

Optimizing Mixing Applications for Water and Wastewater



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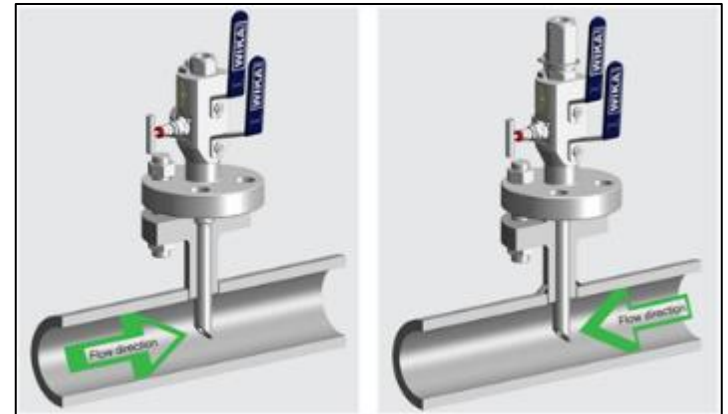
PMG Consulting, Inc.

OTCO 60th Anniversary Workshop

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Agenda

- Review mixing concepts
- Optimum mixing characteristics
- Mixing designs
 - Pipe mixing
 - Static mixers
 - Weir mixing
 - Pump mixers
 - Rapid mixers
 - Vertical or horizontal flocculators
- Questions



Mixing Concepts

- Rapid dispersion of chemicals into water (or wastewater) stream
 - Better distribution of chemical application
 - Fewer byproduct formations
 - Assure chemical interfaces with particulate (or biological) matter
 - Assure chemical interfaces with inorganic contaminants
- G value relationship to process control
 - Step-by-step procedures to determine process design parameters
 - G value and Gt calculations
 - Head loss creates mixing intensity
 - Impeller design criteria

Mixing Concepts

- Detention or reaction time

- Time required for specific chemical reaction or development of settleable particles

- Generally accepted equation

$$d_t = \frac{V}{Q}$$

- d_t = detention or reaction time
- V = basin volume, gallons
- Q = fluid flow rate, (gpm, gph, gpd, etc.)



Mixing Concepts

■ Mixing Intensity (G Value)

- Smoluchowski develop flocculation kinetics concepts 1916
 - Mathematics Theory for Coagulation and Colloidal Kinetics Using Laminar Flow Conditions and Brownian Movement
- Camp and Stein (1943) applied turbulent flow conditions to theories for G value concepts
- Camp (1953) extended practical use of G values and developed Gt concept for flocculator design
- Kawamura (1981) extended Gt concepts to mixing design
 - Possible to improve mixing by altering detention or reaction time

Mixing Concepts

■ Mixing Intensity (G value)

- Calculated using basin configuration and mixer characteristics
- G value (Camp and Stein 1943)
- Later researchers further define power input (P) for mixing

$$G = \sqrt{P / \mu V}$$

$$P = \frac{N_p n^3 D^5 \rho}{g}$$

μ - dynamic viscosity

V - basin volume, ft³

P - power input, ft-lbs/sec

N_p - impeller power number

n - rotational speed, rps

D - impeller diameter, ft.

ρ - water density (temp.)

g - gravitational constant (32.174)

Mixing Concepts

- **Mixing intensity (G value)**
 - Researchers also defined input power (P)
 - Paddle mixers

$$G = \sqrt{\frac{C_d A \sigma v^3}{2gV\mu}} \quad P = \frac{C_d A \sigma v^3}{2g}$$

C_d - drag coefficient (1.8 for paddles)

A - cross-sectional area of paddles, ft²

σ - specific weight of water, lbs./ft³ (temp)

v - relative velocity between paddles and water, fps

g - gravitational constant, 32.174 ft/sec²

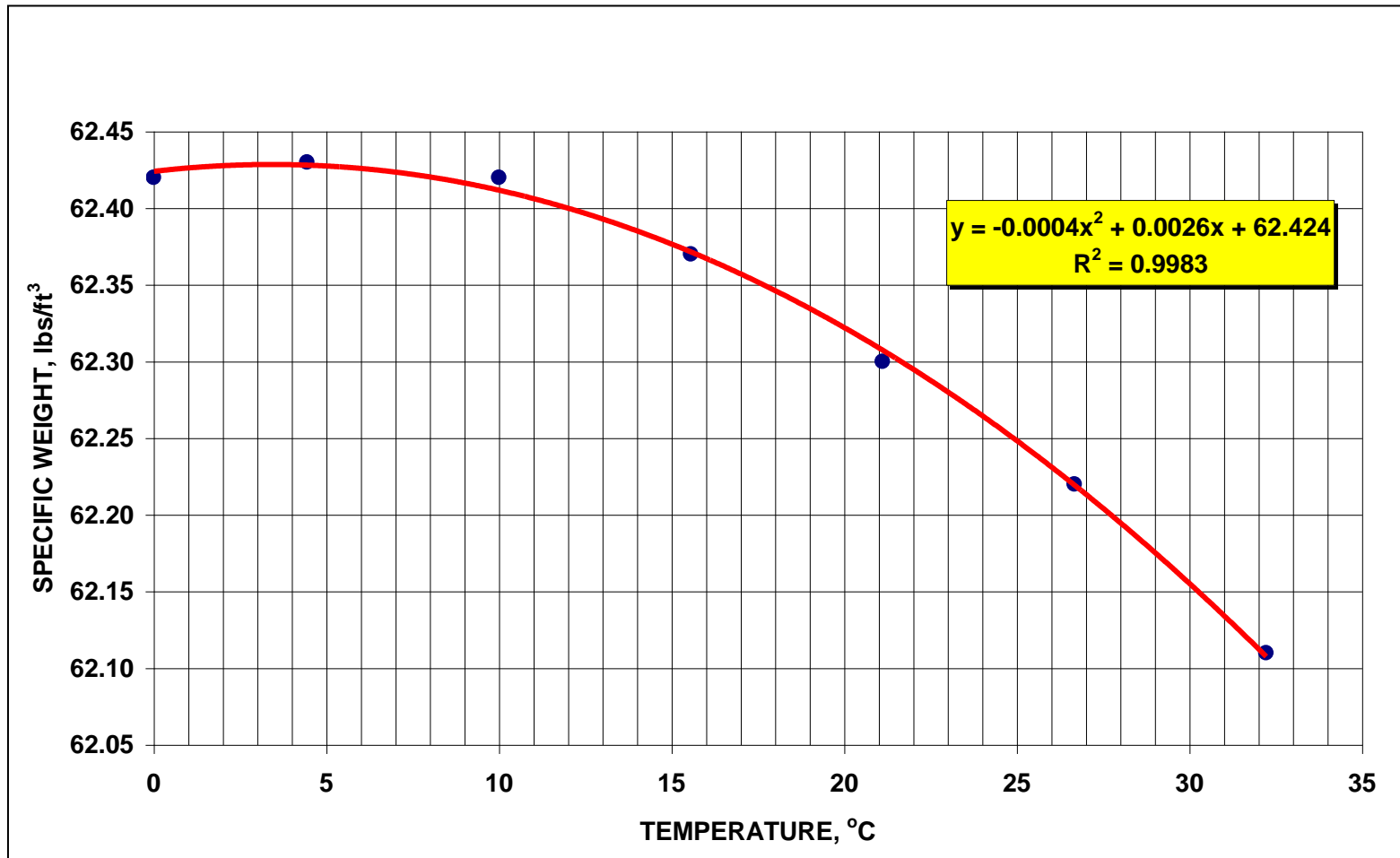
V - volume each stage, ft³

μ - viscosity, lb.-sec/ft² (temp)



