





Let p denote the probability of having defective item, so

$$p = 6\% = \frac{6}{100} = \frac{3}{50}$$

So,
$$q = 1 - p$$
$$= 1 - \frac{3}{50}$$
$$= \frac{47}{50}$$

[Since
$$p + q = 1$$
]

Let X denote the number of defective items in a sample of 8 items. Then, the proof getting r defective bulks is

$$P(X = r) = {^{n}C_{r}p^{r}q^{n-r}}$$

$$P(X = r) = {}^{8}C_{r} \left(\frac{3}{50}\right)^{r} \left(\frac{47}{50}\right)^{8-r}$$

[Using equation (1)]

Therefore, probability of getting not more then one defective item

$$= P\left(X=0\right) + P\left(X=1\right)$$

$$= {}^{8}C_{0} \left(\frac{3}{50}\right)^{0} \left(\frac{47}{50}\right)^{8-0} + {}^{8}C_{1} \left(\frac{3}{50}\right)^{1} \left(\frac{47}{50}\right)^{8-1}$$

$$= 1.1 \cdot \left(\frac{47}{50}\right)^8 + 8 \cdot \frac{3}{50} \cdot \left(\frac{47}{50}\right)^7$$

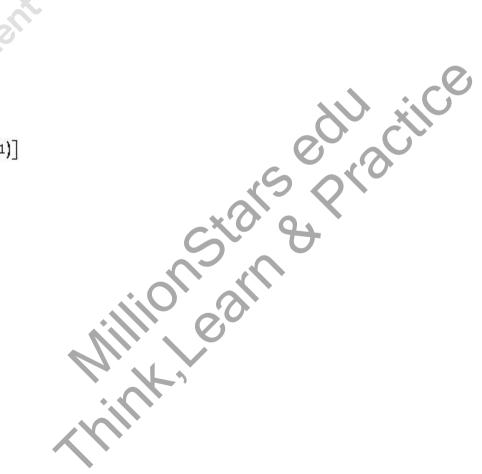
$$= \left(\frac{47}{50}\right)^7 \left(\frac{47}{50} + \frac{24}{50}\right)$$

$$= \left(\frac{71}{50}\right) \left(\frac{47}{50}\right)^7$$

$$= (1.42) \times (0.94)^7$$

The required probability is,

$$(1.42) \times (0.94)^7$$



[Using **(1)**]

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Probability of getting head on one throw of coin = $\frac{1}{2}$

So,
$$p = \frac{1}{2}$$

$$q = 1 - \frac{1}{2}$$

$$q = \frac{1}{2}$$
 [Since $p + q = 1$]

The coin is tossed 5 times. Let X denote the number of getting head as 5 tosses of coins. So probability of getting r heads in n tosses of coin is given by

$$P(X = r) = {^nC_r}p^rq^{n-r}$$

$$P(X = r) = {^5C_r}\left(\frac{1}{2}\right)^r\left(\frac{1}{2}\right)^{5-r} \qquad ---(1)$$

Probability of getting at least 3 heads

$$= P(X = 3) + P(X = 4) + P(X = 5)$$

$$= {}^{5}C_{3} \left(\frac{1}{2}\right)^{3} \cdot \left(\frac{1}{2}\right)^{5-3} + {}^{5}C_{4} \left(\frac{1}{2}\right)^{4} \left(\frac{1}{2}\right)^{5-4} + {}^{5}C_{5} \left(\frac{1}{2}\right)^{5} \left(\frac{1}{2}\right)^{0}$$

$$= {}^{5}C_{3} \left(\frac{1}{2}\right)^{3} \left(\frac{1}{2}\right)^{2} + {}^{5}C_{4} \left(\frac{1}{2}\right)^{4} \left(\frac{1}{2}\right) + {}^{5}C_{5} \left(\frac{1}{2}\right)^{5} \cdot 1$$

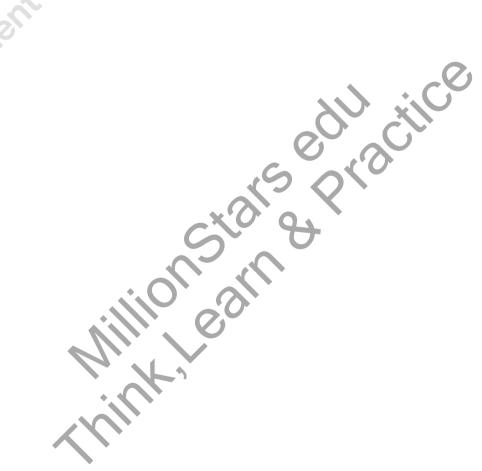
$$= {}^{5 \cdot 4} \cdot \left(\frac{1}{2}\right)^{5} + 5 \left(\frac{1}{2}\right)^{5} + 1 \cdot \left(\frac{1}{2}\right)^{5}$$

$$= \left(\frac{1}{2}\right)^{5} \left[10 + 5 + 1\right]$$

$$= 16 \cdot \frac{1}{32}$$

$$= \frac{1}{2}$$

The required probability is = $\frac{1}{2}$





$$p = \frac{1}{2}$$

$$q = 1 - \frac{1}{2}$$

$$q = \frac{1}{2}$$
 [Since $p + q = 1$]

Let X denote the number tail obtained on the toss of coin 5 times. So probability of getting r tails in n tosses of coin is given by

$$P(X = r) = {}^{n}C_{r}p^{r}q^{n-r}$$

$$= {}^{5}C_{r}\left(\frac{1}{2}\right)^{r}\left(\frac{1}{2}\right)^{5-r}$$
---(1)

Probability of getting tail an odd number of times

$$= P(X = 1) + P(X = 3) + P(X = 5)$$

$$= {}^{5}C_{3} \left(\frac{1}{2}\right)^{3} \left(\frac{1}{2}\right)^{5-1} + {}^{5}C_{3} \left(\frac{1}{2}\right)^{3} \left(\frac{1}{2}\right)^{5-3} + {}^{5}C_{5} \left(\frac{1}{2}\right)^{5} \left(\frac{1}{2}\right)^{0}$$

$$= 5 \cdot \left(\frac{1}{2}\right)^{5} + \frac{5 \cdot 4}{2} \cdot \left(\frac{1}{2}\right)^{5} + 1 \cdot \left(\frac{1}{2}\right)^{5}$$

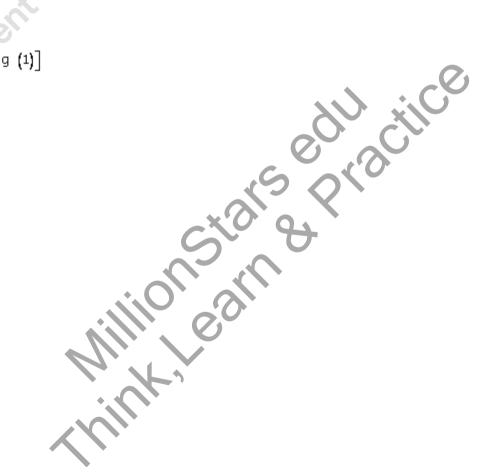
$$= \left(\frac{1}{2}\right)^{5} \left[5 + 10 + 1\right]$$

$$= 16 \cdot \left(\frac{1}{2}\right)^{5}$$

$$= 16 \cdot \frac{1}{32}$$

$$= \frac{1}{2}$$

The required probability is $=\frac{1}{2}$





Let *p* be the probability of getting a sum of 9 and it considered as success.

Sum of a 9 on a pair of dice

$$= \{(3,6), (4,5), (5,4), (6,3)\}$$

So,
$$p = \frac{4}{36}$$
$$p = \frac{1}{9}$$
$$q = 1 - \frac{1}{9}$$
$$q = \frac{8}{9}$$

Since
$$p + q = 1$$

Let X denote the number of success in throw of a pair of dice 6 times. So probability of qetting r success out of n is given by

$$P\left(X=r\right)={}^{n}C_{r}p^{r}q^{n-r}$$

Probability of getting at least 5 success

$$= P(X = 5) + P(X = 6)$$

$$= {}^{6}C_{5} \left(\frac{1}{9}\right)^{5} \left(\frac{8}{9}\right)^{6-5} + {}^{6}C_{6} \left(\frac{1}{9}\right)^{6} \left(\frac{8}{9}\right)^{6-6}$$

$$= 6\left(\frac{1}{9}\right)^{5} \left(\frac{8}{9}\right)^{1} + 1 \cdot \left(\frac{1}{9}\right)^{6} \left(\frac{8}{9}\right)^{0}$$

$$= \left(\frac{1}{9}\right)^{5} \left[\frac{48}{9} + \frac{1}{9}\right]$$

$$= \frac{49}{9} \times \left(\frac{1}{9}\right)^{5}$$

$$= \frac{49}{9} 6$$

Using (1)



Required probability =
$$\frac{49}{96}$$





 $p = \frac{1}{2}$ $q = 1 - \frac{1}{2}$ $q = \frac{1}{2}$ [Since p + q = 1]

Let X denote the number of heads on tossing the ∞ in 6 times. Probability of getting r in tossing the ∞ in n times is given by

$$P\left(X=r\right) = {^{n}C_{r}}p^{r}q^{n-r} \qquad \qquad ---\left(1\right)$$

Probability of getting at least three heads

$$= P(X = 3) + P(X = 4) + P(X = 5) + P(X = 6)$$

$$= 1 - [P(X = 0) + P(X = 1) + P(X = 2)]$$

$$= 1 - \left[{}^{6}C_{0} \left(\frac{1}{2}\right)^{0} \left(\frac{1}{2}\right)^{6-0} + {}^{6}C_{1} \left(\frac{1}{2}\right)^{1} \left(\frac{1}{2}\right)^{6-1} + {}^{6}C_{2} \left(\frac{1}{2}\right)^{2} \left(\frac{1}{2}\right)^{6-2} \right]$$

$$= 1 - \left[1 \cdot \left(\frac{1}{2}\right)^{6} + 6 \left(\frac{1}{2}\right)^{6} + \frac{6 \cdot 5}{2} \cdot \left(\frac{1}{2}\right)^{6} \right]$$

$$= 1 - \left[\left(\frac{1}{2}\right)^{6} \left(1 + 6 + 15\right) \right]$$

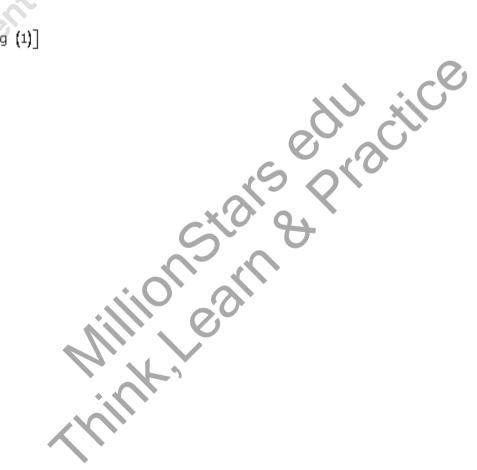
$$= 1 - \left[\frac{22}{64} \right]$$

$$= \frac{64 - 22}{64}$$

$$= \frac{42}{64}$$

$$= 21$$

Required probability = $\frac{21}{32}$





 $p = \frac{1}{6}$ $q = 1 - \frac{1}{6}$ $q = \frac{5}{6}$ [Since p + q = 1]

Let X denote the variable showing the number of turning 4 up in 2 tosses of die. Probability of getting 4, r times in n tosses of a die is given by

$$P(X = r) = {}^{n}C_{r}p^{r}q^{n-r}$$

$$= {}^{2}C_{r}\left(\frac{1}{6}\right)^{2}\left(\frac{5}{6}\right)^{2-r}$$
---(1)

Probability of getting 4 at least once in tow tosses of a fair die

$$= P(X = 1) + P(X = 2)$$

$$= 1 - P(X = 0)$$

$$= 1 - \left[{}^{2}C_{0}\left(\frac{1}{6}\right)^{0}\left(\frac{5}{6}\right)^{2-0}\right]$$

$$= 1 - \left[1 \cdot 1 \cdot \left(\frac{5}{6}\right)^{2}\right]$$

$$= 1 - \left[\frac{25}{36}\right]$$

$$= \frac{36 - 25}{36}$$

$$= \frac{11}{36}$$

[Using **(1)**]



Required probability = $\frac{11}{36}$





$$p = \frac{1}{2}$$

$$q = 1 - \frac{1}{2}$$

$$q = \frac{1}{2}$$
[Since $p + q = 1$]

Let X denote the variable representing number of heads on 5 tosses of a fair coin. Probability of getting r an n tosses of a fair coin, so

$$P(X = r) = {^nC_r}p^rq^{n-r}$$

$$P(X = r) = {^5C_r}\left(\frac{1}{2}\right)^r\left(\frac{1}{2}\right)^{5-r}$$

$$---(1)$$

Probability of getting head on an even number of tosses of coin

$$= P(X = 0) + P(X = 2) + P(X = 4)$$

$$= {}^{5}C_{0} \left(\frac{1}{2}\right)^{0} \left(\frac{1}{2}\right)^{5-0} + {}^{5}C_{2} \left(\frac{1}{2}\right)^{2} \left(\frac{1}{2}\right)^{5-2} + {}^{5}C_{4} \left(\frac{1}{2}\right)^{4} \left(\frac{1}{2}\right)^{5-4}$$

