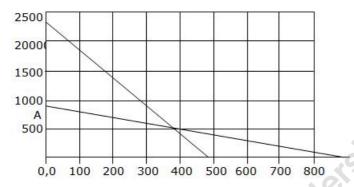
First product = 2 units, second product = 4 unit

Maximum profit = 16 monetary units

	Hardcover	Paperback	
111	X	у	
Printing time	5x	5y	≤ 4800
Binding time	10x	2y	≤ 4800
Selling price Rs.	72x	40y	Maximize

The above LPP can be presented in a table above.

Aim is to find the values of x & y that maximize the function Z = 72x + 40y, subject to the conditions $5x + 5y \le 4800$; gives x=0, y=960 & y=0, x=960 $10x + 2y \le 4800$; gives x=0, y=2400 & y=0, x=480 &, $y \ge 0$. Plotting the constraints,



The feasible region is A-B-480-0,0 Tabulating the value of Z at the corner points

Corner point	Value of $Z = 72x + 40y$
0,0	0
0,480	19200
360, 600	49920
480, 0	34560

The maximum occurs with the production of 360 units of Hardcover books and 600 units of Paperback books, with a value of Rs. 49920/-. This the selling price.

Cost price = fixed cost + variable cost

= 9600 + 56x360 + 28x600 = 46560

Profit = Selling price - cost price = 49920-46560

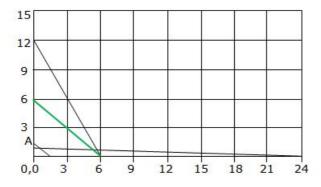
= Rs. 3360

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	Pill size A	Pill size B	
	X	У	
Aspirin	2x	1.y	≥ 12
Bicarbonate	5x	8y	≥ 7.4
Codeine	1.x	66y	≥ 24
Relief	x	У	Minimize

The above LPP can be presented in a table above. Aim is to find the values of x & y that minimize the function Z=x+y, subject to the conditions $2x+y\geq 12$; gives x=0, y=12 & y=0, x=6 $5x+8y\geq 7.4$; gives x=0, y=7.4/8 & y=0, x=7.4/5 $x+66y\geq 24$; gives x=0, y=4/11 & y=0, x=24 &, $y\geq 0$. Plotting the constraints,



The feasible region is 12-C-24 Tabulating the value of Z at the corner points

Corner point	Value of $Z = x + y$
0, 12	12
24, 0	24
5.86, 0.27	6.13

The minimum occurs with 5.86 pills of size A and 0.27 pills of size B. since the feasible region is unbounded plot x+y < 6.13. the green line shows here are no common points with the unbounded feasible region so the obtained point is the point that gives minimum pills to be consumed.

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Let required quantity of compound A and B are x and y kg.

Since, cost of one kg of compound A and B are Rs 4 and Rs 6 per kg.So, cost of x kg. of compound A and y kg. of compound B are Rs 4x and Rs 6y respectively, Let Z be the total cost of compounds, so,

$$Z = 4x + 6y$$

Since, compound A and B contain 1 and 2 units of ingredient C per kg. respectively, so, X kg. of compound A and Y kg. of compound B contain X and Y units of ingredient Y respectively but minimum requirement of ingredient Y is 80 units, so,

$$x + 2y \ge 80$$
 (first constraint)

Since, compound A and B contain 3 and 1 unit of ingredient D per kg. respectively, so, X kg. of compound A and Y kg. of compound B contain A and Y units of ingredient D respectively but minimum requirement of ingredient D is 75 units, so,

$$3x + y \ge 75$$
 (second constraint)

Hence, mathematical formulation of LPP is, Find x and y which minimize Z = 4x + 6y

Subject to constraints,

 $x + 2y \ge 80$

 $3x + y \ge 75$

 $x, y \ge 0$

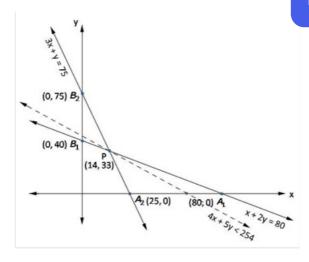
[Since production can not be less than zero]

Region $x + 2y \ge 80$: line x + 2y = 80 meets axes at $A_1 (80, 0), B_1 (0, 40)$ respectively. Region not containing origin represents $x + 2y \ge 80$ as (0,0) does not satisfy $x + 2y \ge 80$.

Region $3x + y \ge 75$: line 3x + y = 75 meets axes at $A_2(25,0), B_2(0,75)$ respectively. Region not containing origin represents $3x + y \ge 75$ as $\{0,0\}$ does not satisfy $3x + y \ge 75$.

Region $x,y \ge 0$: it represents first quadrant.

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Unbouded shaded region A_1PB_2 represents feasible region, point P is obtained by solving x + 2y = 80 and 3x + y = 75

The value of Z = 4x + 6y at

$$A_1(80,0) = 4(80) + 6(0) = 320$$

$$P(14,33) = 4(14) + 6(33) = 254$$

$$B_2(0,75) = 4(0) + 6(75) = 450$$

Smallest value of Z = 254 open half plane 4x + 6y < 254 has no point in common with feasible region, so,

Smallest value is the minimum value.

Minimum cost=Rs 254 quantity of A = 14 kg

quantity of B = 33 kg

Linear Programming Ex 30.4 Q18

Let the company manufacture x souvenirs of type A and y souvenirs of type B. Therefore,

 $x \ge 0$ and $y \ge 0$

The given information can be complied in a table as follows.

	Type A	Туре В	Availability
Cutting (min)	5	8	3 × 60 + 20 =200
Assembling (min)	10	8	4 × 60 = 240

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Anny Francisco The profit on type A souvenirs is Rs 5 and on type B souvenirs is Rs 6. Therefore, the constraints are

$$5x + 8y \le 200$$

$$10x + 8y \le 240$$
 i.e., $5x + 4y \le 120$

Total profit, Z = 5x + 6y

The mathematical formulation of the given problem is

Maximize Z = 5x + 6y ... (1)

subject to the constraints,

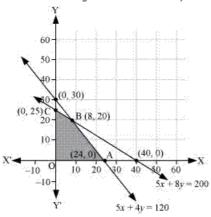
 $5x + 8y \le 200 \dots (2)$

 $5x + 4y \le 120 \dots (3)$

 $x, y \ge 0 ... (4)$



The feasible region determined by the system of constraints is as follows:



The corner points are A (24, 0), B (8, 20), and C (0, 25).

The values of Z at these corner points are as follows.

Corner point	Z = 5x + 6y	
A(24, 0)	120	
B(8, 20)	160	→ Maximum
C(0, 25)	150	

The maximum value of Z is 200 at (8, 20).

Thus, 8 souvenirs of type A and 20 souvenirs of type B should be produced each day to get the maximum profit of Rs 160.









Let required number of product A and B be x and y respectively.

Since, profit on each product A and B are Rs 20 and Rs 30 respectively.So, x number of product A and Y number of product B gain profits of Rs 20x and Rs 30y respectively, Let Z be total profit then,

$$Z = 20x + 30y$$

Since, selling prices of each product A and B are Rs 200 and Rs 300 respectively, so, revenues earned by selling x units of product A and y units of product B are 200x and 300y respectively but weekly turnover must not be less than Rs 10000, so,

$$200x + 300y \ge 10000$$

2x + 3y \ge 100 (first constraint)

Since, each product A and B require $\frac{1}{2}$ and 1 hr.to make so, x units of product A and

y units of product B are $\frac{1}{2}x$ and y hrs. to make respectively but working time available is 40 hrs maximum, so,

$$\frac{1}{2}x + y \le 40$$

$$x + 2y \le 80$$
 (second constraint)

There is a permanent order of 14 and 16 of product A and B respectively, so,

$$x \ge 14$$

 $y \ge 16$ (third and fourth constraint)

Hence, mathematical formulation of LPP is, $\operatorname{Find} x$ and y which miximize

$$Z = 20x + 30y$$

Subject to constraints,

 $2x + 3y \ge 100$ $x + 2y \le 80$

x ≥ 40

y ≥ 14

 $x, y \ge 0$

[Since production can not be less than zero]

Region $2x + 3y \ge 100$: line 2x + 3y = 100 meets axes at $A_1(50,0)$, $B_1(0,\frac{100}{3})$ respectively. Region not containing origin represents $2x + 3y \ge 100$ as (0,0) does not satisfy $2x + 3y \ge 100$.

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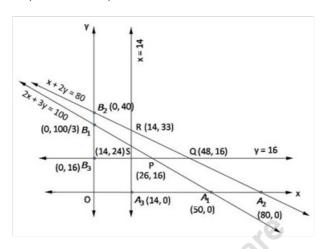


Region $x + 2y \le 80$: line x + 2y = 80 meets axes at $A_2(80,0)$, $B_2(0,40)$ not containing origin represents $x + 2y \le 80$ as (0,0) satisfies $x + 2y \le 80$.

Region $x \ge 14$: line x = 14 is parallel to y-axis and meets x-axis at $A_3(14,0)$. Region not containing origin represents $x \ge 14$ as (0,0) does not satisfy $x \ge 14$.

Region y \geq 16: line y = 16 is parallel to x-axis and meets y-axis at B_3 (0, 16). Region not containing origin represents $y \geq$ 16 as (0,0) does not satisfy $y \geq$ 16.

Region $x,y \ge 0$: it represents first quadrant.



Shaded region PQRS represents feasible region. Point P (26, 16) is obtained by solving y = 16 and 2x + 3y = 100, Q (48, 16) is obtained by solving y = 16 and x + 2y = 80, R (14, 33) is obtained by solving x = 14 and x + 2y = 80, S (14, 24) is obtained by solving x = 14 and 2x + 3y = 100

The value of Z = 20x + 30y at

P(26,16) = 20(26) + 30(16) = 1000 Q(48,16) = 20(48) + 3(16) = 1440 R(14,33) = 20(14) + 3(33) = 1270 S(14,24) = 20(14) + 3(24) = 1000

maximum Z = 1440 at x = 48, y = 16Number product A = 48, product B = 16maximum profit = Rs 1440

Willion Stars by actice

Let required number of trunk I and trunk II be x and y respectively.

Since, profit on each trunk I and trunk II are Rs 30 and Rs 25 respectively. So, profit on x trunk of type I and y trunk of type II are Rs 30x and Rs 25y respectively, Let total profit on trunks be Z, so,

$$Z = 30x + 25y$$

Since, each trunk I and trunk II is reequired to work 3 hrs each on machine A, so, x trunk I and y trunk II is required 3x and 3y hrs

respectively to work on machine A but machine A can work for at most 18 hrs, so,

(first constraint)

Since, each trunk I and II is reequired to work 3 hrs and 2 hrs on machine B, so, x trunk I and y trunk II is required 3x and 2y hrs to work respectively on machine B but machine B can work for at most 15 hrs, so,

$$3x + 2y \le 15$$

(second constraint)

Hence, mathematical formulation of LPP is, Find x and y which miximize Z = 30x + 25y

Subject to constraints,

$$x + y \le 6$$

$$3x + 2y \le 15$$

$$x, y \ge 0$$

[Since production of trunk can not be less than zero]

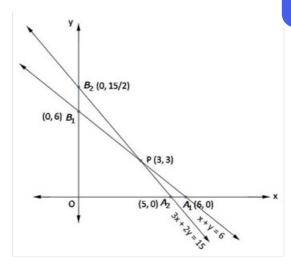
Region $x + y \le 6$: line x + y = 6 meets axes at $A_1(6,0)$, $B_1(0,6)$ respectively. Region containing origin represents $x + y \le 6$ as (0,0) satisfies $x + y \le 6$.