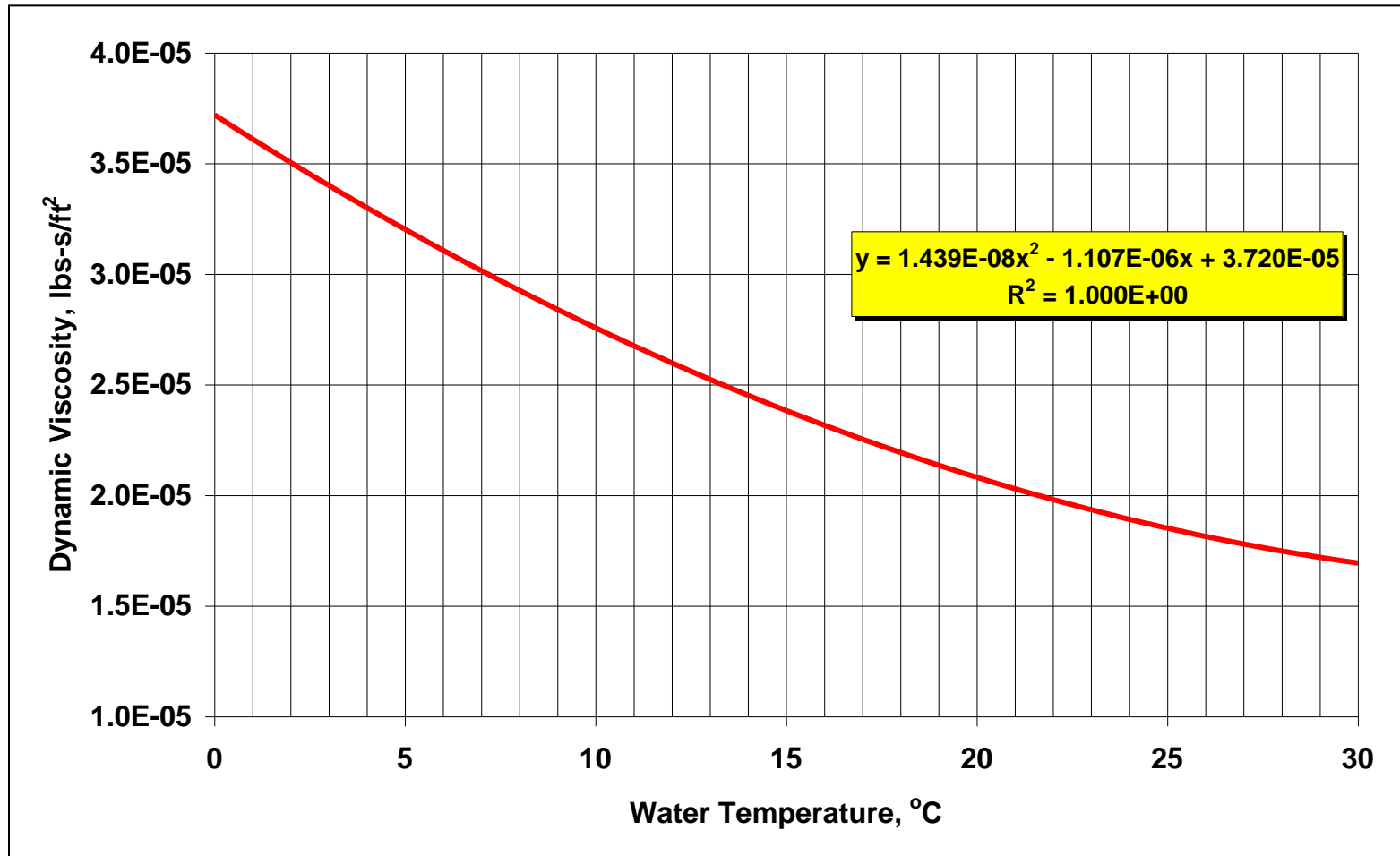
Mixing Concepts

■ Water Density



Mixing Concepts

■ Dynamic Viscosity



Mixing Concepts

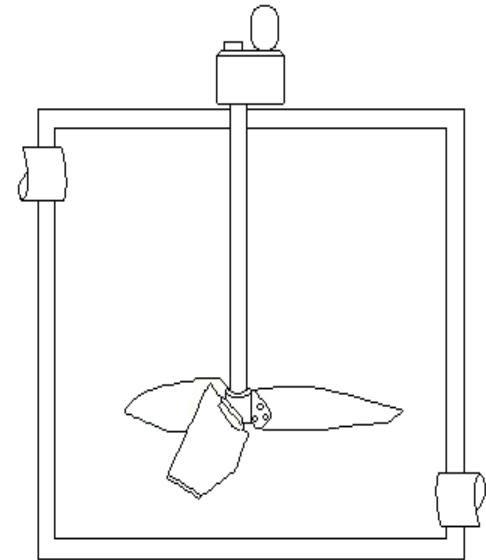
■ Basin Turnover

- Match pumping rate and basin configuration for optimum turnover rate depending on process
- Helps produce optimum degree of blending
- High turnover rate wastes energy and increases mixer wear
- Equation

$$B_t = \frac{Q_i}{V}$$

Q_i = mixed flow, gpm

V = basin volume, gallons



Mixing Concepts

- **Impeller Pumping Capacity**

- Defines turnover rate in rapid mixing and vertical flocculation

$$Q_i = 448.8 N_q n D^3$$

Q_i - pumping rate, gpm

N_q - impeller flow number

n - rotational speed, rps

D - impeller diameter, ft.



Mixing Concepts

- **Impeller Flow Number (N_q)**
 - Great enough to produce turnover
 - Avoid excess turbulence that leads to shearing
- **Impeller Power Number (N_p)**
 - Provide necessary mixing intensity (G value) without increasing electrical requirements
- **Impeller selection important to optimize mixing capabilities**
 - Matched to basin configurations and process needs
 - Avoid chemical shearing while maintaining dispersion and contact with contaminants

Mixing Concepts

■ Degree of Blending

- Depicts blending of water and chemicals within detention time provided
- Prochazka and Landua (1961) proposed fractional unmixedness for impeller performance
- Khang and Levenspiel (1976) proposed relationship approximate concentration fluctuations during mixing

$$a = 2e^{-kt}$$

- Equation used to estimate degree of blending



Mixing Concepts

■ Degree of Blending

$$k = \frac{N(d / T_e)^{2.3}}{0.5} \quad a = 2e^{-kt}$$

$$B\% = (1 - a) * 100$$

e - base e exponential (natural logarithm)

k - decay rate

t - detention time, seconds

N - impeller speed, rps

d/T_e - impeller diameter/basin diameter ratio

Mixing Concepts

- **Displacement Factor (D/F)**
 - E.L. Bean proposed displacement factors for paddle mixers
 - Estimate pumping capacity of paddles (D)
 - Dividing by flow rate gives displacement factor (D/F)
 - >30 for effective mixing and floc development
 - Sum of D for each assembly can be used to estimate turnover each stage