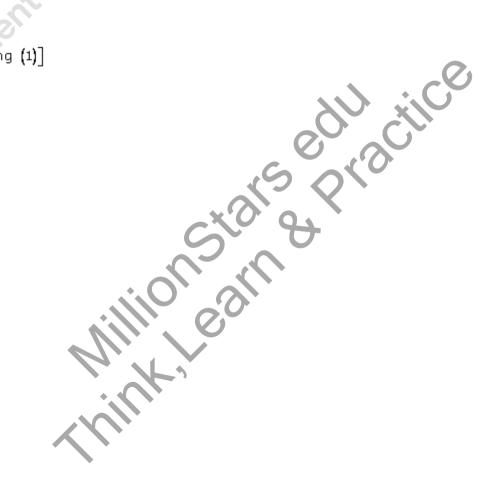
$$= 1 \cdot 1 \cdot \left(\frac{1}{2}\right)^{5} + \frac{5 \cdot 4}{2} \cdot \left(\frac{1}{2}\right)^{5} + 5 \cdot \left(\frac{1}{2}\right)^{5}$$

$$= \left(\frac{1}{2}\right)^{5} \left[1 + 10 + 5\right]$$

$$= 16 \times \frac{1}{32}$$

$$= \frac{1}{2}$$

Required probability = $\frac{1}{2}$





$$p = \frac{1}{4}$$

$$q = 1 - p$$

$$= 1 - \frac{1}{4}$$

$$q = \frac{3}{4}$$
[Since $p + q = 1$]

Let X denote the variable representing the number of times hittintg the target out of 7 fires. Probability of hitting the target r times out of n fires is given by,

$$P\left(X=r\right) = {^{n}C_{r}p^{r}q^{n-r}}$$

$$= {^{7}C_{r}} \left(\frac{1}{4}\right)^{r} \left(\frac{3}{4}\right)^{7-r}$$

$$= ---\left(1\right)^{r}$$

Probability of hitting the target at least twice

$$= P(X = 2) + P(X = 3) + P(X = 4) + P(X = 5) + P(X = 6) + P(X = 7)$$

$$= 1 - \left[P(X = 0) + P(X = 1)\right]$$

$$= 1 - \left[{}^{7}C_{0}\left(\frac{1}{4}\right)^{0}\left(\frac{3}{4}\right)^{7-0} + {}^{7}C_{1}\left(\frac{1}{4}\right)^{1}\left(\frac{3}{4}\right)^{7-1}\right]$$

$$= 1 - \left[1 \cdot 1 \cdot \left(\frac{3}{4}\right)^{7} + 7 \cdot \frac{1}{4} \cdot \left(\frac{3}{4}\right)^{6}\right]$$

$$= 1 - \left(\frac{3}{4}\right)^{6}\left(\frac{3}{4} + \frac{7}{4}\right)$$

$$= 1 - \left(\frac{3}{4}\right)^{6}\left(\frac{10}{4}\right)$$

$$= 1 - \frac{7290}{16384}$$

$$= \frac{9194}{16384}$$

$$= \frac{4547}{8192}$$



Binomial Distribution Ex 33.1 Q9



Let the probability of one telephone number out of 15 is busy between 2 PM and 3 PM be 'p'. then P = 1/15; probability that number is not busy, q = 1-p

Q = 14/16. Binomial distribution is
$$\left(\frac{14}{15} + \frac{1}{15}\right)^6$$

Since 6 numbers are called we find the probability for none of the numbers are busy is P(0)
One number is busy P(1); Two numbers are busy is P(2)
Three numbers are busy is P(3); Four numbers are busy is P(4); Five numbers are busy is P(5); Six numbers are busy is P(6).

$$P(0) = {}^{6}C_{0} \left(\frac{14}{15}\right)^{6}$$

$$P(1) = {}^{6}C_{1} \left(\frac{14}{15}\right)^{5} \left(\frac{1}{15}\right)^{1}$$

$$P(2) = {}^{6}C_{2} \left(\frac{14}{15}\right)^{4} \left(\frac{1}{15}\right)^{2}$$

$$P(3) = {}^{6}C_{3} \left(\frac{14}{15}\right)^{3} \left(\frac{1}{15}\right)^{3}$$

$$P(4) = {}^{6}C_{4} \left(\frac{14}{15}\right)^{2} \left(\frac{1}{15}\right)^{4}$$

$$P(5) = {}^{6}C_{5} \left(\frac{14}{15}\right)^{1} \left(\frac{1}{15}\right)^{5}$$

$$P(6) = {}^{6}C_{6} \left(\frac{14}{15}\right)^{0} \left(\frac{1}{15}\right)^{6}$$

Probability that at least 3 of the numbers will be busy

$$P(3) + P(4) + P(5) + P(6) = 0.05$$

Binomial Distribution Ex 33.1 Q10



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p denote the probability of success

p = Probability of getting 5 or 6 in a throw of die.

$$=\frac{2}{6}$$

$$p = \frac{1}{3}$$

$$q=1-\frac{1}{3}$$

[Since
$$p + q = 1$$
]

$$q=\frac{2}{3}$$

Let X denote the number of success in six throws of a dic. Probability of getting r success in six throws of an unbiased dic is given by

$$P\left(X=r\right) = {^{n}C_{r}p^{r}q^{n-r}}$$
$$= {^{6}C_{r}\left(\frac{1}{3}\right)^{r}\left(\frac{2}{3}\right)^{6-r}}$$

$$P(X \ge 4)$$

= $P(X = 4) + P(X = 5) + P(X = 6)$

$$\begin{split} &= {}^{6}C_{4} \left(\frac{1}{3}\right)^{4} \left(\frac{2}{3}\right)^{6-4} + {}^{6}C_{5} \left(\frac{1}{3}\right)^{5} \left(\frac{2}{3}\right)^{6-5} + {}^{6}C_{6} \left(\frac{1}{3}\right)^{6} \left(\frac{2}{3}\right)^{6-6} \\ &= \frac{6.5}{2} \left(\frac{1}{3}\right)^{4} \left(\frac{2}{3}\right)^{2} + 6 \left(\frac{1}{3}\right)^{5} \left(\frac{2}{3}\right) + 1 \cdot \left(\frac{1}{3}\right)^{6} \cdot 1 \\ &= 15 \cdot \frac{1}{81} \cdot \frac{4}{9} + 6 \cdot \frac{1}{243} \cdot \frac{2}{3} + \frac{1}{729} \\ &= \frac{60}{729} + \frac{12}{729} + \frac{1}{729} \end{split}$$

$$= \frac{729}{729} + \frac{729}{729}$$
$$= \frac{73}{729}$$

Required probability =
$$\frac{73}{729}$$





$$p = \frac{1}{2}$$

$$q = 1 - \frac{1}{2}$$
 [Since $p + q = 1$]
$$q = \frac{1}{2}$$

Let X denote the variable representing the number of getting heads on throw of 8 coins. Probability of getting r heads in a throw of n coins is given by

$$P(X = r) = {}^{n}C_{r}p^{r}q^{n-r}$$

$$= {}^{8}C_{r}\left(\frac{1}{2}\right)^{r}\left(\frac{1}{2}\right)^{8-r}$$
---(1)

Probability of getting at least six heads

$$= P(X = 6) + P(X = 7) + P(X = 8)$$

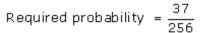
$$= {}^{8}C_{6} \left(\frac{1}{2}\right)^{8} \left(\frac{1}{2}\right)^{8-6} + {}^{8}C_{7} \left(\frac{1}{2}\right)^{7} \left(\frac{1}{2}\right)^{8-7} + {}^{8}C_{8} \left(\frac{1}{2}\right)^{8} \left(\frac{1}{2}\right)^{8-8}$$

$$= \frac{8 \cdot 7}{2} \left(\frac{1}{2}\right)^{8} + 8 \left(\frac{1}{2}\right)^{8} + 1 \cdot \left(\frac{1}{2}\right)^{8} \cdot 1$$

$$= \left(\frac{1}{2}\right)^{8} \left[28 + 8 + 1\right]$$

$$= \frac{1}{256} (37)$$

$$= \frac{37}{256}$$



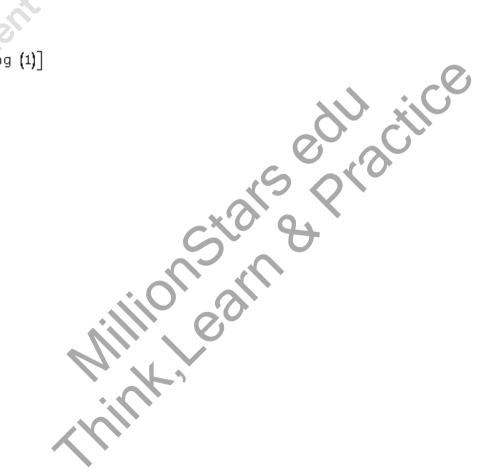
Binomial Distribution Ex 33.1 Q12

Let p denote the probability of getting one spade out of a deck of 52 cards, so

$$p = \frac{13}{52}$$
$$p = \frac{1}{4}$$

$$q=1-\frac{1}{4}$$

[Since p + q = 1]



$$q = \frac{1}{4}$$

Let ${\it X}$ denote the radom variable of number of spades out of 5 cards. Probability of getting r spades out of n cards is given by

$$P\left(X=r\right) = {^{n}C_{r}}p^{r}q^{n-r}$$

$$= {^{5}C_{r}}\left(\frac{1}{4}\right)^{r}\left(\frac{3}{4}\right)^{5-r}$$

$$= --- (1)$$

(i)

Probability of getting all five spades

$$= P(X = 5)$$

$$= {}^{5}C_{5}\left(\frac{1}{4}\right)^{5}\left(\frac{3}{4}\right)^{5-5}$$

$$= \frac{1}{1024}$$

Probability of getting 5 spades = $\frac{1}{1024}$

(ii)

Probability of getting only 3 spades

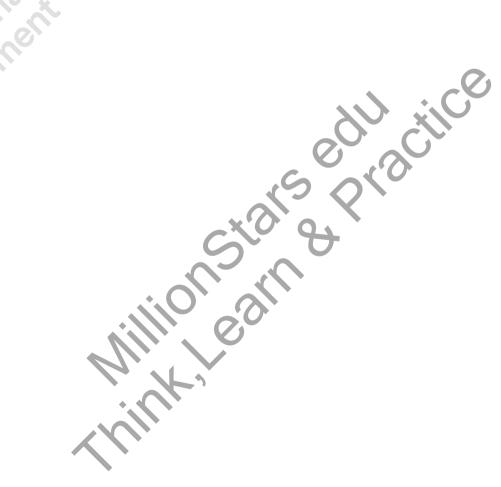
$$= P(X = 3)$$

$$= {}^{5}C_{3}\left(\frac{1}{4}\right)^{3}\left(\frac{3}{4}\right)^{5-3}$$

$$= \frac{5.4}{2}\left(\frac{1}{64}\right)\left(\frac{9}{16}\right)$$

$$= \frac{45}{512}$$

Probability of getting 3 spades = $\frac{45}{512}$





Probability that none is spade

$$= P (X = 0)$$

$$= {}^{5}C_{0} \left(\frac{1}{4}\right)^{0} \left(\frac{3}{4}\right)^{5-0}$$

$$= \frac{243}{1024}$$

Probability of getting non spade = $\frac{243}{1024}$

Binomial Distribution Ex 33.1 Q13

Let p be the probability of getting 1 white ball out of 7 red, 5 white and 8 black balls. So

$$p = \frac{5}{20}$$

$$p = \frac{1}{4}$$

$$q = 1 - \frac{1}{4}$$

$$q = \frac{3}{4}$$
[Since $p + q = 1$]

Let X denote the random variable of number of selecting white ball with replacement out of 4 balls. Probability of getting r white balls out of n balls is given by

$$P(X = r) = {}^{n}C_{r}p^{r}q^{n-r}$$

$$= {}^{4}C_{r}\left(\frac{1}{4}\right)^{r}\left(\frac{3}{4}\right)^{4-r}$$
---(1)

(i)

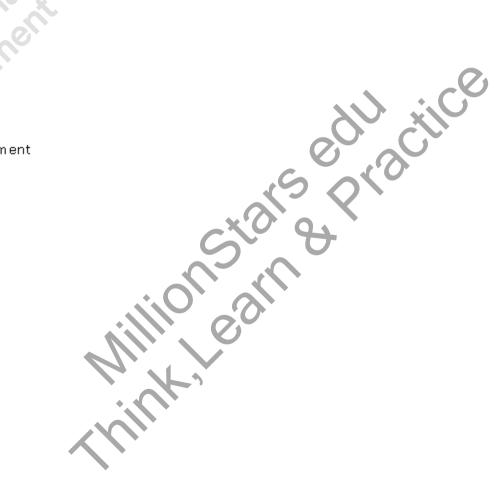
Probability of getting none white ball

Simily of getting from writte ball
$$= P\left(X = 0\right)$$

$$= {}^{4}C_{0}\left(\frac{1}{4}\right)^{0}\left(\frac{3}{4}\right)^{4-0}$$

$$= \left(\frac{3}{4}\right)^{4}$$

$$= \frac{81}{256}$$
[Using (1)]





Probability of getting none white ball = $\frac{81}{256}$

(ii)

Probability of getting all white balls

$$= P(X = 4)$$

$$= {}^{4}C_{4}\left(\frac{1}{4}\right)^{4}\left(\frac{3}{4}\right)^{4-0}$$

$$= \left(\frac{1}{4}\right)^{4}$$

$$= \frac{1}{256}$$

Probability of getting all white balls = $\frac{1}{256}$

(iii)