Region $3x + 2y \le 15$: line 3x + 2y = 15 meets axes at $A_2(5,0)$, $B_2(0,\frac{15}{2})$ respectively. Region containing origin represents $3x + 2y \le 15$ as (0,0) satisfies $3x + 2y \le 15$.

Region $x,y \ge 0$: it represents first quadrant.

Shaded region A_2PB_1 represents feasible region. Point P (3, 3) is obtained by solving x + y = 6 and 3x + 2y = 15,

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The value of
$$Z = 30x + 25y$$
 at $A_2(5,0) = 30(5) + 25(0) = 150$ $P(3,3) = 30(3) + 25(3) = 165$ $B_1(0,6) = 30(0) + 25(6) = 150$ $O(0,0) = 30(0) + 25(0) = 0$

maximum Z = 165 at x = 3, y = 3Trunk of type A = 3, type B = 3maximum profit = Rs 165





Let production of each bottle of A and B are x and y respectively.

Since, profits on each bottle of A and B are Rs 8 and Rs 7 per bottle respectively. So, profit on X bottles of A and Y bottles of B are BX and BX respectively, Let BX be total profit on bottles so,

$$Z = 8x + 7y$$

Since, it takes 3 hrs and 1 hr to prepare enough material to fill 1000 bottlesof type A and B respectively, so, X bottles of A and Y bottles of B are preparing is $\frac{3X}{1000}$ hrs and $\frac{Y}{100}$ hrs respectively but total 66 hrs are available, so,

$$\frac{3x}{1000} + \frac{y}{1000} \le 66$$

$$\Rightarrow 3x + y \le 66000$$
 (first constraint)

Since, row material available to make 2000 bottles of A and 4000 bottles of B but there are 45000 bottles into which either of medicines can be put so,

$$\Rightarrow x \le 20000 \qquad \text{(second constraint)}$$

$$y \le 40000 \qquad \text{(third constraint)}$$

$$x + y \le 45000 \qquad \text{(fourth constraint)}$$

$$x, y \ge 0$$

[Since production of bottles can not be less than zero]

Hence, mathematical formulation of LPP is find x and y which

$$maximize Z = 8x + 7y$$

Subject to constriants,

 $3x + y \le 66000$ $x \le 20000$

A 2 2000

y ≤ 40000

 $x + y \le 45000$ $x, y \ge 0$

Region $3x + y \le 66000$: line 3x + y = 66000 meets axes at A_1 (22000,0), B_1 (0,66000) respectively. Region containing origin represents $3x + y \le 66000$ as (0,0) satisfies $3x + y \le 66000$.

Million Stars Practice

(Nink, earns Practice)

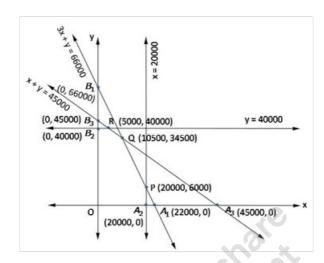


Region $x \le 20000$: line x = 20000 is parallel to y-axis and meets x-axis containing origin represents $x \le 20000$ as (0,0) satisfies $x \le 20000$.

Region y \leq 40000: line y = 40000 is parallel to x-axis and meets y-axis at $B_2(0, 40000)$. Region taken to give the expression of the

Region $x + y \le 45000$: line x + y = 45000 meets axes at A_3 (45000,0), B_3 (0,45000) respective containing origin represents $x + y \le 45000$ as (0,0) satisfies $x + y \le 45000$.

Region $x,y \ge 0$: it represents first quadrant.



Shaded region OA_2PRB_2 represents feasible region. Point P (20000, 6000) is obtained by solving X=20000 and 3X+y=66000, Q (10500, 34500) is obtained by solving X+y=45000 and 3X+y=66000, Q (15000,40000) is obtained by solving X+y=45000, Y=40000

```
The value of Z = 8x + 7y at
```

$$O(0,0)$$
 = 8(0) + 7(0) = 0
 $A_2(20000,0)$ = 8(20000) + 7(0) = 160000
 $P(20000,6000)$ = 8(20000) + 7(6000) = 202000
 $Q(10500,34500)$ = 8(10500) + 7(34500) = 325500
 $R(5000,4000)$ = 8(5000) + 7(40000) = 32000
 $B_2(0,40000)$ = 8(0) + 7(40000) = 250000

maximum Z = 325500 at x = 10500, y = 34500 Number bottles A type = 10500, B type = 34500 maximum profit = Rs 325500

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Let required number of first class and economy class tickets be x and y re-



Each ticket of first class and economy class make profit of Rs 400 and Rs 600 respectively. So, x ticket of first class and y tickets of economy class make profits of Rs 400x and Rs 600yrespectively, Let total profit be Z, so,

$$Z = 400x + 600y$$

Given, aeroplane can carry a miximum of 200 passengers,so,

(first constraint) $x + y \le 200$

Given, airline reservesa at least 20 seats for first class, so,

(second constraint) x ≥ 20

Given, at least 4 times as mnay passengers prefer totravel by economy class to the first class ,so,

y ≥ 4x

(third constraint) $4x - y \le 0$

Hence, mathematical formulation of LPP is find x and y which maximize Z = 400x + 600y

Subject to constriants,

 $x + y \le 200$

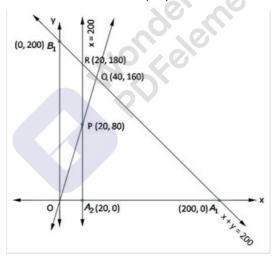
 $x \ge 20$

 $4x - y \le 0$

 $x, y \ge 0$

[Since seats of both the classes can not be less than zero]

Region $x + y \le 200$: line x + y = 200 meets axes at A_1 (200,0), B_1 (0,200) respectively. Region containing origin represents $x + y \le 200$ as (0,0) satisfies $x + y \le 200$.



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Anny Property of the Control of the Contr Shaded region PQR represents feasible region, Q (40,160) is obtained by solving x + y = 200 and 4x - y = 0, R (20,180) is obtained by solving x = 20 and x + y = 200

The value of Z = 400x + 600y at

= 400 (20) + 600 (80) = 56000 P (20,80)

Q(40,160) = 400(40) + 600(160) = 112000

R (20,180) =400(20)+600(180)=116000

so.

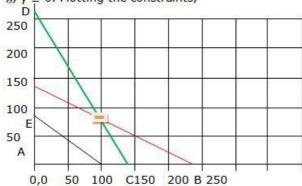
maximum Z = Rs 116000 at x = 20, y = 180

Number of first class ticket = 20. Number of economy class ticket= 180 maximum profit = Rs 116000



	Type I	Type II	
	X	У	18
Nitrogen	0.1x	0.05y	≥ 14
Bicarbonate	0.06x	0.1y	≥ 14
Cost	0.6x	0.4y	Minimize

The above LPP can be presented in a table above. Aim is to find the values of x & y that minimize the function Z = 0.6x + 0.4y, subject to the conditions $0.1x + 0.05y \ge 14$; gives x=0, y= $280 \times y=0$, x= $140 \times 0.06x + 0.1y \ge 14$; gives x=0, y= $140 \times y=0$, x= $233.33 \times y=0$. Plotting the constraints,



The feasible region is the unbounded region D-C-B

Corner point	Value of $Z = 0.6x + 0.4y$
0, 280	112
233.33, 0	140
100, 80	92

The minimum occurs at x=100, y=80 with a value of 92 Since the region is unbounded plot $0.6x + 0.4y \le 92$ Plotting the points, we get line E-100. There are no common points so x=100, y=80 with a value of 92 is the optimal minimum.

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Remove Watermark



Linear Programming Ex 30.4 Q24

Let he invests $\operatorname{Rs} x$ and $\operatorname{Rs} y$ in saving certificate (sc) and National saving bond (NSB) respectively.

Since, rate of interest on SC is 8% annual and on NSB is 10% annual,So, interest on Rsx of SC is $\frac{8x}{100}$ and Rsy of NSB is $\frac{10x}{100}$ per annum.

Let Z be total interest earned so,

$$Z = \frac{8x}{100} + \frac{10y}{100}$$

Given he wants to invest Rs 12000 is total

 $x + y \le 12000$

(third constraint)

Hence, mathematical formulation of LPP is find \boldsymbol{x} and \boldsymbol{y} which

$$maximize Z = \frac{8x}{100} + \frac{10y}{100}$$

Subject to constriants,

x ≥ 2000

y ≥ 4000

 $x+y \leq 12000$

 $x, y \ge 0$

[Since investment can not be less than zero]

Region $x \ge 2000$: line x = 2000 is parallel to y-axis and meets x-axis at A_1 (2000,0). Region not containing origin represents $x \ge 2000$ as (0,0) does not satisfy $x \ge 2000$

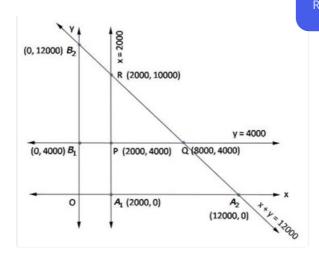
Region y \geq 4000: line y = 4000 is parallel to x-axis and meets y-axis at B_1 (0, 4000). Region not containing origin represents $y \geq$ 4000 as (0,0) does not satisfy $y \geq$ 4000.

Region $x+y \le 12000$: line x+y=12000 meets axes at A_2 (12000,0), b_2 (0,1200) respectively. Region containing represents $x+y \le 12000$ as (0,0) satisfies $x+y \le 12000$.

Region $x,y \ge 0$: it represents first quadrant.

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Shaded region PQR represents feasible region. $P\left(2000,4000\right)$ is obtained by solving X=2000 and $y=4000,Q\left(8000,4000\right)$ is obtained by solving X+y=12000 and y=4000 $R\left(2000,10000\right)$ is obtained by solving X=2000 and Y+X=1200

The value of $Z = \frac{8x}{100} + \frac{10y}{100}$ at

$$P(2000, 4000) = \frac{8}{100}(2000) + \frac{10}{100}(4000) = 560$$

$$Q(8000, 4000) = \frac{8}{100}(8000) + \frac{10}{100}(4000) = 1040$$

$$R(2000, 10000) = \frac{8}{1000}(2000) + \frac{10}{100}(10000) = 1160$$

so, maximum Z = Rs 1160 at x = 2000, y = 10000

> He should invest Rs 2000 in Saving Certificates and 1000 in National Saving scheme, maximum Interest = Rs 1160

Remove Watermark

Linear Programming Ex 30.4 Q25

Let required number of trees of type A and B be Rs x and Rs y respectively.