Mixing Concepts

■ Displacement Factor (D/F)

$$d = 2a\pi r(\text{rpm}) \quad D = \sum d \quad \frac{D}{F} \geq 30$$

D - sum of individual d for paddles, ft^3/min

F - basin flow rate, ft^3/min

d - displacement each paddle, ft^3/min

a - area of each paddle, ft^2

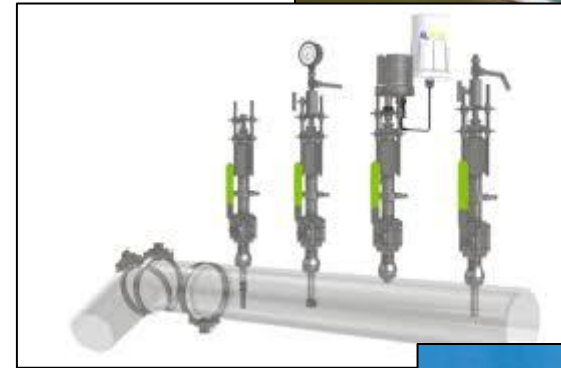
π - 3.1416

r - radius from outer edge each paddle, ft

rpm - rotational speed, rpm

Optimal Mixing Characteristics

- **Optimal Mixing Characteristics**
 - Dependent on process used
 - Important features include
 - Detention time
 - Chemical injection point
 - Mixing intensity (G value)
 - Basin turnover
 - Counter-current flow
 - Degree of blending
 - Gt values
 - Displacement factor (flocculation)
 - Impeller selection and pumping capacity



Optimal Mixing Characteristics - Pipe Mixing

Detention time, sec.	1 to 3
Turnover rate, per sec.	0.6 to 3.5
Pipe length/diameter ratio	≥ 10
G value, sec^{-1}	≥ 500
Gt value	500 to 2,500

Optimal Mixing Characteristics - Static Mixing

Detention time, sec.	<1
Pipe length/diameter ratio	$\geq 10, \geq 5$
G value, sec^{-1}	≥ 500
Gt value	200 to 500

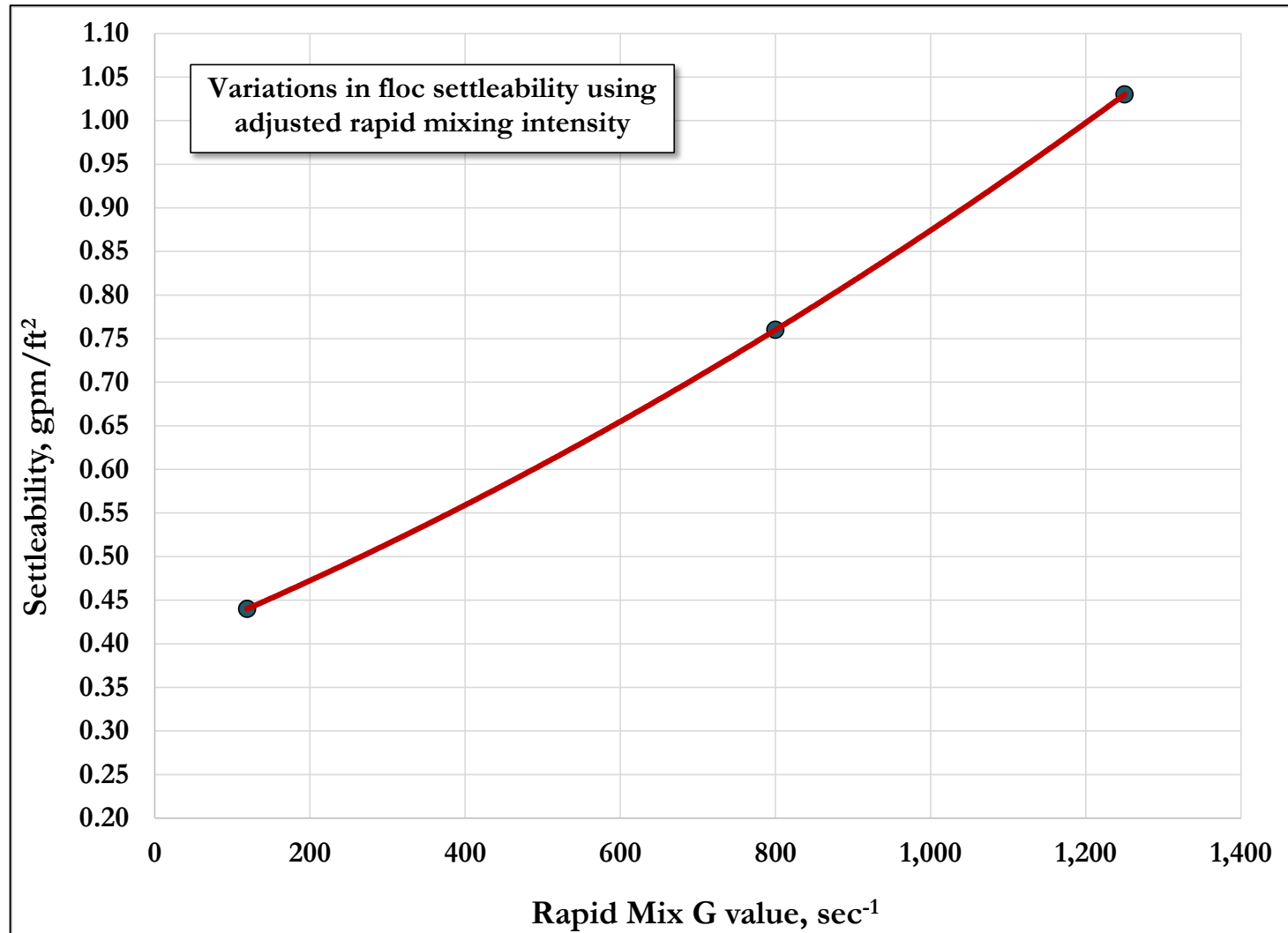
Optimal Mixing Characteristics - Inline Mixing

Detention time, sec.	± 1
Turnover rate, per min.	≥ 1.5
Impeller/pipe diameter ratio	0.3 to 0.6
Length/diameter ratio	2 to 2.5
G value, sec^{-1}	$\geq 2,400$
Gt value	500 to 2,400

Optimal Mixing Characteristics -Rapid Mixing

Detention time, sec.	10 to 15	Degree of blending, %	>99.5
Turnover rate, per min.	≥ 8 , <13	G value, sec^{-1}	750 to 1,400
Imp/basin diameter ratio	0.3 to 0.6	Gt value	5,000 to 20,000

