

**PART 1**  
**BUILDING ENVELOPE THERMAL ANALYSIS (BETA) GUIDE**

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## 1.1 OVERVIEW

The evaluation of energy use in buildings requires a reasonably accurate assessment of heat transfer through the building envelope which includes the heat passing through thermal bridges at interfaces and penetrations. A previous study, ASHRAE 1365-RP “Thermal Performance of Building Envelope Details for Mid- and High-Rise Buildings” (Morrison Hershfield Ltd, 2011), put forward procedures and data that allowed practitioners to evaluate the impact of thermal bridging in a comprehensive and straightforward method. This has started a market transformation to better evaluate building performance and design for energy conservation. 1365-RP, which contained 40 common building envelope assemblies for mid- and high-rise construction, was a good start in creating a building envelope thermal performance catalogue. However, that report only scratched the surface, particularly in identifying how to effectively mitigate thermal bridging in design. Part of the intent of this guide is to expand on the previous work, including showing where opportunities exist to incentivize improving industry practice.

In preparation for this guide, the analysis of the thermal performance of typical building assemblies was expanded upon, including evaluation of many more assembly details that are in common use in the BC building industry. Also, emerging technologies and construction practices were explored that offer substantial improvements to current construction practice.

This section of the report, the Building Envelope Thermal Analysis (B.E.T.A.) guide, focuses on summarizing the impact of thermal bridging on the thermal performance of building envelope assemblies and how to utilize this information in practice.

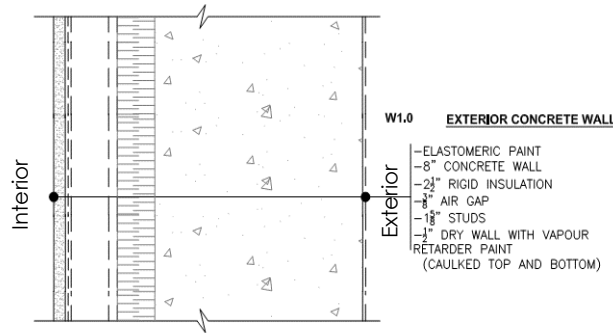
From a high level awareness perspective, the information provided in this section is relevant to all the target audiences. All stakeholders should be aware of the information, understand the benefits of the methodology, and understand in concept how the methodology and data can be used in practice. Only designers, architects, engineers, energy modelers, and building envelope consultants really need to delve deep into the methodology and fully understand how to utilize the thermal performance data in practice.

## 1.2 METHODOLOGY FOR DETERMINING THERMAL PERFORMANCE OF BUILDING ENVELOPE ASSEMBLIES

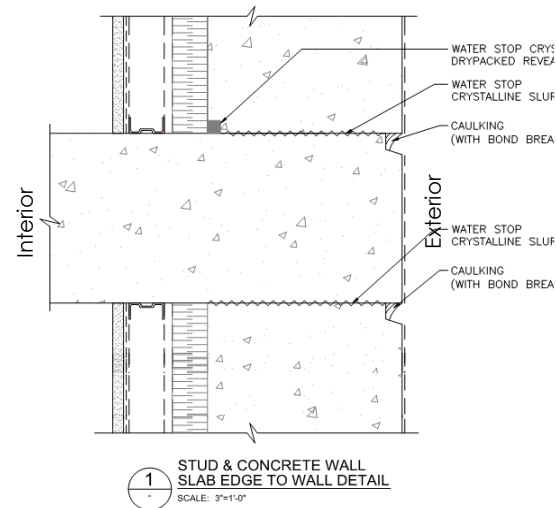
### 1.2.1 METHODOLOGY SUMMARY

The performance data prepared for this guide was determined by following the same methodology as 1365-RP and using the same 3D thermal modeling package that was extensively calibrated and validated as part of that work. Detailed information on the background of the methodology can be found in the final report for 1365-RP. What follows is an outline of the important points of that methodology.

In determining the thermal performance of the building envelope that includes thermal bridging, a basic distinction must be made between two types of opaque building components, clear field assemblies and interface details, examples of which are shown in Figures 1.1 and 1.2 respectively.