Since, selling price of 1 kg of type A is Rs 2 and growth is 20 kg per tree, so, revenue from type A is Rs 40x, selling price of 1 kg of type B is Rs 1.5 and growth 40 kg per tree, so, revenue from type B is Rs 60y. Total revenue is $\left(40x+60y\right)$. Costs of each tree of type A and B are Rs 20 and Rs 25, so,costs of x trees of type A and y trees of type B are Rs 20x and 25y respectively. Total cost is Rs $\left(20x+25y\right)$

Let Z be total profit so,

$$Z = (40x - 60y) - (20x + 25y)$$

$$Z = 20x + 35y$$

Since he has Rs 1400 to invest so,

cost ≤ 1400

 \Rightarrow 20x + 35y \leq 1400

 \Rightarrow 4x + 5y \le 280 (first constraint)

Since each tree of type A and B needs 10 sq. m and 20 sq. m of ground respectively so, x trees of type A and y trees of type B need 10x sq. m and 20y sq. m of ground respectively. but total ground available is 1000 sq. m so,

$$10x + 20y \le 1000$$

$$\Rightarrow x + 2y \le 100$$
 (second constraint)
 $x, y \ge 0$

Hence, mathematical formulation of LPP is find x and y which maximize Z = 20x + 35y

Subject to constriants,

 $4x+5y \le 280$

 $\Rightarrow x + 2y \le 100$

x,y ≥ 0

[Since number of trees can not be less than zero]

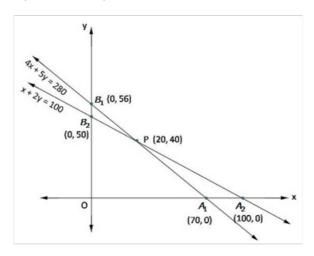




Region $4x + 5y \le 280$: line 4x + 5y = 280 meets axes at A_1 (70,0), B_1 (0. Region containing origin represents $4x + 5y \le 280$ as (0,0) satisfies $4x + 5y \le 280$.

Region $x + 2y \le 100$: line x + 2y = 100 meets axes at A_2 (100,0), B_2 (0,50) respectively. Region containing origin represents $x + 2y \le 100$ as (0,0) satisfies $x + 2y \le 100$.

Region $x,y \ge 0$: it represents first quadrant.



Shaded region OA_1PB_2 the feasible region. P (20,40) is obtained by solving x + 2y = 100 and 4x + 5y = 280,

The value of Z = 20x + 35y at

$$O(0,0) = 20(0) + 35(0) = 0$$

$$A_1(70,0) = 20(0) + 35(0) = 1400$$

$$P(20,40) = 20(20) + 35(40) = 1800$$

$$B_2(0,50) = 20(0) + 35(50) = 1750$$

maximum Z = 1800 at x = 20, y = 40

20 trees of type A, 40 trees of type B, profit = Rs 1800

Linear Programming Ex 30.4 Q26

Let the cottage industry manufacture \boldsymbol{x} pedestal lamps and \boldsymbol{y} wooden shades. Therefore,

 $x \ge 0$ and $y \ge 0$

The given information can be compiled in a table as follows.

	Lamps	Shades	Availability
Grinding/Cutting Machine (h)	2	1	12
Sprayer (h)	3	2	20

The profit on a lamp is Rs 5 and on the shades is Rs 3. Therefore, the constraints are

$$2x + y \le 12$$

$$3x + 2y \le 20$$

Total profit, Z = 5x + 3y

The mathematical formulation of the given problem is

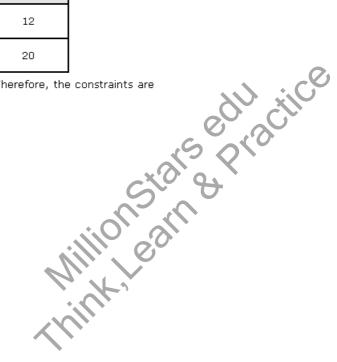
Maximize Z = 5x + 3y ... (1)

subject to the constraints,

$$2x + y \le 12...(2)$$

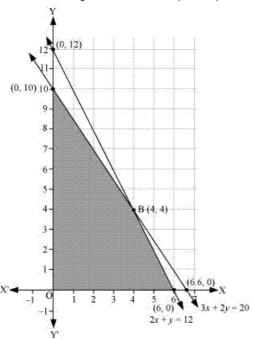
$$3x + 2y \le 20 \dots (3)$$

$$x, y \ge 0 \dots (4)$$





The feasible region determined by the system of constraints is as follow



The corner points are A (6, 0), B (4, 4), and C (0, 10).

The values of Z at these corner points are as follows

Corner point	Z = 5x + 3y	
A(6, 0)	30	
B(4, 4)	32	→ Maximum
C(0, 10)	30	70,

The maximum value of Z is 32 at (4, 4).

Thus, the manufacturer should produce 4 pedestal lamps and 4 wooden shades to maximize his profits.

Linear Programming Ex 30.4 Q27

Let required number of goods of type x and y be x_1 and x_2 respectively.

Since, selling prices of each goods of type x and y are Rs 100 and Rs 120 respectively, so, selling price of x_1 units of goods of type x and x_2 units of goods of type y are Rs 100x and Rs 120y respective respectively

Let Z be total revenue, so

$$Z = 100x_1 + 120x_2.$$

Allion editions of the state of Since each unit of goods x and y require 2 and 3 units of labour, so, x_1 unit of xand x_2 unit of y require $2x_1$ and $3x_2$ units of labour units but maximum labour units available is 30 units, so,

$$2x_1 + 3x_2 \le 30$$
 (first constraint)

Since each unit of goods x and y require 3 and 1 unit of capital so, x_1 unit of x and x_2 unit of y require $3x_1$ and x_2 units of capital respectively but maximum units available for capital is 17, so,

$$3x_1 + x_2 \le 17$$
 (second constraint)

Hence, mathematical formulation of LPP is find x and y which maximize Z = 20x + 35y

Subject to constriants,

$$2x_1 + 3x_2 \le 30$$

$$\Rightarrow 3x_1 + x_2 \le 17$$

$$x_1, x_2 \ge 0$$

[Since production of goods can not be less than zero]





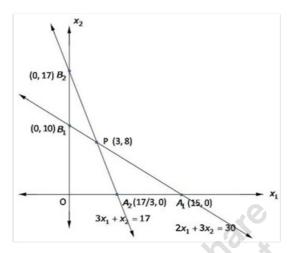
Region $2x_1 + 3x_2 \le 30$: line 2x + 3y = 30 meets axes at A_1 (15,0), B_1 (0, 2). Region containing origin represents $2x_1 + 3x_2 \le 30$ as (0,0) satisfies $2x_1 + 3x_2 = 30$.

 $\text{Region } 3x_1+x_2 \leq 17: \text{ line } 3x_1+x_2 \leq 17 \text{ meets axes at } A_2\left(\frac{17}{3},0\right), B_2\left(0,17\right) \text{ respectively.}$

Region containing origin represents $3x_1 + x_2 \le 17$ as (0,0) satisfies $3x_1 + x_2 \le 17$.

Region $x_1, x_2 \ge 0$: it represent first quandrant shaded region OA_2PB_1 represents feasible region. Point P (3, 8) is obtained by solving

$$2x_1 + 3x_2 = 30$$
 and $3x_1 + x_2 = 17$



The value of $Z = 100x_1 + 120x_2$ at

$$O(0,0)$$
 = 100(0) + 120(0) = 0

$$A_2\left(\frac{17}{3},0\right) = 100\left(\frac{17}{3}\right) + 120\left(0\right) = \frac{1700}{3} = 566\frac{2}{3}$$

$$P(3,8) = 100(3) + 120(8) = 1260$$

$$B_1(0,10) = 100(0) + 120(10) = 1200$$

maximum Z = 1260 at x = 3, y = 8

goods of type x = 3, type y = 8

maximum profit = Rs 12160



Let required number of product A and B be x and y respectively.

Since,profit on each product A and B are Rs 5 and Rs 3 respectively, so, profits on x product A and y product B are Rs Sx and Rs Sy respectively Let Z be total profit so

$$Z = 5x + 3y$$

Since each unit of product A and B require—one min. each on machine M_1 , so, x unit of product A and y units of product B require x and y min. respectivley on machine M_1 but M_1 can work at most $5\times60=300$ min., so

$$x + y \le 300$$
 (first constraint)

Since each unit of product A and B require 2 and one min.respectively on machine M_2 , so, x unit of product A and y units of product B require 2x and y min. respectivley on machine M_2 but M_2 can work at most $6 \times 60 = 360$ min., so

$$2x + y \le 360$$
 (second constraint)

Hence, mathematical formulation of LPP is find x and y which maximize Z = 5x + 3y

Subject to constriants,

 $x + y \le 300$

 \Rightarrow 2x + y \le 360

 $x, y \ge 0$

[Since production can not be less than zero]







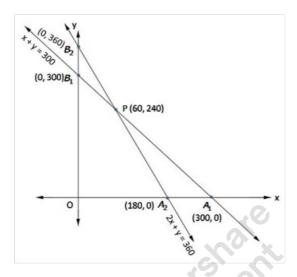
Region $x + y \le 300$: line x + y = 300 meets axes at $A_1 (300,0)$, $B_1 (0,30)$. Region containing origin represents $x + y \le 300$ as (0,0) satisfies x + y = 300.

Region $2x + y \le 360$: line 2x + y = 360 meets axes at $A_2(180,0)$, $B_2(0,360)$ respectively. Region containing origin represents $2x + y \le 360$ as (0,0) satisfies $2x + y \le 360$.

Region $x, y \ge 0$: it represent first quandrant

Shaded region OA_2PB_1 represents feasible region. Point P (60,240) is obtained by solving

$$x + y = 300$$
 and $2x + y = 360$



The value of Z = 5x + 3y at

$$O(0,0) = 5(0) + 3(0) = 0$$

$$A_2(180,0) = 5(180) + 3(0) = 900$$

$$P(60,240) = 5(60) + 3(240) = 1020$$

$$B_1(0,300) = 5(0) + 3(300) = 900$$

maximum Z = 1020 at x = 60, y = 240

Number of product A = 60, product B = 240 maximum profit = Rs 1020



Let required quantity of item A and B produced be x and y respectively.

Since,profits on each item A and B are Rs 300 and Rs 160 respectively, so, profits on x unit of item A and Y units of item B are Rs 300x and Rs 160y respectively Let Z be total profit so

$$Z = 300x + 160y$$

Since one unit of item A and B require one and $\frac{1}{2}$ hr respectively, so, x units of item A and y units of item B require x and $\frac{1}{2}y$ hr. respectively but maximum time available is 16 hours.,so

$$x+\frac{1}{2}y\leq 16$$

(first constraint)

Given, manufacturer can produce at most 24 items, so,

(second constraint)

Hence, mathematical formulation of LPP is find x and y which maximize Z = 300x + 160y

Subject to constriants,

$$2x + y \le 32$$

$$x+y \le 24$$

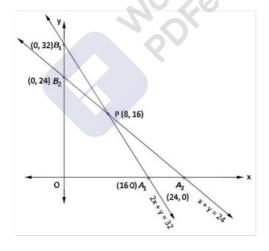
$$x, y \ge 0$$

[Since production can not be less than zero]

Region $2x + y \le 32$: line 2x + y = 32 meets axes at A_1 (16,0), B_1 (0,32) respectively. Region containing origin represents $2x + y \le 32$ as (0,0) satisfies $2x + y \le 32$.