Probability of getting any two are white

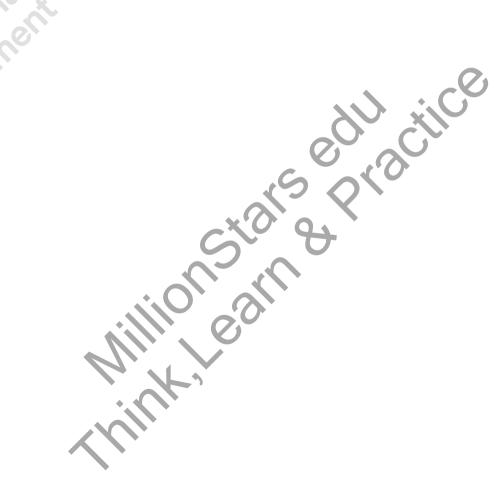
$$= P (X = 2)$$

$$= {}^{4}C_{2} \left(\frac{1}{4}\right)^{2} \left(\frac{3}{4}\right)^{4-2}$$

$$= \frac{4.3}{2} \cdot \frac{1}{16} \cdot \frac{9}{16}$$

$$= \frac{27}{128}$$

Probability of getting any two are white balls = $\frac{27}{128}$





https://millionstar.godaddysites.com/ Let p denote the probability of getting a ticket bearing number divisible by 10, So

$$p = \frac{10}{100}$$
 Since there are 10,20,30,40,50,60,70,80, 90,100 which are divisible by 10

$$p = \frac{1}{10}$$

$$q = 1 - \frac{1}{10}$$

$$q = \frac{9}{10}$$

[Since
$$p+q=1$$
]

Let X denote the variable representing the number of tickets bearing a number divisible by 10 out of 5 tickets. Probability of getting r tickets bearing a number divisible by 10 out of n tickets is given by

$$P\left(X=r\right) = {^{n}C_{r}p^{r}q^{n-r}}$$
$$= {^{5}C_{r}}\left(\frac{1}{10}\right)^{r}\left(\frac{9}{10}\right)^{5-r}$$

Probability of getting all the tickets bearing a number divisible by 10

$$= {}^{5}C_{5} \left(\frac{1}{10}\right)^{5} \left(\frac{9}{10}\right)^{5-5}$$

$$=1.\left(\frac{1}{10}\right)^5\left(\frac{9}{10}\right)^0$$

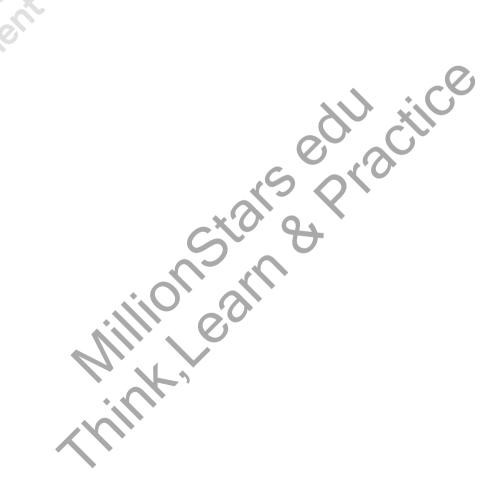
$$=\left(\frac{1}{10}\right)^5$$





Required probability = $\left(\frac{1}{10}\right)^5$







$$q = 1 - \frac{1}{10}$$

[Since
$$p + q = 1$$
]

$$q = \frac{9}{10}$$

Let X denote the variable presenting the number of balls marked with 0 out of four balls drawn. Probability of drawing r balls out of n balls that are marked 0 is given by

$$P(X = r) = {}^{n}C_{r}p^{r}q^{n-r}$$

$$= {}^{4}C_{r}\left(\frac{1}{10}\right)^{r}\left(\frac{9}{10}\right)^{4-r}$$
---(1)

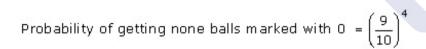
Probability of getting none balls marked with 0

$$= P\left(X = 0\right)$$

$$= {}^{4}C_{0} \left(\frac{1}{10}\right)^{0} \left(\frac{9}{10}\right)^{4-0}$$

$$= 1.1. \left(\frac{9}{10}\right)^4$$

$$= \left(\frac{9}{10}\right)^4$$









$$p = 5\%$$
 [Since 5% are defective items]
$$= \frac{5}{100}$$

$$p = \frac{1}{20}$$

$$q = 1 - \frac{1}{20}$$
 [Since $p + q = 1$]
$$q = \frac{19}{20}$$

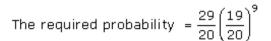
Let X denote the random variable representing the number of defective items out of 10 items. Probability of getting r defective items out of n items selected is given by,

$$P(X = r) = {}^{n}C_{r}p^{r}q^{n-r}$$

$$= {}^{10}C_{r}\left(\frac{1}{20}\right)^{r}\left(\frac{19}{20}\right)^{10-r}$$
---(1)

Probability of getting not more than one defective items

$$\begin{split} &= P\left(X=0\right) + P\left(X=1\right) \\ &= {}^{10}C_0 \left(\frac{1}{20}\right)^0 \left(\frac{19}{20}\right)^{10-0} + {}^{10}C_1 \left(\frac{1}{20}\right)^1 \left(\frac{19}{20}\right)^{10-1} \\ &= 1.1. \left(\frac{19}{20}\right)^{10} + 10. \frac{1}{20} \left(\frac{19}{20}\right)^9 \\ &= \left(\frac{19}{20}\right)^9 \left[\frac{19}{20} + \frac{10}{20}\right] \\ &= \frac{29}{20} \left(\frac{19}{20}\right)^9 \end{split}$$



Binomial Distribution Ex 33.1 Q17

Let p denote the probability that one bulb produced will fuse after 150 days, so

$$p = 0.05$$
$$= \frac{5}{100}$$

[It is given]







$$q = 1 - \frac{1}{20}$$

$$q = \frac{19}{20}$$

[Since
$$p + q = 1$$
]

Let X denote the number of fuse bulb out of 5 bulbs. Probability that r bulbs out of n will fuse in 150 days is given by

$$P(X = r) = {^{n}C_{r}p^{r}q^{n-r}}$$
$$= {^{5}C_{r}} \left(\frac{1}{20}\right)^{r} \left(\frac{19}{20}\right)^{5-r}$$

(i)

Probability that none is fuse = P(X = 0)

$$= {}^{5}C_{0} \left(\frac{1}{20}\right)^{0} \left(\frac{19}{20}\right)^{5-0}$$
$$= \left(\frac{19}{20}\right)^{5}$$

Probability that none will fuse = $\left(\frac{19}{20}\right)^5$



Probability that not more than 1 will fuse

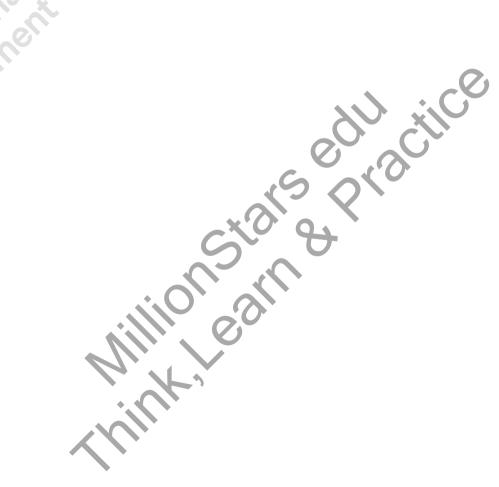
$$= P(X = 0) + P(X = 1)$$

$$= \left(\frac{19}{20}\right)^5 + {}^5C_1\left(\frac{1}{20}\right)^1 \left(\frac{19}{20}\right)^{5-1}$$

$$= \left(\frac{19}{20}\right)^4 \left[\frac{19}{20} + \frac{5}{20}\right]$$

$$= \left(\frac{24}{20}\right) \left(\frac{19}{20}\right)^4$$

Probability not more than one will fuse $=\left(\frac{6}{5}\right)\left(\frac{19}{20}\right)^4$



(iii)

Probability that more than one will fuse

$$= P(X = 2) + P(X = 3) + P(X = 4) + P(X = 5)$$

$$= 1 - [P(X = 0) + P(X = 1)]$$

$$= 1 - \left[\frac{6}{5}\left(\frac{19}{20}\right)^4\right]$$

Probability that more than one will fuse = $1 - \left[\frac{6}{5} \left(\frac{19}{20} \right)^4 \right]$

(iv)

Probability that that at least one will fuse

$$= P(X = 1) + P(X = 2) + P(X = 3) + P(X = 4) + P(X = 5)$$

$$= 1 - P(X = 0)$$

$$= 1 - \left[{}^{5}C_{0} \left(\frac{1}{20} \right)^{0} \left(\frac{19}{20} \right)^{5-0} \right]$$

$$= 1 - \left[\left(\frac{19}{20} \right)^{5} \right]$$

Probability that that at least one will fuse = $1 - \left(\frac{19}{20}\right)^5$





It is given that 90% of the people are right-handed.

$$\therefore p = P(\text{right-handed}) = \frac{9}{10}$$

$$q = P(\text{left-handed}) = 1 - \frac{9}{10} = \frac{1}{10}$$

Using binomial distribution, the probability that more than 6 people are right-handed is given by,

$$\sum_{r=7}^{10} {}^{10}C_r p^r q^{n-r} = \sum_{r=7}^{10} {}^{10}C_r \left(\frac{9}{10}\right)^r \left(\frac{1}{10}\right)^{10-r}$$

Therefore, the probability that at most 6 people are right-handed

= 1 - P (more than 6 are right-handed)

$$=1-\sum_{r=2}^{10} {}^{10}C_r (0.9)^r (0.1)^{10-r}$$







 $p = \frac{5}{16}$

$$q = 1 - \frac{5}{16}$$

Since
$$p + q = 1$$

$$q = \frac{11}{16}$$

Let X denote the number of red balls drawn out of four balls. Probability of getting r red balls out of n drawn balls is given by

$$\begin{split} P\left(X=r\right) &= \ ^{n}C_{r}p^{r}q^{n-r} \\ &= \ ^{4}C_{r}\left(\frac{5}{16}\right)^{r}\left(\frac{11}{16}\right)^{4-r} \end{split}$$

Probability of getting one red ball

$$= P(X = 1)$$

$$= {}^{4}C_{1} \left(\frac{5}{16}\right)^{1} \left(\frac{11}{16}\right)^{4-1}$$

$$= 4 \cdot \left(\frac{5}{16}\right) \left(\frac{11}{16}\right)^{3}$$

$$= \left(\frac{5}{4}\right) \left(\frac{11}{16}\right)^{3}$$



Required probability = $\left(\frac{5}{4}\right)\left(\frac{11}{16}\right)^3$



	Titipo://Titimorrotar:
X	P(X)
0	$\frac{7}{9} \times \frac{6}{8} = \frac{21}{36}$
1	$\frac{7}{9} \times \frac{2}{8} \times 2 = \frac{14}{36}$
2	$\frac{2}{9} \times \frac{1}{8} = \frac{1}{36}$

Binomial Distribution Ex 33.1 Q21

X	P (X)
0	${}^{3}C_{0}\left(\frac{3}{7}\right)^{0}\left(\frac{4}{7}\right)^{3-0} = \left(\frac{4}{7}\right)^{3} = \frac{64}{343}$
1	${}^{3}C_{1}\left(\frac{3}{7}\right)^{1}\left(\frac{4}{7}\right)^{3-1} = 3\cdot\left(\frac{3}{7}\right)\left(\frac{4}{7}\right)^{2} = \frac{144}{343}$
2	${}^{3}C_{2}\left(\frac{3}{7}\right)^{2}\left(\frac{4}{7}\right)^{3-2} = 3\cdot\left(\frac{3}{7}\right)^{2}\left(\frac{4}{7}\right) = \frac{108}{343}$
3	${}^{3}C_{3}\left(\frac{3}{7}\right)^{3}\left(\frac{4}{7}\right)^{3-0} = \left(\frac{3}{7}\right)^{3} = \frac{27}{343}$

Binomial Distribution Ex 33.1 Q22

Let p be the probability of getting doublet is a throw of a pair of dice, so

$$p = \frac{6}{36}$$

[Since
$$(1,1),(2,2),(3,3),(4,4),(5,5),(6,6)$$
 are doublets]

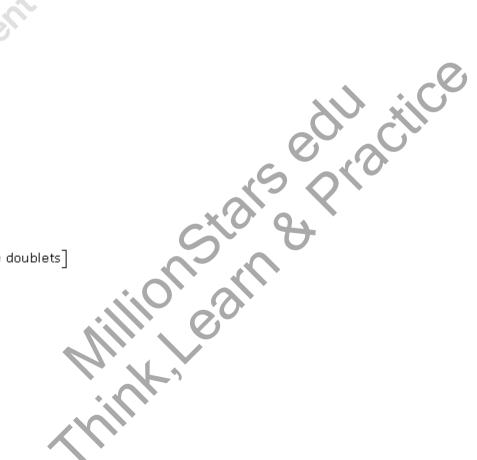
$$p = \frac{1}{6}$$

$$q=1-\frac{1}{6}$$

Since
$$p + q = 1$$

$$=\frac{5}{6}$$

Let X denote the number of getting doublets out of 4 times. So probability distribution is given by



Binomial Distribution Ex 33.1 Q23



X	P (X)
0	${}^{3}C_{0}\left(\frac{1}{6}\right)^{0}\left(\frac{5}{6}\right)^{3-0} = \left(\frac{5}{6}\right)^{3} = \frac{125}{216}$
1	${}^{3}C_{1}\left(\frac{1}{6}\right)^{1}\left(\frac{5}{6}\right)^{3-1} = 3\left(\frac{1}{6}\right)\left(\frac{1}{6}\right)^{2} = \frac{25}{72}$
2	${}^{3}C_{2}\left(\frac{1}{6}\right)^{2}\left(\frac{5}{6}\right)^{3-2} = 3\left(\frac{1}{6}\right)^{2}\left(\frac{5}{6}\right) = \frac{5}{72}$
3	${}^{3}C_{3}\left(\frac{1}{6}\right)^{3}\left(\frac{5}{6}\right)^{3-3} = \left(\frac{1}{6}\right)^{3} = \frac{1}{216}$