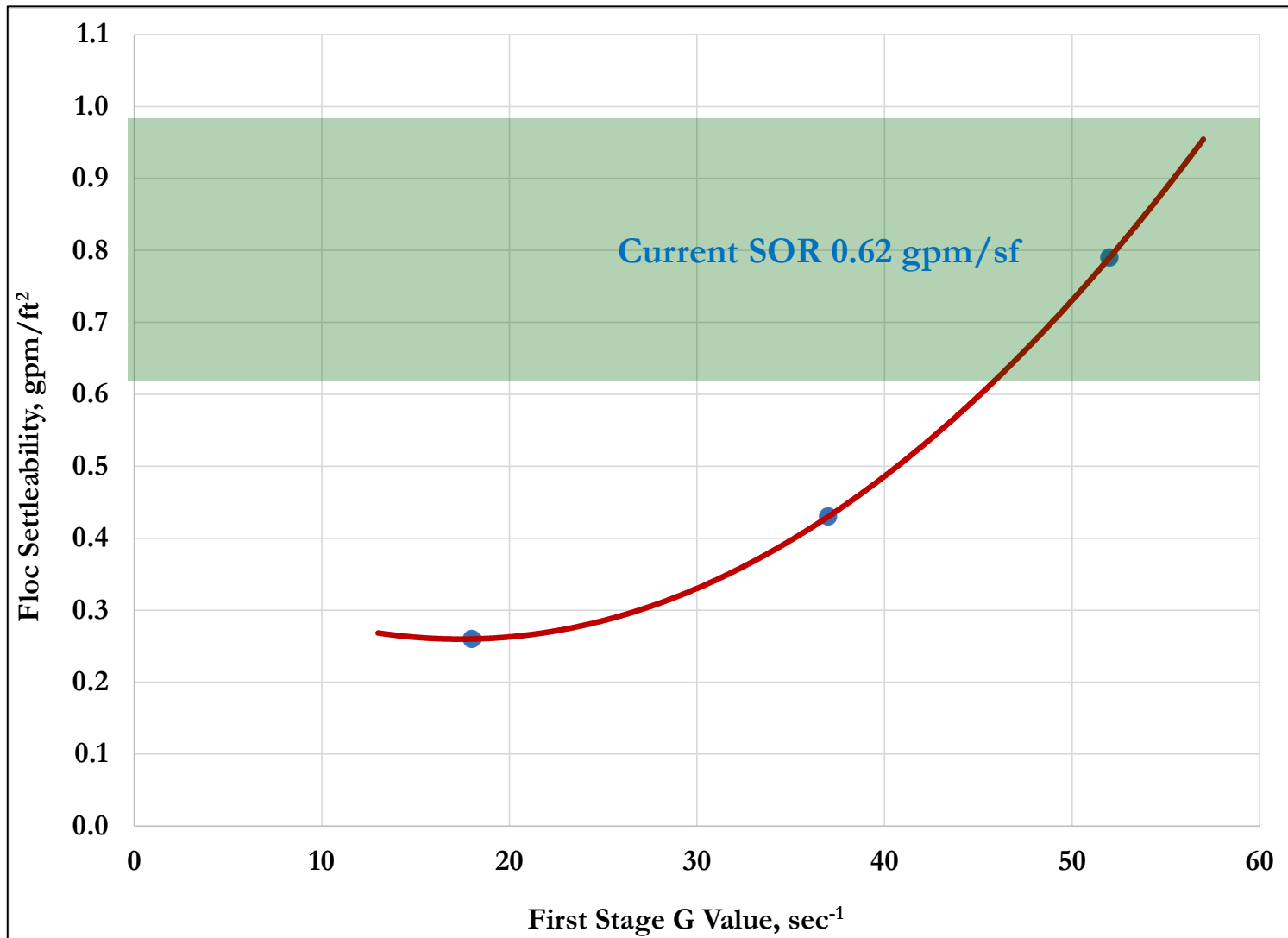
Optimal Mixing Characteristics -Rapid Mixing



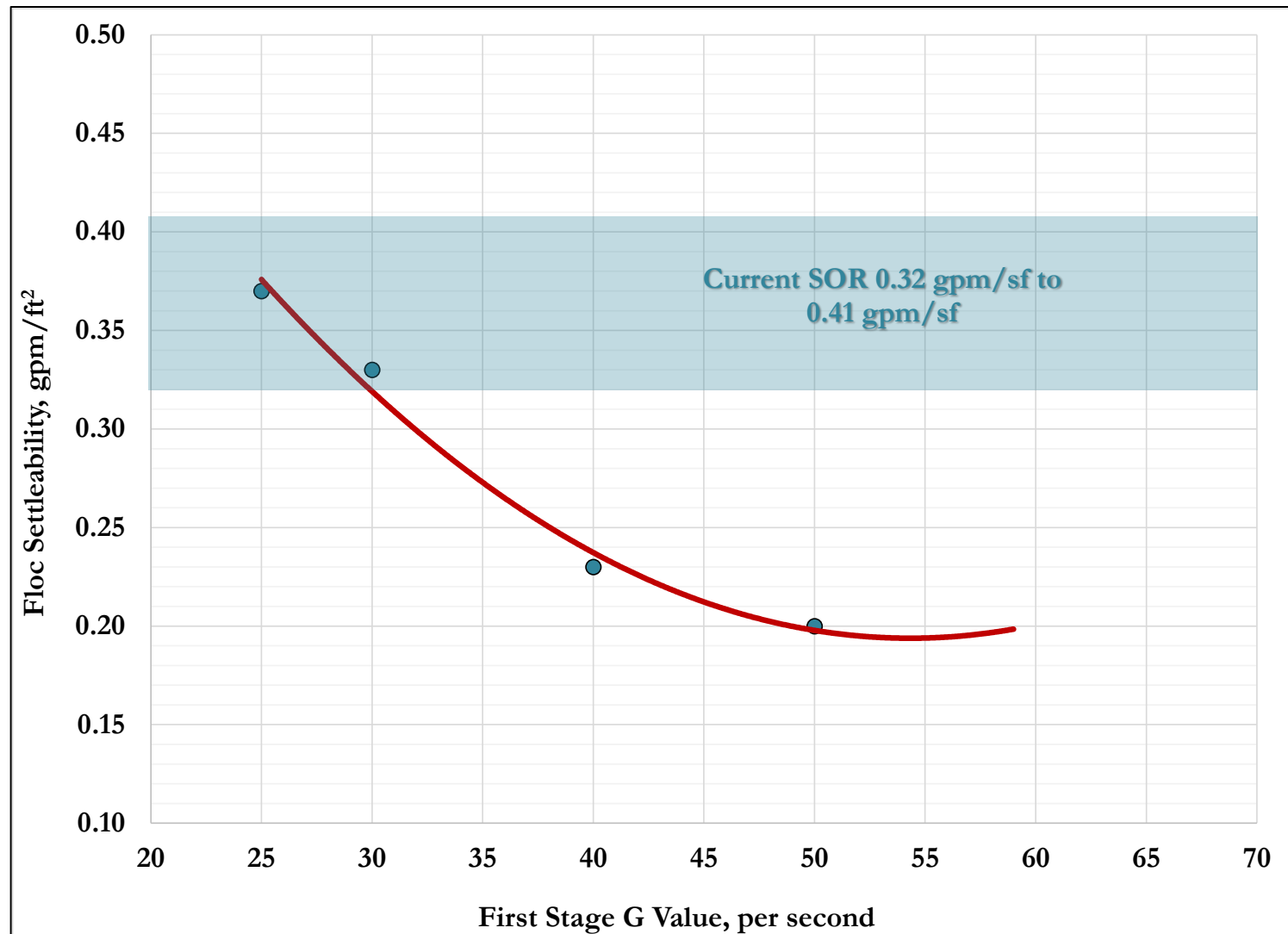
Optimal Mixing Characteristics - Flocculation Mixing

Detention time, min.	≥ 30	Channel velocity, fps	1.0 to 2.0
Flow thru velocity, fpm	0.5 to 1.5	d/T_e ratio horiz.	0.3 to 0.85
Stages	2 to 6	d/T_e ratio vert.	0.35 to 0.7
Area between stages, %	8 to 10	Displacement factor (D/F)	>30
Paddle area, %	10 to 25	Turnover, per min.	0.4 to 2.0
Paddle speed, fps	0.5 to 3.0	G value, sec^{-1}	10 to 80
Mixer speed, fps	2 to 8	Tapered G values, per stage	10 to 15
Outlet velocity, fps	0.75 minimum	Gt value	30,000 to 200,000