Region $x+y \le 24$: line x+y=24 meets axes at A_2 (24,0), B_2 (0,24) respectively. Region containing origin represents $x+y \le 24$ as (0,0) satisfies $x+y \le 24$.

 $\mathsf{Region}\, \varkappa, y \geq 0: \ \mathsf{it} \ \mathsf{represent} \ \mathsf{first} \ \mathsf{quandrant}$



Shaded region OA_1PB_2 represents feasible region.

Point
$${\it P}$$
 is obtained by solving

$$x + y = 24$$
 and $2x + y = 32$

The value of Z = 300x + 160y at

$$B_2(0,24)$$

maximum Z = 4960

Number of item
$$A = 8$$
, item $B = 16$
maximum profit = Rs 4960

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Programming Ex 30.4 Q30

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MILLIONST $\stackrel{\bullet}{R}$ per of toys of type A and B produced are x and y respectively.

ofits on each unit of toys A and B are Rs 50 and Rs 60 respectively, so, profits on x units of toys A and y units of toy B are Rs 50x and Rs 60y respectively Let Z be total profit so

$$Z = 50x + 60y$$

Since each unit of toy A and toy B require 5 min. and 8 min. on cutting, so, x units of toy A and y units of toy B require 5x and 8y min. respectivley but maximum time available for cutting $3 \times 60 = 180 \text{ min.,so}$

$$5x + 8y \le 180$$
 (first constraint)

Since each unit of toy A and toy B require 10 min. and 8 min. for assembling, so, x units of toy A and y units of toy B require 10x and 8y min. for assembling respectivley but maximum time available for assembling is $4 \times 60 = 240 \text{ min.,so}$

$$10x + 8y \le 240$$

$$\Rightarrow$$
 5x + 4y \leq 120

(second constraint)

Hence, mathematical formulation of LPP is find x and y which maximize Z = 50x + 60y

Subject to constriants,

 $5x + 8y \le 180$

 $5x + 4y \le 120$

 $x, y \ge 0$

[Since production can not be less than zero]

Region $5x + 8y \le 180$: line 5x + 8y = 180 meets axes at $A_1(36,0)$, $B_1(0,\frac{45}{2})$ respectively.

Region containing origin represents $5x + 8y \le 180$ as (0,0) satisfies $5x + 8y \le 180$.

Region $5x + 4y \le 120$: line 5x + 4y = 120 meets axes at $A_2(24,0)$, $B_2(0,30)$ respectively.

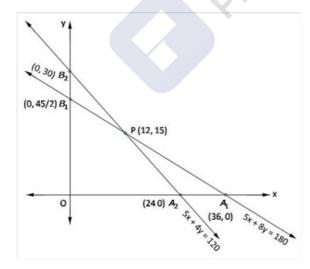
Region containing origin represents $5x + 4y \le 120$ as (0,0) satisfies $5x + 4y \le 120$.

Region $x, y \ge 0$: it represent first quandrant

Shaded region OA-PB, represents feasible region.

Point P(12, 15) is obtained by solving

$$5x + 8y = 180$$
 and $5x + 4y = 120$



The value of Z = 50x + 60y at

$$P(12,15) = 50(12) + 60(15) = 1500$$

$$B_1 \left[0, \frac{45}{2} \right]$$

$$= 50 (0) + 60 (\frac{45}{2}) = 1350$$

Maximum Z = 1500 at x = 12, y = 15

Number of toys
$$A = 12$$
, toys $B = 15$
maximum profit = Rs 1500

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required number of product A and B are x and y respectively.

Since,profits on each unit of product A and product B are Rs 6 and Rs 8 respectively, so, profits on X units of product A and B units of product B are Rs 6B and Rs 8B respectively Let B be total profit so

$$Z = 6x + 8y$$

Since each unit of product A and B require 4 and 2 hrs for assembling respectively, so, X units of product A and B units of product B require B require B hrs for assembling respectively but maximum time available for assembling is 60 hrs.,so

$$4x + 2y \le 60$$

$$2x + y \le 30$$

(first constraint)

Since each unit of product A and B require 2 and 4 hrs for finishing, so, X units of product A and B units of product B require B0 and B1 hrs for finishing respectively but maximum time available for finishing is 48 hrs.,so

$$2x + 4y \le 48$$

$$x + 2y \le 24$$

(second constraint)

Hence, mathematical formulation of LPP is find x and y which maximize Z = 6x + 8y

Subject to constriants,

$$2x+y \le 30$$

$$x + 2y \le 24$$

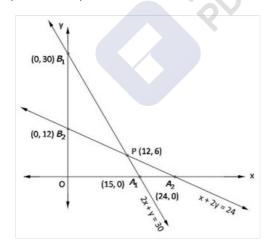
$$x, y \ge 0$$

[Since production of both can not be less than zero]

Region $2x + y \le 30$: line 2x + y = 24 meets axes at $A_1(15,0)$, $B_1(0,30)$ respectively. Region containing origin represents $2x + y \le 30$ as (0,0) satisfies $2x + y \le 30$.

Region $x+2y \le 24$: line x+2y=24 meets axes at $A_2(24,0)$, $B_2(0,12)$ respectively. Region containing origin represents $x+2y \le 24$ as (0,0) satisfies $x+2y \le 24$.

Region $x, y \ge 0$: it represent first quandrant



Shaded region OA_1PB_2 represents feasible region.

Point P(12,6) is obtained by solving

$$x + 2y = 24$$
 and $x + 2y = 30$

The value of Z = 6x + 8y at

$$O(0,0) = 6(0) + 8(0) = 0$$

$$A_1(15,0) = 6(15) + 8(0) = 90$$

$$P(12,6) = 6(12) + 8(6) = 120$$

$$B_2(0,12) = 6(0) + 8(12) = 96$$

maximum
$$Z = 120$$
 at $x = 12$, $y = 6$

Number of product
$$A = 12$$
, product $B = 6$ maximum profit = Rs 120

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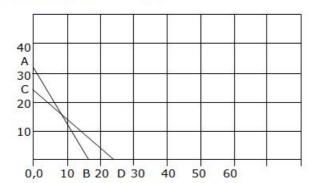
Let x & y be the No. of items of A & B respectively.

x + y = 24 (total No. of items constraint)

 $x + 0.5y \le 16$ (time constraint)

 $x, y \ge 0$

Z = 300x + 160y (profit function to be maximized) Plotting the inequalities gives,



The feasible region is 0,0-C-F-B

Corner point	Value of $Z = 300x + 160y$
0, 0	0
0, 24	3840
16, 0	4800
8,16	4960

The firm must produce 8 items of A and 16 items of B to maximize the profit at Rs. 4960/-

Linear Programming Ex 30.4 Q33

Let required number of product A and B are x and y respectively.

Since, profits on each unit of product A and product B are Rs 20 and Rs 15 respectively, so, x units of product A and Y units of product B give profit of Rs 20X and Rs 15Y respectively Let Z be total profit so

$$Z = 20x + 15y$$

Since each unit of product A and B require 5 and 3 man-hrs respectively, so, x units of product A and Y units of product B require 5X and 3Y man-hrs respectively but maximum time available for is 500 man-hrs., so

$$5x + 3y \le 500$$
 (first constraint)

Since maximum number that product A and B can be sold is 70 and 125 respectively, so,

 $x \le 70$ (second constraint)

 $y \le 125$ (third constraint)

Hence, mathematical formulation of LPP is find x and y which maximize Z = 20x + 15y

Subject to constriants,

 $5x + 3y \le 500$

 $x \le 70$

y ≤ 70

x,y≥0

[Since production of both can not be less than zero]



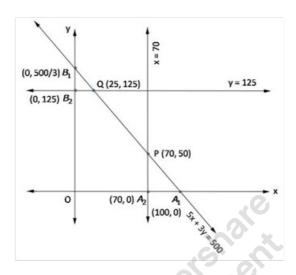
Region $5x + 3y \le 500$: line 5x + 3y = 500 meets axes at $A_1(100,0)$, $B_1(0,\frac{1}{3})$ respectively

Region containing origin represents $5x + 3y \le 500$ as (0,0) satisfies $5x + 3y \le 500$.

Region $x \le 70$: line x = 70 is parallel to y - axis meets x-axes at A_2 (70,0). Region containing origin represents $x \le 70$ as (0,0) satisfies $x \le 70$.

Region $y \le 125$: line y = 125 is parallel to x - axis meets y-axes at B_2 (0,125), with y - axis. Region containing origin represents $y \le 125$ as (0,0) satisfies $y \le 125$.

Region $x, y \ge 0$: it represent first quandrant.



Shaded region OA_2PQB_2 represents feasible region. Point P (70,50) is obtained by solving x = 70Point Q (25,125) is obtained by solving y = 125 and 5x + 3y = 500.

The value of Z = 20x + 15y at

$$O(0,0)$$
 = 20(0) + 15(0) = 0
 $A_2(70,0)$ = 20(70) + 15(0) = 1400
 $P(70,50)$ = 20(70) + 15(50) = 2150
 $Q(25,125)$ = 20(25) + 15(125) = 2375
 $B_2(0,125)$ = 20(0) + 15(125) = 1875

maximum Z = 2375 at x = 25, y = 125

Number of product A = 25, product B = 125 maximum profit = Rs 2375

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Let required quantity of large and small boxes are x and y respectively.

Since, profits on each unit of large and small boxes are Rs 3 and Rs 2 respectively, so, profit on x units of large and y units of small boxes are Rs 3x and Rs 2y respectively Let Z be total profit so

$$Z = 3x + 2y$$

Since each large and small box require 4 sq. m. and 3 sq. m. cardboard respectively, so, x units of large and y units of small boxes require 4x and 3y sq.m. cardboard respectively but only 60 sq. m. of cardboard is available, so

$$4x + 3y \le 60$$
 (first constraint)

Since manufacturer is required to make at least three large boxes, so,

```
x \ge 3 (second constraint)
```

Since manufacturer is required to make at least twice as many small boxes as large boxes ,so,

```
y \ge 2x (third constraint)
```

Hence, mathematical formulation of LPP is find x and y which maximize Z = 20x + 15y

Subject to constriants,

 $4x + 3y \le 60$

x ≥ 3

y ≥ 2x

 $x, y \ge 0$

[Since production can not be less than zero]

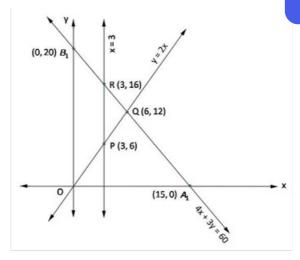
Region $4x + 3y \le 60$: line 4x + 3y = 60 meets axes at A_1 (15,0), B_1 (0,20) respectively. Region containing origin represents $4x + 3y \le 60$ as (0,0) satisfies $4x + 3y \le 60$.

Region $x \ge 3$: line x = 3 is parallel to y -axis meets x-axes at $A_2(3,0)$. Region containing origin represents $x \ge 70$ as (0,0) satisfies $x \ge 3$.