**Figure 1.1:** An example of a clear field assembly drawing



**Figure 1.2:** An example of an envelope interface detail drawing

Clear field assemblies are wall, roof or floor assemblies that include all the components that make up a wall, including structural framing. These are typically found in the architectural drawings in the wall/roof/floor schedules. Clear field assemblies can contain thermal bridges from uniformly distributed secondary structural components which are needed for the wall to resist loads, but do not include thermal bridges related to intersections to the primary structure or between assemblies. Examples of components included in clear field assemblies are brick ties, girts that support cladding and/or studs.

Interface details are changes in construction or geometry that interrupt the uniformity of the clear field. These are typically found in the detail sections in architectural drawings. These include slab edges, opaque to glazing or wall transitions, parapets, corners and through wall penetrations.

Determining the impact of heat flows through the clear field and through interface details is necessary to accurately assess the thermal transmittance of building envelope assemblies.

### A Note on Glazing

Glazing in buildings can have an incredibly large influence on building energy use, especially in designs that have high window to wall ratios. Glazing portions of the building envelope are often dealt with separately from the opaque elements because of the additional effects of solar heat gain. Thermal analysis and testing of glazing systems in North America typically follow standards by the National Fenestration Rating Council (Mitchell, et al., Rev 2013). Following this guide to determine the thermal performance of opaque elements and NFRC standards for glazing is compatible. While the thermal performance of glazing assemblies can affect the thermal resistance of adjacent wall or roof assemblies, the heat loss is accounted for through the **window to wall transition** thermal values described later in this guide.

### 1.2.2 DETERMINING THERMAL PERFORMANCE OF CLEAR FIELD ASSEMBLIES

The thermal performance of clear field assemblies can be determined through calculation, modeling or physical testing. Typically this takes the form of a U-value or effective R-value.

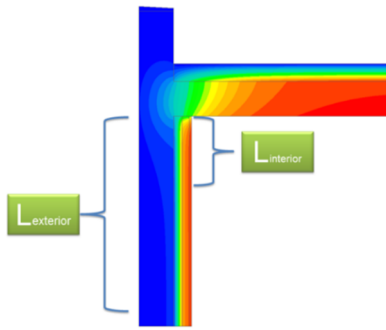
- The **ASHRAE Handbook of Fundamentals** (ASHRAE, 2013) provides several methods to determine clear field U-values using hand calculations. These hand calculations are meant for simple assemblies with only thermal bridges in one or two dimensions. These methods are described in more detail in the Handbook of Fundamentals.
- For assemblies where the 2D heat flow paths can influence each other and are more complex than appropriate for hand calculations, then 2D thermal modeling can be utilized to approximate the thermal performance of building envelope details. Software for this type of modeling (such as **THERM**, (Mitchell, et al., Rev 2013) is widely available and used in industry for two-dimensional thermal modeling. Approximations need to be made for components that are not continuous or occur in three dimensions, such as creating an equivalent thermal conductivity. These approximations can be sufficient in many cases for determining the expected thermal transmittance of opaque assemblies, but cannot be used to determine surface temperatures.
- For complex geometries and configurations where 2D heat flow assumptions are no longer valid, then 3D modeling or physical testing is often necessary for more accurate approximations of thermal performance. As stated previously, the clear field and detail values prepared for this guide were determined through 3D modeling.

It is typically only necessary to model or test a clear wall assembly if it is a new or unique design when information is not available. The construction industry has a wide variety of resources accessible to designers which contain thermal performance values for many types of clear field assemblies. Clear field assemblies analyzed for this guide are discussed in section 1.3.1 with additional information and thermal performance values provided in Appendices A and B. Other sources of information beyond this guide are discussed further in section 1.3.3.

### 1.2.3 DETERMINING THERMAL PERFORMANCE OF INTERFACE DETAILS – AREA WEIGHTED APPROACH

Area weighted calculations are commonly used to calculate U-values or effective R-values of the combined effect of assemblies and interface details. Typically, this is done by weighting the heat flow through the materials by the area they take up. While this can be applied easily to simple clear field assemblies, the question that arises when applied to interface details is **what is the area of a thermal bridge?**

Using only the physical area of a thermal bridge assumes that the heat flow paths through an interface detail are one-dimensional and parallel. Unfortunately, this is rarely true, and highly conductive building components create lateral heat flows to other components in three dimensions that are not accounted for in basic parallel flow assumptions. A steel shelf angle holding up a brick wall may seem small from the outside, but it is connected to many other components behind the brick and heat can easily flow around the insulation.



