# **Chapter 4. Quadratic Equation**

# Question-1

Check whether the following equation is quadratic or not:  $x^2$  - 6x - 4 = 0.

# Solution:

The degree of the equation is 2

 $x^2$ -6x - 4 = 0 is quadratic equation.

# **Question-2**

Check whether the following equation is quadratic or not:  $3x^2 - 7x - 2 = 0$ .

### Solution:

The degree of the equation is 2

 $\therefore$  3x<sup>2</sup> - 7x - 2 = 0 is quadratic equation.

# Question-3

Check whether the following equation is quadratic or  $not:x^3 - 6x^2 + 2x - 1 = 0$ .

### Solution:

The degree of the equation is 3

 $x^3 - 6x^2 + 2x - 1 = 0$  is not a quadratic equation.

### Question-4

Check whether the following equation is quadratic or not:  $7x = 2x^2$ .

#### Solution:

The degree of the equation  $2x^2 - 7x = 0$  is 2

 $\div$  7x = 2x<sup>2</sup> is a quadratic equation.

### **Question-5**

Check whether the following equation is quadratic or not:  $x^2 + \frac{1}{x^2} = 2(x \neq 0)$ .

# Solution:

The given equation also written as

$$x^4 - 2x^2 + 1 = 0$$

⇒The degree of the equation is 4

∴  $x^2 + \frac{1}{x^2} = 2(x \neq 0)$  is not a quadratic equation.

Check whether the following equation is quadratic or not:  $3x^2 - 4 = 0$ .

# Solution:

The degree of the given equation is 2  $\therefore 3x^2 - 4 = 0$  is a quadratic equation.

### Question-7

Check whether the following equation is quadratic or not: (x + 1)(x + 3) = 0.

### Solution:

The degree of the given equation is 2  $\therefore$  (x + 1)(x + 3) = 0 is a quadratic equation.

# **Question-8**

Check whether the following equation is quadratic or not: (2x + 1)(3x + 2) = 6(x - 1)(x - 2).

# Solution:

By solving the given equation (2x + 1)(3x + 2) = 6(x - 1)(x - 2) we get,  $6x^2 + 7x + 2 = 6x^2 - 18x + 12$ 25x - 10 = 0

The degree of the given equation is 1  $\therefore (2x + 1)(3x + 2) = 6(x - 1)(x - 2)$  is not a quadratic equation.

#### Question-9

Check whether the following equation is quadratic or not:  $x + \frac{1}{2} = x^2(x \neq 0)$ .

### Solution:

$$x + \frac{1}{x} = x^2 \Rightarrow x^2 + 1 = x^4$$

The degree of the given equation is 4.

 $\therefore x + \frac{1}{x} = x^2 (x \neq 0)$  is not a quadratic equation.

# Question-10

Check whether the following equation is quadratic or not:  $16x^2 - 3 = (2x + 5)(5x - 3)$ .

# Solution:

By solving the given equation we get,

$$6x^2 - 19x + 12 = 0$$

 $\therefore 16x^2 - 3 = (2x + 5)(5x - 3)$  is a quadratic equation.

Determine whether the given value of x is a solution of the given equation or not:  $3x^2 - 2x - 1 = 0$ ; x = 1.

### Solution:

$$3x^2 - 2x - 1 = 0$$

Let 
$$x = 1$$
,  $3(1)^2 - 2(1) - 1 = 3 - 2 - 1 = 0$ .

Therefore the given value of x is a solution of the given equation.

# Question-12

Determine whether the given value of x is a solution of the given equation or not:  $2x^2 - 6x + 3 = 0$ ;  $x = \frac{1}{2}$ .

# Solution:

$$2x^2 - 6x + 3 = 0$$

Let, 
$$x = \frac{1}{2} \Rightarrow 2(\frac{1}{2})^2 - 6(\frac{1}{2}) + 3 = \frac{1}{2} - 3 + 3 = \frac{1}{2}$$
.

Therefore the given value of x is not a solution of the given equation.

#### Question-13

Determine whether the given value of x is a solution of the given equation or not: (2x + 3)(3x - 2) = 0;  $x = \frac{2}{3}$ .

### Solution:

$$(2x + 3)(3x - 2) = 0;$$

Let 
$$x = \frac{2}{3} \Rightarrow (2 \times \frac{2}{3} + 3)(3 \times \frac{2}{3} - 2) = (\frac{4}{3} + 3)(2 - 2)$$
  
=  $(\frac{4}{3} + 3) = 0$ .

Therefore the given value of x is a solution of the given equation.