Binomial Distribution Ex 33.1 Q24

We know that, probability of getting head in a toss of coin $p = \frac{1}{2}$

Probability of not getting head $q = 1 - \frac{1}{2}$

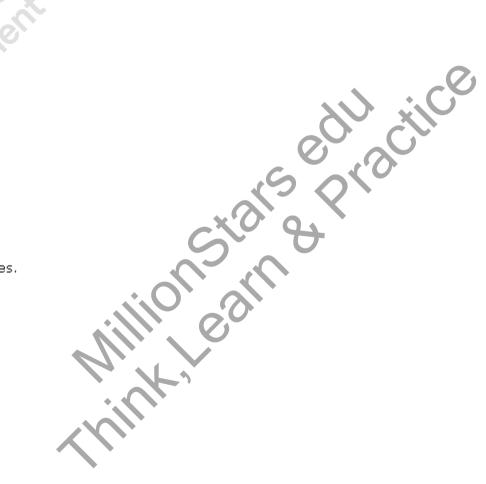
$$q = \frac{1}{2}$$

The coin is tossed 5 times. Let X denote the number of times head occur is 5 tosses.

$$P\left(X=r\right) = {^nC_r}p^rq^{n-r}$$
$$= {^5C_r}\left(\frac{1}{2}\right)^r\left(\frac{1}{2}\right)^{5-r}$$

Probability distribution is given by







[Since, numbers greater than 4 ∞ in a die = 5,6]

$$p = \frac{1}{3}$$

$$q=1-\frac{1}{3}$$

Since
$$p + q = 1$$

$$q = \frac{2}{3}$$

Let X denote the number of success in 2 throws of a die. Probability of getting r success in n thrown of a die is given by

$$P\left(X=r\right) = {^nC_r}p^rq^{n-r}$$

$$= {^2C_r}\left(\frac{1}{3}\right)^r\left(\frac{2}{3}\right)^{2-r}$$

$$= ---\left(1\right)$$

Probability distribution of number of success is given by

X	P (X)
0	${}^{2}C_{0}\left(\frac{1}{3}\right)^{0}\left(\frac{2}{3}\right)^{2-0} = \left(\frac{2}{3}\right)^{2} = \frac{4}{9}$
1	${}^{2}C_{1}\left(\frac{1}{3}\right)^{1}\left(\frac{2}{3}\right)^{2-1} = 2\cdot\left(\frac{1}{3}\right)\left(\frac{2}{3}\right) = \frac{4}{9}$
2	${}^{2}C_{2}\left(\frac{1}{3}\right)^{2}\left(\frac{2}{3}\right)^{2-2} = \left(\frac{1}{3}\right)^{2} = \frac{1}{9}$







 $\frac{\text{https://millionstar.godaddysites.com/}}{\text{Let } n \text{ denote the number of throws required to get a head and } X \text{ denote the amount}}$

He may get head on first toss or lose first and 2nd toss or lose first and won second toss probability distribution for X

Number of throws (n):

0

Amount won/lost (X):

1

2 -2

Probability P(X):

won/lost.

So probability distribution is given by

X	P(X)
0	1/4
1	$\frac{1}{2}$
-2	$\frac{1}{4}$

Binomial Distribution Ex 33.1 Q27



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p = probability of success

$$=\frac{3}{6}$$

$$p = \frac{1}{2}$$

$$q = 1 - \frac{1}{2}$$

[Since
$$p + q = 1$$
]

$$q = \frac{1}{2}$$

Let X denote the number of success in throw of 5 dice simultaneously. Probability of getting r success out of n throws of die is given by

$$P(X = r) = {}^{n}C_{r}p^{r}q^{n-r}$$

$$= {}^{5}C_{r}\left(\frac{1}{2}\right)^{r}\left(\frac{1}{2}\right)^{5-r}$$
---(1)

Probability getting at least 3 success

$$= P(X = 3) + P(X = 4) + P(X = 5)$$

$$= {}^{5}C_{3} \left(\frac{1}{2}\right)^{3} \left(\frac{1}{2}\right)^{5-3} + {}^{5}C_{4} \left(\frac{1}{2}\right)^{4} \left(\frac{1}{2}\right)^{5-4} + {}^{5}C_{5} \left(\frac{1}{2}\right)^{5} \left(\frac{1}{2}\right)^{5-5}$$

$$= \frac{5 \cdot 4}{2} \left(\frac{1}{2}\right)^{5} + 5 \cdot \left(\frac{1}{2}\right)^{5} + \left(\frac{1}{2}\right)^{5}$$

$$= \left(\frac{1}{2}\right)^{5} \left[10 + 5 + 1\right]$$

$$= \frac{16}{32}$$

$$= \frac{1}{2}$$

Required probability = $\frac{1}{2}$





p = 10% $= \frac{10}{100}$

$$p = \frac{1}{10}$$

$$q = 1 - \frac{1}{10}$$

$$q = \frac{9}{10}$$

[Since p + q = 1]

Let X denote the number of defective items drawn out of 8 items. Probability of qetting r defective items out of a sample of 8 items is given by

$$P\left(X=r\right) = {^nC_r}p^rq^{n-r}$$
$$= {^8C_r}\left(\frac{1}{10}\right)^r\left(\frac{9}{10}\right)^{8-r}$$

---(

Probability of getting 2 defective items

$$= P\left(X = 2\right)$$

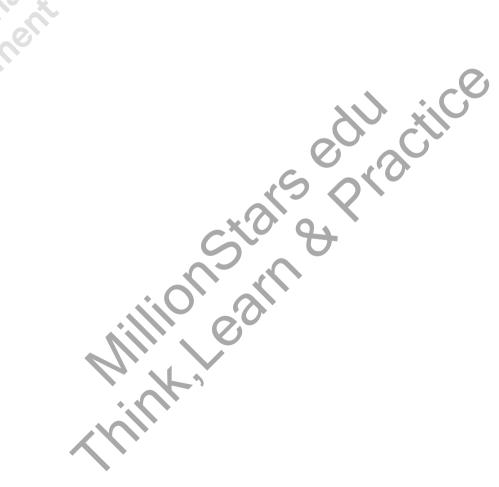
$$= {}^{8}C_{2} \left(\frac{1}{10}\right)^{2} \left(\frac{9}{10}\right)^{8-2}$$

$$=\frac{8\times7}{2}\left(\frac{1}{10}\right)^2\left(\frac{9}{10}\right)^6$$

$$=\frac{28\times9^6}{10^8}$$



Required probability = $\frac{28 \times 9^6}{10^8}$







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Here
$$x = 8, p = \frac{1}{2}, q = \frac{1}{2}$$

Let there be k desks and X be the number of students studying in office.

Then we want that

$$P(X \le k) > .90$$

$$\Rightarrow$$
 $P(X > k) < .10$

$$\Rightarrow$$
 $P(X = k + 1, k + 2, ...8) < .10$

Clearly
$$P(X > 6) = P(X = 7 \text{ or } X = 8)$$

$$= {}^{8}C_{7} \left(\frac{1}{2}\right)^{8} + {}^{8}C_{8} \left(\frac{1}{2}\right)^{8}$$
$$= .04$$

$$P(X > 5) = P(...)$$

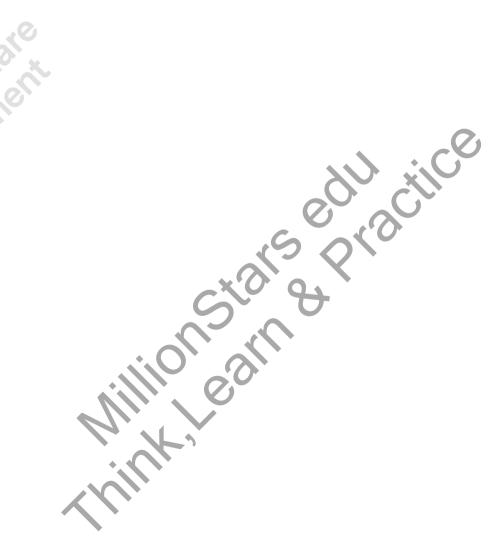
and
$$P(X > 5) = P(X = 6, X = 7 \text{ or } X = 8)$$

= .15

$$P(X > 6) < 0.10$$

If there are 6 desks then there is at least 90% chance for \Rightarrow every graduate assistant to get a desk.





Wondershare



Binomial Distribution formula is given by

$$P(x) = {}^{n}C_{x} p^{x} q^{n-x}$$
, where $x = 0, 1, 2, ...n$

Let x = No. of heads in a toss

We need probability of 6 or more heads

$$X = 6, 7, 8$$

Here $p = \frac{1}{2}$ and $q = \frac{1}{2}$

P(6) = Prob of getting 6 heads, 2 tails =
$${}^8C_6 \left(\frac{1}{2}\right)^6 \times \left(\frac{1}{2}\right)^2$$

P(7) = Prob of getting 7 heads, 1tails =
$${}^{8}C_{7} \left(\frac{1}{2}\right)^{7} \times \left(\frac{1}{2}\right)^{1}$$

P(8) = Prob of getting 8 heads, 0 tails =
$${}^8C_8 \left(\frac{1}{2}\right)^8 \times \left(\frac{1}{2}\right)^0$$

The probability of getting at least 6 heads (not more than 2 tails) is then

$${}^{8}C_{6}\left(\frac{1}{2}\right)^{6}\times\left(\frac{1}{2}\right)^{2}+{}^{8}C_{1}\left(\frac{1}{2}\right)^{7}\times\left(\frac{1}{2}\right)^{1}+{}^{8}C_{2}\left(\frac{1}{2}\right)^{8}\times\left(\frac{1}{2}\right)^{0}$$

$$=\frac{1}{256}+8\frac{1}{256}+28\frac{1}{256}=\frac{37}{256}$$





Let p represents the probability of getting head in a toss of fair coin, so

$$p = \frac{1}{2}$$

$$Q = 1 - \frac{1}{2}$$

$$Q = \frac{1}{2}$$

[Since
$$p + q = 1$$
]

Let X denote the random variable representing the number heads in 6 tosses of coin. Probability of getting r sixes in n tosses of a fair coin is given by,

$$P\left(X = r\right) = {^{n}C_{r}p^{r}q^{n-r}}$$
$$= {^{6}C_{r}} \left(\frac{1}{2}\right)^{r} \left(\frac{1}{2}\right)^{6-r}$$

(i)

Probability of getting 3 heads

$$= P(X = 3)$$

$$= {}^{6}C_{3}\left(\frac{1}{2}\right)^{3}\left(\frac{1}{2}\right)^{6-3}$$

$$= \frac{6 \times 5 \times 4}{3 \times 2}\left(\frac{1}{2}\right)^{3}\left(\frac{1}{2}\right)^{3}$$

$$= \frac{20}{64}$$

Probability of getting 3 heads =
$$\frac{20}{64} = \frac{5}{16}$$





(ii)

Probability of getting no heads

$$= P(X = 0)$$

$$= {}^{6}C_{0}\left(\frac{1}{2}\right)^{0}\left(\frac{1}{2}\right)^{6-0}$$

$$= \left(\frac{1}{2}\right)^{6}$$

$$= \frac{1}{64}$$

Probability of getting no heads = $\frac{1}{64}$

(iii)

Probability of getting at least one head

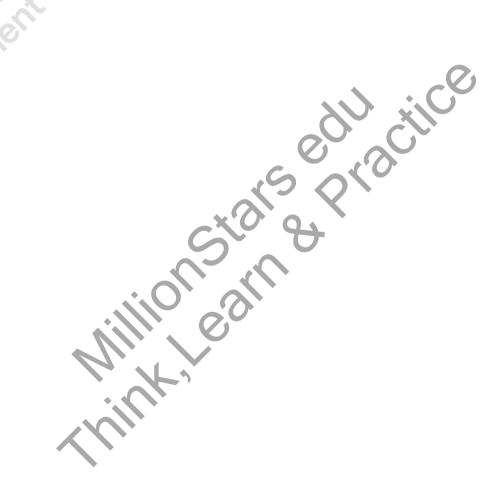
bility of getting at least one head
$$= P(X = 1) + P(X = 2) + P(X = 3) + P(X = 4) + P(X = 5) + P(X = 6)$$

$$= 1 - P(X = 0)$$

$$= 1 - \frac{1}{64}$$

$$= \frac{63}{64}$$

Probability of getting at least one head = $\frac{63}{64}$





 $\frac{\text{https://millionstar.godaddysites.com/}}{\text{Let }p\text{ be the probability that a tube function for more than 500 hours. So}}$

$$p = 0.2$$

$$p = \frac{1}{5}$$

$$q=1-\frac{1}{5}$$

[Since
$$p+q=1$$
]

Let X denote the random variable representing the number of tube that functions for more than 500 hours out of 4 tubes. Probability of functioning r tubes out n tubes selected for more than 500 hours is given by,

$$P(X = r) = {}^{n}C_{r}p^{r}q^{n-r}$$

$$= {}^{4}C_{r}\left(\frac{1}{5}\right)^{r}\left(\frac{4}{5}\right)^{4-r}$$

$$= ---($$

Probability that exactly 3 tube will function for more than 500 hours

$$= {}^{4}C_{3} \left(\frac{1}{5}\right)^{3} \left(\frac{4}{5}\right)^{4-3}$$
$$= 4 \cdot \left(\frac{1}{5}\right)^{3} \left(\frac{4}{5}\right)$$



Required probability = $\frac{16}{625}$

Binomial Distribution Ex 33.1 Q34



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Wondershare



Let p be the probability that component survive the shock test. So

$$p = \frac{3}{4}$$

$$q = 1 - \frac{3}{4}$$

Since
$$p + q = 1$$

$$q = \frac{1}{4}$$

Let X denote the random variable representing the number of components that survive shock test out of 5 components. Probability of that r components that survive shock test out of n components is given by

$$P\left(X=r\right) = {^nC_r}p^rq^{n-r}$$

$$= {^5C_r}\left(\frac{3}{4}\right)^r\left(\frac{1}{4}\right)^{5-r}$$

$$= ---\left(1\right)$$

(i)

