Catalog

Chapter 15

Visualising Solid Shapes

0756CH15

15.1 Introduction: Plane Figures and Solid Shapes

In this chapter, you will classify figures you have seen in terms of what is known as *dimension*.

In our day to day life, we see several objects like books, balls, ice-cream cones etc., around us which have different shapes. One thing common about most of these objects is that they all have some length, breadth and height or depth.

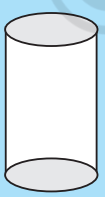
That is, they all occupy space and have three dimensions.

Hence, they are called three dimensional shapes.

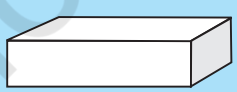
Do you remember some of the three dimensional shapes (i.e., solid shapes) we have seen in earlier classes?

Try These

Match the shape with the name:

(i) 

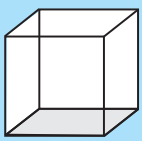
(ii) 

(iii) 

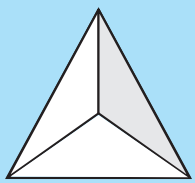
(a) Cuboid

(b) Cylinder

(c) Cube

(iv) 

(v) 

(vi) 

(d) Sphere

(e) Pyramid

(f) Cone

Fig 15.1

Try to identify some objects shaped like each of these.

By a similar argument, we can say figures drawn on paper which have only length and breadth are called two dimensional (i.e., plane) figures. We have also seen some two dimensional figures in the earlier classes.

Match the 2 dimensional figures with the names (Fig 15.2):

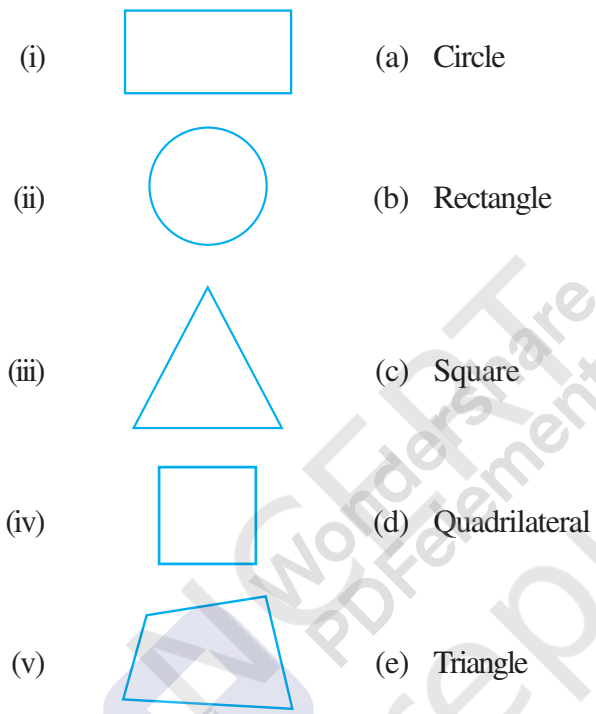


Fig 15.2

Note: We can write 2-D in short for 2-dimension and 3-D in short for 3-dimension.

15.2 Faces, Edges and Vertices

Do you remember the Faces, Vertices and Edges of solid shapes, which you studied earlier? Here you see them for a cube:

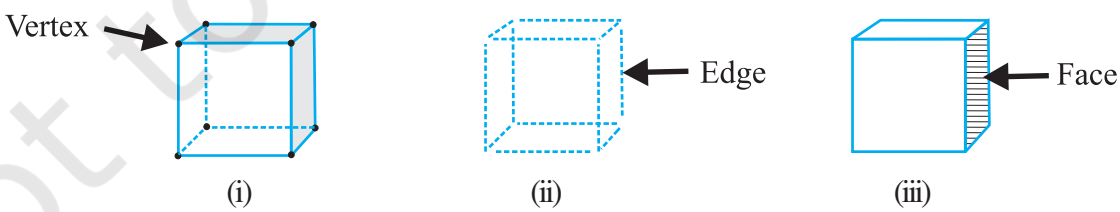


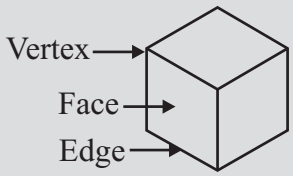
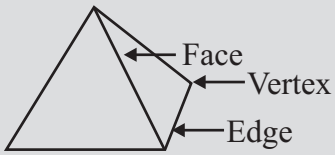
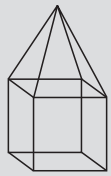
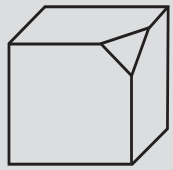
Fig 15.3

The 8 corners of the cube are its **vertices**. The 12 line segments that form the skeleton of the cube are its **edges**. The 6 flat square surfaces that are the skin of the cube are its **faces**.

Do This

Complete the following table:

Table 15.1

				
Faces (**F**)	6	4		
Edges (**E**)	12			
Vertices (**V**)	8	4		

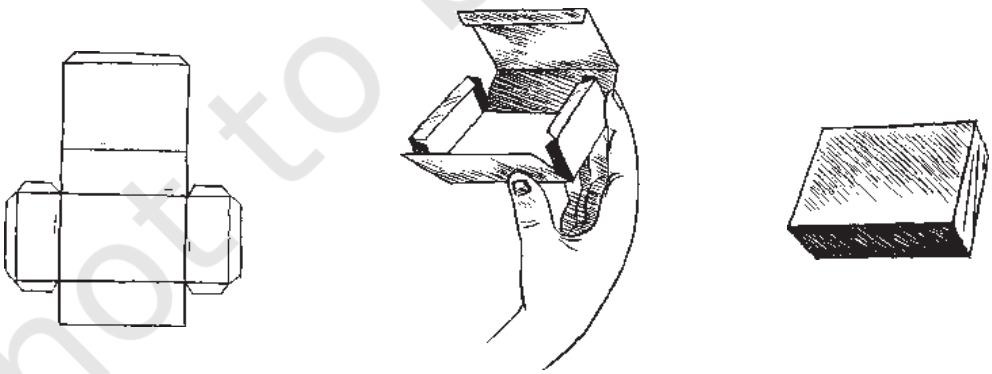
Can you see that, the two dimensional figures can be identified as the faces of the three dimensional shapes? For example a cylinder  has two faces which are circles, and a pyramid, shaped like this  has triangles as its faces.

We will now try to see how some of these 3-D shapes can be visualised on a 2-D surface, that is, on paper.

In order to do this, we would like to get familiar with three dimensional objects closely. Let us try forming these objects by making what are called nets.

15.3 Nets for Building 3-D Shapes

Take a cardboard box. Cut the edges to lay the box flat. You have now a **net** for that box. A net is a sort of skeleton-outline in 2-D [Fig154 (i)], which, when folded [Fig154 (ii)], results in a 3-D shape [Fig154 (iii)].



(i) (ii) (iii)

Fig 15.4

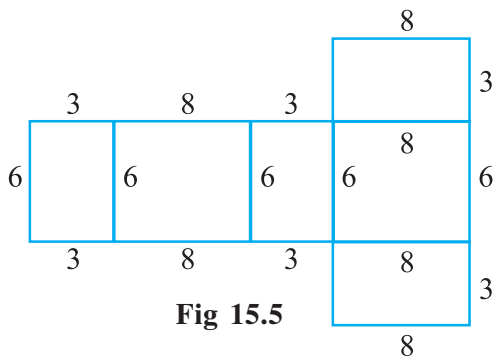


Fig 15.5

Here you got a **net** by suitably separating the edges. Is the reverse process possible?

Here is a net pattern for a box (Fig 15.5). Copy an enlarged version of the net and try to make the box by suitably folding and gluing together. (You may use suitable units). The box is a solid. It is a 3-D object with the shape of a cuboid.

Similarly, you can get a net for a cone by cutting a slit along its slant surface (Fig 15.6).

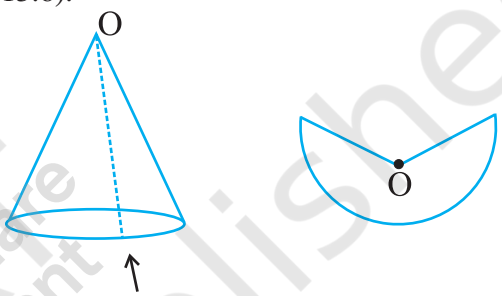
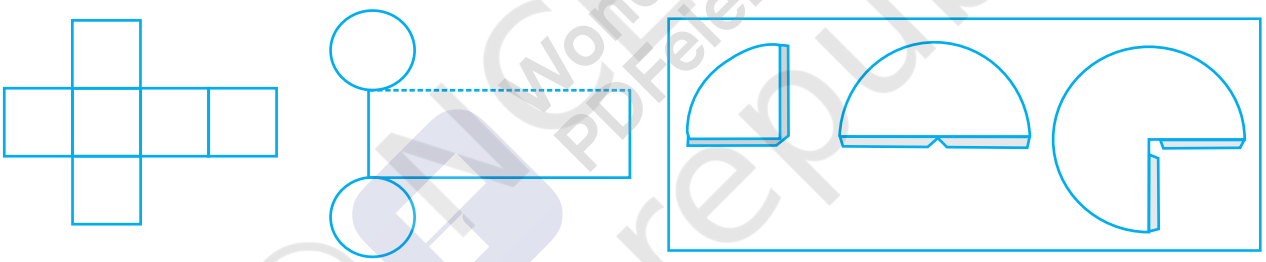


Fig 15.6

You have different nets for different shapes. Copy enlarged versions of the nets given (Fig 15.7) and try to make the 3-D shapes indicated. (You may also like to prepare skeleton models using strips of cardboard fastened with paper clips).



Cube (i) Cylinder (ii) Cone (iii)

Fig 15.7

We could also try to make a net for making a pyramid like the Great Pyramid in Giza (Egypt) (Fig 15.8). That pyramid has a square base and triangles on the four sides.

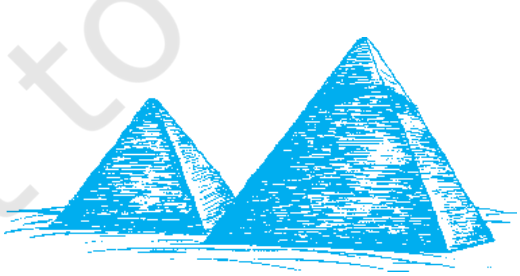


Fig 15.8

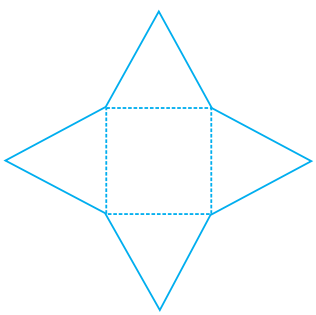


Fig 15.9

See if you can make it with the given net (Fig 15.9).

TRY THESE

Here you find four nets (Fig 15.10). There are two *correct* nets among them to make a tetrahedron. See if you can work out which nets will make a tetrahedron.