Optimal Mixing Characteristics - Flocculation Mixing



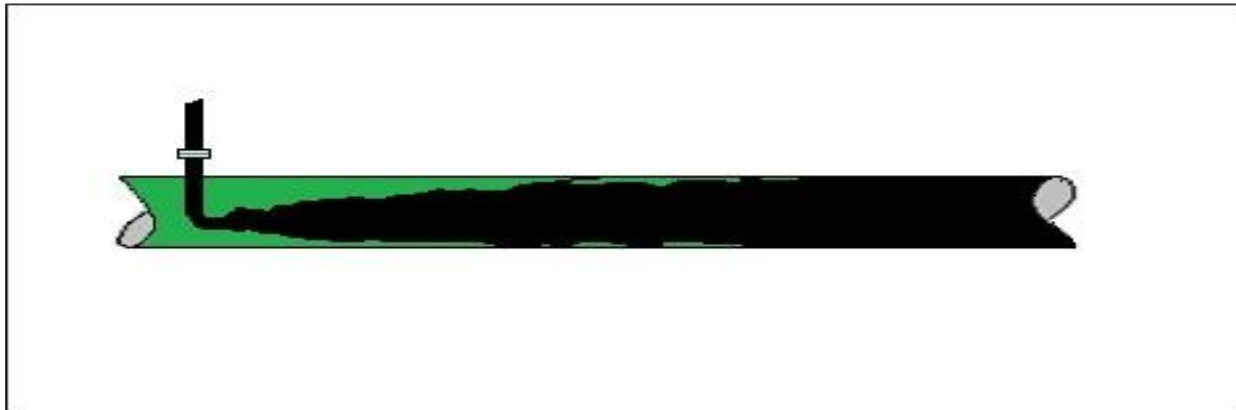
Optimal Mixing Characteristics - Flocculation Mixing



Mixing Designs

■ Pipe Mixing

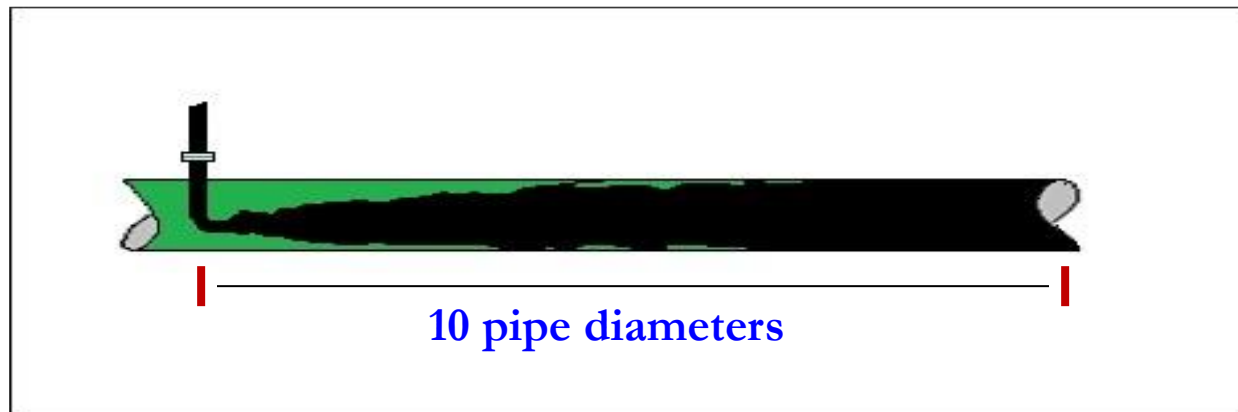
- Chemical dispersion using pipe turbulence and retention
- Turbulence should be verified using Reynolds number ($>4,000$)
- Generally, G values $\approx 500 \text{ sec}^{-1}$ needed to disperse applied chemical
 - Most researchers agree on 500 G for adequate chemical dispersion
 - Promotes more thorough mixing and contact between water and reactants



Mixing Designs

■ Pipe Mixing

- Chemical applied at least 10 pipe diameters upstream of reacted water zone



- G values then function of head losses in pipe system
- 500 sec^{-1} creates adequate mixing for dispersion
- $>300 \text{ sec}^{-1}$ shears polymers (caution)

Mixing Designs

- Pipe Mixing

- Equation

$$G, sec^{-1} = \left(\frac{QwH}{V\mu} \right)$$

G = G value

Q = pipe flow rate, cubic feet per second

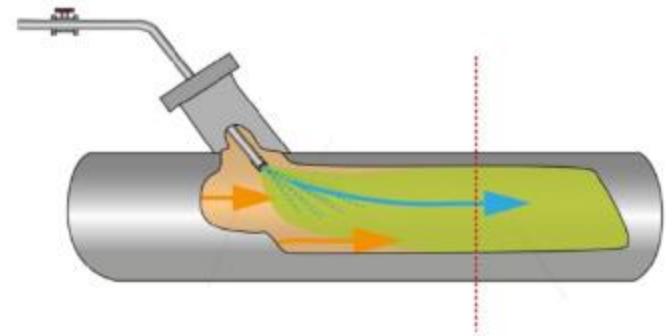
w = specific weight of water (temp. dependent)

H = head loss in pipe, ft.

V = volume of pipe under mixing, ft³

μ = dynamic viscosity, lb-s/ft²

- 12-inch pipe flow at 6.3 ft/sec @20°C will exhibit G of 466 sec⁻¹



Mixing Designs

■ Static Mixers

- Pipeline mixers with no moving parts
 - Sizes up to 60-inch diameter
- Mixing veins produce turbulence within mixer body
 - Turbulence proportional to flow and head loss (from manufacturer)
- Particularly effective for chlorine feed and phosphate feed chemicals



Mixing Designs

■ Static Mixers

- Need 10 pipe diameters upstream and 5 pipe diameters downstream
 - Aids in flow stabilization at inlet and outlet
- Good for chemical dispersion
- Detention times typically one second or less
- Should be sized so that customary flow is near maximum for mixer body



Mixing Designs

■ Static Mixers

■ Equation

$$G, sec^{-1} = \left(\frac{QwH}{V\mu} \right)$$

G = G value

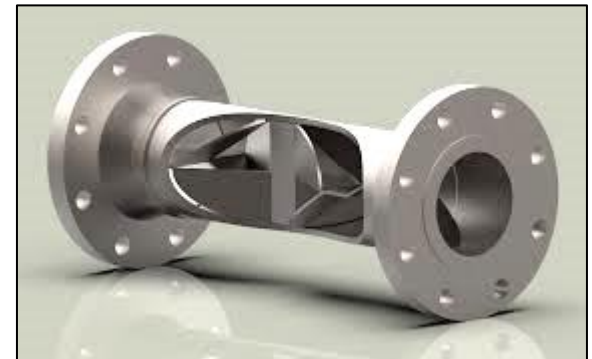
Q = mixer flow rate, cubic feet per second

w = specific weight of water (temp. dependent)

H = head loss in mixer body, ft.