Probability that exactly 2 will survive the shock test

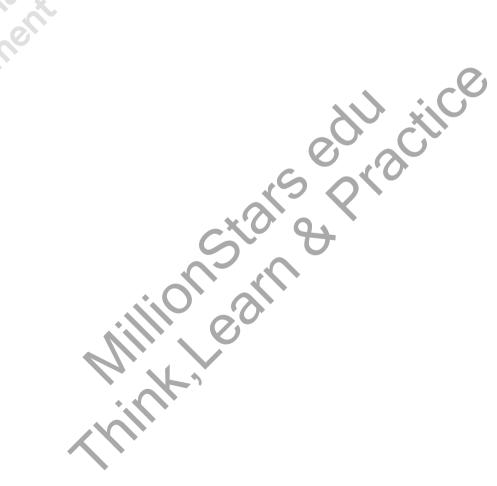
$$= P(X = 2)$$

$$= {}^{5}C_{2} \left(\frac{3}{4}\right)^{2} \left(\frac{1}{4}\right)^{5-2}$$

$$= \frac{5.4}{2} \left(\frac{9}{16}\right) \left(\frac{1}{64}\right)$$

$$= \frac{45}{512} = 0.0879$$









Probability that at most 3 will survive

$$= P(X = 0) + P(X = 1) + P(X = 3) + P(X = 4)$$

$$= 1 - [P(X = 4) + P(X = 5)]$$

$$= 1 - \left[{}^{5}C_{4} \left(\frac{3}{4} \right)^{4} \left(\frac{1}{4} \right)^{5-4} + {}^{5}C_{5} \left(\frac{3}{4} \right)^{5} \left(\frac{1}{4} \right)^{5-5} \right]$$

$$= 1 - \left[5 \cdot \frac{81}{1024} + \frac{243}{1024} \right]$$

$$= 1 - \left[\frac{405 + 243}{1024} \right]$$

$$= \frac{1024 - 648}{1024}$$

$$= \frac{376}{1024} = 0.3672$$

Binomial Distribution Ex 33.1 Q35

Probability that bomb strikes a target p = 0.2Probability that a bomb misses the target = 0.8 n = 6

let x = number of bombs that strike the target P(x=2) = exactly 2 bombs strike the target

$$= {}^{6}C_{2} \left(\frac{2}{10}\right)^{2} \times \left(\frac{8}{10}\right)^{4} = 15 \times \frac{16384}{10^{6}} = 0.24576$$

P(x≥2) = at least 2 bombs strike the target

$$= 1 - P(x < 2)$$

$$= 1 - [P(x=0) + P(x=1)]$$

= 1 - [
$${}^{6}C_{0} \left(\frac{2}{10}\right)^{0} \times \left(\frac{8}{10}\right)^{6} + {}^{6}C_{1} \left(\frac{2}{10}\right)^{1} \times \left(\frac{8}{10}\right)^{5}$$
]

$$= 1 - [0.0.262144 + 0.393216] = 1 - 0.65536$$

 $= 0.34464$



Binomial Distribution Ex 33.1 Q36

Let p be the probability that a mouse get contract the desease. So

$$p = 40\%$$

$$= \frac{40}{100}$$

$$= \frac{2}{5}$$

$$q = 1 - \frac{2}{5}$$
[Since $p + q = 1$]
$$q = \frac{3}{5}$$

Let X denote the variable representing number of mice contract the disease out of 5 mice. Probability the r mice get contract the disease out of n mice inoculated is given by

$$P(X = r) = {}^{n}C_{r}p^{r}q^{n-r}$$

$$= {}^{5}C_{r}\left(\frac{2}{5}\right)^{r}\left(\frac{3}{5}\right)^{5-r}$$
---(1)

(i)

Probability that none contract the disease = P(X = 0)

$$= {}^{5}C_{0} \left(\frac{2}{5}\right)^{0} \left(\frac{3}{5}\right)^{5-0}$$
$$= \left(\frac{3}{5}\right)^{5}$$

Probability that none contract the disease $= \left(\frac{3}{5}\right)^5$

(ii)

Probability that more than 3 contract disease

$$= P(X = 4) + P(X = 5)$$

$$= {}^{5}C_{4} \left(\frac{2}{5}\right)^{4} \left(\frac{3}{5}\right)^{5-4} + {}^{5}C_{5} \left(\frac{2}{5}\right)^{5} \left(\frac{3}{5}\right)^{5-5}$$

$$= 5 \cdot \left(\frac{2}{5}\right)^{4} \left(\frac{3}{5}\right) + \left(\frac{2}{5}\right)^{5}$$





$$= \left(\frac{1}{5}\right) \left[\frac{3+5}{5}\right]$$
$$= \frac{17}{5} \left(\frac{2}{5}\right)^4$$

Binomial Distribution Ex 33.1 Q37





Willion Stars Practice



Given, P = 2qp + a = 1 2g + g = 13q = 1 $p = \frac{2}{3}$

Let X denote the random variable representing the number of success out of 6 experiments. Probability of getting r success out of n experiments is given by

$$P\left(X=r\right) = {^{n}C_{r}}p^{r}q^{n-r}$$

$$= {^{6}C_{r}}\left(\frac{2}{3}\right)^{r}\left(\frac{1}{3}\right)^{6-r}$$

$$= --- (1)$$

Probability of getting at least 4 success

$$P\left(X = r\right) = {}^{n}C_{r}p^{r}q^{n-r}$$

$$= {}^{6}C_{r}\left(\frac{2}{3}\right)^{r}\left(\frac{1}{3}\right)^{6-r}$$
---(1)

ability of getting at least 4 success
$$= P\left(X = 4\right) + P\left(X = 5\right) + P\left(X = 6\right)$$

$$= {}^{6}C_{4}\left(\frac{2}{3}\right)^{4}\left(\frac{1}{3}\right)^{6-4} + {}^{6}C_{5}\left(\frac{2}{3}\right)^{5}\left(\frac{1}{3}\right)^{6-5} + {}^{6}C_{6}\left(\frac{2}{3}\right)^{6}\left(\frac{1}{3}\right)^{6-6}$$

$$= {}^{6}C_{4}\left(\frac{2}{3}\right)^{4}\left(\frac{1}{3}\right)^{2} + {}^{6}\left(\frac{2}{3}\right)^{5}\left(\frac{1}{3}\right)^{1} + \left(\frac{2}{3}\right)^{6}$$

$$= {}^{6}C_{5}\left(\frac{2}{3}\right)^{4}\left(\frac{1}{3}\right)^{2} + {}^{6}\left(\frac{2}{3}\right)^{5}\left(\frac{1}{3}\right)^{1} + \left(\frac{2}{3}\right)^{6}$$

$$= {}^{6}C_{5}\left(\frac{2}{3}\right)^{4}\left[\frac{15}{9} + \frac{4}{3} + \frac{4}{9}\right]$$

$$= {}^{6}C_{5}\left(\frac{2}{3}\right)^{4}\left[\frac{15+12+4}{9}\right]$$

$$= {}^{6}C_{5}\left(\frac{2}{3}\right)^{4}\left[\frac{15+12+4}{9}\right]$$

$$= {}^{6}C_{5}\left(\frac{2}{3}\right)^{4}\left[\frac{15+12+4}{9}\right]$$

$$= {}^{6}C_{5}\left(\frac{2}{3}\right)^{4}\left[\frac{15+12+4}{9}\right]$$

$$= {}^{6}C_{5}\left(\frac{2}{3}\right)^{4}\left[\frac{15+12+4}{9}\right]$$

$$= {}^{6}C_{5}\left(\frac{2}{3}\right)^{4}\left[\frac{15+12+4}{9}\right]$$

Required probability = $\frac{496}{729}$



Let x = number of out of service machines https://millionstar.godaddysites.com/ p = probability that machine will be out of service on the same day = 2/100

q = probability that machine will be in service on the same day = 8/100

P(x=3) = probability exactly 3 machines will be out of service on the same day

$$P(x=3) = {}^{20}C_3 \times \left(\frac{2}{100}\right)^3 \left(\frac{8}{100}\right)^0 = 1140 \times 0.000008$$

= 0.00912

For low probability events Poisson' distribution is used instead of Binomial distribution. Then, $\lambda = np = 20x0.02 = 0.4$

$$P(x=r) = \frac{e^{-\lambda} \times \lambda^{s}}{r!}$$

$$P(x=3) = \frac{e^{-0.4} \times 0.4^{8}}{3!} = 0.6703 \times 0.064/6 = 0.0071$$

Binomial Distribution Ex 33.1 Q39

Let p be the probability that a student entering a university will graduate, so

$$p = 0.4$$

 $q = 1 - 0.4$ [Since $p + q = 1$]
 $= 0.6$

Let X denote the random variable representing the number of students entering a university will graduate out of 3 students of university. Probability that r students will graduate out of n entering the university is given by

$$P(X = r) = {^{n}C_{r}p^{r}(q)^{n-r}}$$

$$= {^{3}C_{r}(0.4)^{r}(0.6)^{3-r}}$$
---(1)

(i)

Probability that none will graduate

$$= P(X = 0)$$
$$= {}^{3}C_{0}(0.4)^{0}(0.6)^{3-0}$$

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Probability that none will graduate = 0.216

(ii)

Probability that one will graduate

$$= P\left(X = 1\right)$$

$$= {}^{3}C_{1}(0.4)^{1}(0.6)^{3-1}$$

$$= 3 \times (0.4) (0.36)$$

$$= 0.432$$

Probability that only one will graduate = 0.432

(iii)

Probability that all will graduate

$$= P \left(X = 3 \right)$$

$$= {}^{3}C_{3}(0.4)^{3}(0.6)^{3-3}$$

$$= (0.4)^3$$

Probability that all will graduate = 0.064

Binomial Distribution Ex 33.1 Q40

Let $\, \times \,$ denote the number of defective eggs in the 10 eggs drawn.

Since the drawing is done with replacement, the trials are Bernoulli trials.

Clearly, X has the binomial distribution with n=10 and p= $\frac{10}{100} = \frac{1}{10}$

Therefore,
$$q = 1 - \frac{1}{10} = \frac{9}{10}$$

Now, P(at least one defective egg) = $P(X \ge 1) = 1 - P(X = 0)$

$$=1-^{10} C_0 \left(\frac{9}{10}\right)^{10} = 1-\frac{9^{10}}{10^{10}}$$





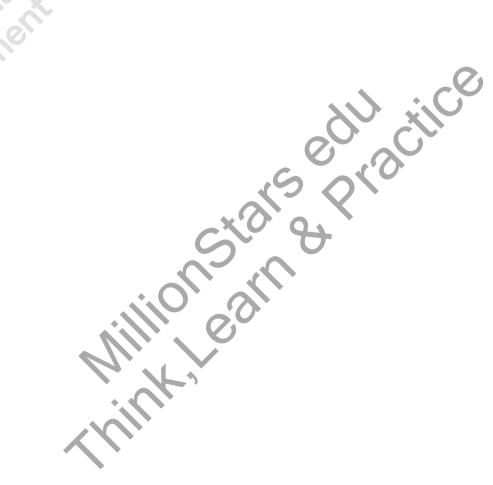
 $p = \frac{1}{2}$ $q = 1 - \frac{1}{2}$ [Since p + q = 1] $= \frac{1}{2}$

Thus the probability that he answers at least 12 questions correctly among 20 questions is $P(X \ge 12) = P(X = 12) + P(X = 13) + P(X = 14) + P(X = 15) + P(X = 16) + P(X = 17) + P(X = 18) + P(X = 19) + P(X = 20)$ $= \left(\frac{1}{2}\right)^{20} \left\{ {}^{20}C_{12} + {}^{20}C_{13} + {}^{20}C_{14} + {}^{20}C_{15} + {}^{20}C_{16} + {}^{20}C_{17} + {}^{20}C_{18} + {}^{20}C_{19} + {}^{20}C_{20} \right\}$ $= \frac{{}^{20}C_{12} + {}^{20}C_{13} + {}^{20}C_{14} + {}^{20}C_{15} + {}^{20}C_{17} + {}^{20}C_{18} + {}^{20}C_{19} + {}^{20}C_{20}}{2^{20}}$

Therefore, the required answer is

$$\frac{{}^{20}C_{12} + {}^{20}C_{13} + {}^{20}C_{14} + {}^{20}C_{15} + {}^{20}C_{16} + {}^{20}C_{17} + {}^{20}C_{18} + {}^{20}C_{19} + {}^{20}C_{20}}{2^{20}}$$





 \times is the random variable whose binomial distribution is $B\left(6,\frac{1}{2}\right)$.

Therefore, n = 6 and $p = \frac{1}{2}$

$$\therefore q = 1 - p = 1 - \frac{1}{2} = \frac{1}{2}$$

Then,
$$P(X = x) = {}^{n}C_{x}q^{n-x}p^{x}$$

$$= {}^{6}C_{x}\left(\frac{1}{2}\right)^{6-x} \cdot \left(\frac{1}{2}\right)^{x}$$

$$= {}^{6}C_{x}\left(\frac{1}{2}\right)^{6}$$

It can be seen that P(X = x) will be maximum, if ${}^6\mathrm{C}_{\scriptscriptstyle X}$ will be maximum.

Then,
$${}^{6}C_{0} = {}^{6}C_{6} = \frac{6!}{0! \cdot 6!} = 1$$

$${}^{6}C_{1} = {}^{6}C_{5} = \frac{6!}{1! \cdot 5!} = 6$$

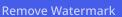
$${}^{6}C_{2} = {}^{6}C_{4} = \frac{6!}{2! \cdot 4!} = 15$$

$$^{6}C_{3} = \frac{6!}{3! \cdot 3!} = 20$$

The value of ${}^6\mathrm{C}_3$ is maximum. Therefore, for x=3, $\mathrm{P}(\mathrm{X}=\mathrm{x})$ is maximum.