### Question-14

Determine whether the given value of x is a solution of the given equation or not:  $x^2 + x + 1 = 0$ ; x = -1.

# Solution:

$$x^2 + x + 1 = 0$$

Let 
$$x = -1 \Rightarrow (-1)^2 + (-1) + 1 = 1 - 1 + 1 = 1$$
.

Therefore the given value of x is not a solution of the given equation.

# Question-15

Determine whether the given values of x are solutions of the given equation or not:

$$x^2 + 6x + 5 = 0$$
;  $x = -1$ ,  $x = -5$ .

#### Solution:

$$x^2 + 6x + 5 = 0$$

Put 
$$x = -1$$

$$\Rightarrow$$
  $(-1)^2 + 6(-1) + 5 = 1 - 6 + 5 = 0$ 

Put 
$$x = -5$$

$$\Rightarrow$$
(-5)<sup>2</sup> + 6(-5) + 5 = 25 - 30 + 5 = 0

Therefore the given value of x is a solution of the given equation.

Determine whether the given values of x are solutions of the given equation or not:  $9x^2 - 3x - 2 = 0$ ;  $x = -\frac{1}{2}$ ,  $x = \frac{2}{3}$ .

#### Solution:

$$9x^{2} - 3x - 2 = 0$$
Put  $x = -\frac{1}{3}$ 

$$9(-\frac{1}{3})^{2} - 3(-\frac{1}{3}) - 2 = 1 + 1 - 2 = 0$$
Put  $x = \frac{2}{3}$ 

$$9x^{2} - 3x - 2 = 9(\frac{2}{3})^{2} - 3(\frac{2}{3}) - 2 = 4 - 2 - 2 = 0$$

Therefore the given value of x is a solution of the given equation.

#### Question-17

Determine whether the given values of x are solutions of the given equation or not:

$$(x + 4)(x - 5) = 0; x = -4, x = 5.$$

#### Solution:

Put 
$$x = -4$$
  
 $(x + 4)(x - 5) = (-4 + 4)(-4 - 5) = 0(-9) = 0$   
Put  $x = 5$   
 $(x + 4)(x - 5) = (5 + 4)(5 - 5) = 9(0) = 0$ 

Therefore the given value of x is a solution of the given equation.

# Question-18

Determine whether the given values of x are solutions of the given equation or not:

$$(3x + 8)(2x + 5) = 0$$
;  $x = 2\frac{2}{3}$ ,  $x = 2\frac{1}{2}$ .

### Solution:

Put 
$$x = 2\frac{2}{3} = \frac{8}{3}$$
  
 $(3x + 8)(2x + 5) = (3 \times \frac{8}{3} + 8)(2 \times \frac{8}{3} + 5) = (8 + 8)(\frac{16}{3} + 5) = 16 \times \frac{31}{3} = \frac{496}{3} \neq 0$   
Put  $x = 2\frac{1}{2} = \frac{5}{2}$   
 $(3x + 8)(2x + 5) = (3 \times \frac{5}{2} + 8)(2 \times \frac{5}{2} + 5) = (\frac{15}{2} + 8)(5 + 5) = \frac{31}{2} \times 10 = 155 \neq 0$ 

Therefore the given value of x is not the solution of the given equation.

# Question-19

Using factorization, find the roots of the quadratic equation:  $9x^2 - 16 = 0$ .

$$9x^{2}-16=0$$

$$(3x)^{2}-4^{2}=0$$

$$(3x-4)(3x+4)=0$$

$$x = 4/3, -4/3.$$

Using factorization, find the roots of the quadratic equation:  $64x^2 - 9 = 0$ .

# Solution:

$$64x^{2} - 9 = 0$$

$$(8x)^{2} - 3^{2} = 0$$

$$(8x - 3)(8x + 3) = 0$$

$$x = 3/8, -3/8.$$

# Question-21

Using factorization, find the roots of the quadratic equation:  $(x - 2)^2 - 25 = 0$ .

### Solution:

$$(x-2)^2 - 25 = 0$$

$$(x-2)^2 - 5^2 = 0$$

$$(x-2-5)(x-2+5) = 0$$

$$(x-7)(x+3) = 0$$

$$x = 7, -3.$$

# **Question-22**

Using factorization, find the roots of the quadratic equation:  $(x + 5)^2 - 36 = 0$ .

#### Solution:

$$(x + 5)^{2} - 36 = 0$$

$$(x + 5)^{2} - 6^{2} = 0$$

$$(x + 5 - 6)(x + 5 + 6) = 0$$

$$(x - 1)(x + 11) = 0$$

$$x = 1, -11$$

# Question-23

Using factorization, find the roots of the quadratic equation:  $(2x + 3)^2 = 81$ .