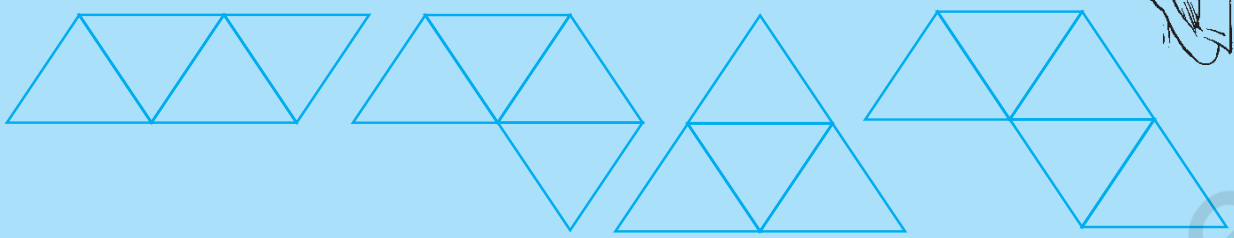
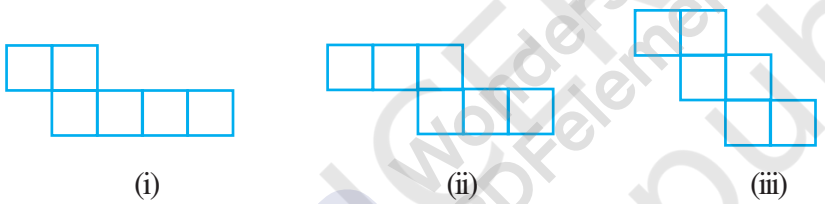


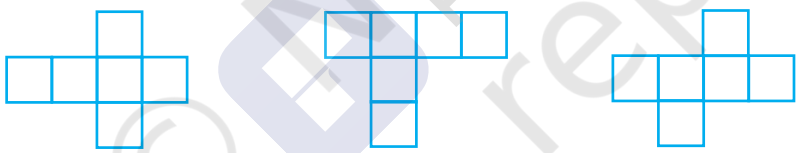
Fig 15.10

EXERCISE 15.1

1. Identify the nets which can be used to make cubes (cut out copies of the nets and try it):

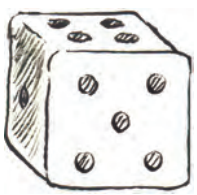


(i) (ii) (iii)



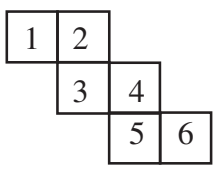
(iv) (v) (vi)

2. Dice are cubes with dots on each face. Opposite faces of a die always have a total of seven dots on them.



Here are two nets to make dice (cubes); the numbers inserted in each square indicate the number of dots in that box.

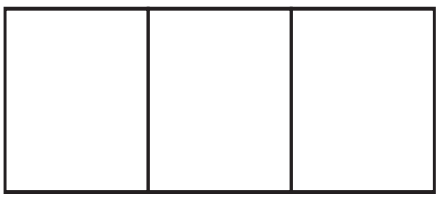
Insert suitable numbers in the blanks, remembering that the number on the opposite faces should total to 7.



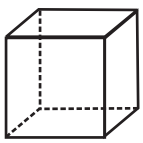
3. Can this be a net for a die?

Explain your answer.

4. Here is an incomplete net for making a cube. Complete it in at least two different ways. Remember that a cube has six faces. How many are there in the net here? (Give two separate diagrams. If you like, you may use a squared sheet for easy manipulation.)



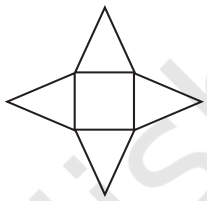
5. Match the nets with appropriate solids:

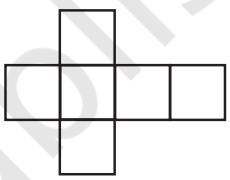
(a) 

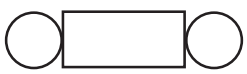
(b) 

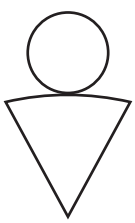
(c) 

(d) 

(i) 

(ii) 

(iii) 

(iv) 

Play this game

You and your friend sit back-to-back. One of you reads out a net to make a 3-D shape, while the other attempts to copy it and sketch or build the described 3-D object.

15.4 Drawing Solids on a Flat Surface

Your drawing surface is paper, which is flat. When you draw a solid shape, the images are somewhat distorted to make them appear three-dimensional. It is a visual illusion. You will find here two techniques to help you.

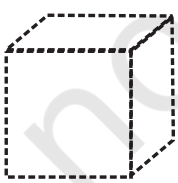


Fig 15.11

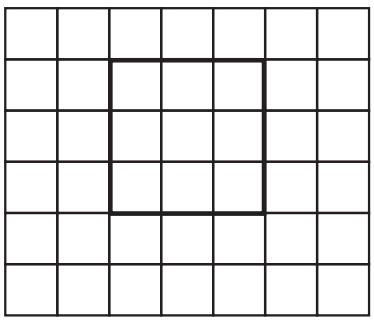
15.4.1 Oblique Sketches

Here is a picture of a cube (Fig 15.11). It gives a clear idea of how the cube looks like, when seen from the front. You do not see certain faces. In the drawn picture, the lengths

are not equal, as they should be in a cube. Still, you are able to recognise it as a cube. Such a sketch of a solid is called an **oblique sketch**.

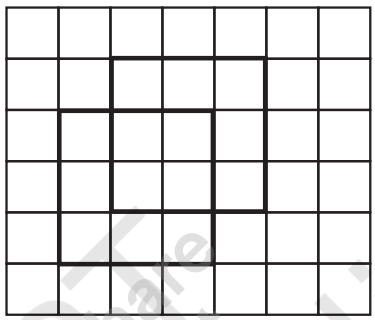
How can you draw such sketches? Let us attempt to learn the technique.

You need a squared (lines or dots) paper. Initially practising to draw on these sheets will later make it easy to sketch them on a plain sheet (without the aid of squared lines or dots!) Let us attempt to draw an oblique sketch of a $3 \times 3 \times 3$ (each edge is 3 units) cube (Fig 15.12).



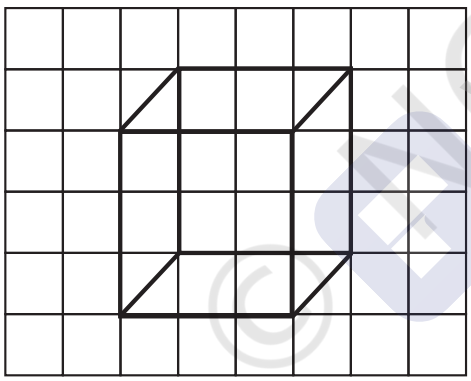
Step 1

Draw the **front** face.



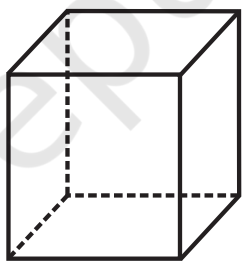
Step 2

Draw the **opposite** face. Sizes of the faces have to be same, but the sketch is somewhat off-set from step 1.



Step 3

Join the corresponding corners



Step 4

Redraw using dotted lines for hidden edges. (It is a convention) The sketch is ready now.

Fig 15.12

In the oblique sketch above, did you note the following?

(i) The sizes of the front faces and its opposite are same; and

(ii) The edges, which are all equal in a cube, appear so in the sketch, though the actual measures of edges are not taken so.

You could now try to make an oblique sketch of a cuboid (remember the faces in this case are rectangles)

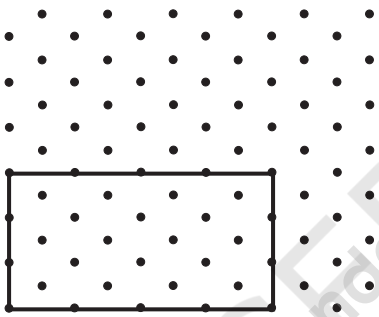
Note: You can draw sketches in which measurements also agree with those of a given solid. To do this we need what is known as an **isometric sheet**. Let us try to

make a cuboid with dimensions 4 cm length, 3 cm breadth and 3 cm height on given isometric sheet.

15.4.2 Isometric Sketches

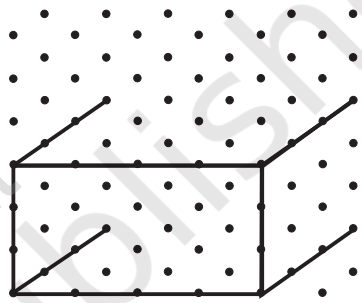
Have you seen an isometric dot sheet? (A sample is given at the end of the book). Such a sheet divides the paper into small equilateral triangles made up of dots or lines. *To draw sketches in which measurements also agree with those of the solid,* we can use isometric dot sheets. [Given on inside of the back cover (3rd cover page).]

Let us attempt to draw an isometric sketch of a cuboid of dimensions $4 \times 3 \times 3$ (which means the edges forming length, breadth and height are 4, 3, 3 units respectively) (Fig 15.13).



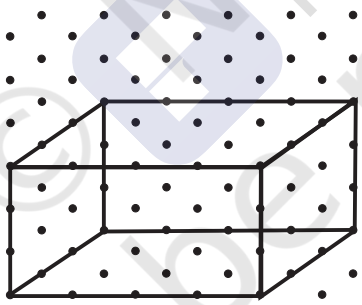
Step 1

Draw a rectangle to show the front face.



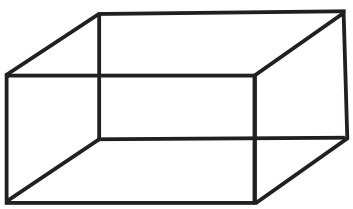
Step 2

Draw four parallel line segments of length 3 starting from the four corners of the rectangle.



Step 3

Connect the matching corners with appropriate line segments.



Step 4

This is an isometric sketch of the cuboid.

Fig 15.13

Note that the measurements are of exact size in an isometric sketch; this is not so in the case of an oblique sketch.

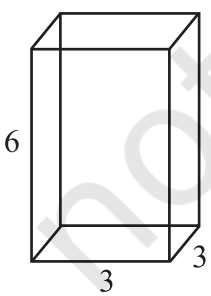


Fig 15.14 (i)

EXAMPLE 1 Here is an oblique sketch of a cuboid [Fig 15.14(i)]. Draw an isometric sketch that matches this drawing.

SOLUTION Here is the solution [Fig 15.14(ii)]. Note how the measurements are taken care of.

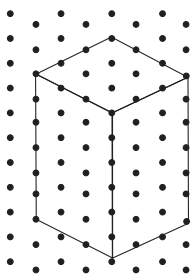
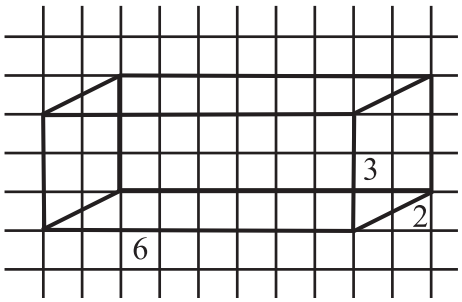


Fig 15.14 (ii)

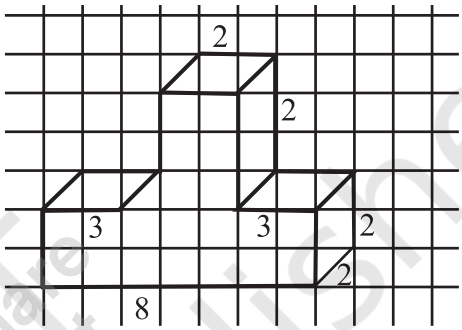
How many units have you taken along (i) 'length'? (ii) 'breadth'? (iii) 'height'? Do they match with the units mentioned in the oblique sketch?

Exercise 15.2

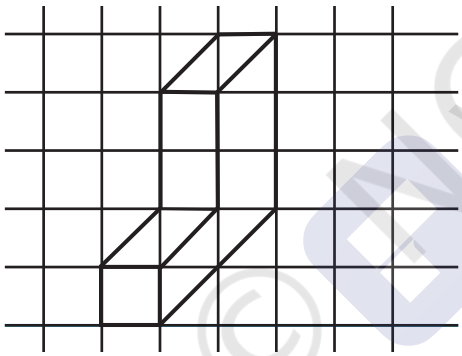
1. Use isometric dot paper and make an isometric sketch for each one of the given shapes:



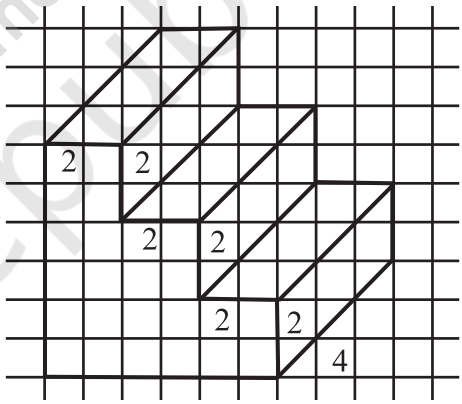
(i)



(ii)



(iii)



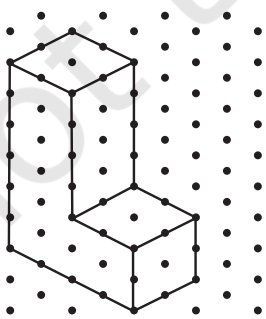
(iv)

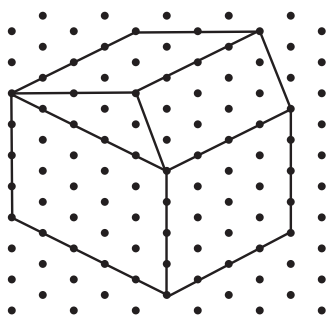
Fig 15.15

2. The dimensions of a cuboid are 5 cm, 3 cm and 2 cm. Draw three different isometric sketches of this cuboid.

3. Three cubes each with 2 cm edge are placed side by side to form a cuboid. Sketch an oblique or isometric sketch of this cuboid.