Thus, X = 3 is the most likely outcome.







The repeated guessing of correct answers from multiple choice questions are Bernoulli trials. Let X represent the number of correct answers by guessing in the set of 5 multiple choice questions.

Probability of getting a correct answer is, $p = \frac{1}{3}$

$$\therefore q = 1 - p = 1 - \frac{1}{3} = \frac{2}{3}$$

Clearly, \times has a binomial distribution with n=5 and $p=\frac{1}{3}$

$$\therefore P(X = x) = {}^{n}C_{x}q^{n-x}p^{x}$$
$$= {}^{5}C_{x}\left(\frac{2}{3}\right)^{5-x} \cdot \left(\frac{1}{3}\right)^{x}$$

P (guessing more than 4 correct answers) = $P(X \ge 4)$

$$= P(X = 4) + P(X = 5)$$

$$= {}^{5}C_{4} \left(\frac{2}{3}\right) \cdot \left(\frac{1}{3}\right)^{4} + {}^{5}C_{5} \left(\frac{1}{3}\right)^{5}$$

$$= 5 \cdot \frac{2}{3} \cdot \frac{1}{81} + 1 \cdot \frac{1}{243}$$

$$= \frac{10}{243} + \frac{1}{243}$$

$$= \frac{11}{243}$$

Binomial Distribution Ex 33.1 Q44

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(b) P (winning exactly once) = P(X = 1)

$$= {}^{50}C_1 \left(\frac{99}{100}\right)^{49} \cdot \left(\frac{1}{100}\right)^{1}$$
$$= 50 \left(\frac{1}{100}\right) \left(\frac{99}{100}\right)^{49}$$
$$= \frac{1}{2} \left(\frac{99}{100}\right)^{49}$$

(c) P (at least twice) = P(X ≥ 2)

$$= 1 - P(X < 2)$$

$$= 1 - P(X \le 1)$$

$$= 1 - [P(X = 0) + P(X = 1)]$$

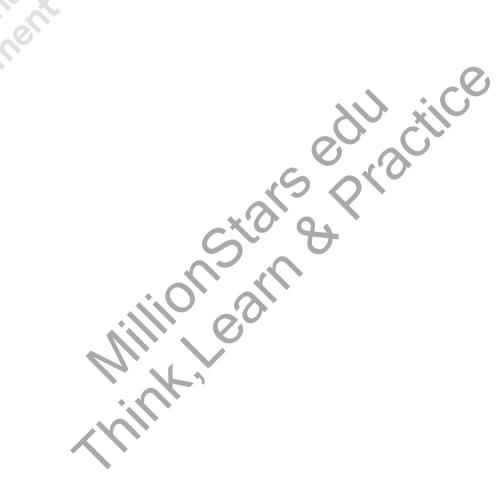
$$= [1 - P(X = 0)] - P(X = 1)$$

$$= 1 - (\frac{99}{100})^{50} - \frac{1}{2} \cdot (\frac{99}{100})^{49}$$

$$= 1 - (\frac{99}{100})^{49} \cdot [\frac{99}{100} + \frac{1}{2}]$$

$$= 1 - (\frac{99}{100})^{49} \cdot (\frac{149}{100})$$

$$= 1 - (\frac{149}{100})(\frac{99}{100})^{49}$$





Let the shooter fire n times. n fires are Bernoulli trials.

In each trial, p= probability of hitting the target= $\frac{3}{4}$

And q = probability of not hitting the target= $1 - \frac{3}{4} = \frac{1}{4}$

Then,
$$P(X = X) = {}^{n}C_{X} q^{n-X} p^{X} = {}^{n}C_{X} \left(\frac{1}{4}\right)^{n-X} \left(\frac{3}{4}\right)^{X} = {}^{n}C_{X} \frac{3^{X}}{4^{n}}$$

Now, given that

P (hitting the target atleast once) > 0.99

i.e.
$$P(x \ge 1) > 0.99$$

$$\Rightarrow \qquad 1 - P(x = 0) > 0.99$$

$$\Rightarrow 1 - {}^{\mathsf{n}} \mathsf{C}_0 \frac{1}{4^{\mathsf{n}}} > 0.99$$

$$\Rightarrow$$
 ${}^{\mathsf{n}}\mathsf{C}_0 \frac{1}{4^{\mathsf{n}}} < 0.01$

$$\Rightarrow \frac{1}{4^{\mathsf{n}}} < 0.01$$

$$\Rightarrow$$
 $4^{\text{n}} > \frac{1}{0.01} = 100$

The minimum value of n to satisfy this inequality is 4 Thus, the shooter must fire 4 times.





$$\Rightarrow p = \frac{1}{2} \Rightarrow q = \frac{1}{2}$$

$$\therefore P(X = x) = {^{n}C_{x}}p^{n-x}q^{x} = {^{n}C_{x}}\left(\frac{1}{2}\right)^{n-x}\left(\frac{1}{2}\right)^{x} = {^{n}C_{x}}\left(\frac{1}{2}\right)^{n}$$

It is given that,

P (getting at least one head) > $\frac{90}{100}$

$$P(x \ge 1) > 0.9$$

$$1 - P(x = 0) > 0.9$$

$$1 - {^{n}C_{0}} \cdot \frac{1}{2^{n}} > 0.9$$

$$^{n}C_{0}.\frac{1}{2^{n}} < 0.1$$

$$\frac{1}{2^n} < 0.1$$

$$2'' > \frac{1}{0.1}$$

$$2^n > 10$$



The minimum value of n that satisfies the given inequality is 4.

...(1)

Thus, the man should toss the coin 4 or more than 4 times.

Binomial Distribution Ex 33.1 Q47



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Probability (p) of getting a head at the toss of a coin is $\frac{1}{2}$.

So,

$$p = \frac{1}{2}$$

$$q = 1 - \frac{1}{2} \qquad [\text{Since } p + q = 1]$$

$$= \frac{1}{2}$$

$$\therefore P(X = x) = {}^{n}C_{x}p^{n-x}q^{x}$$

$$= {}^{n}C_{x}\left(\frac{1}{2}\right)^{n-x}\left(\frac{1}{2}\right)^{x}$$

 $= {}^{\kappa}C_{x} \left(\frac{1}{2}\right)^{\kappa}$

It is given that

verified
$$p$$
 (getting at least one head) $> \frac{80}{100}$

$$P(x \ge 1) > 0.8$$

$$1 - P(x = 0) > 0.8$$

$$1 - {}^{\kappa}C_0 \cdot \frac{1}{2^{\kappa}} > 0.8$$

$${}^{\kappa}C_0 \cdot \frac{1}{2^{\kappa}} < 0.2$$

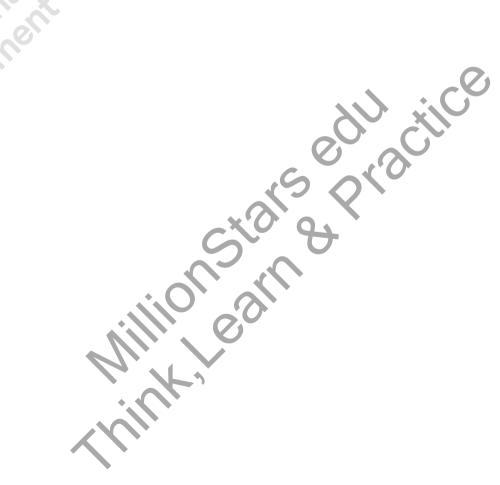
$$\frac{1}{2^{\kappa}} < 0.2$$

$$2^{\kappa} > \frac{1}{0.2}$$

$$2^{\kappa} > 5$$

The minimum value of n that satisfies the given inequality is 3. Thus, the man should toss the coin 3 or more than 3 times.







e the probab	ility of getting a doublet in a throw of a pair of d
$p = \frac{6}{36}$	[Since $(1,1),(2,2),(3,3),(4,4),(5,5),(6,6)$]
$=\frac{1}{6}$	
$q = 1 - \frac{1}{6}$	[Since $p+q=1$]
$=\frac{5}{6}$	

Let X denote the number of getting doublets i.e. success out of 4 times. So, probability distribution is given by

X	P(X)	Ī
0	${}^{4}C_{0}\left(\frac{1}{6}\right)^{0}\left(\frac{5}{6}\right)^{4-0} = \left(\frac{5}{6}\right)^{4}$	
1	${}^{4}C_{1}\left(\frac{1}{6}\right)^{1}\left(\frac{5}{6}\right)^{4-1} = 4\left(\frac{1}{6}\right)\left(\frac{5}{6}\right)^{3} = \frac{2}{3}\left(\frac{5}{6}\right)^{3}$	
2	${}^{4}C_{2}\left(\frac{1}{6}\right)^{2}\left(\frac{5}{6}\right)^{4-2} = \frac{4\cdot3}{2}\left(\frac{1}{6}\right)^{2}\left(\frac{5}{6}\right)^{2} = \frac{25}{216}$	
3	${}^{4}C_{3}\left(\frac{1}{6}\right)^{3}\left(\frac{5}{6}\right)^{4-3} = \frac{4\cdot3}{2}\left(\frac{1}{6}\right)^{3}\left(\frac{5}{6}\right) = \frac{5}{324}$	
4	${}^{4}C_{4}\left(\frac{1}{6}\right)^{4}\left(\frac{5}{6}\right)^{4-4} = \left(\frac{1}{6}\right)^{4} = \frac{1}{1296}$	





$$=\frac{1}{5}$$

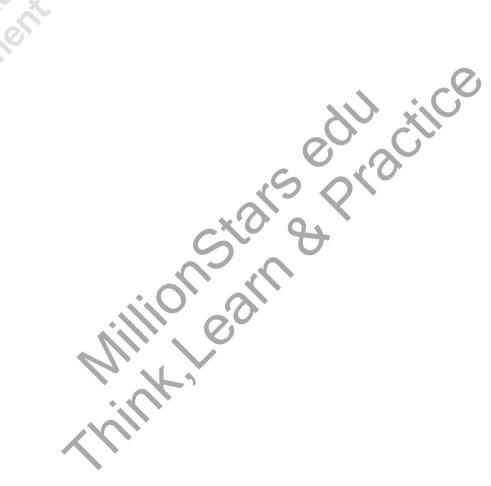
$$q = 1 - \frac{1}{5}$$
 [Since $p + q = 1$]

 $=\frac{4}{5}$

Here, 4 bulbs is drawn at random with replacement. So, probability distribution is given by

X	P(X)	
0	${}^{4}C_{0}\left(\frac{1}{5}\right)^{0}\left(\frac{4}{5}\right)^{4-0}=\frac{256}{625}$	
1	${}^{4}C_{1}\left(\frac{1}{5}\right)^{1}\left(\frac{4}{5}\right)^{4-1} = \frac{4}{5} \times \frac{4^{3}}{5^{3}} = \frac{256}{625}$	
2	${}^{4}C_{2}\left(\frac{1}{5}\right)^{2}\left(\frac{4}{5}\right)^{4-2} = \frac{6}{5^{2}} \times \frac{4^{2}}{5^{2}} = \frac{96}{625}$	
3	${}^{4}C_{3}\left(\frac{1}{5}\right)^{3}\left(\frac{4}{5}\right)^{4-3} = \frac{4}{5^{3}} \times \frac{4}{5} = \frac{16}{625}$	
4	${}^{4}C_{4}\left(\frac{1}{5}\right)^{4}\left(\frac{6}{5}\right)^{4-4} = 1 \cdot \frac{1}{625} = \frac{1}{625}$	







Here success is a score which is multiple of 3 i.e. 3 or 6.

$$p(3 \text{ or } 6) = \frac{2}{6} = \frac{1}{3}$$

The probability of r successes in 10 throws is given by

$$P(r) = {}^{10}C_r \left(\frac{1}{3}\right)^r \left(\frac{2}{3}\right)^{10-r}$$

Now P(at least 8 successes) = P(8) + P(9) + P(10)

$$= {}^{10}C_{8} \left(\frac{1}{3}\right)^{8} \left(\frac{2}{3}\right)^{2} + {}^{10}C_{9} \left(\frac{1}{3}\right)^{9} \left(\frac{2}{3}\right)^{1} + {}^{10}C_{10} \left(\frac{1}{3}\right)^{10} \left(\frac{2}{3}\right)^{0}$$

$$= \frac{1}{3^{10}} \left[45 \times 4 + 10 \times 2 + 1\right]$$

$$= \frac{201}{3^{10}} \left[45 \times 4 + 10 \times 2 + 1\right]$$

$$= \frac{1}{3^{10}} [45 \times 4 + 10 \times 2 + 1]$$

$$=\frac{201}{3^{10}}$$





Here success is an odd number i.e. 1,3 or 5.

$$p(1,3 \text{ or } 5) = \frac{3}{6} = \frac{1}{2}$$

The probability of r successes in 5 throws is given by

$$P(r) = {}^{5}C_{r} \left(\frac{1}{2}\right)^{r} \left(\frac{1}{2}\right)^{5-r}$$

Now P(exactly 3 times) = P(3)

$$= {}^{5}C_{3}\left(\frac{1}{2}\right)^{3}\left(\frac{1}{2}\right)^{2}$$

$$=\frac{10}{2^{5}}$$





Probablity of a man hitting a target is 0.25.

$$\therefore p = 0.25 = \frac{1}{4}, q = 1 - p = \frac{3}{4}$$

The probability of r successes in 7 shoots is given by

$$P(r) = {}^{7}C_{r}(0.25)^{r}(0.75)^{7-r}$$

Now P(at least twice) = 1 - P(less than 2)

$$= 1 - {}^{7}C_{0}(0.25)^{0}(0.75)^{7} + {}^{7}C_{1}(0.25)^{1}(0.75)^{6}$$

$$= 1 - \frac{3^7}{4^7} + 7 \times \frac{3^6}{4^7}$$





Probablity of a bulb to be defective is $\frac{1}{50}$.