Region $y \ge 2x$: line y = 2x is passes through origin and P(3,6). Region containing $B_1(0,20)$ represents $y \ge 2x$ as $\{0,20\}$ satisfies $y \ge 2x$.

Region $x,y \ge 0$: it represent first quandrant.

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Shaded region PQR represents feasible region. Point Q(6,12) is obtained by solving y = 2x and 4x + 3y = 60Point R(3,16) is obtained by solving x = 3 and 4x + 3y = 60.

The value of Z = 3x + 2y at

$$P(3,6) = 3(3) + 2(6) = 21$$

$$Q(6,12) = 3(6) + 2(12) = 42$$

$$R(3,16) = 3(3) + 2(16) = 41$$

maximum
$$Z = 42$$
 at $x = 6$, $y = 12$

Number of large box = 6, small box = 12 maximum profit = Rs 42

Linear Programming Ex 30.4 Q35

The given data can be written in the tabular form as follows:

Product	Α	В	Working week Turn over
Time	0.5	1	40
Prise	200	300	10000
Profit	20	30	
Permanent order	14	16	

Let x be the number of units of A and y be the number of units of B produced to earn the maximum profit.

Then the mathematical model of the LPP is as follows:

Maximize Z = 20x + 30y

Subject to $0.5x + y \le 40$,

200× + 300y ≥ 10000

and $x \ge 14$, $y \ge 16$

To solve the LPP we draw the lines,

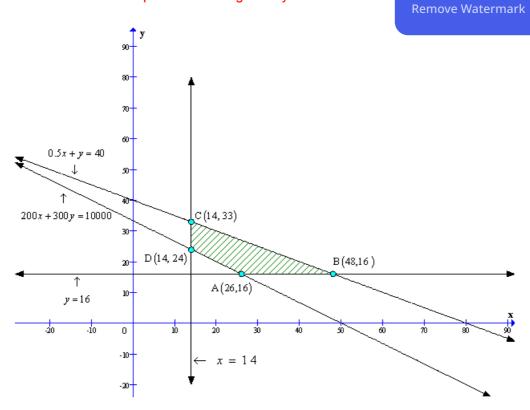
$$0.5x + y = 40$$
,

$$200 \times + 300 y = 10000$$

×= 14

$$y = 16$$

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The coordinates of the vertices (Corner - points) of shaded feasible region ABCD are A(26, 16), B(48, 16), C(14, 33) and D(14, 24).

The values of the objective of function at these points are given in the following table:

Point (x_1, x_2)	Value of objective function Z = 20x + 30y
A(26, 16)	Z = 1000
B(48, 16)	Z = 1440
C(14, 33)	Z = 1270
D(14,24)	Z = 600

48 units of product A and 16 units of product B should be produced to earn the maximum profit of Rs. 1440.

Linear Programming Ex 30.4 Q36

Let the distance covered with the speed of 25 km/hr be \times . Let the distance covered with the speed of 40 km/hr be y.

Then the mathematical model of the LPP is as follows:

Maximize Z = x + y

Subject to $2x + 5y \le 100$,

$$\frac{\times}{25} + \frac{y}{40} \le 1$$

and $x \ge 0$, $y \ge 0$

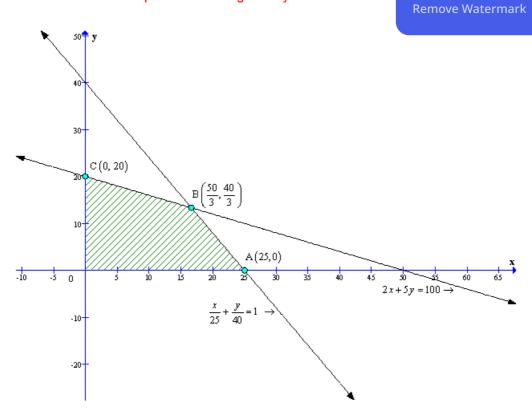
To solve the LPP we draw the lines,

$$2x + 5y = 100$$
,

$$\frac{x}{25} + \frac{y}{40} = 1$$

The feasible region of the LPP is shaded in graph.

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The coordinates of the vertices (Corner - points) of shaded feasible region ABC are $A(25, 0), B\left(\frac{50}{3}, \frac{40}{3}\right)$ and C(0, 20).

The values of the objective of function at these points are given in the following table:

Point (x_1, x_2)	Value of objective function $Z = x + y$
A (25, 0)	Z = 25
$B\left(\frac{50}{3}, \frac{40}{3}\right)$	Z = 30
C(0, 20)	Z = 20

The distance covered at the speed of 25km/hr is $\frac{50}{3}$ km and The distance covered at the speed of 40km/hr is $\frac{40}{3}$ km. Maximum distance travelled is 30 km.

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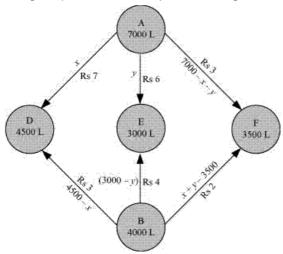
Linear Programming Ex 30.4 Q37

Let x and y litres of oil be supplied from A to the petrol pumps, D and E. Then, (7000 -x-y) will be supplied from A to petrol pump F.

The requirement at petrol pump D is 4500 L. Since x L are transported from depot A, the remaining (4500 -x) L will be transported from petrol pump B.

Similarly, (3000 -y) L and 3500 - (7000 -x-y) = (x+y-3500) L will be transported from depot B to petrol pump E and F respectively.

The given problem can be represented diagrammatically as follows.



$$x \ge 0$$
, $y \ge 0$, and $(7000 - x - y) \ge 0$

$$\Rightarrow x \ge 0, y \ge 0, \text{ and } x + y \le 7000$$

$$4500-x \ge 0$$
, $3000-y \ge 0$, and $x+y-3500 \ge 0$

$$\Rightarrow x \le 4500, y \le 3000, \text{ and } x + y \ge 3500$$

Cost of transporting 10 L of petrol = Re 1

Cost of transporting 1 L of petrol = $Rs \frac{1}{10}$

Therefore, total transportation cost is given by,

$$z = \frac{7}{10} \times x + \frac{6}{10}y + \frac{3}{10}(7000 - x - y) + \frac{3}{10}(4500 - x) + \frac{4}{10}(3000 - y) + \frac{2}{10}(x + y - 3500)$$

= 0.3x + 0.1y + 3950

The problem can be formulated as follows.

Minimize z = 0.3x + 0.1y + 3950 ... (1)

subject to the constraints,

$$x + y \le 7000$$
 ...(2)

$$x \le 4500$$
 ...(3)

$$y \le 3000$$
 ...(4)

$$x + y \ge 3500$$
 ...(5)

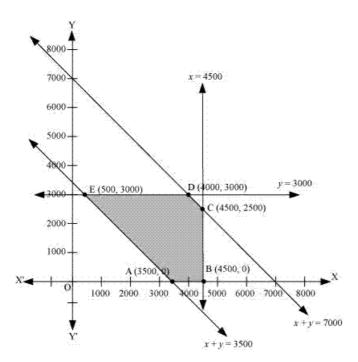
$$x, y \ge 0 \qquad \dots (6)$$

The feasible region determined by the constraints is as follows.

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The corner points of the feasible region are A (3500, 0), B (4500, 0), C (4500, 2500), D (4000, 3000), and E (500, 3000).

The values of z at these corner points are as follows.

Corner point	z = 0.3x + 0.1y + 3950	
A (3500, 0)	5000	20 4
B (4500, 0)	5300	0,0
C (4500, 2500)	5550	Ko
D (4000, 3000)	5450	
E (500, 3000)	4400	→ Minimum

The minimum value of z is 4400 at (500, 3000).

Thus, the oil supplied from depot A is 500 L, 3000 L, and 3500 L and from depot B is 4000 L, 0 L, and 0 L to petrol pumps D, E, and F respectively.

The minimum transportation cost is Rs 4400.

Willions are a practice



Let required number of gold rings and chains are x and y respectively.

Since,profits on each ring and chains are Rs 300 and Rs 190 respectively, so, profit on x units of ring and y units of chains are Rs 300x and Rs 190y respectively Let Z be total profit so

$$Z = 300x + 190y$$

Since each unit of ring and chain require 1 hr and 30 min. to make respectively, so, x units of rings and y units of rings require 60x and 30y min. to make respectively, but total time available to make is $16 \times 60 = 960$, so

$$60x + 30y \le 960$$

$$\Rightarrow$$
 $2x + y \le 32$

(first constraint)

Given, total number of rings and chains manufactured is at most 24, so,

(second constraint)

Hence, mathematical formulation of LPP is find x and y which maximize Z = 300x + 160y

Subject to constriants,

$$2x + y \le 32$$

$$x+y \le 24$$

$$x, y \ge 0$$

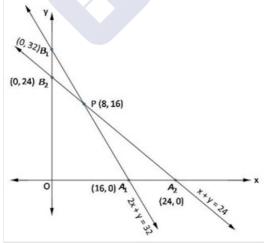
[Since production can not be less than zero]

Region $2x + y \le 32$: line 2x + y = 32 meets axes at A_1 (16,0), B_1 (0,32) respectively. Region containing origin represents $2x + y \le 32$ as (0,0) satisfies $2x + y \le 32$.

Region $x+y \le 24$: line x+y=24 meets axes at A_2 (24,0), B_2 (0,24) respectively. Region containing origin represents $x+y \le 24$ as (0,0) satisfies $x+y \le 24$.

Region $x, y \ge 0$: it represent first quandrant

Shaded region OA_1PB_2 represents feasible region. Point P(8,16) is obtained by solving 2x + y = 32 and x + y = 24.



The value of Z = 300x + 160y at

$$=300(0)+160(0)=0$$

$$A_1 (16, 0)$$

$$=300(16)+160(0)=4800$$

$$=300(8)+160(16)=4960$$

$$B_2(0,24)$$

maximum Z = 4960 at x = 8 , y = 16

Number of rings = 8, chains = 16

maximum profit = Rs 4960

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Linear Programming Ex 30.4 Q39

Let required number of books of type I and II be x and y respectively.

Let ${\cal Z}$ be total number of books in the shelf ,so,

$$Z = x + y$$

Since 1 book of type I and II 6 cm and 4 cm. thick respectively, so, x books of type I and y books of type II has thickness of 6x and 4y cm. respectivley, but shelf is 96 cm. long ,so

$$\Rightarrow$$
 $3x + 2y \le 48$

(first constraint)

Since 1 book of type I and II weight 1 kg and $1\frac{1}{2}$ kg respectively, so, x books of type

I and y books of type II weight x kg and $\frac{3}{2}y$ kg respectivley, but shelf can support at most 21 kg,so

$$x + \frac{3}{2}y \le 21$$

$$\Rightarrow$$
 2x + 3v \leq 42

(second constraint)

Hence, mathematical formulation of LPP is find x and y which maximize Z = x + y

Subject to constriants,

$$3x + 2y \le 48$$

$$2x + 3y \le 42$$

$$x, y \ge 0$$

[Since number of books can not be less than zero]

Region $3x + 2y \le 48$: line 3x + 2y = 48 meets axes at $A_1(16,0)$, $B_1(0,24)$ respectively. Region containing origin represents $3x + 2y \le 48$ as (0,0) satisfies $3x + 2y \le 48$.