4. Make an oblique sketch for each one of the given isometric shapes:



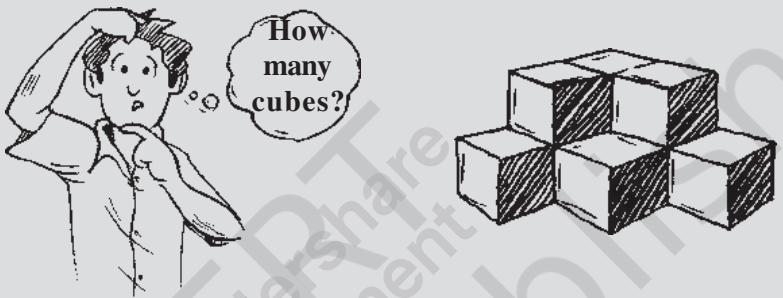


5. Give (i) an oblique sketch and (ii) an isometric sketch for each of the following:
   (a) A cuboid of dimensions 5 cm, 3 cm and 2 cm. (Is your sketch unique?)
   (b) A cube with an edge 4 cm long.

An isometric sheet is attached at the end of the book. You could try to make on it some cubes or cuboids of dimensions specified by your friend.

15.4.3 Visualising Solid Objects

Do This



Sometimes when you look at combined shapes, some of them may be hidden from your view.

Here are some activities you could try in your free time to help you visualise some solid objects and how they look. Take some cubes and arrange them as shown in Fig 15.16.

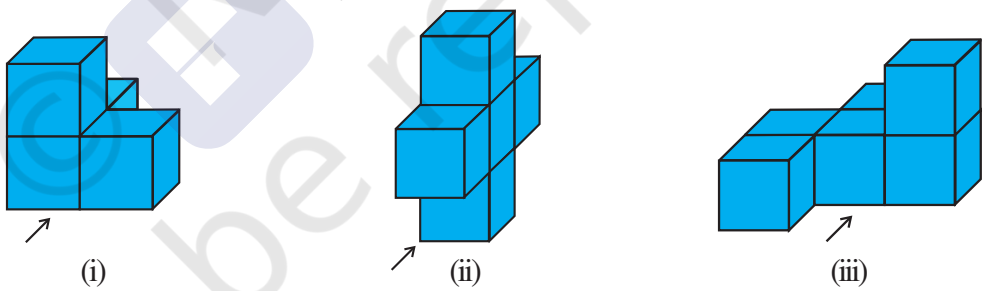


Fig 15.16

Now ask your friend to guess how many cubes there are when observed from the view shown by the arrow mark.

Try These

Try to guess the number of cubes in the following arrangements (Fig 15.17).

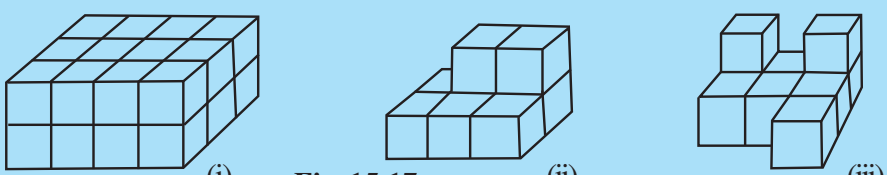


Fig 15.17

Such visualisation is very helpful. Suppose you form a cuboid by joining such cubes. You will be able to guess what the length, breadth and height of the cuboid would be.

EXAMPLE 2 If two cubes of dimensions 2 cm by 2cm by 2cm are placed side by side, what would the dimensions of the resulting cuboid be?

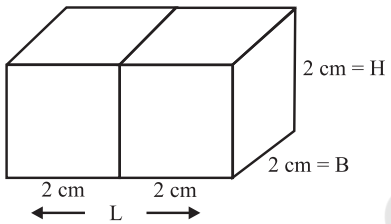


Fig 15.18

SOLUTION As you can see (Fig 15.18) when kept side by side, the length is the only measurement which increases, it becomes 2 + 2 = 4 cm.

The breadth = 2 cm and the height = 2 cm.

TRY THESE

1. Two dice are placed side by side as shown: Can you say what the total would be on the face opposite to

   (a) 5 + 6 (b) 4 + 3

   (Remember that in a die sum of numbers on opposite faces is 7)


Fig 15.19

2. Three cubes each with 2 cm edge are placed side by side to form a cuboid. Try to make an oblique sketch and say what could be its length, breadth and height.

15.5 VIEWING DIFFERENT SECTIONS OF A SOLID

Now let us see how an object which is in 3-D can be viewed in different ways.

15.5.1 One Way to View an Object is by Cutting or Slicing

Slicing game

Here is a loaf of bread (Fig 15.20). It is like a cuboid with a square face. You 'slice' it with a knife.

When you give a 'vertical' cut, you get several pieces, as shown in the Figure 15.20. Each face of the piece is a square! We call this face a **'cross-section'** of the whole bread. The cross section is nearly a square in this case.

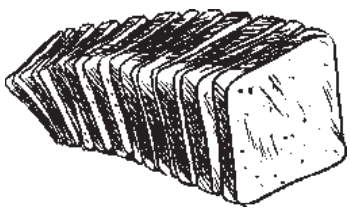


Fig 15.20

Beware! If your cut is not 'vertical' you may get a different cross section! Think about it. The boundary of the cross-section you obtain is a plane curve. Do you notice it?

A kitchen play

Have you noticed cross-sections of some vegetables when they are cut for the purposes of cooking in the kitchen? Observe the various slices and get aware of the shapes that result as cross-sections.

Play this

Make clay (or plasticine) models of the following solids and make vertical or horizontal cuts. Draw rough sketches of the cross-sections you obtain. Name them wherever you can.

Fig 15.21

EXERCISE 15.3

1. What cross-sections do you get when you give a

(i) vertical cut (ii) horizontal cut

to the following solids?

(a) A brick (b) A round apple (c) A die

(d) A circular pipe (e) An ice cream cone

Fig 15.22

15.5.2 Another Way is by Shadow Play

A shadow play

Shadows are a good way to illustrate how three-dimensional objects can be viewed in two dimensions. Have you seen a **shadow play**? It is a form of entertainment using solid articulated figures in front of an illuminated back-drop to create the illusion of moving images. It makes some indirect use of ideas in Mathematics.

Fig 15.23

You will need a source of light and a few solid shapes for this activity. (If you have an overhead projector, place the solid under the lamp and do these investigations.)

Keep a torchlight, *right in front of* a Cone. What type of shadow does it cast on the screen? (Fig 15.23)

The solid is three-dimensional; what is the dimension of the shadow?

If, instead of a cone, you place a cube in the above game, what type of shadow will you get?

Experiment with different positions of the source of light and with different positions of the solid object. Study their effects on the shapes and sizes of the shadows you get.

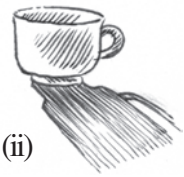
(i)

Here is another funny experiment that you might have tried already: Place a circular plate in the open when the Sun at the noon time is just *right above* it as shown in Fig 15.24 (i). What is the shadow that you obtain?

Will it be same during

(a) forenoons? 

(b) evenings? 



(ii)

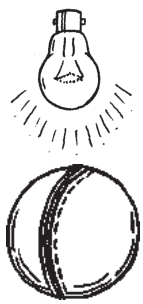
(iii)

Fig 15.24 (i) - (iii)

Study the shadows in relation to the position of the Sun and the time of observation.

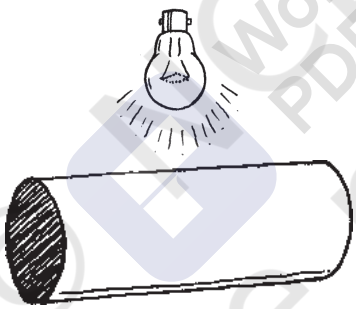
EXERCISE 15.4

1. A bulb is kept burning just right above the following solids. Name the shape of the shadows obtained in each case. Attempt to give a rough sketch of the shadow. (You may try to experiment first and then answer these questions).



A ball

(i)



A cylindrical pipe

(ii)

A book

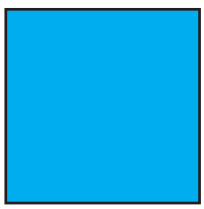
(iii)

2. Here are the shadows of some 3-D objects, when seen under the lamp of an overhead projector. Identify the solid(s) that match each shadow. (There may be multiple answers for these!)

A circle

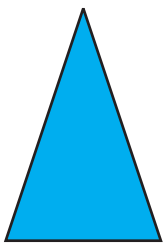
(i)

A square



(ii)

A triangle



(iii)

A rectangle

(iv)

3. Examine if the following are true statements:
   (i) The cube can cast a shadow in the shape of a rectangle.
   (ii) The cube can cast a shadow in the shape of a hexagon.

15.5.3 A Third Way is by Looking at it from Certain Angles to Get Different Views

One can look at an object standing in front of it or by the side of it or from above. Each time one will get a different view (Fig 15.25).

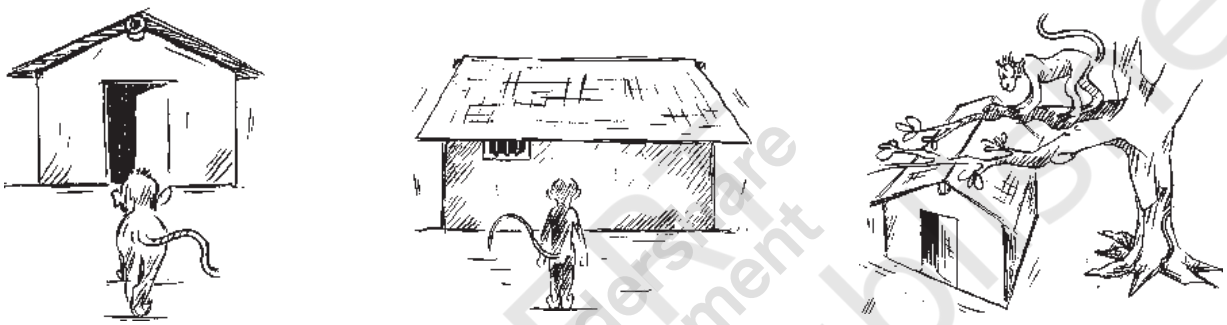


Fig 15.25

Here is an example of how one gets different views of a given building. (Fig 15.26)

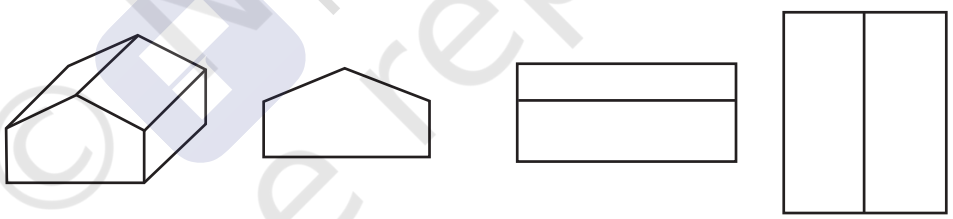


Fig 15.26

You could do this for figures made by joining cubes.