V = volume of mixer body, ft³

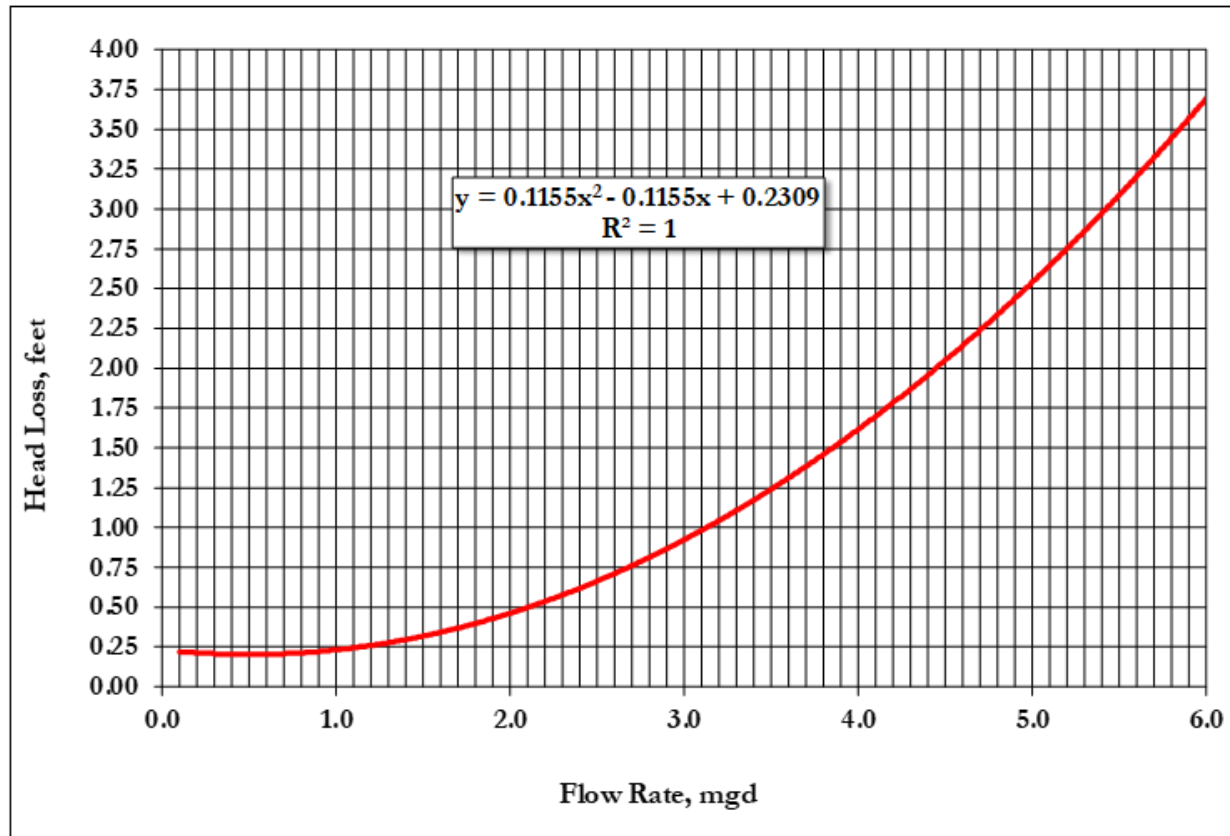
μ = dynamic viscosity, lb-s/ft²



Mixing Designs

■ Static Mixers

- Head loss proportional to flow (manufacturer's data)



Mixing Designs

■ Weir Mixing

- Head loss over weir creates turbulence
- Chemical application at the point of greatest turbulence
- Turbulence induces mixing intensity (G value)
- Good for chemical dispersion
 - Very efficient for polymer treatments at low head loss or longer retention times



Mixing Designs

- Weir Mixing

- Equation

$$G, \text{sec}^{-1} = \left(62.5 \frac{H}{t\mu} \right)^{0.5}$$

G = G value

H = head loss over weir, ft.

t = mixing retention time, sec

μ = dynamic viscosity, lb-s/ft²

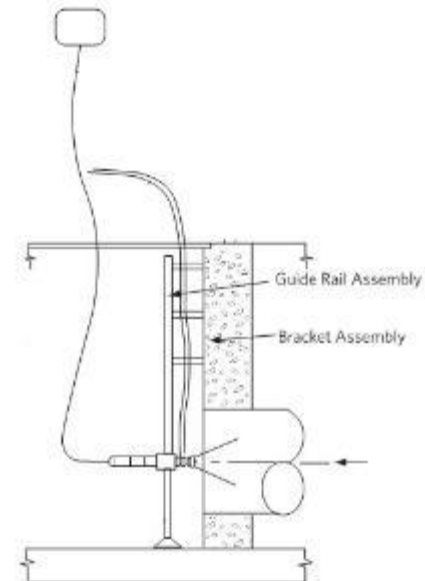
- Rectangular weir with retention time zone of 8 seconds and 2-inches head loss @20°C creates G of 250 sec⁻¹



Mixing Designs

■ Pump Mixers

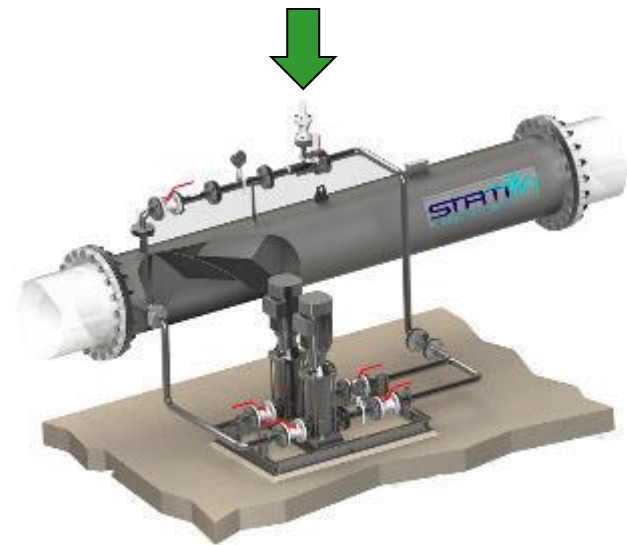
- Chemical feed pumped directly into pipe flow path
- Chemical injection in pump impeller or through orifice
 - Water Champ is an example
 - Other systems exist
- Rapid chemical dispersion actively increases contact with water
 - Conical discharge plume fills pipe area
 - Prone to scale build up at spray nozzles



Mixing Designs

■ Pump Mixers

- Chemical feed pumped directly into pipe flow path
- Chemical injection in pump impeller or through orifice
- Designed chemical pumping system can be used to improve mixing efficiency
 - Pump draws suction from pipe system and re-injects chemical solution back into pipe through a jet or orifice
 - Chemical injected into pump discharge pipe prior to re-entry into main pipeline



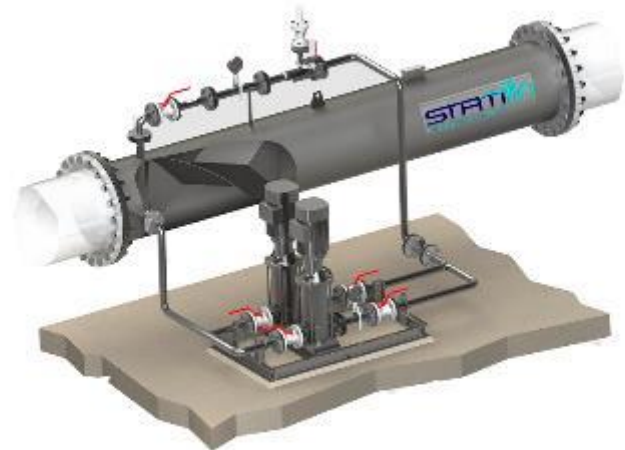
Mixing Designs

■ Pump Mixers

- G value equation can vary

$$P = QH\rho g\eta$$

- P = power input,
 - Q = pump flow rate. ft³/sec
 - H = pump head, ft
 - ρ = water density, lbs/ft³
 - g = gravitational constant 32.174 lbs/ft
 - η = pump efficiency, %
-
- Then insert into G value equation



Mixing Designs

- Rapid mixing concepts for chemical dispersion
- Flocculation concepts for effective floc development
- G value relationship to process control