Region $2x + 3y \le 42$: line 2x + 3y = 42 meets axes at $A_2(21,0)$, $B_2(0,14)$ respectively. Region containing origin represents $2x + 3y \le 42$ as (0,0) satisfies $2x + 3y \le 42$.

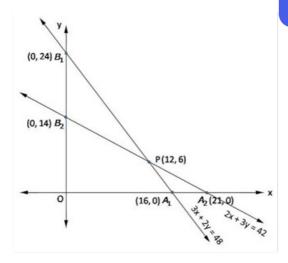
Region $x, y \ge 0$: it represent first quandrant

Shaded region OA_1PB_2 represents feasible region.

Point P(12,6) is obtained by solving 2x + 3y = 42 and 3x + 2y = 48

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The value of Z = x + y at

$$= 0 + 0 = 0$$

$$A_1 (16, 0)$$

$$B_2(0,14)$$

$$= 0 + 14 = 14$$

maximum
$$Z = 18$$
 at $x = 12$, $y = 6$

Number of books of type I = 12, type II = 6

Linear Programming Ex 30.4 Q40

Let x & y be the No. of tennis rackets and cricket bats produced.

 $1.5x + 3y \le 42$

(constraint on machine time)

 $3x + y \le 24$

(constraint on craftsman's time)

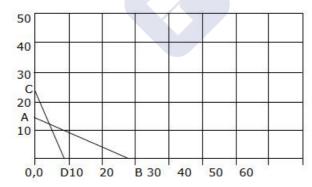
Z = 20x + 10y

(Maximize profit)

 $x, y \ge 0$

plotting the inequalities we have,

when x=0, y=14 and when y=0, x=28 and when x=0, y=24 and when y=0, x=8



The feasible region is given by 0,0-A-F-D Tabulating Z and corner points we have

Corner point	Value of $Z = 20x + 10y$
0, 0	0
0, 14	140
4, 12	200
8.0	160

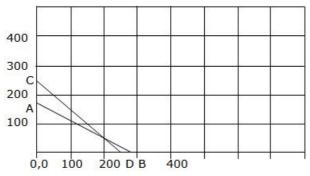
The factory must manufacture 4 tennis rackets and 12 cricket bats to earn the maximum profit of Rs. 200/-

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Let x & y be the No. of desktop model and portable model of personal computers stocked.

 $x + y \le 250$ (constraint on total demand of computers) $25000x + 40000y \le 70,00,000$ (constraint on cost) Z = 4500x + 5000y (Maximize profit) $x, y \ge 0$

plotting the inequalities we have, when x=0, y=250 and when y=0, x=250 and line CD when x=0, y=175 and when y=0, x=280



The feasible region is given by 0,0-A-E-D-0,0

Tabulating Z and corner points we have

Corner point	Value of Z = 4500x + 5000y
0, 0	0
0, 175	8,75,000
250, 0	11,25,000
200, 50	11,50,000

The merchant must stock 200 desktop models and 50 portable models to earn a maximum profit of Rs. 11,50,000/-

Linear Programming Ex 30.4 Q42

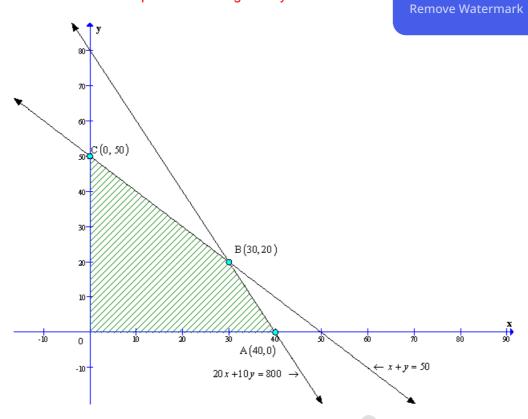
Let x hectores of land grows crop X. Let y hectores of land grows crop Y.

Then the mathematical model of the LPP is as follows: Maximize Z = 10,500x + 9,000ySubject to $x + y \le 50$, $20x + 10y \le 800$ and $x \ge 0$, $y \ge 0$

To solve the LPP we draw the lines, x + y = 50, 20x + 10y = 800

The feasible region of the LPP is shaded in graph.

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The coordinates of the vertices (Corner - points) of shaded feasible region ABC are A(40, 0), B(30, 20) and C(0, 50).

The values of the objective of function at these points are given in the following table:

Point (x_1, x_2)	Value of objective function $Z = 10,500x + 9,000y$
A(40, 0)	Z = 4,20,000
B(30, 20)	Z = 4,95,000
C(0, 50)	Z = 4,50,000

30 hectors of land should be allocated to crop X and

20 hectors of land should be allocated to crop Y to maximize the profit.

The maximum profit that can be eared is Rs. 4,95,000.

Linear Programming Ex 30.4 Q43

The given data can be written in the tabular form as follows:

Model	Α	В	Maximum hours
Fabricating	9	12	180
Finishing	1	3	30
Profit	8000	12000	

Let x be the number of pieces of A and y be the number of pieces of B manufactured to earn the maximum profit.

Then the mathematical model of the LPP is as follows: Maximize Z=8000x+12000y

Subject to $9x + 12y \le 180$,

x + 3y ≤ 30

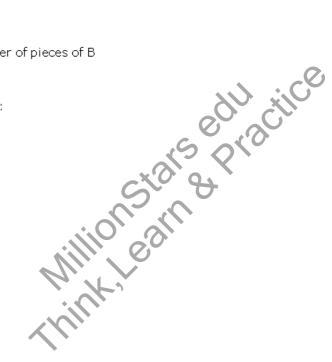
and $x \ge 0$, $y \ge 0$

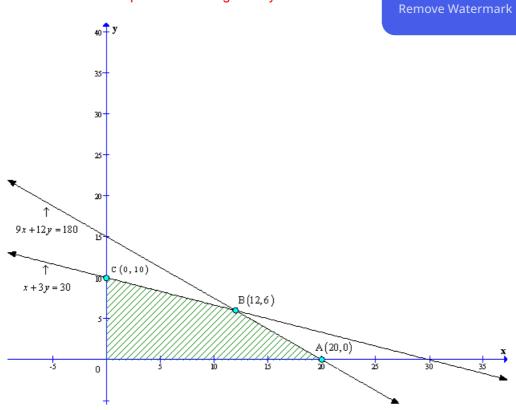
To solve the LPP we draw the lines,

$$9x + 12y = 180$$
,

$$x + 3y = 30$$

The feasible region of the LPP is shaded in graph.





The coordinates of the vertices (Corner - points) of shaded feasible region ABC are A(20, 0), B(12,6) and C(0, 10).

The values of the objective of function at these points are given in the following table:

P	oint (x_1, x_2)	Value of objective function Z = 8,000x + 12,000y
	A(20, 0)	Z = 1,60,000
	B(12, 6)	Z = 1,68,000
	C(0, 10)	Z = 1,20,000

 $12\ \mathrm{pieces}$ of Model A and 6 pieces of Model B should be eaned maximize the profit.

The maximum profit that can be eared is Rs. 1,68,000.

Linear Programming Ex 30.4 Q44

The given data can be written in the tabular form as follows:

Product	Racket	Bat	Maximum hours
Machine	1.5	3	42
Craftman	3	1	24
Profit	20	10	

Let \mathbf{x} be the number of rackets and \mathbf{y} be the number of bats made to earn the maximum profit.

Then the mathematical model of the LPP is as follows:

Maximize Z = 20x + 10y

Subject to $1.5x + 3y \le 42$,

 $3x + y \le 24$

and $x \ge 0$, $y \ge 0$

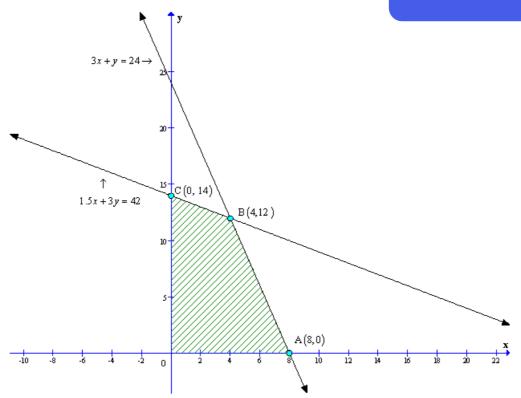
To solve the LPP we draw the lines,

$$1.5x + 3y = 42$$

$$3x + y = 24$$

The feasible region of the LPP is shaded in graph.





The coordinates of the vertices (Corner - points) of shaded feasible region ABC are A(8, 0), B(4,12) and C(0, 14).

The values of the objective of function at these points are given in the following table:

Point (x_1, x_2)	(x_2) Value of objective function $Z = 20x + 10$			
A(8, 0)	Z = 160			
B(4, 12)	Z = 200			
C(0, 14)	Z = 140			

4 rackets and 12 bats must be made if the factory is to work at full capacity. The maximum profit that can be eared is Rs. 200.

Linear Programming Ex 30.4 Q45

Let x be the number of desktop computers and y be the number of portable computers which merchant should stock to earn the maximum profit.

Then the mathematical model of the LPP is as follows:

Maximize Z = 4500x + 5000y

Subject to 25000x + 40000y ≤70,00,000

 $x + y \le 250$

and $x \ge 0$, $y \ge 0$

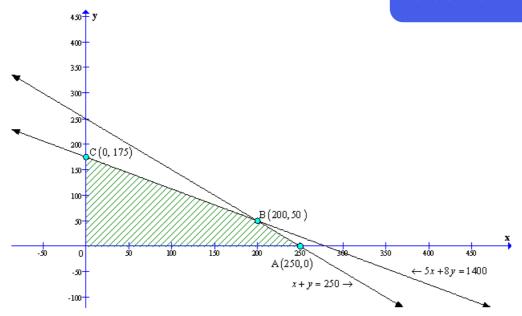
To solve the LPP we draw the lines,

5x + 8y = 1,400

x + y = 250

The feasible region of the LPP is shaded in graph.

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The coordinates of the vertices (Corner - points) of shaded feasible region ABC are A (250, 0),B(200,50) and C(0, 175).

The values of the objective of function at these points are given in the following table:

Point (x_1, x_2)	Value of objective function Z = 4500x + 5000y
A (250, 0)	Z = 11,25,000
B(200, 50)	Z = 11,50,000
C(0, 175)	Z = 8, 75, 000

The merchant should stock 200 personal computer and 50 portable computers to earn maximum profit. The maximum profit that can be eared is Rs. 11,50,000.

Linear Programming Ex 30.4 Q46

Let x be the number of dolls of type A and y be the number of dolls of type B should be produced to earn the maximum profit.