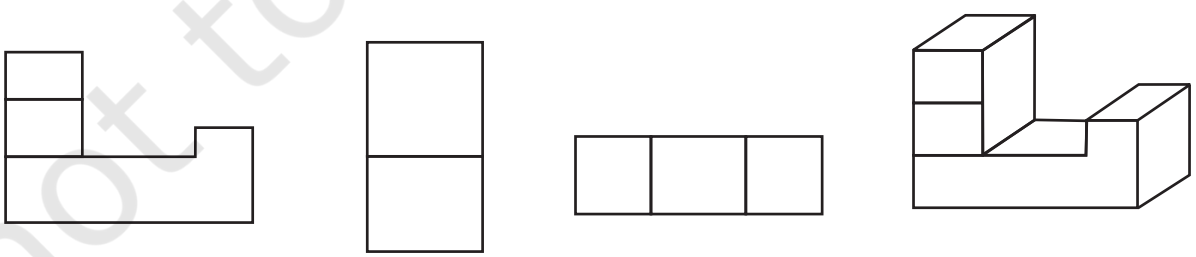


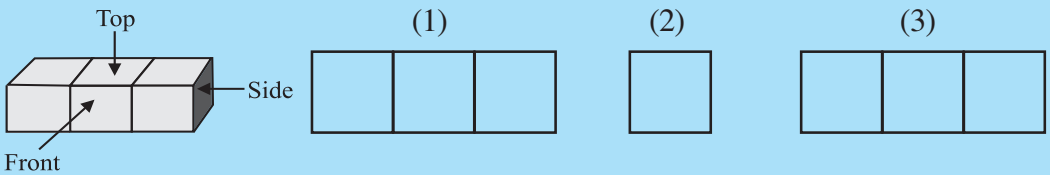
Fig 15.27

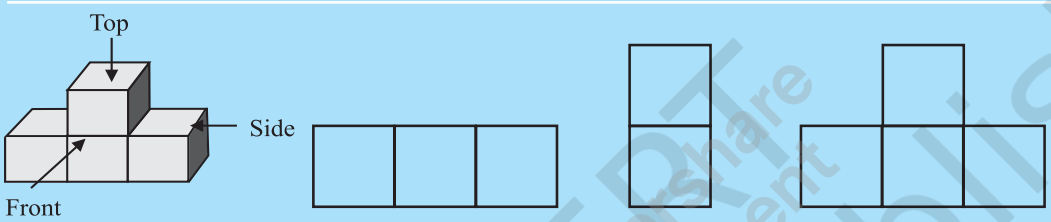
Try putting cubes together and then making such sketches from different sides.

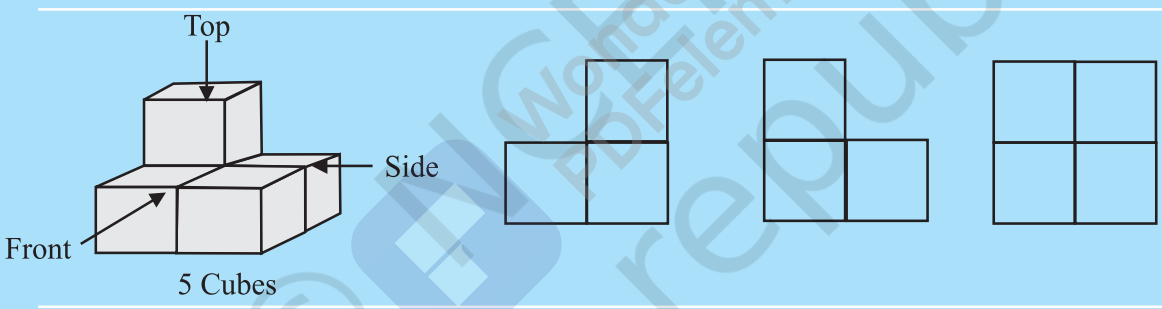
Try These

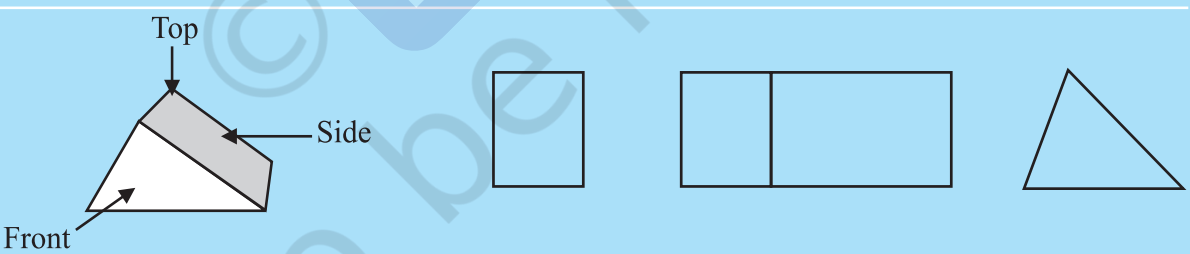
1. For each solid, the three views (1), (2), (3) are given. Identify for each solid the corresponding top, front and side views.

Solid **Its views**

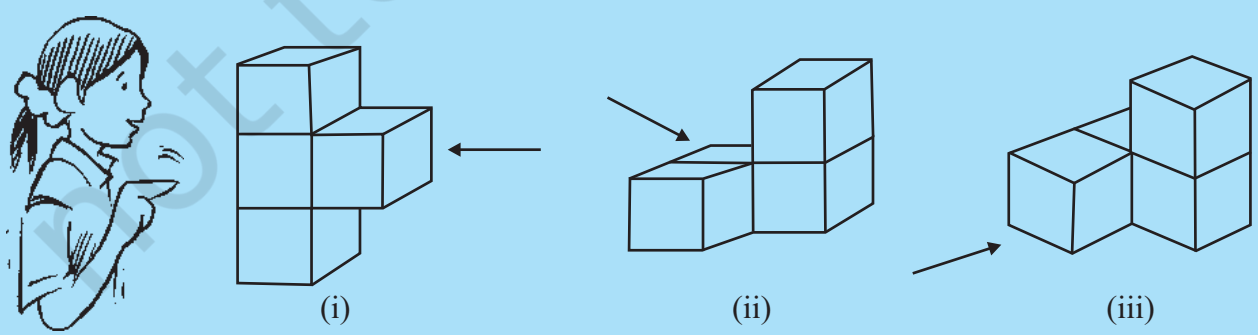








2. Draw a view of each solid as seen from the direction indicated by the arrow.



What have We Discussed?

1. The circle, the square, the rectangle, the quadrilateral and the triangle are examples of **plane figures**; the cube, the cuboid, the sphere, the cylinder, the cone and the pyramid are examples of **solid shapes**.
2. Plane figures are of **two-dimensions** (**2-D**) and the solid shapes are of three-dimensions (**3-D**).
3. The corners of a solid shape are called its **vertices**; the line segments of its skeleton are its **edges**; and its flat surfaces are its **faces**.
4. A **net** is a skeleton-outline of a solid that can be folded to make it. The same solid can have several types of nets.
5. Solid shapes can be drawn on a flat surface (like paper) realistically. We call this **2-D representation of a 3-D solid**.
6. Two types of sketches of a solid are possible:
   (a) An **oblique sketch** does not have proportional lengths. Still it conveys all important aspects of the appearance of the solid.
   (b) An **isometric sketch** is drawn on an isometric dot paper, a sample of which is given at the end of this book. In an isometric sketch of the solid the measurements kept proportional.
7. **Visualising solid shapes** is a very useful skill. You should be able to see 'hidden' parts of the solid shape.
8. Different sections of a solid can be viewed in many ways:
   (a) One way is to view by cutting or **slicing** the shape, which would result in the cross-section of the solid.
   (b) Another way is by observing a 2-D **shadow** of a 3-D shape.
   (c) A third way is to look at the shape from different angles; the **front-view**, the **side-view** and the **top-view** can provide a lot of information about the shape observed.

ANSWERS

EXERCISE 1.1

1. (a) Lahulspiti: –8°C, Srinagar: –2°C, Shimla: 5°C, Ooty: 14°C, Bangalore: 22°C
(b) 30°C (c) 6°C (d) Yes; No **2.** 35

3. –7°C; –3°C **4.** 6200 m **5.** By a positive integer; Rs 358

6. By a negative integer; – 10. **7.** (ii) is the magic square

9. (a) < (b) < (c) > (d) s<
(e) >

10. (i) 11 jumps (ii) 5 jumps (iii) (a) –3 + 2 –3 + 2 – 3 + 2 – 3 + 2 –3 + 2 –3 = – 8
(b) 4 – 2 + 4 – 2 + 4 = 8
8 in (b) represents going up 8 steps.

EXERCISE 1.2

1. One such pair could be:
(a) –10, 3 (b) – 6, 4; (– 6 – 4 = –10) (c) –3, 3

2. One such pair could be:
(a) –2, –10; [–2 – (–10) = 8] (b) – 6, 1
(c) –1, 2; (–1 – 2 = –3)

3. Scores of both the teams are same, i.e., –30; Yes

4. (i) –5 (ii) 0 (iii) –17 (iv) –7
(v) –3

EXERCISE 1.3

1. (a) –3 (b) –225 (c) 630 (d) 316 (e) 0
(f) 1320 (g) 162 (h) –360 (i) –24 (j) 36

3. (i) $-a$ (ii) (a) 22 (b) –37 (c) 0

4. –1 × 5 = –5, –1 × 4 = – 4 = – 5 + 1, – 1 × 3 = – 3 = – 4 + 1,
–1 × 2 = – 2 = – 3 + 1, – 1 × 1 = – 1 = – 2 + 1, – 1 × 0 = 0 = – 1 + 1 so, – 1 × (–1) = 0 + 1 = 1.

5. (a) 480 (b) – 53000 (c) – 15000 (d) – 4182
(e) – 62500 (f) 336 (g) 493 (h) 1140

6. – 10°C **7.** (i) 8 (ii) 15 (iii) 0

8. (a) Loss of Rs 1000 (b) 4000 bags

9. (a) – 9 (b) – 7 (c) 7 (d) – 11

EXERCISE 1.4

1. (a) –3 (b) –10 (c) 4 (d) –1
(e) –13 (f) 0 (g) 1 (h) –1 (i) 1

3. (a) 1 (b) 75 (c) – 206 (d) –1
(e) – 87 (f) – 48 (g) –10 (h) –12

4. (–6, 2), (–12, 4), (12, – 4), (9, –3), (–9, 3) (There could be many such pairs)

5. 9 p.m.; – 14°C **6.** (i) 8 (ii) 13 **7.** 1 hour

EXERCISE 2.1

1. (i) $\frac{7}{5}$ (ii) $\frac{39}{8}\left(=4\frac{7}{8}\right)$ (iii) $\frac{31}{35}$ (iv) $\frac{91}{165}$

(v) $\frac{13}{5}\left(=2\frac{3}{5}\right)$ (vi) $\frac{37}{6}\left(=6\frac{1}{6}\right)$ (vii) $\frac{39}{8}\left(=4\frac{7}{8}\right)$

2. (i) $\frac{2}{3}, \frac{8}{21}, \frac{2}{9}$ (ii) $\frac{7}{10}, \frac{3}{7}, \frac{1}{5}$ **3.** Yes **4.** $\frac{139}{3}\left(=46\frac{1}{3}\right)$ cm

5. (i) $8\frac{17}{20}$ cm (ii) $7\frac{5}{6}$ cm ; Perimeter of ΔABE is greater.

6. $\frac{3}{10}$ cm **7.** $\frac{2}{5}$; Ritu; $\frac{1}{5}$ **8.** Vaibhav; by $\frac{1}{6}$ of an hour.