#### Solution:

$$(2x + 3)^2 = 81$$
  
 $(2x + 3)^2 - 9^2 = 0$   
 $(2x + 3 - 9)(2x + 3 + 9) = 0$   
 $(2x - 6)(2x + 12) = 0$   
 $x = 3, -6$ 

#### Question-24

Using factorization, find the roots of the quadratic equation:  $y^2-3=0$  [Hint:  $3=(\sqrt{3})^2$ ].

$$y^{2} - 3 = 0$$
  
 $y^{2} - (\sqrt{3})^{2} = 0$   
 $(y - \sqrt{3})(y + \sqrt{3}) = 0$   
 $y = \sqrt{3}, -\sqrt{3}$ .

Using factorization, find the roots of the quadratic equation:  $a^2z^2-b^2=0$ .

### Solution:

$$a^{2}z^{2} - b^{2} = 0$$
  
 $(az)^{2} - b^{2} = 0$   
 $(az - b)(az + b) = 0$   
 $z = b/a$ , - b/a.

### Question-26

Using factorization, find the roots of the quadratic equation:  $3z-z^2 = 0$ .

#### Solution:

$$3z - z^2 = 0$$
  
 $z(3 - z) = 0$   
 $z = 0$  or  $(3 - z) = 0$   
 $z = 0$ ,  $z = 3$ .

# **Question-27**

Using factorization, find the roots of the quadratic equation:  $5z^2-30 = 0$ .

#### Solution:

$$5z^{2} - 30 = 0$$

$$5(z^{2} - 6) = 0$$

$$z^{2} - (\sqrt{\epsilon})^{2} = 0$$

$$(z - \sqrt{\epsilon})(z + \sqrt{\epsilon}) = 0$$

$$z = \sqrt{\epsilon}, -\sqrt{\epsilon}.$$

# **Question-28**

Using factorization, find the roots of the quadratic equation:  $ax^2-2abx = 0$ .

### Solution:

$$ax^{2} - 2abx = 0$$
  
 $ax(x - 2b) = 0$   
 $ax = 0$  or  $(x - 2b) = 0$   
 $x = 0$  or  $x = 2b$ .

#### Question-29

Using factorization, find the roots of the quadratic equation:  $4y^2+4y+1=0$ .

$$4y^{2} + 4y + 1 = 0$$

$$4y^{2} + 2y + 2y + 1 = 0$$

$$2y(2y + 1) + (2y + 1) = 0$$

$$(2y + 1)(2y + 1) = 0$$

$$(2y + 1) = 0 \text{ or } (2y + 1) = 0$$

$$y = -1/2 \text{ or } y = -1/2.$$

Using factorization, find the roots of the quadratic equation:  $y^2$ -8y+16 = 0.

#### Solution:

$$y^{2} - 8y + 16 = 0$$
  
 $y^{2} - 4y - 4y + 16 = 0$   
 $y(y - 4) - 4(y - 4) = 0$   
 $(y - 4)(y - 4) = 0$   
 $y = 4$  or  $y = 4$ .

# Question-31

Using factorization, find the roots of the quadratic equation:  $z^2-z+\frac{1}{4}=0$ .

### Solution:

$$Z^{2} - Z + \frac{1}{4} = 0$$

$$Z^{2} - \frac{1}{2}Z - \frac{1}{2}Z + \frac{1}{4} = 0$$

$$Z(Z - \frac{1}{2}) - \frac{1}{2}(Z - \frac{1}{2}) = 0$$

$$(Z - \frac{1}{2})(Z - \frac{1}{2}) = 0$$

$$Z = \frac{1}{2} \text{ or } Z = \frac{1}{2}.$$

# Question-32

Using factorization, find the roots of the quadratic equation:  $\frac{1}{9}x^2 - \frac{2}{3}x + 1 = 0$ .

#### Solution:

$$\frac{1}{9}x^{2} - \frac{2}{3}x + 1 = 0$$

$$\frac{1}{9}x^{2} - \frac{1}{3}x - \frac{1}{3}x + 1 = 0$$

$$\frac{1}{3}x(\frac{1}{3}x - 1) - (\frac{1}{3}x - 1) = 0$$

$$(\frac{1}{3}x - 1)(\frac{1}{3}x - 1) = 0$$

$$x = 3 \text{ or } x = 3.$$

# **Question-33**

Using factorization, find the roots of the quadratic equation:  $y^2+2\sqrt{3}y+3=0$ .