Then the mathematical model of the LPP is as follows:

Maximize Z = 12x + 16y

Subject to $x + y \le 1200$

$$\frac{1}{2}$$
x - y ≥ 0

and
$$x \ge 0$$
, $y \ge 0$

To solve the LPP we draw the lines,

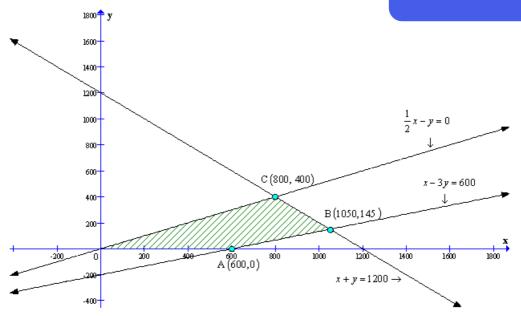
$$x + y = 1200$$

$$\frac{1}{2} \times - y = 0$$

$$x - 3y = 600$$

The feasible region of the LPP is shaded in graph.

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The coordinates of the vertices (Corner - points) of shaded feasible region ABC are A(600, 0), B(1050, 145) and C(800, 400).

The values of the objective of function at these points are given in the following table:

Point (x_1, x_2)	Value of objective function Z = 12x + 16y		
A (600, 0)	Z = 7200		
B(1050, 145)	Z = 14920		
C(800, 400)	Z = 16000		

The toy company should manufacture 800 dolls of type A and 400 dolls of type B to earn maximum profit. The maximum profit that can be eared is Rs. 16,000.

Linear Programming Ex 30.4 Q47

Let x kg of fertiliser F_1 and y kg of fertiliser F_2 should be used to minimise the cost.

Then the mathematical model of the LPP is as follows:

Maximize Z = 6x + 5ySubject to $10x + 5y \ge 1400$ $6x + 10y \ge 1400$ and $x \ge 0$, $y \ge 0$

To solve the LPP we draw the lines,

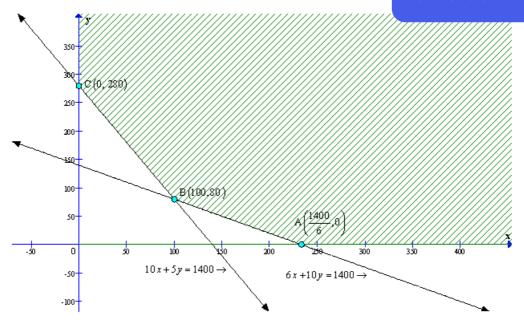
10x + 5y = 1400

6x + 10y = 1400

The feasible region of the LPP is shaded in graph.

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The coordinates of the vertices (Corner - points) of shaded feasible region ABC are $A\left(\frac{1400}{6},\,0\right)$, B(100,80) and $C(0,\,280)$.

The values of the objective of function at these points are given in the following table:

Point (x_1, x_2)	Value of objective function Z = 6x + 5y
$A\left(\frac{1400}{6}, 0\right)$	Z = 1400
B(100, 80)	Z = 1000
C(0, 280)	Z = 1400

100 kg of fertiliser $\rm F_1$ and 80 kg of fertiliser $\rm F_2$ to earn minimise the cost. The maximum cost Rs. 1,000.

Linear Programming Ex 30.4 Q48

Let x units of item M and y units of item N should be produced to maximise the cost.

Then the mathematical model of the LPP is as follows:

Maximize Z = 600x + 400y

Subject to $\times + 2y \le 12$

 $2x + y \le 12$

× + 1.25y ≥ 5

and $x \ge 0$, $y \ge 0$

To solve the LPP we draw the lines,

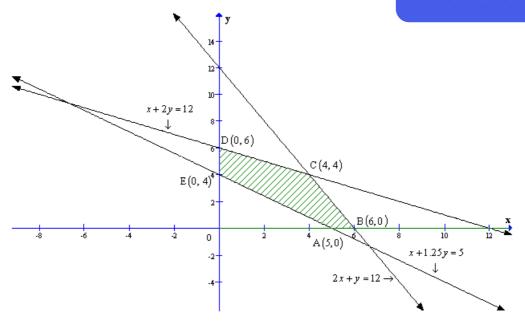
x + 2y = 12

2x + y = 12

x + 1.25y = 5

The feasible region of the LPP is shaded in graph.

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The coordinates of the vertices (Corner - points) of shaded feasible region ABCDE are A(5, 0), B(6, 0), C(4, 4), D(0, 6) and E(0, 4).

The values of the objective of function at these points are given in the following table:

Point (x_1, x_2)	Value of objective function Z = 600x + 400y
A(5, 0)	Z = 3000
B(6, 0)	Z = 3600
C(4, 4)	Z = 4000
D(0,6)	Z = 2400
E(0, 4)	Z = 1600

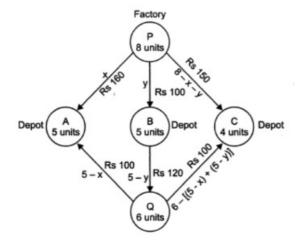
4 units of item M and 4 units of item N should be produced to maximise the profit. The maximum profit is Rs. 4,000.

Linear Programming Ex 30.4 Q49

Let x and y units of commodity be transported from factory P to the depots at A and B respectively.

Then (8 - x - y) units will be transported to depot at C.

The flow is shown below.



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Hence we have, $x \ge 0$, $y \ge 0$ and $8 - x - y \ge 0$

i.e. $\times \ge 0$, $y \ge 0$ and $\times + y \ge 8$

Now, the weekly requirement of the depot at A is 5 units of the commodity. Since \times units are transported from the factory at P, remaining (5 - \times) units need to be transported from the factory at Q.

:5-x≥0 ⇒ x≤5

Similarly, (5 - y) and 6 - (5 - x + 5 - y) = x + y - 4 units are to be transported from the factory at Q to the depots at B and C respectively.

$$\therefore$$
 5 - y ≥ 0 and x + y - 4 ≥ 0
⇒ y ≤ 5 and x + y ≥ 4

Total transportation cost Z is given by

$$Z = 160x+100y+100(5-x)+120(5-y)+100(x+y-4)+150(8-x-y)$$

$$Z = 10(x - 7y + 190)$$

So the mathematical model of given LPP is as follows.

Minimize Z = 10(x - 7y + 190)

Subject to x + y ≤ 8

 $x \le 5, y \le 5$

 $x + y \ge 4$

 $x \ge 0, y \ge 0$

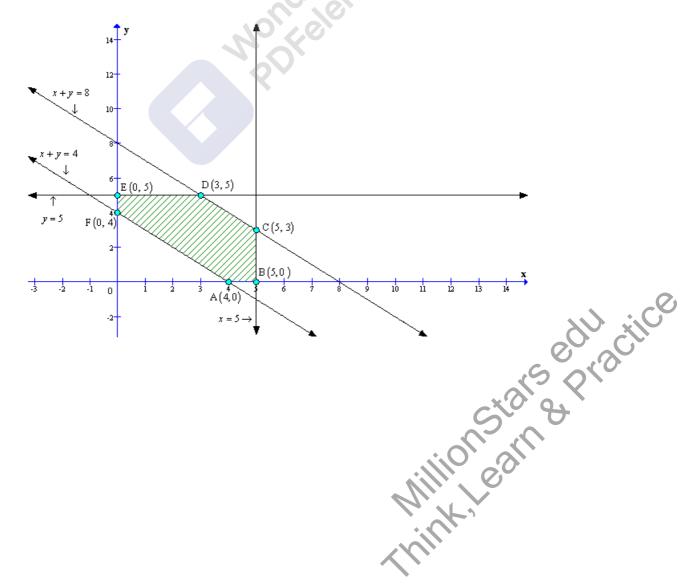
To solve the LPP we draw the lines,

x + y = 8

x = 5, y = 5

x + y = 4

The feasible region of the LPP is shaded in graph.





The coordinates of the vertices (Corner - points) of shaded feasible region ABCDEF A(4, 0), B(5, 0), C(5, 3), D(3, 5), E(0, 5) and F(0, 4).

The values of the objective of function at these points are given in the following table:

Point (x_1, x_2)	Value of objective function $Z = 10(x - 7y + 190)$
A(4, 0)	Z = 1940
B(5, 0)	Z = 1950
C(5, 3)	Z = 1740
D(3,5)	Z = 1580
E(0,5)	Z = 1550
F(0,4)	Z = 1620

Deliver 0, 5, 3 units from factory at P and 5, 0, 1 from the factory at Q to the depots at A, B and C respectively. The minimum transportation $\cos t$ is Rs. 1550.

Linear Programming Ex 30.4 Q50

Let the mixture contains x toys of type A and y toys of type B.

Tuno of tous	No. of toys	Machine I	Machine II	Machine III	Profit
Type or toys		(in min)	(in min)	(in min)	Rs.
Α	×	12x	18×	6x	7.5x
В	У	6у	0	9у	5у
Total	х+у	12x + 6y	18×	6x + 9y	7.5x + 5y
Requirement		360	360	360	

Then the mathematical model of the LPP is as follows:

Maximize Z = 7.5x + 5y

Subject to $12x + 6y \le 360 \Rightarrow 2x + y \le 60$

18x ≤ 360 ⇒ x ≤ 20

 $6x + 9y \le 360 \Rightarrow 2x + 3y \le 120$

and $x \ge 0$, $y \ge 0$

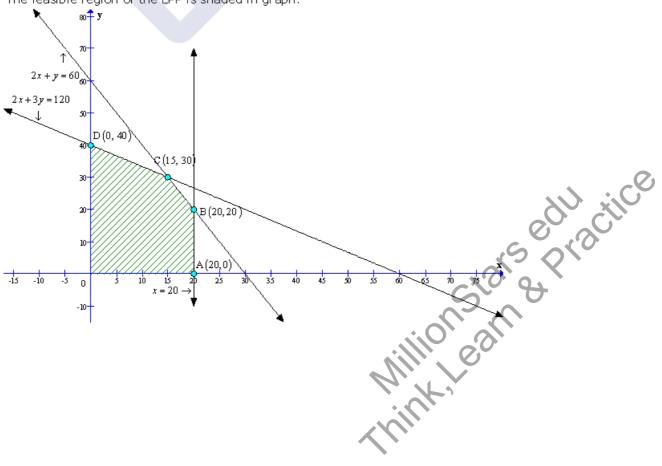
To solve the LPP we draw the lines,

$$2x + y = 60$$

$$x = 20$$

$$2x + 3y = 120$$

The feasible region of the LPP is shaded in graph.





The coordinates of the vertices (Corner - points) of shaded feas A(20, 0), B(20, 20), C(15, 30) and D(0, 40).

The values of the objective of function at these points are given in the following table:

Point (x_1, x_2)	Value of objective function Z = 7.5x+5y
A (20, 0)	Z = 150
B(20, 20)	Z = 250
C(15, 30)	Z = 262.5
D(0,40)	Z = 200

Manufacturer should make 15 toys of type A and 30 toys of type B to maximize the profit.

The maximum profit that can be earned is Rs. 262.5

Linear Programming Ex 30.4 Q51

Let x be the number of executive dass tickets and y be the number of economic class tickets.