$$p = \frac{1}{50}, q = 1 - p = \frac{49}{50}$$

The probability of r defective bulbs in 10 bulbs is given by

$$P(r) = {}^{10}C_r \left(\frac{1}{50}\right)^r \left(\frac{49}{50}\right)^{10-r}$$

(i) P(none of the bulb is defective) = P(0)

$$= {}^{10}C_0 \left(\frac{1}{50}\right)^0 \left(\frac{49}{50}\right)^{10}$$
$$= \left(\frac{49}{50}\right)^{10}$$

(ii) P(exactly two bulbs are defective) = P(2)

$$= {}^{10}C_2 \left(\frac{1}{50}\right)^2 \left(\frac{49}{50}\right)^8$$
$$= 45 \times \frac{\left(49\right)^8}{\left(50\right)^{10}}$$









(iii) P(more than 8 bulbs work properly)

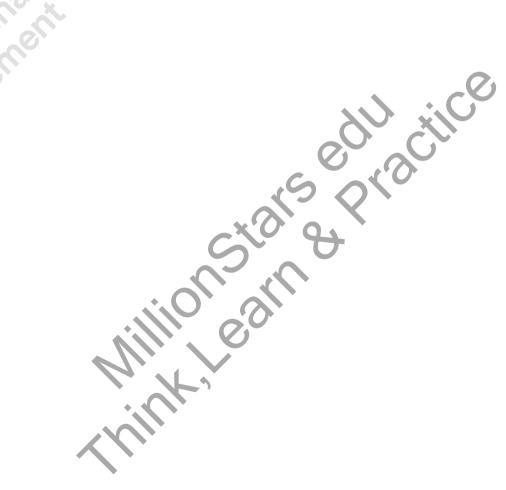
= P(at most two bulbs are defective)

$$= {}^{10}C_0 \left(\frac{1}{50}\right)^0 \left(\frac{49}{50}\right)^{10} + {}^{10}C_1 \left(\frac{1}{50}\right)^1 \left(\frac{49}{50}\right)^9 + {}^{10}C_2 \left(\frac{1}{50}\right)^2 \left(\frac{49}{50}\right)^8$$

$$= \left(\frac{49}{50}\right)^{10} + 10 \times \frac{\left(49\right)^9}{\left(50\right)^{10}} + 45 \times \frac{\left(49\right)^8}{\left(50\right)^{10}}$$

$$= \frac{\left(49\right)^8}{\left(50\right)^{10}} \left[\left(49\right)^2 + 490 + 45 \right]$$

$$= \frac{\left(49\right)^8 \times 2936}{\left(50\right)^{10}}$$





Binomial Distribution Ex 33.2 Q1

Let X be a binomial variate with parameters n and p.

Mean =
$$np$$

Varience = npq

Mean - Variance =
$$np - npq$$

= $np (1 - q)$
= $np.p$
= np^2

Mean - Variance > 0

Mean > Variance

So, mean can never be less than varience.

Binomial Distribution Ex 33.2 Q2

Let X denote the variance with parameters n and p

$$p+q=1$$
$$q=1-p$$

Goven, Mean
$$= np = 9$$

Variance =
$$npq = \frac{9}{4}$$

$$\frac{npq}{np} = \frac{\frac{9}{4}}{9}$$

$$Q = \frac{1}{4}$$

So,
$$p = 1 - q$$
$$= 1 - \frac{1}{4}$$
$$p = \frac{3}{4}$$

Put p in equation (i),

$$n\left(\frac{3}{4}\right) = 9$$

$$\Rightarrow n = \frac{36}{3}$$

So,
$$n = 12$$

The distribution is given by

$$= {^nC_r}p^r \left(q\right)^{n-r}$$

$$P(X = r) = {}^{12}C_r \left(\frac{3}{4}\right)^r \left(\frac{1}{4}\right)^{12-r}$$
for $r = 0, 1, 2, ... 12$



Binomial Distribution Ex 33.2 Q3

MILLIONSTYR et n and p be parameters of binomial distribution. Here

$$Mean = np = 9$$

Variance =
$$npq = 6$$

$$\frac{npq}{np} = -$$

$$q = \frac{2}{3}$$

So,
$$p = 1 - \frac{2}{3}$$

 $p = \frac{1}{3}$

Since
$$p + q = 1$$

Using equation (i), np = 9

$$n\left(\frac{1}{3}\right) = 9$$

$$n = 27$$

Hence, binomial distribution is given by

$$P(X = r) = {}^{27}C_r \left(\frac{1}{3}\right)^r \left(\frac{2}{3}\right)^{27-r}$$
$$r = 0, 1, 2, \dots 27$$

Binomial Distribution Ex 33.2 Q4

Given that,

$$n = 5$$

$$np + npq = 4.8$$

$$np\left(1+q\right) = 4.8$$

$$5p(1+q) = 4.8$$

$$5(1-q)(1+q) = 4.8$$

$$5\left(1-q^2\right) = 4.8$$

$$1 - q^2 = \frac{4.8}{5}$$

$$q^2 = 1 - \frac{4.8}{5}$$

$$=\frac{0.2}{5}$$

$$q^2 = \frac{1}{25}$$

$$q = \frac{1}{r}$$

$$= 1 - \frac{1}{5}$$

$$p = \frac{4}{5}$$

So,
$$n = 5$$
, $p = \frac{4}{5}$, $q = \frac{1}{5}$

Here binomial distribution is

$$P(X=r) = {^nC_r}p^rq^{n-r}$$

$$P(X = r) = 5C_r \left(\frac{4}{5}\right)^r \left(\frac{1}{5}\right)^{5-r}$$

 $r = 0, 1, 2, 3, ... 5$

[Since
$$p+q=1$$
]

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Binomial Distribution Ex 33.2 Q5

Given that,

Let n and p be the parameters of distribution dividing equation (ii) by (i)

$$\frac{npq}{np} = \frac{16}{20}$$
$$q = \frac{4}{5}$$

So,
$$p = 1 - q$$
$$= 1 - \frac{4}{5}$$
$$p = \frac{1}{5}$$

[Since
$$p + q = 1$$
]

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Put p in equation (i),

$$np = 20$$

$$n\left(\frac{1}{5}\right) = 20$$

$$n = 20 \times 5$$

$$n = 100$$

So, binomial distribution is given by

$$P(X = r) = {^{n}C_{r}p^{r}q^{n-r}}$$

$$P(X = r) = {^{100}C_{r}\left(\frac{1}{5}\right)^{r}\left(\frac{4}{5}\right)^{100-r}}$$

$$r = 0, 1, 2, 3, \dots 100$$





Let n and ho be the parameters of distribution binomial distribution. So

$$q = 1 - p$$
 as $p + q = 1$

Mean + Variance =
$$\frac{25}{3}$$

$$np + npq = \frac{25}{3}$$

$$np(1+q) = \frac{25}{3}$$
$$np = \frac{25}{3(1+q)}$$

$$Mean \times Variance = \frac{50}{3}$$

$$np \times npq = \frac{50}{3}$$

$$n^2p^2q = \frac{50}{3}$$

$$\left[\frac{25}{3\left(1+q\right)}\right]^2.q = \frac{50}{3}$$

$$625q = \frac{50}{3} \left[9 \left(1 + q \right)^2 \right]$$

$$625q = 150 (1+q)^{2}$$
$$25q = 6 (1+q)^{2}$$

$$6 + 6q^2 + 12q - 25q = 0$$

$$6q^2 - 13q + 6 = 0$$

$$6q^2 - 9q - 4q + 6 = 0$$

$$3q(2q-3)-2(2q-3)=0$$

$$(2q-3)(3q-2)=0$$

$$\Rightarrow$$
 2q - 3 = 0 or

$$\Rightarrow$$
 $q = \frac{3}{2}$

$$q = \frac{2}{3}$$

Since
$$q \le 1$$
, so

$$Q = \frac{2}{3}$$

$$q = \frac{2}{3}$$

$$p = 1 - q$$

$$= 1 - \frac{2}{3}$$

$$= 1 - \frac{2}{3}$$

$$p = \frac{1}{3}$$

[Using (1)]

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Let n and p be the parameters of binomial distribution.

Given that,

Standard deviation = \sqrt{npq} = 4

Squaring both the sides,

$$npq = 16 ---(ii)$$

Dividing equation (ii) by (i),

$$\frac{npq}{np} = \frac{16}{20}$$

$$q = \frac{4}{5}$$

So,
$$p = 1 - q$$

= $1 - \frac{4}{5}$

$$\begin{bmatrix} -q & [Since p + q = 1] \end{bmatrix}$$

$$p = \frac{1}{5}$$

Put value of p in equation (i),

$$np = 20$$

$$\frac{n}{5} = 20$$

$$n = 100$$

$$p = \frac{1}{5}$$

Binomial Distribution Ex 33.2 Q8

Let p denotes the probability of selecting a defective bolt, so

$$p = 0.1$$

$$p = \frac{1}{10}$$

$$q = 1 - \frac{1}{10}$$

[Since
$$p + q = 1$$
]

$$q = \frac{9}{10}$$

Given, n = 400

(i)

$$=400 \times \frac{1}{10}$$

Mean = 40

(ii)

Standard deviation =
$$\sqrt{npq}$$

= $\sqrt{400 \times \frac{1}{10} \times \frac{9}{10}}$
= $\sqrt{36}$

Standard deviation = 6

Binomial Distribution Ex 33.2 Q9

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Let n and p be the parameters of binomial distribution.

Variance =
$$npq = \frac{10}{3}$$

Dividing (ii) by (i)

$$\frac{npq}{np} = \frac{\frac{10}{3}}{5}$$
$$q = \frac{2}{3}$$

So,
$$p = 1 - q$$

= $1 - \frac{2}{3}$

Since
$$p+q=1$$

$$p = \frac{1}{3}$$

Put the value of p in equation (i),

$$np = 5$$

$$n = 5 \times 3$$

$$n = 15$$

Hence, the binomial distribution is given by

$$P\left(X=r\right) = {^{n}C_{r}p^{r}q^{n-r}}$$

$$P(X = r) = {}^{15}C_r \left(\frac{1}{3}\right)^r \left(\frac{2}{3}\right)^{15-r}$$
$$r = 0, 1, 2, \dots 15$$

Binomial Distribution Ex 33.2 Q10

Let p be the probability of a ship returning safely to parts, so

$$p = \frac{9}{10}$$

$$q = 1 - \frac{9}{10}$$

Since
$$p + q = 1$$

$$q = \frac{1}{10}$$

Given, n = 500

$$= 500 \times \frac{9}{10}$$

Standard deviation =
$$\sqrt{npq}$$

= $\sqrt{500 \times \frac{9}{10} \times \frac{1}{10}}$
= $\sqrt{45}$
= 6.71

Mean = 450

Standard deviation = 6.71

Binomial Distribution Ex 33.2 Q11

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Given that, parameters for binomial distribution are n and p.

Also, Mean =
$$np = 16$$

$$Variance = npq = 8$$

Dividing (ii) by (i)

$$\frac{npq}{np} = \frac{8}{16}$$

$$q = \frac{1}{2}$$

So,
$$p = 1 - \frac{1}{2}$$
$$p = \frac{1}{2}$$

$$\left[\operatorname{as} p + q = 1\right]$$

Put the value of p in equation (i),

$$n\left(\frac{1}{2}\right) = 16$$

$$n = 32$$

Hence, binomial distribution is given by,

$$P\left(X=r\right) = {^nC_r}p^rq^{n-r}$$

$$P\left(X=r\right)={}^{32}C_r\left(\frac{1}{2}\right)^r\left(\frac{1}{2}\right)^{32-r}$$

$$P\left(X=0\right)$$

$$= {}^{32}C_0 \left(\frac{1}{2}\right)^0 \left(\frac{1}{2}\right)^{32-0}$$

$$= \left(\frac{1}{2}\right)^{32}$$

$$P(X = 1)$$

$$= {}^{32}C_1 \left(\frac{1}{2}\right)^1 \left(\frac{1}{2}\right)^{32-1}$$

$$= 32.\frac{1}{2} \left(\frac{1}{2}\right)^{31}$$

$$=\left(\frac{1}{2}\right)^{27}$$

$$P(X \ge 2)$$

$$=1-[P(X=0)+P(X=1)]$$

$$= 1 - \left[\left(\frac{1}{2} \right)^{32} + \left(\frac{1}{2} \right)^{27} \right]$$

$$= 1 - \left(\frac{1}{2}\right)^{27} \left(\frac{1}{32} + 1\right)$$

$$=1-\left(\frac{1}{2}\right)^{27}\left(\frac{33}{32}\right)$$

$$=1-\frac{33}{2^{32}}$$

Hence

$$P(X = 0) = \left(\frac{1}{2}\right)^{32}, P(X = 1) = \left(\frac{1}{2}\right)^{27}, P(X \ge 2) = 1 - \frac{33}{2^{32}}$$

Binomial Distribution Ex 33.2 Q12

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Wondershare **PDFelement**

Let p be the probability of success in a single throw of die

$$D = \frac{2}{6}$$

[Since success is occurance of 5 or 6]

$$p = \frac{1}{3}$$

$$q = 1 - \frac{1}{3}$$

Since
$$p + q = 1$$

$$Q = \frac{2}{3}$$

Given, n = 8

$$Mean = np$$
$$= \frac{8}{3}$$
$$= 2.66$$

Standard deviation =
$$\sqrt{npq}$$

= $\sqrt{8 \times \frac{1}{3} \times \frac{2}{3}}$
= $\frac{4}{3}$
= 1.33

Mean = 2.66, Standard deviation = 1.33

Binomial Distribution Ex 33.2 Q13

Nondershare Nondershare Let n and p be the parameters of binomial distribution. Let p = probability of having a boy in the family