EXERCISE 2.2

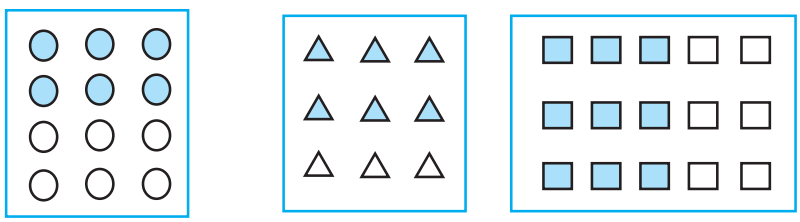
1. (i) (d) (ii) (b) (iii) (a) (iv) (c)

2. (i) (c) (ii) (a) (iii) (b)

3. (i) $4\frac{1}{5}$ (ii) $1\frac{1}{3}$ (iii) $1\frac{5}{7}$ (iv) $1\frac{1}{9}$ (v) $2\frac{2}{3}$

(vi) 15 (vii) $6\frac{2}{7}$ (viii) 16 (ix) $4\frac{1}{3}$ (x) 9

4. One way of doing this is:



(i) (ii) (iii)

5. (a) (i) 12 (ii) 23 (b) (i) 12 (ii) 18 (c) (i) 12 (ii) 27 (d)(i) 16 (ii) 28

6. (a) $15\frac{3}{5}$ (b) $33\frac{3}{4}$ (c) $15\frac{3}{4}$ (d) $25\frac{1}{3}$

(e) $19\frac{1}{2}$ (f) $27\frac{1}{5}$

7. (a) (i) $1\frac{3}{8}$ (ii) $2\frac{1}{9}$ (b) (i) $2\frac{19}{48}$ (ii) $6\frac{1}{24}$ **8.** (i) 2 litres (ii) $\frac{3}{5}$

Exercise 2.3

1. (i) (a) $\frac{1}{16}$ (b) $\frac{3}{20}$ (c) $\frac{1}{3}$ (ii) (a) $\frac{2}{63}$ (b) $\frac{6}{35}$ (c) $\frac{3}{70}$

2. (i) $1\frac{7}{9}$ (ii) $\frac{2}{9}$ (iii) $\frac{9}{16}$ (iv) $1\frac{2}{25}$

(v) $\frac{5}{8}$ (vi) $1\frac{13}{20}$ (vii) $1\frac{13}{35}$

3. (i) $2\frac{1}{10}$ (ii) $4\frac{44}{45}$ (iii) 8 (iv) $2\frac{1}{42}$ (v) $1\frac{33}{35}$ (vi) $7\frac{4}{5}$ (vii) $2\frac{1}{7}$

4. (i) $\frac{3}{5}$ of $\frac{5}{8}$ (ii) $\frac{1}{2}$ of $\frac{6}{7}$ **5.** $2\frac{1}{4}$ m **6.** $10\frac{1}{2}$ hours **7.** 44 km

8. (a) (i) $\frac{5}{10}$ (ii) $\frac{1}{2}$ (b) (i) $\frac{8}{15}$ (ii) $\frac{8}{15}$

Exercise 2.4

1. (i) 16 (ii) $\frac{84}{5}$ (iii) $\frac{24}{7}$ (iv) $\frac{3}{2}$ (v) $\frac{9}{7}$ (vi) $\frac{7}{5}$

2. (i) $\frac{7}{3}$ (improper fraction) (ii) $\frac{8}{5}$ (improper fraction) (iii) $\frac{7}{9}$ (proper fraction)

(iv) $\frac{5}{6}$ (proper fraction) (v) $\frac{7}{12}$ (proper fraction) (vi) 8(whole number)

(vii) 11 (whole number)

3. (i) $\frac{7}{6}$ (ii) $\frac{4}{45}$ (iii) $\frac{6}{91}$ (iv) $\frac{13}{9}$ (v) $\frac{7}{8}$ (vi) $\frac{31}{49}$

4. (i) $\frac{4}{5}$ (ii) $\frac{2}{3}$ (iii) $\frac{3}{8}$ (iv) $\frac{35}{9}$ (v) $\frac{21}{16}$ (vi) $\frac{4}{15}$

(vii) $\frac{48}{25}$ (viii) $\frac{11}{6}$

Exercise 2.5

1. (i) 0.5 (ii) 0.7 (iii) 7 (iv) 1.49 (v) 2.30 (vi) 0.88

2. (i) ₹ 0.07 (ii) ₹ 7.07 (iii) ₹ 77.77 (iv) ₹ 0.50 (v) ₹ 2.35

3. (i) 0.05m, 0.00005 km (ii) 3.5 cm, 0.035m, 0.000035 km

4. (i) 0.2 kg (ii) 3.470 kg (iii) 4.008 kg

5. (i) $2 \times 10 + 0 \times 1 + 0 \times \frac{1}{10} + 3 \times \frac{1}{100}$ (ii) $2 \times 1 + 0 \times \frac{1}{10} + 3 \times \frac{1}{100}$

(iii) $2 \times 100 + 0 \times 10 + 0 \times 1 + 0 \times \frac{1}{10} + 3 \times \frac{1}{100}$

(iv) $2 \times 1 + 0 \times \frac{1}{10} + 3 \times \frac{1}{100} + 4 \times \frac{1}{1000}$

6. (i) Ones (ii) Tens (iii) Tenths (iv) Hundredths (v) Thousandths

7. Ayub travelled more by 0.9 km or 900 m **8.** Sarala bought more fruits **9.** 14.6 km

Exercise 2.6

1. (i) 1.2 (ii) 36.8 (iii) 13.55 (iv) 80.4 (v) 0.35 (vi) 844.08
(vii) 1.72

2. 17.1 cm^2

3. (i) 13 (ii) 368 (iii) 1537 (iv) 1680.7 (v) 3110 (vi) 15610
(vii) 362 (viii) 4307 (ix) 5 (x) 0.8 (xi) 90 (xii) 30

4. 553 km **5.** (i) 0.75 (ii) 5.17 (iii) 63.36 (iv) 4.03 (v) 0.025
(vi) 1.68 (vii) 0.0214 (viii) 10.5525 (ix) 1.0101 (x) 110.011

Exercise 2.7

1. (i) 0.2 (ii) 0.07 (iii) 0.62 (iv) 10.9 (v) 162.8 (vi) 2.07
(vii) 0.99 (viii) 0.16

2. (i) 0.48 (ii) 5.25 (iii) 0.07 (iv) 3.31 (v) 27.223 (vi) 0.056
(vii) 0.397

3. (i) 0.027 (ii) 0.003 (iii) 0.0078 (iv) 4.326 (v) 0.236 (vi) 0.9853

4. (i) 0.0079 (ii) 0.0263 (iii) 0.03853 (iv) 0.1289 (v) 0.0005

5. (i) 2 (ii) 180 (iii) 6.5 (iv) 44.2 (v) 2 (vi) 31
(vii) 510 (viii) 27 (ix) 2.1 **6.** 18 km

Exercise 3.1

2.

Marks	Tally Marks	Frequency
1	I	1
2	II	2

3	|	1
4	|||	3
5	|||\	5
6	||||	4
7	||	2
8	|	1
9	|	1

(i) 9 (ii) 1 (iii) 8 (iv) 5

3. 2 **4.** 50 **5.** (i) 12.5 (ii) 3 (iii) $\frac{0+8+6+4}{4} = \frac{18}{4}$ or $\frac{9}{2}$ (iv) A

6. (i) Highest marks = 95, Lowest marks = 39 (ii) 56 (iii) 73 **7.** 2058

8. (i) 20.5 (ii) 5.9 (iii) 5 **9.** (i) 151 cm (ii) 128 cm (iii) 23 cm (iv) 141.4 cm (v) 5

Exercise 3.2

1. Mode = 20, Median = 20, Yes.

2. Mean = 39, Mode = 15, Median = 15, No.

3. (i) Mode = 38, 43; Median = 40 (ii) Yes, there are 2 modes.

4. Mode = 14, Median = 14

5. (i) T (ii) F (iii) T (iv) F

Exercise 3.3

1. (a) Cat (b) 8

4. (i) Maths (ii) S. Science (iii) Hindi

5. (ii) Cricket (iii) Watching sports

6. (i) Jammu (ii) Jammu, Bangalore

(iii) Bangalore and Jaipur or Bangalore and Ahmedabad (iv) Mumbai

Exercise 3.4

1. (i) Certain to happen (ii) Can happen but not certain (iii) Imposible

(iv) Can happen but not certain (v) Can happen but not certain

2. (i) $\frac{1}{6}$ (ii) $\frac{1}{6}$ **3.** $\frac{1}{2}$

Exercise 4.1

1. (i) No. (ii) No (iii) Yes (iv) No (v) Yes (vi) No

(vii) Yes (viii) No (ix) No (x) No (xi) Yes

2. (a) No (b) No (c) Yes (d) No (e) No (f) No

3. (i) $p = 3$ (ii) $m = 6$

4. (i) $x + 4 = 9$ (ii) $y - 2 = 8$ (iii) $10a = 70$ (iv) $\frac{b}{5} = 6$

(v) $\frac{3t}{4} = 15$ (vi) $7m + 7 = 77$ (vii) $\frac{x}{4} - 4 = 4$ (viii) $6y - 6 = 60$

(ix) $\frac{z}{3} + 3 = 30$

5. (i) The sum of p and 4 is 15 (ii) 7 subtracted from m is 3

(iii) Twice a number m is 7 (iv) One-fifth of a number m is 3

(v) Three-fifth of a number m is 6 (vi) Three times a number p when added to 4 gives 25

(vii) 2 subtracted from four times a number p is 18

(viii) Add 2 to half of a number p to get 8

6. (i) $5m + 7 = 37$ (ii) $3y + 4 = 49$ (iii) $2l + 7 = 87$ (iv) $4b = 180°$

Exercise 4.2

1. (a) Add 1 to both sides; $x = 1$ (b) Subtract 1 from both sides; $x = -1$

(c) Add 1 to both sides; $x = 6$ (d) Subtract 6 from both sides; $x = -4$

(e) Add 4 to both sides; $y = -3$ (f) Add 4 to both sides; $y = 8$

(g) Subtract 4 from both sides; $y = 0$ (h) Subtract 4 from both sides; $y = -8$

2. (a) Divide both sides by 3; $l = 14$ (b) Multiply both sides by 2; $b = 12$

(c) Multiply both sides by 7; $p = 28$ (d) Divide both sides by 4; $x = \frac{25}{4}$

(e) Divide both sides by 8; $y = \frac{36}{8}$ (f) Multiply both sides by 3; $z = \frac{15}{4}$

(g) Multiply both sides by 5; $a = \frac{7}{3}$ (h) Divide both sides by 20; $t = \frac{1}{2}$

3. (a) Step 1: Add 2 to both sides (b) Step 1: Subtract 7 from both sides

Step 2: Divide both sides by 3; $n = 16$ Step 2: Divide both sides by 5; $m = 2$

(c) Step 1: Multiply both sides by 3 (d) Step 1: Multiply both sides 10

Step 2: Divide both sides by 20; $p = 6$ Step 2: Divide both sides by 3; $p = 20$

4. (a) $p = 10$ (b) $p = 9$ (c) $p = 20$ (d) $p = -15$ (e) $p = 8$ (f) $s = -3$

(g) $s = -4$ (h) $s = 0$ (i) $q = 3$ (j) $q = 3$ (k) $q = -3$ (l) $q = 3$

Exercise 4.3

1. (a) $y = 8$ (b) $t = \frac{-18}{5}$ (c) $a = -5$ (d) $q = -8$ (e) $x = -4$ (f) $x = \frac{5}{2}$

(g) $m = \frac{1}{2}$ (h) $z = -2$ (i) $l = \frac{4}{9}$ (j) $b = 12$

2. (a) $x = 2$ (b) $n = 12$ (c) $n = -2$ (d) $x = -4$ (e) $x = 0$

3. (a) $p = \frac{12}{5}$ (b) $p = \frac{6}{5}$ (c) $t = 2$ (d) $p = 7$ (e) $m = 2$

4. (a) Possible equations are: $10x + 2 = 22$; $\frac{x}{5} = \frac{2}{5}$; $5x - 3 = 7$

(b) Possible equations are: $3x = -6$; $3x + 7 = 1$; $3x + 10 = 4$

Exercise 4.4

1. (a) $8x + 4 = 60$; $x = 7$ (b) $\frac{x}{5} - 4 = 3$; $x = 35$ (c) $\frac{3}{4}y + 3 = 21$; $y = 24$

(d) $2m - 11 = 15$; $m = 13$ (e) $50 - 3x = 8$; $x = 14$ (f) $\frac{x+19}{5} = 8$; $x = 21$

(g) $\frac{5n}{2} - 7 = 23$; $n = 12$

2. (a) Lowest score = 40 (b) 70° each (c) Sachin: 132 runs, Rahul: 66 runs

3. (i) 6 (ii) 15 years (iii) 25 **4.** 30

Exercise 5.1

1. (i) 70° (ii) 27° (iii) 33°

2. (i) 75° (ii) 93° (iii) 26°

3. (i) supplementary (ii) complementary (iii) supplementary
(iv) supplementary (v) complementary (vi) complementary

4. 45° **5.** 90° **6.** $\angle 2$ will increase with the same measure as the decrease in $\angle 1$.