Mixing Designs

■ Rapid Mixing

- Importance well documented
- Turbulence to disperse chemicals and water to initiate coagulation
- Matched to coagulation mechanism used
 - Adsorption and charge neutralization
 - Enmeshment in a precipitate (sweep coagulation)
 - Adsorption and interparticle bridging
 - Mixing disinfection chemicals reduces unwanted byproducts



Mixing Designs

■ In-line Rapid Mixing

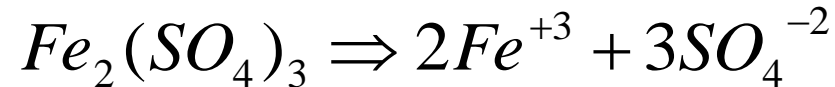
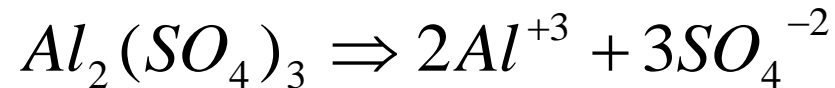
- Instantaneous high energy mixing for charge neutralization
- Destabilization of particles requires collision and transport of particles and formed hydrolyzed coagulant species
- Chemical dissociation to metal cations (M^{+n}) and salt anions (S^{-n})



Mixing Designs

- Chemical dispersion

- Dissociation reactions



- Generalized chemical species - $M_x(OH)_y^{+n}$

- Dissociation reactions takes less than one second

Mixing Designs

- Chemical dispersion

- Common chemical reactions



- Reaction times for metal hydroxide development - seven (7) seconds

Mixing Designs

- **Conventional Rapid Mixing**
 - Detention times for chemical mixing are longer
 - Create metal hydroxides that do the treatment
 - Precipitation of phosphates and adsorption of organics and turbidity particles
 - Use conventional mixing basin
 - Most treatment occurs in flocculation as collisions occur between floc and particles in water
 - Lower mixing intensity used in floc development



Mixing Designs

- **Adsorption and Interparticle Bridging**
 - Simultaneous treatment with polymers
 - Polymer strand length depends on MW
 - Charged sites along polymer strand
 - Foster adsorption of opposite charged particles
 - Multiple strands or looping on single strand creates bridging effect
 - Increase size, density, settleability of floc formed
- Polymers generally shear at G values greater than 300 sec^{-1}
 - Make take 45 minutes to 2 hours to reform polymer strand after shearing



Mixing Designs

■ Flocculation

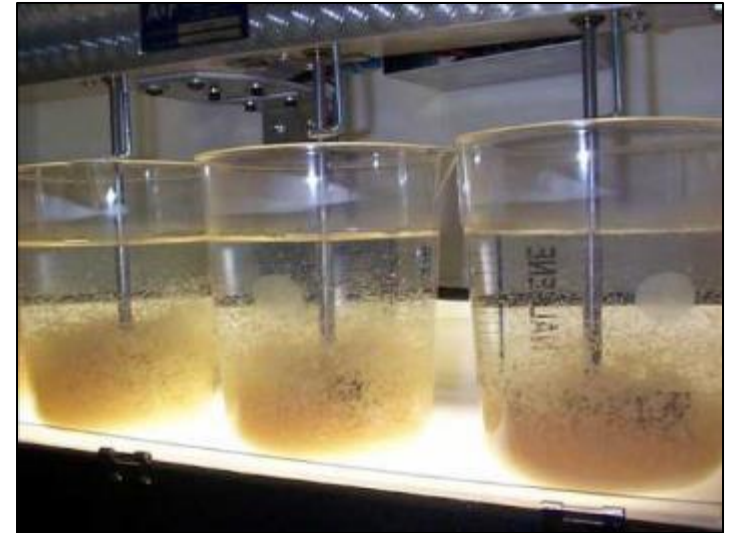
- Gentle mixing to transform initial floc formations into dense settleability material
- Treatment governed by number of particles in suspension, collisions between particles to increase size and density
- Operational control over chemical dosage and mixing intensity (energy) applied - *particle collisions*
- Tertiary treatment in wastewater for phosphorus removals using chemical precipitation (pH important)



Mixing Designs

■ Flocculation

- Orthokinetic flocculation most common method
 - Involves bulk fluid motion using mixing intensity to gather chemical and particles into floc
- Horizontal or vertical flocculation assemblies used
- Mixing energy successively lowered as process proceeds
 - Tapered mixing promotes dense floc formation for effective settling
 - G values and tapering sequences optimized using jar tests



Mixing Designs

■ Flocculation

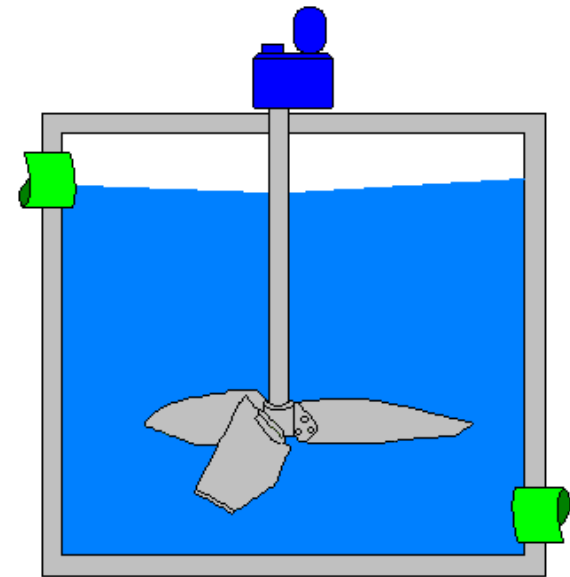
- Two or more chambers or stages
- Floc develops increasing size to maximum diameter
 - Floc formation 12 minutes to 17 minutes
- Further mixing promotes compaction of floc reducing size and increasing density
 - Total detention 17 minutes to 25 minutes optimizes floc development
- Long detention times (>45 minutes) increase potential for floc shear and poor settling



Mixing Designs

■ Flocculation

- TSS recommends 30 minutes at design flow for flocculation
 - Can lead to more than 45 minutes at operating flows
- Typical floc diameter range 0.5 mm to 3 mm
- Match mixing and floc development to optimize density and settleability
 - Conduct floc settleability at different mixing conditions



Mixing Designs - Impellers

■ Conventional Mixing

- Impeller selection important to basin configuration and design
- Radial flow impellers 90° outward from shaft
 - Produces pumping action with basin walls
 - Flow both upward and downward returning to impeller shaft
 - Reduces short-circuiting
 - Bulk rotation can be corrected with baffles