Given,
$$p = q$$

Since,
$$p+q=1$$

$$p + p = 1$$

$$p = \frac{1}{2}$$

$$Q = \frac{1}{2}$$

The expected number of boys = np

$$= 8 \times \frac{1}{2}$$
$$= 4$$

The expected number of boys = 4

Binomial Distribution Ex 33.2 Q14

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Let ho denot the probability of a defective item produced in the factory, $rac{1}{2}$

$$p = 0.02$$

$$= \frac{2}{100}$$

$$p = \frac{1}{50}$$

$$q = 1 - \frac{1}{50}$$

$$= \frac{49}{50}$$
[Since $p + q = 1$]

Given n = 10,000

Expected number of defective item = np

$$= 10000 \times \frac{1}{50}$$
$$= 200$$

Standard deviation =
$$\sqrt{npq}$$

= $\sqrt{10000 \times \frac{1}{50} \times \frac{49}{50}}$
= 14

Expected No. of defective items = 200 Standard deviation = 14

Binomial Distribution Ex 33.2 Q15

Let p be the probability of success, so

$$p = \frac{2}{6}$$
$$p = \frac{1}{3}$$

[Since success in occurance of 1 or 6 on the die]

Given,
$$n = 3$$

 $q = 1 - p$
 $= 1 - \frac{1}{3}$
 $q = \frac{2}{3}$

[Since p+q=1]

Mean =
$$np$$

= $3\left(\frac{1}{3}\right)$
= 1

Variance =
$$npq$$

= $3 \times \left(\frac{1}{3}\right) \left(\frac{2}{3}\right)$
= $\frac{2}{3}$

Mean = 1 $Variance = \frac{2}{3}$





Let n and p be the parameters of binomial distribution Given,

Mean
$$= np = 3$$

Variance =
$$npq = \frac{3}{2}$$

Dividing equation (ii) by (i),

$$\frac{npq}{np} = \frac{\frac{3}{2}}{3}$$
$$q = \frac{1}{2}$$

$$q = \frac{1}{2}$$

$$p = 1 - \frac{1}{2}$$

$$\left[\operatorname{as} p + q = 1\right]$$

$$p = \frac{1}{2}$$

Put the value of p in equation (i)

$$n\left(\frac{1}{2}\right) = 3$$

$$n = 6$$

Hence, binomial distribution is given by

$$P\left(X=r\right) = {^{n}C_{r}p^{r}q^{n-r}}$$

$$P\left(X=r\right)=\ ^{6}C_{r}\left(\frac{1}{2}\right)^{r}\left(\frac{1}{2}\right)^{6-r}$$

$$P(X \leq 5)$$

$$= P(X = 0) + P(X = 1) + P(X = 2) + P(X = 3) + P(X = 4) + P(X = 5)$$

$$= 1 - P(X = 6)$$

$$= 1 - P(X = 6)$$

$$= 1 - {}^6\mathrm{C}_6 \left(\frac{1}{2}\right)^6 \left(\frac{1}{2}\right)^{6-6} \, ,$$

$$=1-\left(\frac{1}{2}\right)^6$$

$$=1-\frac{1}{64}$$

$$=\frac{63}{64}$$

$$P(X \le 5) = \frac{63}{64}$$

Binomial Distribution Ex 33.2 Q17

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Let n and p be the parameters of binomial distribution.

Given,

Dividing equation (ii) by (i),

$$\frac{npq}{np} = \frac{2}{4}$$

$$q = \frac{1}{2}$$

$$p = 1 - \frac{1}{2}$$

$$p = \frac{1}{2}$$
[Since $p + q = 1$]

Put the value of p in equation (i),

$$np = 4$$

$$n\left(\frac{1}{2}\right) = 4$$

$$n = 8$$

Hence, binomial distribution is given by

$$P(X = r) = {}^{n}C_{r}p^{r}q^{n-r}$$

$$P(X = r) = {}^{8}C_{r}\left(\frac{1}{2}\right)^{r}\left(\frac{1}{2}\right)^{8-r}$$

$$---(iii)$$

$$P(X \ge 5)$$

$$= P(X = 5) + P(X = 6) + P(X = 7) + P(X = 8)$$

$$= {}^{8}C_{5}\left(\frac{1}{2}\right)^{5}\left(\frac{1}{2}\right)^{3} + {}^{8}C_{6}\left(\frac{1}{2}\right)^{6}\left(\frac{1}{2}\right)^{2} + {}^{8}C_{7}\left(\frac{1}{2}\right)^{7}\left(\frac{1}{2}\right) + {}^{8}C_{8}\left(\frac{1}{2}\right)^{8}$$
[Using equation (iii)]
$$= \frac{8 \times 7 \times 6}{3 \times 2}\left(\frac{1}{2}\right)^{8} + \frac{8 \times 7}{2}\left(\frac{1}{2}\right)^{8} + 8\left(\frac{1}{2}\right)^{8} + \left(\frac{1}{2}\right)^{8}$$

$$= \left(\frac{1}{2}\right)^{8}\left[56 + 28 + 8 + 1\right]$$

$$= \frac{93}{256}$$

$$P(X \ge 5) = \frac{93}{256}$$

Binomial Distribution Ex 33.2 Q18

$$= 1 - \left(\frac{2}{3}\right)^4$$

$$= 1 - \frac{16}{81}$$

$$= \frac{65}{81}$$

$$P(X \ge 1) = \frac{65}{81}$$





Let n and p be the parameters of binomial distribution,

Given, n = 6

Given,
$$n = 6$$

Mean + Variance $= \frac{10}{3}$
 $np + npq = \frac{10}{3}$
 $6p + 6pq = \frac{10}{3}$
 $6p (1+q) = \frac{10}{3}$
 $6(1-q)(1+q) = \frac{10}{3}$
 $6(1-q^2) = \frac{10}{3}$
 $1-q^2 = \frac{10}{18}$
 $-q^2 = \frac{5}{9} - 1$
 $-q^2 = -\frac{4}{9}$

 $q^2 = \frac{4}{9}$

 $q = \frac{2}{3}$ p = 1 - q $= 1 - \frac{2}{3}$

 $p = \frac{1}{2}$

[Since
$$p + q = 1$$
]

Hence, the binomial distribution is given by,

$$P\left(X=r\right) = {^{n}C_{r}p^{r}q^{n-r}}$$

$$P(X = r) = {}^{6}C_{r} \left(\frac{1}{3}\right)^{r} \left(\frac{2}{3}\right)^{6-r}$$

Binomial Distribution Ex 33.2 Q20

Throwing a doublet i.e. $\{(1,1),(2,2),(3,3),(4,4),(5,5),(6,6)\}$

Total number of outcomes = 36

Let p be the probability of success therefore

$$p = 6/36 = 1/6$$

Let q be the probability of failure therefore q = 1 - p = 1 - 1/6 = 5/6

Since the dice is thrown 4 times, n = 4

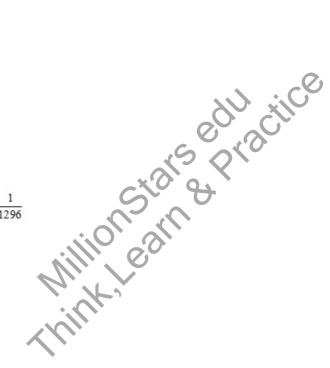
Let X be the random variable for getting doublet, therefore X can take at max 4

$$\begin{split} P(X=0) &= {}^{4}C_{0}p^{0}q^{4} = \left(\frac{5}{6}\right)^{4} = \frac{625}{1296} \\ P(X=1) &= {}^{4}C_{1}p^{1}q^{3} = 4 \cdot \frac{1}{6} \cdot \left(\frac{5}{6}\right)^{3} = \frac{500}{1296} \\ P(X=2) &= {}^{4}C_{2}p^{2}q^{2} = \frac{4 \cdot 3}{2} \cdot \left(\frac{1}{6}\right)^{2} \cdot \left(\frac{5}{6}\right)^{2} = \frac{150}{1296} \\ P(X=3) &= {}^{4}C_{3}p^{3}q^{1} = 4 \cdot \left(\frac{1}{6}\right)^{3} \cdot \frac{5}{6} = \frac{20}{1296} \\ P(X=4) &= {}^{4}C_{4}p^{4}q^{0} = 1 \cdot \left(\frac{1}{6}\right)^{4} \left(\frac{5}{6}\right)^{0} = \frac{1}{1296} \end{split}$$

Mean

$$\begin{split} \mu &= \sum_{i=1}^{4} X_i P \left(X_i \right) = 0 \cdot \frac{625}{1296} + 1 \cdot \frac{500}{1296} + 2 \cdot \frac{150}{1296} + 3 \cdot \frac{20}{1296} + 4 \cdot \frac{1}{1296} \\ &= \frac{500 + 300 + 60 + 4}{1296} = \frac{54}{81} = \frac{2}{3} \end{split}$$

Hence the mean is $=\frac{2}{3}$



Throwing a doublet i.e. $\{(1,1),(2,2),(3,3),(4,4),(5,5),(6,6)\}$

Total number of outcomes = 36

Let p be the probability of success therefore

$$p = 6/36 = 1/6$$

Let q be the probability of failure therefore q = 1 - p = 1 - 1/6 = 5/6

Since there is three rows of dice so n=3

Let X be the random variable for getting doublet, therefore X can take at max 3 values.

$$P(X=0) = {}^{3}C_{0}p^{0}q^{3} = \left(\frac{5}{6}\right)^{3} = \frac{125}{216}$$

$$P(X=1) = {}^{3}C_{1}p^{1}q^{2} = 3 \cdot \frac{1}{6} \cdot \left(\frac{5}{6}\right)^{2} = \frac{75}{216}$$

$$P(X=2) = {}^{3}C_{2}p^{2}q^{1} = 3 \cdot \left(\frac{1}{6}\right)^{2} \cdot \left(\frac{5}{6}\right) = \frac{15}{216}$$

$$P(X=3) = {}^{3}C_{3}p^{3}q^{0} = \left(\frac{1}{6}\right)^{3} = \frac{1}{216}$$

Mean

$$\mu = \sum_{i=1}^{3} X_i P(X_i) = 0 \cdot \frac{125}{216} + 1 \cdot \frac{75}{216} + 2 \cdot \frac{15}{216} + 3 \cdot \frac{1}{216}$$
$$= \frac{75 + 30 + 3}{216} = \frac{108}{216} = \frac{1}{2}$$

Hence the mean is $=\frac{1}{2}$

Binomial Distribution Ex 33.2 Q22

Out of 15 bulbs 5 are defective.

Hence, the probability that the drawn bulb is defective is

$$P(Defective) = \frac{5}{15} = \frac{1}{3}$$

P(Not defective) =
$$\frac{10}{15} = \frac{2}{3}$$

Let X denote the number of defective bulbs out of 4.

Then, X follows binomial distribution with

$$n = 4$$
, $p = \frac{1}{2}$ and $q = \frac{2}{3}$ such that

$$P(X = r) = {}^{4}C_{r} \left(\frac{1}{3}\right)^{r} \left(\frac{2}{3}\right)^{4-r}; r = 0, 1, 2, 3, 4$$

$$\begin{aligned} \text{Mean} &= \sum_{r=0}^{4} r P(r) = 1 \times {}^{4} C_{1} \left(\frac{1}{3} \right) \left(\frac{2}{3} \right)^{3} + 2 \times {}^{4} C_{2} \left(\frac{1}{3} \right)^{2} \left(\frac{2}{3} \right)^{2} \\ &+ 3 \times {}^{4} C_{3} \left(\frac{1}{3} \right)^{3} \left(\frac{2}{3} \right) + 4 \times {}^{4} C_{4} \left(\frac{1}{3} \right)^{4} \left(\frac{2}{3} \right)^{0} \end{aligned}$$

$$= \frac{32}{81} + \frac{48}{81} + \frac{24}{81} + \frac{4}{81} = \frac{108}{81} = \frac{4}{3}$$

Binomial Distribution Ex 33.2 Q23

Let p be the probablity of getting 2 when a dice is thrown.

Then
$$p = \frac{1}{6}$$

Clearly, X follows binomial distribution with n = 3, p = $\frac{1}{6}$.

: Expectation =
$$E(X) = np = 3x \frac{1}{6} = \frac{1}{2}$$

Binomial Distribution Ex 33.2 Q24

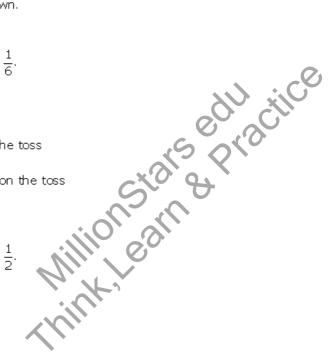
Let p be the probablity of getting an even number on the toss when a dice is thrown.

Let q be the probablity of not getting an even number on the toss when a dice is thrown.

Then p =
$$\frac{3}{6} = \frac{1}{2}$$
 and q = $\frac{1}{2}$

Clearly, X follows binomial distribution with n = 2, $p = \frac{1}{2}$.

:. Variance = npq =
$$2 \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{2}$$







Binomial Distribution Ex 33.2 Q25

Let p be the probablity of getting a spade card. Let q be the probablity of getting a spade card.

Then p =
$$\frac{13}{52} = \frac{1}{4}$$
 and q = $\frac{3}{4}$

Clearly, X follows binomial distribution with n = 3, p = $\frac{1}{4}$ and q = $\frac{3}{4}$.

Probablity distribution is given by,

$$P(X = r) = {}^{3}C_{r} \left(\frac{1}{4}\right)^{r} \left(\frac{3}{4}\right)^{3-r}; r = 0, 1, 2$$

: Mean = np =
$$3 \times \frac{1}{4} = \frac{3}{4}$$



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