7. (i) No (ii) No (iii) Yes **8.** Less than 45°

9. (i) Yes (ii) No (iii) Yes (iv) Yes (v) Yes (vi) $\angle COB$

10. (i) $\angle 1, \angle 4$; $\angle 5, \angle 2 + \angle 3$ (ii) $\angle 1, \angle 5$; $\angle 4, \angle 5$

11. $\angle 1$ and $\angle 2$ are not adjacent angles because their vertex is not common.

12. (i) $x = 55°$, $y = 125°$, $z = 125°$ (ii) $x = 115°$, $y = 140°$, $z = 40°$

13. (i) 90° (ii) 180° (iii) supplementary (iv) linear pair (v) equal
(vi) obtuse angles

14. (i) $\angle AOD, \angle BOC$ (ii) $\angle EOA, \angle AOB$ (iii) $\angle EOB, \angle EOD$
(iv) $\angle EOA, \angle EOC$ (v) $\angle AOB, \angle AOE$; $\angle AOE, \angle EOD$; $\angle EOD, \angle COD$

Exercise 5.2

1. (i) Corresponding angle property (ii) Alternate interior angle property
(iii) Interior angles on the same side of the transversal are supplementary

2. (i) $\angle 1, \angle 5$; $\angle 2, \angle 6$; $\angle 3, \angle 7$; $\angle 4, \angle 8$ (ii) $\angle 2, \angle 8$; $\angle 3, \angle 5$
(iii) $\angle 2, \angle 5$; $\angle 3, \angle 8$ (iv) $\angle 1, \angle 3$; $\angle 2, \angle 4$; $\angle 5, \angle 7$; $\angle 6, \angle 8$

3. $a = 55°$; $b = 125°$; $c = 55°$; $d = 125°$; $e = 55°$; $f = 55°$

4. (i) $x = 70°$ (ii) $x = 100°$

5. (i) $\angle DGC = 70°$ (ii) $\angle DEF = 70°$

6. (i) l is not parallel to m (ii) l is not parallel to m
(iii) l is parallel to m (iv) l is not parallel to m

Exercise 6.1

1. Altitude, Median, No.

Exercise 6.2

1. (i) 120° (ii) 110° (iii) 70° (iv) 120° (v) 100° (vi) 90°

2. (i) 65° (ii) 30° (iii) 35° (iv) 60° (v) 50° (vi) 40°

Exercise 6.3

1. (i) 70° (ii) 60° (iii) 40° (iv) 65° (v) 60° (vi) 30°

2. (i) $x = 70°, y = 60°$ (ii) $x = 50°, y = 80°$ (iii) $x = 110°, y = 70°$
(iv) $x = 60°, y = 90°$ (v) $x = 45°, y = 90°$ (vi) $x = 60°, y = 60°$

Exercise 6.4

1. (i) Not possible (ii) Possible (iii) Not possible

2. (i) Yes (ii) Yes (iii) Yes **3.** Yes **4.** Yes **5.** Yes

6. Between 3 and 27

Exercise 6.5

1. 26 cm **2.** 24 cm **3.** 9 m **4.** (i) and (iii) **5.** 18m **6.** (ii)

7. 98 cm **8.** 68 cm

Exercise 7.1

1. (a) they have the same length (b) 70° (c) $m\angle A = m\angle B$

3. $\angle A \leftrightarrow \angle F, \angle B \leftrightarrow \angle E, \angle C \leftrightarrow \angle D$, $\overline{AB} \leftrightarrow \overline{FE}$, $\overline{BC} \leftrightarrow \overline{ED}$, $\overline{AC} \leftrightarrow \overline{FD}$

4. (i) $\angle C$ (ii) $\overline{CA}$ (iii) $\angle A$ (iv) $\overline{BA}$

Exercise 7.2

1. (a) SSS Congruence criterion (b) SAS Congruence criterion
(c) ASA Congruence criterion (d) RHS Congruence criterion

2. (a) (i) PE (ii) EN (iii) PN (b) (i) EN (ii) AT
(c) (i) $\angle RAT = \angle EPN$ (ii) $\angle ATR = \angle PNE$

3. (i) Given (ii) Given (iii) Common (iv) SAS Congruence criterion **4.** No

5. ΔWON **6.** ΔBTA, ΔTPQ **9.** BC = QR, ASA Congruence criterion

Exercise 8.1

1. (a) 10:1 (b) 500:7 (c) 100:3 (d) 20:1 **2.** 12 computers

3. (i) Rajasthan : 190 people ; UP : 830 people (ii) Rajasthan

Exercise 8.2

1. (a) 12.5% (b) 125% (c) 7.5% (d) $28\frac{4}{7}\%$

2. (a) 65% (b) 210% (c) 2% (d) 1235%

3. (i) $\frac{1}{4}$, 25% (ii) $\frac{3}{5}$; 60% (iii) $\frac{3}{8}$; 37.5%

4. (a) 37.5 (b) $\frac{3}{5}$ minute or 36 seconds (c) ₹ 500
(d) 0.75 kg or 750 g

5. (a) 12000 (b) ₹ 9,000 (c) 1250 km (d) 20 minutes (e) 500 litres

6. (a) 0.25; $\frac{1}{4}$ (b) 1.5; $\frac{3}{2}$ (c) 0.2; $\frac{1}{5}$ (d) 0.05; $\frac{1}{20}$ **7.** 30%

8. 40%; 6000 **9.** ₹ 40,000 **10.** 5 matches

Exercise 8.3

1. (a) Profit = ₹ 75; Profit % = 30 (b) Profit = ₹ 1500; Profit % = 12.5
(c) Profit = ₹ 500; Profit % = 20 (d) Loss = ₹ 100; Loss % = 40

2. (a) 75%; 25% (b) 20%, 30%, 50% (c) 20%; 80% (d) 12.5%; 25%; 62.5%

3. 2% **4.** $5\frac{5}{7}\%$ **5.** ₹ 12,000 **6.** ₹ 16,875

7. (i) 12% (ii) 25 g **8.** ₹ 233.75 **9.** (a) ₹ 1,632 (b) ₹ 8,625

10. 0.25% **11.** ₹ 500

EXERCISE 9.1

1. (i) $\frac{-2}{3}, \frac{-1}{2}, \frac{-2}{5}, \frac{-1}{3}, \frac{-2}{7}$ (ii) $\frac{-3}{2}, \frac{-5}{3}, \frac{-8}{5}, \frac{-10}{7}, \frac{-9}{5}$

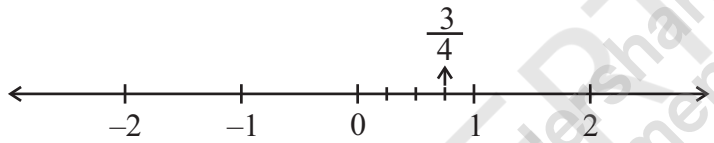
(iii) $\frac{-35}{45} = \frac{-7}{9}, \frac{-34}{45}, \frac{-33}{45} = \frac{-11}{15}, \frac{-32}{45}, \frac{-31}{45}$ (iv) $\frac{-1}{3}, \frac{-1}{4}, 0, \frac{1}{3}, \frac{1}{2}$

2. (i) $\frac{-15}{25}, \frac{-18}{30}, \frac{-21}{35}, \frac{-24}{40}$ (ii) $\frac{-4}{16}, \frac{-5}{20}, \frac{-6}{24}, \frac{-7}{28}$

(iii) $\frac{5}{-30}, \frac{6}{-36}, \frac{7}{-42}, \frac{8}{-48}$ (iv) $\frac{8}{-12}, \frac{10}{-15}, \frac{12}{-18}, \frac{14}{-21}$

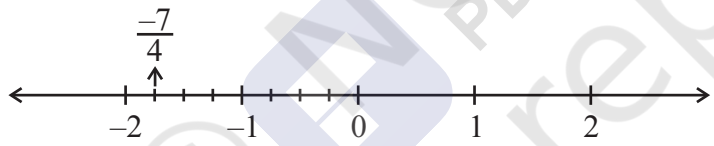
3. (i) $\frac{-4}{14}, \frac{-6}{21}, \frac{-8}{28}, \frac{-10}{35}$ (ii) $\frac{10}{-6}, \frac{15}{-9}, \frac{20}{-12}, \frac{25}{-15}$ (iii) $\frac{8}{18}, \frac{12}{27}, \frac{16}{36}, \frac{28}{63}$

4. (i)

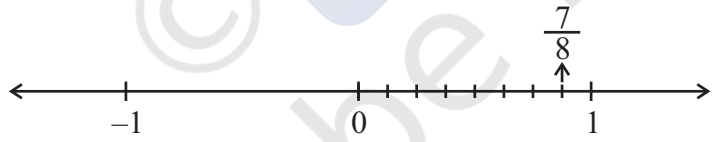


(ii)

(iii)



(iv)



5. P represents $\frac{7}{3}$ Q represents $\frac{8}{3}$ R represents $\frac{-4}{3}$ S represents $\frac{-5}{3}$

6. (ii), (iii), (iv), (v)

7. (i) $\frac{-4}{3}$ (ii) $\frac{5}{9}$ (iii) $\frac{-11}{18}$ (iv) $\frac{-4}{5}$

8. (i) < (ii) < (iii) = (iv) > (v) < (vi) = (vii) >

9. (i) $\frac{5}{2}$ (ii) $\frac{-5}{6}$ (iii) $\frac{2}{-3}$ (iv) $\frac{1}{4}$ (v) $-3\frac{2}{7}$

10. (i) $\frac{-3}{5}, \frac{-2}{5}, \frac{-1}{5}$ (ii) $\frac{-4}{3}, \frac{-1}{3}, \frac{-2}{9}$ (iii) $\frac{-3}{2}, \frac{-3}{4}, \frac{-3}{7}$

Exercise 9.2

1. (i) $\frac{-3}{2}$ (ii) $\frac{34}{15}$ (iii) $\frac{17}{30}$ (iv) $\frac{82}{99}$

(v) $\frac{-26}{57}$ (vi) $\frac{-2}{3}$ (vii) $\frac{34}{15}$

2. (i) $\frac{-13}{72}$ (ii) $\frac{23}{63}$ (iii) $\frac{1}{195}$ (iv) $\frac{-89}{88}$ (v) $\frac{-73}{9}$

3. (i) $\frac{-63}{8}$ (ii) $\frac{-27}{10}$ (iii) $\frac{-54}{55}$ (iv) $\frac{-6}{35}$ (v) $\frac{6}{55}$

(vi) 1

4. (i) – 6 (ii) $\frac{-3}{10}$ (iii) $\frac{4}{15}$ (iv) $\frac{-1}{6}$ (v) $\frac{-14}{13}$

(vi) $\frac{91}{24}$ (vii) $\frac{-15}{4}$

Exercise 11.1

1. (i) 150000 m^2 (ii) ₹ 1,500,000,000

2. 6400 m^2 **3.** 20 m **4.** 15 cm; 525 cm^2 **5.** 40 m

6. 31cm; Square **7.** 35cm; 1050 cm^2 **8.** ₹ 284

Exercise 11.2

1. (a) 28 cm^2 (b) 15 cm^2 (c) 8.75 cm^2 (d) 24 cm^2 (e) 8.8 cm^2

2. (a) 6 cm^2 (b) 8 cm^2 (c) 6 cm^2 (d) 3 cm^2

3. (a) 12.3 cm (b) 10.3 cm (c) 5.8 cm (d) 1.05 cm

4. (a) 11.6 cm (b) 80 cm (c) 15.5 cm

5. (a 91.2 cm^2 (b) 11.4 cm

6. length of BM = 30cm; length of DL = 42 cm

7. Area of ΔABC = 30 cm^2; length of AD = $\frac{60}{13}$ cm

8. Area of ΔABC = 27 cm^2; length of CE = 7.2 cm

Exercise 11.3

1. (a) 88 cm (b) 176 mm (c) 132 cm

2. (a) 616 mm^2 (b) 1886.5 m^2 (c) $\frac{550}{7}$ cm^2

3. 24.5 m; 1886.5 m^2 **4.** 132 m; ₹ 528 **5.** 21.98 cm^2

6. 4.71 m; ₹ 70.65 **7.** 25.7 cm **8.** ₹ 30.14 (approx.) **9.** 7 cm; 154 cm^2; 11cm; circle.