Then the mathematical model of the LPP is as follows:

Maximize Z = 1000x + 600ySubject to $x + y \le 200$

x ≥ 20

 $y \ge 4x \Rightarrow -4x + y \ge 0$

and $x \ge 0$, $y \ge 0$

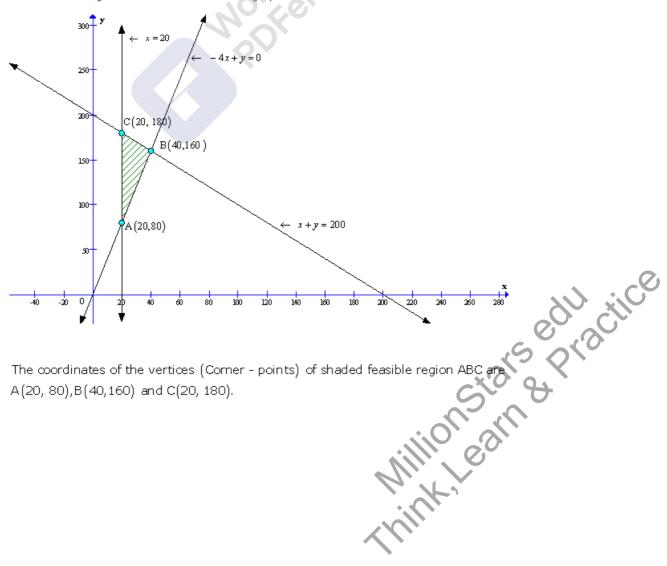
To solve the LPP we draw the lines,

x + y = 200

x = 20

-4x + y = 0

The feasible region of the LPP is shaded in graph





The values of the objective of function at these points are given

Paint (x_1, x_2)	Value of objective function Z = 1000x+600y
A (20, 80)	Z = 68,000
B(40, 160)	Z = 1,36,000
C(20, 180)	Z = 1,28,000

40 tickets of executive class and 160 tickets of economic dass must be sold to maximize the profit.

The maximum profit that can be earned is Rs. 1,36,000.

Linear Programming Ex 30.4 Q52

Then the mathematical model of the LPP is as follows: Maximize Z = 100x + 120ySubject to $2x + 3y \le 30$

 $3x + y \le 17$ and $x \ge 0$, $y \ge 0$

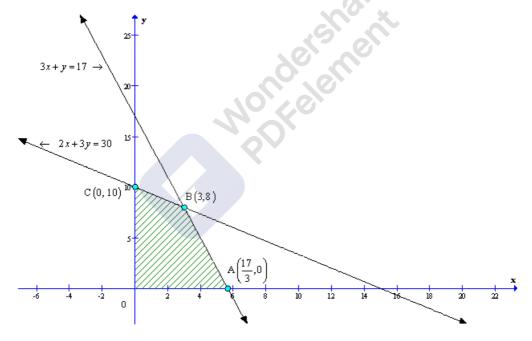
To solve the LPP we draw the lines,

2x + 3y = 30

3x + y = 17

The feasible region of the LPP is shaded in graph.

The feasible region of the LPP is shaded in graph.



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The coordinates of the vertices (Corner - points) of shaded feasis.

$$A\bigg(\frac{17}{3},\;0\bigg),B\big(3,8\big)$$
 and C(0, 10).

The values of the objective of function at these points are given in the following table:

Point (x_1, x_2)	Value of objective function Z = 100x + 120y
$A\left(\frac{17}{3}, 0\right)$	Z = 566.67
B(3, 8)	Z = 1260
C(0, 10)	Z = 1200

3 units of workers and 8 units of capital must be used to maximize the profit.

The maximum profit that can be earned is Rs. 1260.

Yes, because efficiency of a person does not depend on sex (male or female).



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Ex - 30.5

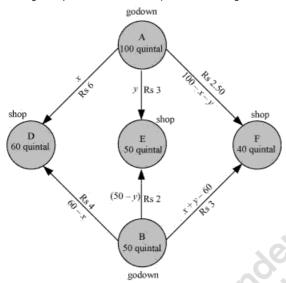
Linear Programming Ex 30.5 Q1

Let godown A supply x and y quintals of grain to the shops D and E respectively. Then, (100 - x - y) will be supplied to shop F.

The requirement at shop D is 60 quintals since x quintals are transported from godown A. Therefore, the remaining (60 -x) quintals will be transported from godown B.

Similarly, (50 -y) quintals and 40 -(100 - x - y) = (x + y - 60) quintals will be transported from godown B to shop E and F respectively.

The given problem can be represented diagrammatically as follows.



$$x \ge 0$$
, $y \ge 0$, and $100 - x - y \ge 0$
 $\Rightarrow x \ge 0$, $y \ge 0$, and $x + y \le 100$

 $\Rightarrow x \le 60, y \le 50, \text{ and } x + y \ge 60$

$$60-x \ge 0$$
, $50-y \ge 0$, and $x+y-60 \ge 0$

Total transportation cost z is given by,

$$z = 6x + 3y + 2.5(100 - x - y) + 4(60 - x) + 2(50 - y) + 3(x + y - 60)$$

= 6x + 3y + 250 - 2.5x - 2.5y + 240 - 4x + 100 - 2y + 3x + 3y - 180
= 2.5x + 1.5y + 410

The given problem can be formulated as

Minimize z = 2.5x + 1.5y + 410 ... (1)

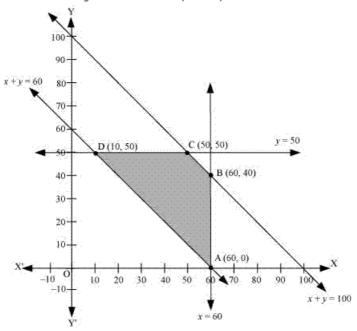
subject to the constraints,

$x + y \le 100$	(2)
$x \le 60$	(3)
$y \le 50$	(4)
$x + y \ge 60$	(5)
$x, y \ge 0$	(6)

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The feasible region determined by the system of constraints is as follows



The corner points are A (60, 0), B (60, 40), C (50, 50), and D (10, 50).

The values of z at these corner points are as follows.

Corner point	z = 2.5x + 1.5y + 410	
A (60, 0)	560	36
B (60, 40)	620	70.0
C (50, 50)	610	10
D (10, 50)	510	→ Minimum

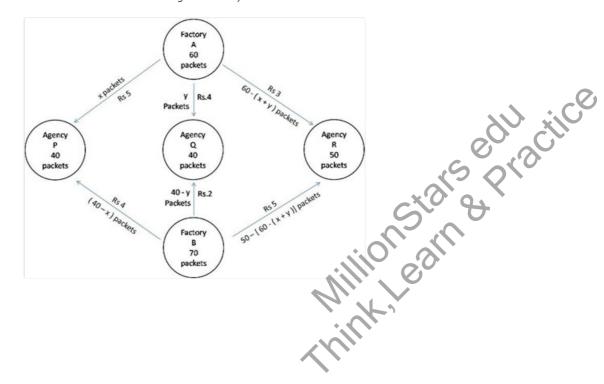
The minimum value of z is 510 at (10, 50).

Thus, the amount of grain transported from A to D, E, and F is 10 quintals, 50 quintals, and 40 quintals respectively and from B to D, E, and F is 50 quintals, 0 quintals, and 0 quintals respectively.

The minimum cost is Rs 510.

Linear Programming Ex 30.5 Q2

The given information can be exhibited diagramatically as below:





Let factory A transports x packets to agency P and y packet to agency factory A has capacity of 60 packets so, rest [60 - (x + y)] packets transported to agency R.

Since requirements are always non negative so,

$$\Rightarrow x, y \ge 0$$
 (first constraint)

and
$$60 - (x + y) \ge 0$$

 $(x + y) \le 60$ (second constraint)

Since requirement of agency P is 40 packet but it has recieved x packet, so (40 - x)packets are transported from factory B, requirement of agency Q is 40 packets but it has recieved y packets, so (40 - y) packets are transported from factory B. Requirement of agency R is 50 packets but it has recieved (60 - x - y) packets from factory A, so 50 - [60 - x - y] = (x + y - 10) is transported from factory B, As the requirements of agencies P,Q,R are always non negative, so,

$$40 - x \ge 0$$

$$\Rightarrow x \le 40$$
 (third constraint)

$$\Rightarrow$$
 $y \le 40$ (fourth constraint)

$$x + y - 10 \ge 0$$

$$\Rightarrow x+y \ge 10$$
 (fifth constraint)

Costs of transportation of each packet from factory A to agency P, Q, R are Rs 5,4,3 respectively and costs of transportation of each packet from factory B to agency P,Q,R are Rs 4,2,5 respectively,

Let Z be total cost of transportation so,

$$Z = 5x + 4y + 3[60 - x - y] + 4(40 - x) + 2(40 - y) + 5(x + y - 10)$$

= $5x + 4y + 180 - 3x - 3y + 160 - 4x + 80 - 2y + 5x + 5y - 50$
= $3x + 4y + 370$

Hence, mathematical formulation of LPP is find x and y which maximize Z = 3x + 4y + 370



subject to constraints,

 $x, y \ge 0$

 $x + y \le 60$

x ≤ 40

y ≤ 0

 $x + y \ge 10$

Region $x, y \ge 0$: It is represents first quandrant.

Region $x+y \le 60$: line x+y=60 meets axes at A_1 (60,0), B_1 (0,60) respectively. Region containing origin represents $x+y \le 60$ as (0,0) satisfies $x+y \le 60$.

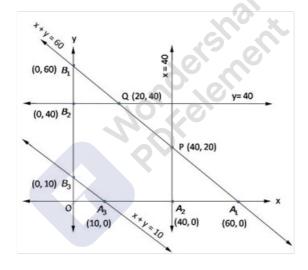
Region $x \le 40$: line x = 40 is parallel to y-axis and meets x-axis at A_2 (40,0). Region containing origin represents $x \le 40$ as (0,0) satisfies $x \le 40$.

Region $y \le 40$: line y = 40 is parallel to x-axis and meets y-axis at $B_2(0,40)$. Region containing origin represents $y \le 40$ as $\{0,0\}$ satisfies $y \le 40$.

Region $x+y \ge 10$: line x+y=10 meets axes at A_2 (10,0), B_3 (0,10) respectively. Region containing origin represents $x+y \ge 10$ as (0,0) does not satisfy $x+y \ge 10$.

Shaded region $A_3A_2PQB_2B_3$ represents feasible region. Point P (40,20) is obtained by solving x = 40 and x + y = 60

Point Q (20, 40) is obtained by solving y = 40 and x + y = 60



The value of Z = 3x + 4y + 370 at

 $A_3(10,0) = 3(10) + 4(0) + 370 = 400$

 $A_2(40,0) = 3(40) + 4(0) + 370 = 490$

P(40,20) = 3(40) + 4(20) + 370 = 570

Q(20,40) = 3(20) + 4(40) + 370 = 590

 $B_2(0,40) = 3(0) + 4(40) + 370 = 530$

 $B_3(0,10) = 3(0) + 4(10) + 370 = 410$

minimum Z = 400 at x = 10, y = 0

From $A \rightarrow P = 10$ packets

From $A \rightarrow Q = 0$ packets

From $A \rightarrow R = 50$ packets

From $B \rightarrow P = 30$ packets

From $B \rightarrow Q = 40$ packets

From $B \rightarrow R = 0$ packets

minimum cost = Rs 400

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