# Solution:

$$y^{2} + 2\sqrt{3}y + 3 = 0$$

$$y^{2} + \sqrt{3}y + \sqrt{3}y + 3 = 0$$

$$y(y + \sqrt{3}) + \sqrt{3}(y + \sqrt{3}) = 0$$

$$(y + \sqrt{3})(y + \sqrt{3}) = 0$$

$$y = -\sqrt{3} \text{ or } y = -\sqrt{3}.$$

### Question-34

Using factorization, find the roots of the quadratic equation:  $x^2-4qx+4q^2=0$ .

$$x^{2} - 4qx + 4q^{2} = 0$$
  
 $x^{2} - 2qx - 2qx + 4q^{2} = 0$   
 $x(x - 2q) - 2q(x - 2q) = 0$   
 $(x - 2q)(x - 2q) = 0$   
 $x = 2q$  or  $x = 2q$ .

Using factorization, find the roots of the quadratic equation:  $z^2$ -2z-8 = 0.

#### Solution:

$$z^{2}-2z-8=0$$
  
 $z^{2}-4z+2z-8=0$   
 $z(z-4)+2(z-4)=0$   
 $(z-4)(z+2)=0$   
 $z=4$  or  $z=-2$ .

#### Question-36

Using factorization, find the roots of the quadratic equation:  $6z^2$ -5z-21 = 0.

#### Solution:

$$6z^{2}-5z-21=0$$
  
 $6z^{2}-14z+9z-21=0$   
 $2z(3z-7)+3(3z-7)=0$   
 $(2z+3)(3z-7)=0$   
 $(2z+3)=0$  or  $(3z-7)=0$   
 $z=-3/2$  or  $z=7/3$ .

#### Question-37

Using factorization, find the roots of the quadratic equation:  $y^2+3y-18=0$ .

#### Solution:

$$y^2 + 3y - 18 = 0$$
  
 $y^2 + 6y - 3y - 18 = 0$   
 $y(y + 6) - 3(y + 6) = 0$   
 $(y - 3)(y + 6) = 0$   
 $y = 3$  or  $y = -6$ .

# Question-38

Using factorization, find the roots of the quadratic equation:  $y^2$ -3y-10 = 0.

# Solution:

$$y^{2}-3y-10=0$$
  
 $y^{2}-5y+2y-10=0$   
 $y(y-5)+2(y-5)=0$   
 $(y+2)(y-5)=0$   
 $y=-2$  or  $y=5$ .

#### Question-39

Using factorization, find the roots of the quadratic equation:  $6y^2-y-2=0$ .

$$6y^{2} - y - 2 = 0$$

$$6y^{2} - 4y + 3y - 2 = 0$$

$$2y(3y - 2) + (3y - 2) = 0$$

$$(2y + 1)(3y - 2) = 0$$

$$2y + 1 = 0 \text{ or } 3y - 2 = 0$$

$$y = -1/2 \text{ or } y = 2/3.$$

Using factorization, find the roots of the quadratic equation:  $9y^2-3y-2=0$ .

# Solution:

$$9y^2-3y-2 = 0$$
  
 $9y^2-6y+3y-2 = 0$   
 $3y(3y-2)+(3y-2) = 0$   
 $(3y+1)(3y-2) = 0$   
 $y = -1/3$  or  $y = 2/3$ .

# Question-41

Using factorization, find the roots of the quadratic equation:  $5z^2-3z-2=0$ .

# Solution:

$$5z^{2} - 3z - 2 = 0$$
  
 $5z^{2} - 5z + 2z - 2 = 0$   
 $5z(z - 1) + 2(z - 1) = 0$   
 $(5z + 2)(z - 1) = 0$   
 $z = -2/5$  or  $z = 1$ .

### Question-42

Using factorization, find the roots of the quadratic equation:  $2z^2 + az - a^2 = 0$ .

#### Solution:

$$2z^{2} + az - a^{2} = 0$$
  
 $2z^{2} + 2az - az - a^{2} = 0$   
 $2z(z + a) - a(z + a) = 0$   
 $(z + a)(2z - a) = 0$   
 $z = -a$  or  $z = a/2$ .

#### Question-43

Using factorization, find the roots of the quadratic equation:  $8x^2-22x-21 = 0$ .

$$8x^{2} - 22x - 21 = 0$$
  
 $8x^{2} + 6x - 28x - 21 = 0$   
 $2x(4x + 3) - 7(4x + 3) = 0$   
 $(2x - 7)(4x + 3) = 0$   
 $x = 7/2 \text{ or } x = -3/4.$