10. 536 cm^2 **11.** 23.44 cm^2 **12.** 5 cm; 78.5 cm^2 **13.** 879.20 m^2

14. Yes **15.** 119.32 m; 56.52m **16.** 200 Times **17.** 94.2 cm

Exercise 11.4

1. 1750 m^2; 0.675 ha **2.** 1176 m^2 **3.** 30 cm^2

4. (i) 63 m^2 (ii) ₹ 12,600 **5.** (i) 116 m^2 (ii) ₹ 31,360

6. 0.99 ha; 20.01 ha **7.** (i) 441 m^2 (ii) ₹ 48,510 **8.** Yes, 9.12 cm cord is left

9. (i) 50m^2 (ii) 12.56 m^2 (iii) 37.44m^2 (iv) 12.56m

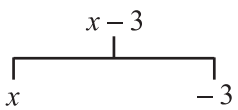
10. (i) 110 cm^2 (ii) 150 cm^2; **11.** 66 cm^2

Exercise 12.1

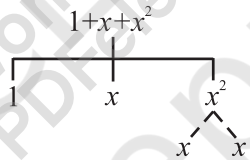
1. (i) $y - z$ (ii) $\frac{1}{2}(x + y)$ (iii) z^2 (iv) $\frac{1}{4}pq$ (v) $x^2 + y^2$ (vi) $5 + 3mn$

(vii) $10 - yz$ (viii) $ab - (a + b)$

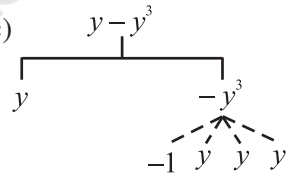
2. (i) (a)



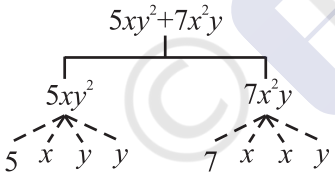
(b)



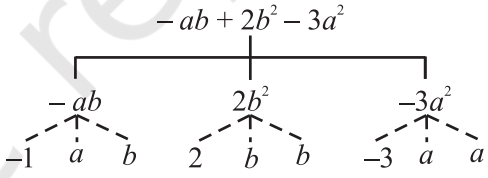
(c)



(d)



(e)



(ii)

	Expression	Terms	Factors
(a)	$-4x + 5$	$-4x$ 5	$-4, x$ 5
(b)	$-4x + 5y$	$-4x$ $5y$	$-4, x$ $5, y$
(c)	$5y + 3y^2$	$5y$ $3y^2$	$5, y$ $3, y, y$
(d)	$xy + 2x^2y^2$	xy $2x^2y^2$	x, y $2, x, x, y, y$
(e)	$pq + q$	pq q	p, q q

(f)	$1.2ab-2.4b+3.6a$	$1.2ab$ $-2.4b$ $3.6a$	$1.2, a, b$ $-2.4, b$ $3.6, a$
(g)	$\frac{3}{4}x+\frac{1}{4}$	$\frac{3}{4}x$ $\frac{1}{4}$	$\frac{3}{4}, x$ $\frac{1}{4}$
(h)	$0.1p^2 + 0.2q^2$	$0.1p^2$ $0.2q^2$	$0.1, p, p$ $0.2, q, q$

3.

	Expression	Terms	Coefficients
(i)	$5 - 3t^2$	$-3t^2$	-3
(ii)	$1 + t + t^2 + t^3$	t t^2 t^3	1 1 1
(iii)	$x + 2xy + 3y$	x $2xy$ $3y$	1 2 3
(iv)	$100m + 1000n$	$100m$ $1000n$	100 1000
(v)	$-p^2q^2 + 7pq$	$-p^2q^2$ $7pq$	-1 7
(vi)	$1.2a + 0.8b$	$1.2a$ $0.8b$	1.2 0.8
(vii)	$3.14r^2$	$3.14r^2$	3.14
(viii)	$2(l + b)$	$2l$ $2b$	2 2
(ix)	$0.1y + 0.01y^2$	$0.1y$ $0.01y^2$	0.1 0.01

4. (a)

	Expression	Terms with x	Coefficient of x
(i)	$y^2x + y$	y^2x	y^2
(ii)	$13y^2-8yx$	$-8yx$	$-8y$
(iii)	$x + y + 2$	x	1
(iv)	$5 + z + zx$	zx	z

(v)	$1 + x + xy$	x xy	1 y
(vi)	$12xy^2 + 25$	$12xy^2$	$12y^2$
(vii)	$7 + xy^2$	xy^2	y^2

(b)

	Expression	Terms with y^2	Coefficient of y^2
(i)	$8 - xy^2$	$- xy^2$	$- x$
(ii)	$5y^2 + 7x$	$5y^2$	5
(iii)	$2x^2y - 15xy^2 + 7y^2$	$-15xy^2$ $7y^2$	$-15x$ 7

5. (i) binomial (ii) monomial (iii) trinomial (iv) monomial
(v) trinomial (vi) binomial (vii) binomial (viii) monomial
(ix) trinomial (x) binomial (xi) binomial (xii) trinomial

6. (i) like (ii) like (iii) unlike (iv) like
(v) unlike (vi) unlike

7. (a) $-xy^2, 2xy^2; -4yx^2, 20x^2y; 8x^2, -11x^2, -6x^2; 7y, y; -100x, 3x; -11yx, 2xy.$

(b) $10pq, -7qp, 78qp; 7p, 2405p; 8q, -100q; -p^2q^2, 12q^2p^2; -23, 41; -5p^2, 701p^2; 13p^2q, qp^2$

Exercise 12.2

1. (i) $8b - 32$ (ii) $7z^3 + 12z^2 - 20z$ (iii) $p - q$ (iv) $a + ab$
(v) $8x^2y + 8xy^2 - 4x^2 - 7y^2$ (vi) $4y^2 - 3y$

2. (i) $2mn$ (ii) $-5tz$ (iii) $12mn - 4$ (iv) $a + b + 3$
(v) $7x + 5$ (vi) $3m - 4n - 3mn - 3$ (vii) $9x^2y - 8xy^2$
(viii) $5pq + 20$ (ix) 0 (x) $-x^2 - y^2 - 1$

3. (i) $6y^2$ (ii) $-18xy$ (iii) $2b$ (iv) $5a + 5b - 2ab$
(v) $5m^2 - 8mn + 8$ (vi) $x^2 - 5x - 5$
(vii) $10ab - 7a^2 - 7b^2$ (viii) $8p^2 + 8q^2 - 5pq$

4. (a) $x^2 + 2xy - y^2$ (b) $5a + b - 6$

5. $4x^2 - 3y^2 - xy$

6. (a) $-y + 11$ (b) $2x + 4$

Exercise 12.3

1. (i) 0 (ii) 1 (iii) –1 (iv) 1 (v) 1

2. (i) –1 (ii) –13 (iii) 3 **3.** (i) –9 (ii) 3 (iii) 0 (iv) 1

4. (i) 8 (ii) 4 (iii) 0 **5.** (i) –2 (ii) 2 (iii) 0 (iv) 2

6. (i) $5x - 13$; –3 (ii) $8x - 1$; 15 (iii) $11x - 10$; 12 (iv) $11x + 7$; 29

7. (i) $2x+4$; 10 (ii) $-4x + 6$; –6 (iii) $-5a + 6$;11 (iv) $-8b + 6$; 22 (v) $3a - 2b - 9$; – 8

8. (i) 1000 (ii) 20 **9.** –5 **10.** $2a^2 + ab + 3$; 38

Exercise 12.4

1.

Symbol	Number of Digits	Number of Segments
6	5	26
	10	51
	100	501
4	5	16
	10	31
	100	301
8	5	27
	10	52
	100	502

2. (i) $2n - 1 \rightarrow$ 100^{th} : 199

(ii) $3n + 2 \rightarrow$ 5^{th} : 17; 10^{th} : 32; 100^{th} : 302

(iii) $4n + 1 \rightarrow$ 5^{th} : 21; 10^{th} : 41; 100^{th} : 401

(iv) $7n + 20 \rightarrow$ 5^{th} : 55; 10^{th} : 90; 100^{th} : 720

(v) $n^2 + 1 \rightarrow$ 5^{th} : 26; 10^{th} : 101

Exercise 13.1

1. (i) 64 (ii) 729 (iii) 121 (iv) 625

2. (i) 6^4 (ii) t^2 (iii) b^4 (iv) $5^2 \times 7^3$ (v) $2^2 \times a^2$ (vi) $a^3 \times c^4 \times d$

3. (i) 2^9 (ii) 7^3 (iii) 3^6 (iv) 5^5

4. (i) 3^4 (ii) 3^5 (iii) 2^8 (iv) 2^{100} (v) 2^{10}

5. (i) $2^3 \times 3^4$ (ii) 5×3^4 (iii) $2^2 \times 3^3 \times 5$ (iv) $2^4 \times 3^2 \times 5^2$

6. (i) 2000 (ii) 196 (iii) 40 (iv) 768 (v) 0

(vi) 675 (vii) 144 (viii) 90000

7. (i) – 64 (ii) 24 (iii) 225 (iv) 8000

8. (i) $2.7 \times 10^{12} > 1.5 \times 10^8$ (ii) $4 \times 10^{14} < 3 \times 10^{17}$

Exercise 13.2

1. (i) 3^{14} (ii) 6^5 (iii) a^5 (iv) 7^{x+2} (v) 5^3 (vi) $(10)^5$

(vii) $(ab)^4$ (viii) 3^{12} (ix) 2^8 (x) 8^{t-2}

2. (i) 3^3 (ii) 5^3 (iii) 5^5 (iv) 7×11^5 (v) 3^0 or 1 (vi) 3

(vii) 1 (viii) 2 (ix) $(2a)^2$ (x) a^{10} (xi) a^3b (xii) 2^8

3. (i) False; $10 \times 10^{11} = 10^{12}$ and $(100)^{11} = 10^{22}$ (ii) False; $2^3 = 8$, $5^2 = 25$
(iii) False; $6^5 = 2^5 \times 3^5$ (iv) True; $3^0 = 1$, $(1000)^0 = 1$

4. (i) $2^8 \times 3^4$ (ii) $2 \times 3^3 \times 5$ (iii) $3^6 \times 2^6$ (iv) $2^8 \times 3$ **5.** (i) 98 (ii) $\frac{5t^4}{8}$ (iii) 1