Mixing Designs - Impellers

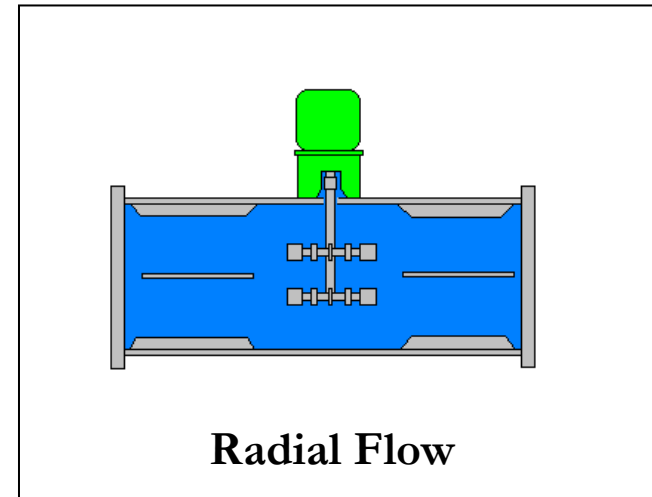
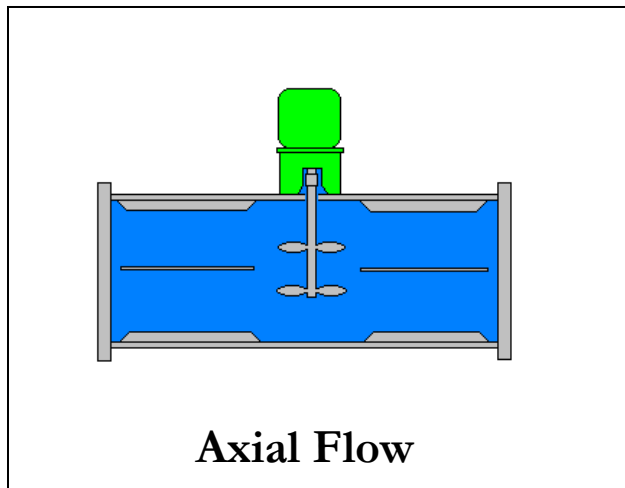
■ Conventional

- Axial flow impellers angled flow from shaft
 - 45° common, but other angles used
 - Produces upward or downward pumping action depending on rotating direction
 - Must specify pumping direction
 - Pumping action opposite inlet flow to reduce short-circuiting (countercurrent flow)



Mixing Designs - Impellers

■ Inline Mixers



Mixing Designs - Impellers

- Inline Mixers







Mixing Designs - Impellers





- Designed for mixing applications
 - Blending, turbulent mixing, viscous solutions, mixing gases and liquids
- Operations verified under lab conditions
 - N_p - *power number*
 - N_q - *flow number*
 - Mixing conditions (velocity profiles)







Mixing Designs - Impellers

Impeller	Manufacturers	Power number	Flow number
	Radial turbine 4 blade Most manufacturers	4.3	0.68
	Radial turbine 5 blade Most manufacturers	5.4	0.73
	Radial turbine 6 blade Most manufacturers	6.0	0.72
	Radial turbine 8 blade Most manufacturers	7.8	0.82

Mixing Designs - Impellers

Impeller	Manufacturers	Power number	Flow number
	Radial turbine 12 blade Some manufacturers	9.9	0.89
	Propeller Lightnin' A100/110 Chemineer AP-3	0.32 (1.0 pitch) 0.62 (1.5 pitch) 1.0 (2.0 pitch) 1.35 (2.5 pitch)	No data
	Pitched blade turbine Lightnin' A200 Chemineer P-4 Philadelphia PBT	1.27	0.79
	Flat turbine Lightnin' A200 Chemineer P-4 Philadelphia PBT	3.4	0.62

Mixing Designs - Impellers

Impeller	Manufacturers	Power number	Flow number
	High % hydrofoil Lightnin' A310/510 Chemineer SC-3	0.30	0.56
	High % Chemineer HE-3 Philadelphia hydrofoil	0.20 to 0.26	0.46 to 0.49
	Pitched fluid foil Lightnin' A320/340 Philadelphia HS	0.64	0.64
	Gas mixing Lightnin' A130 Chemineer CD-6 Philadelphia Smith Turbine	3.2	0.61

Mixing Designs - Paddles

- Different flocculator designs from manufacturers
- Most common
 - Horizontal paddle
 - Vertical mixers
 - Walking beam old technology, but still in use

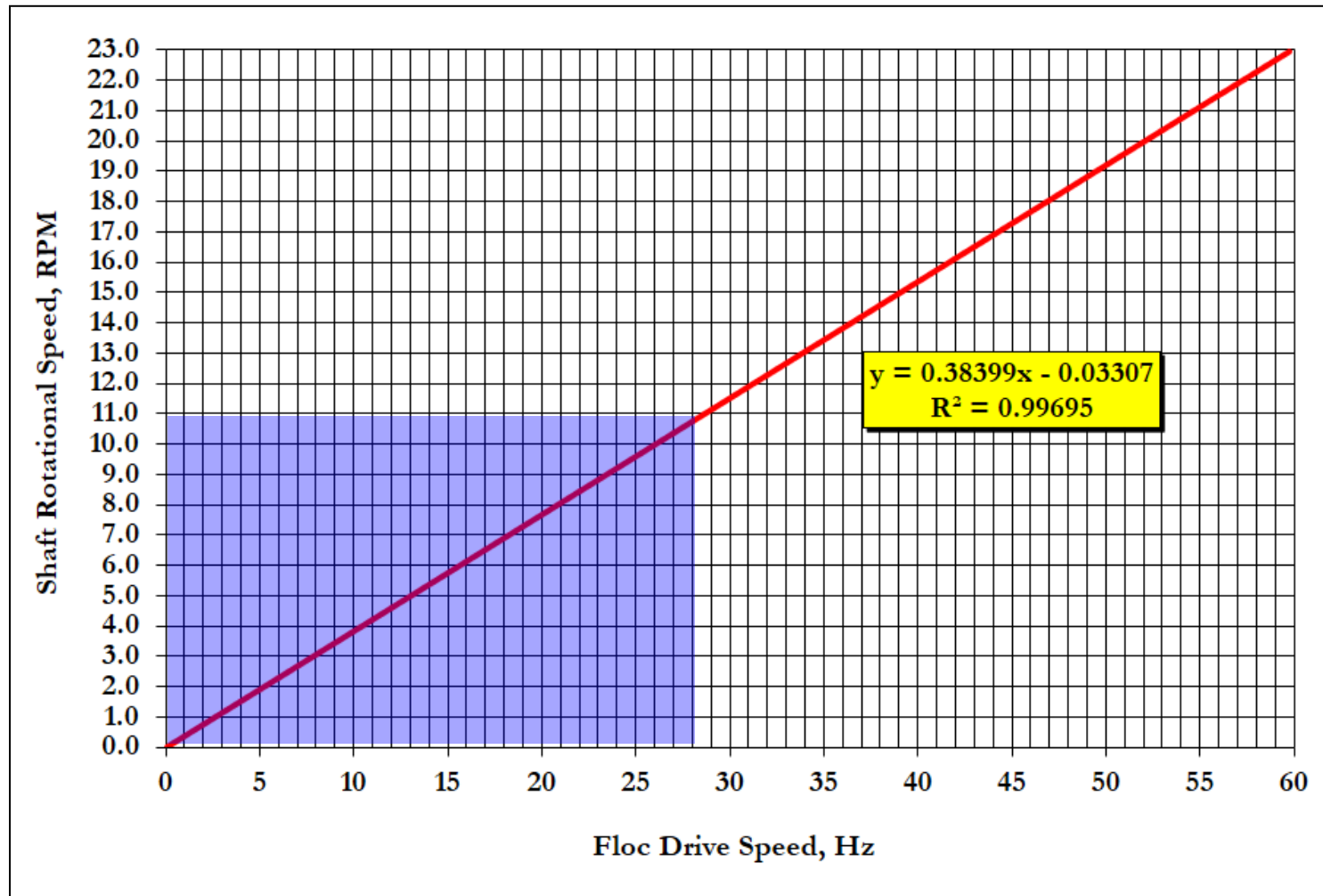


Mixing Designs VFDs

- Variable frequency drives (VFDs)
 - Variable speed needed to adjust mixing based on water temperature and floc development
 - Speed curves typically linear relationship between VFD setting and paddle rotational speed
 - Shaft speed should be correlated to VFD settings
 - Speeds needed for G value calculations



Mixing Designs VFDs





Questions

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