Exercise 13.3

1. $279404 = 2 \times 10^5 + 7 \times 10^4 + 9 \times 10^3 + 4 \times 10^2 + 0 \times 10^1 + 4 \times 10^0$
$3006194 = 3 \times 10^6 + 0 \times 10^5 + 0 \times 10^4 + 6 \times 10^3 + 1 \times 10^2 + 9 \times 10^1 + 4 \times 10^0$
$2806196 = 2 \times 10^6 + 8 \times 10^5 + 0 \times 10^4 + 6 \times 10^3 + 1 \times 10^2 + 9 \times 10^1 + 6 \times 10^0$
$120719 = 1 \times 10^5 + 2 \times 10^4 + 0 \times 10^3 + 7 \times 10^2 + 1 \times 10^1 + 9 \times 10^0$
$20068 = 2 \times 10^4 + 0 \times 10^3 + 0 \times 10^2 + 6 \times 10^1 + 8 \times 10^0$

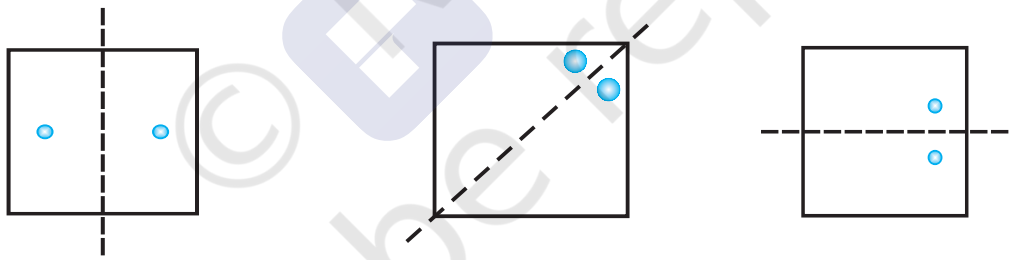
2. (a) 86045 (b) 405302 (c) 30705 (d) 900230

3. (i) 5×10^7 (ii) 7×10^6 (iii) 3.1865×10^9 (iv) 3.90878×10^5
(v) 3.90878×10^4 (vi) 3.90878×10^3

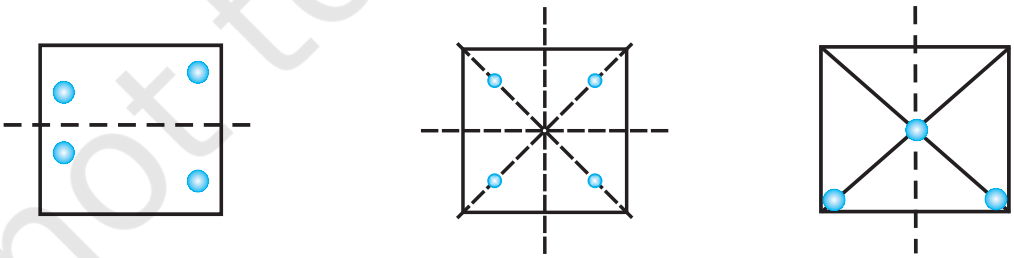
4. (a) 3.84×10^8m (b) 3×10^8 m/s (c) 1.2756×10^7m (d) 1.4×10^9 m
(e) 1×10^{11} (f) 1.2×10^{10} years (g) 3×10^{20} m (h) 6.023×10^{22}
(i) 1.353×10^9 km^3 (j) 1.027×10^9

Exercise 14.1

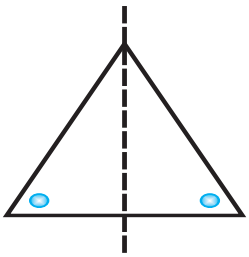
1.



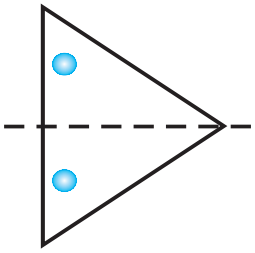
(a) (b) (c)



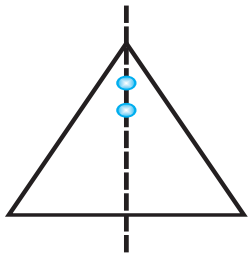
(d) (e) (f)



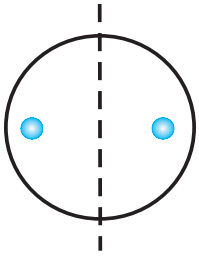
(g)



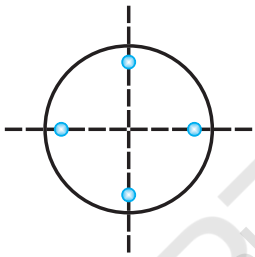
(h)



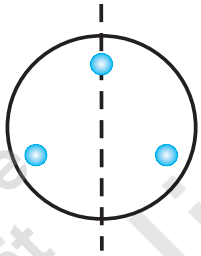
(i)



(j)

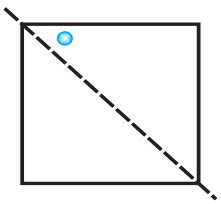


(k)

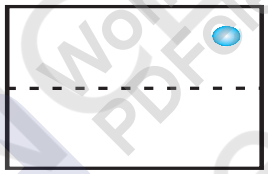


(l)

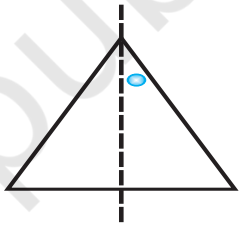
2.



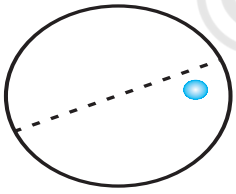
(a)



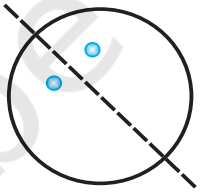
(b)



(c)

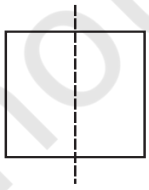


(d)

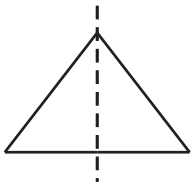


(e)

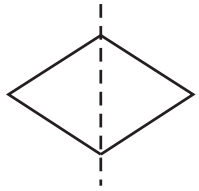
3.



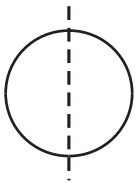
(a) Square



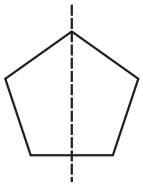
(b) Triangle



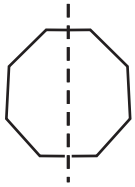
(c) Rhombus



(d) Circle

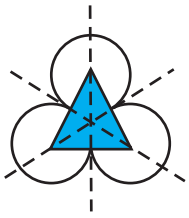


(e) Pentagon

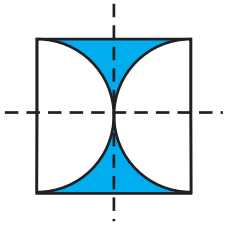


(f) Octagon

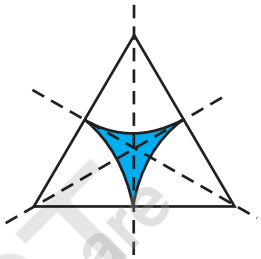
4.



(a)

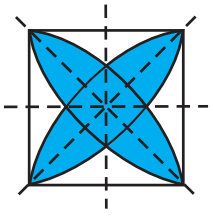


(b)

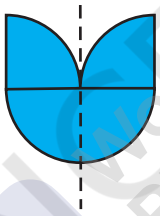


(c)

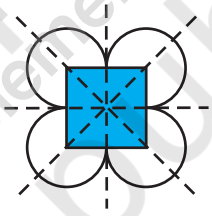
(d)



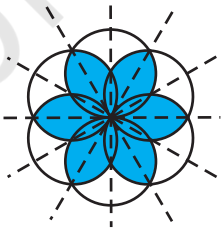
(e)



(f)



(g)



(h)

7. (a) 3 (b) 1 (c) 0 (d) 4 (e) 2 (f) 2
(g) 0 (h) 0 (i) 6 (j) Infinitely many

8. (a) A, H, I, M, O, T, U, V, W, X, Y (b) B, C, D, E, H, I, O, X
(c) O, X, I, H

10. (a) Median (b) Diameter

Exercise 14.2

1. (a), (b), (d), (e), (f)

2. (a) 2 (b) 2 (c) 3 (d) 4 (e) 4 (f) 5
(g) 6 (h) 3

Exercise 14.3

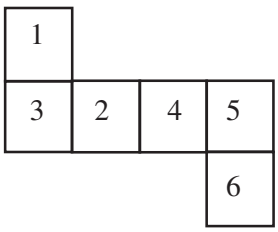
3. Yes **5.** Square **6.** 120°, 180°, 240°, 300°, 360°

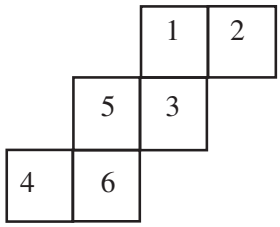
7. (i) Yes (ii) No

Exercise 15.1

1. Nets in (ii), (iii), (iv), (vi) form cubes.

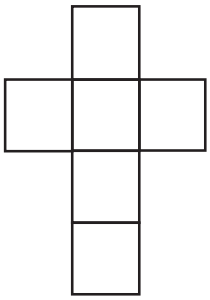
2.

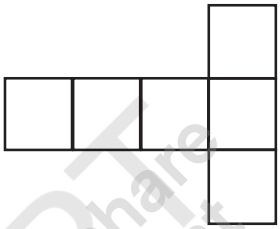




3. No, because one pair of opposite faces will have 1 and 4 on them whose total is not 7, and another pair of opposite faces will have 3 and 6 on them whose total is also not 7.

4. Three faces





5. (a) (ii) (b) (iii) (c) (iv) (d) (i)

BRAIN-TEASERS

1. Solve the number riddles:

(i) Tell me who I am! Who I am!
Take away from me the number eight,
Divide further by a dozen to come up with
A full team for a game of cricket!

(ii) Add four to six times a number,
To get exactly sixty four!
Perfect credit is yours to ask for
If you instantly tell the score!

2. Solve the teasers:

(i) There was in the forest an old Peepal tree
The grand tree had branches ten and three
On each branch there lived birds fourteen
Sparrows brown, crows black and parrots green!
Twice as many as the parrots were the crows
And twice as many as the crows were the sparrows!
We wonder how many birds of each kind
Aren't you going to help us find?

(ii) I have some five-rupee coins and some two-rupee coins. The number of two-rupee coins is twice the number of five-rupee coins. The total money I have is 108 rupees. So how many five-rupee coins do I have? And how many two-rupee coins?

3. I have 2 vats each containing 2 mats. 2 cats sat on each of the mats. Each cat wore 2 funny old hats. On each hat lay 2 thin rats. On each rat perched 2 black bats. How many things are in my vats?

4. Twenty-seven small cubes are glued together to make a big cube. The exterior of the big cube is painted yellow in colour. How many among each of the 27 small cubes would have been painted yellow on

(i) only one of its faces?

(ii) two of its faces?

(iii) three of its faces?

5. Rahul wanted to find the height of a tree in his garden. He checked the ratio of his height to his shadow's length. It was 4:1. He then measured the shadow of the tree. It was 15 feet. So what was the height of the tree?

6. A woodcutter took 12 minutes to make 3 pieces of a block of wood. How much time would be needed to make 5 such pieces?

7. A cloth shrinks 0.5% when washed. What fraction is this?

8. Smita's mother is 34 years old. Two years from now mother's age will be 4 times Smita's present age. What is Smita's present age?

9. Maya, Madhura and Mohsina are friends studying in the same class. In a class test in geography, Maya got 16 out of 25. Madhura got 20. Their average score was 19. How much did Mohsina score?

Answers

1. (i) 140 (ii) 10

2. (i) Sparrows: 104, crows: 52, Parrots: 26

(ii) Number of ₹ 5 coins = 12, Number of ₹ 2 coins = 24

3. 124 **4.** (i) 6 (ii) 10 (iii) 8 **5.** 60 feet

6. 24 minutes **7.** $\frac{1}{200}$ **8.** 7 years **9.** 21