**Figure 1.3:** Areas of influence of a parapet detail differ from the interior and exterior of the wall

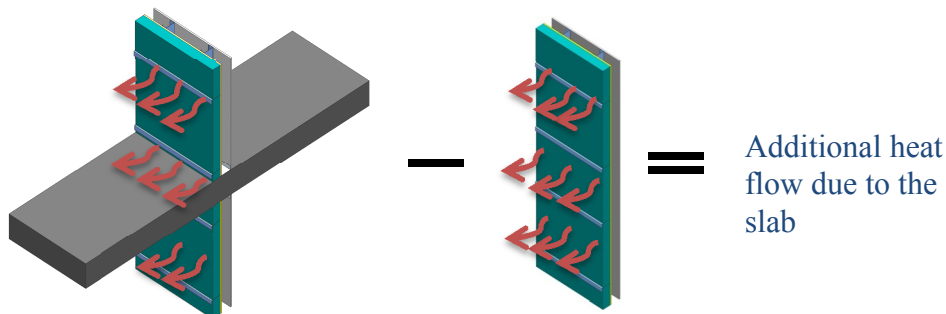
To improve simple parallel path assumptions, an area of influence of a thermal bridge has been utilized in the past. This requires finding out the distance where the heat flow through the assembly is no longer affected by the thermal bridge. The heat flow through this area is then used as a combined U-value for the wall and the thermal bridge. However, determining areas of influence of many common thermal bridges is incredibly difficult. Lateral heat flows caused by conductive elements allow heat to be transferred in multiple directions for large distances. This can create large differences in areas of influence depending on whether you are looking from inside or outside.

Using the area weighted approach can produce reasonable results when analyzing structures with low thermal conductive structural members, such as some wood-frame configurations. However, this approach can be complicated and difficult to use in practice for detailed analysis of the heat transfer through building envelopes constructed with moderate to highly conductive materials like concrete, steel and aluminum.

#### 1.2.4 DETERMINING THERMAL PERFORMANCE OF INTERFACE DETAILS UTILIZING LINEAR TRANSMITTANCES

Linear and point transmittances can simplify things by ignoring the area of thermal bridges altogether. With this approach, the heat flow through the interface detail assembly is compared with and without the thermal bridge, and the difference in heat flow is related to the detail as heat flow per a linear length or as a point heat flow.

To illustrate how this works, let's apply this method to an exterior insulated steel stud wall with a cantilevered balcony slab that is a direct extension of the concrete structural floor slab, as shown in Figure 1.4:



**Figure 1.4:** Determining linear transmittance for a slab

First, the heat flow through the interface detail assembly with the slab is determined. Next, the heat flow is determined through the assembly as if the slab was not there (you may recognize this as the clear field assembly). Since the clear field does not contain the slab, which is a large thermal bridge, the amount of heat flow is less. The difference in overall heat flow between the two assemblies is the extra amount caused by the balcony/floor slab bypassing the thermal insulation. Dividing by the assembly width (linear length of the slab edge) creates the linear transmittance of the slab, which is a heat flow per linear length.

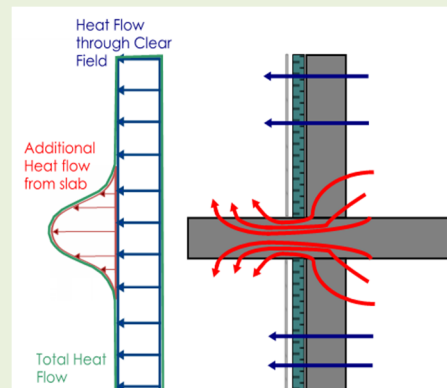
With linear transmittances, the extra heat flow prescribed to the floor slab is not dependent on the area of the thermal bridge, but only by the linear length (width) of the balcony slab. A point transmittance is similar in concept, but is a single point of additional heat flow, not dependent on area or length. Since the linear and point transmittances are separate from the clear field, they can be directly compared to assist in determining the most appropriate details for a building. Calculated linear and point transmittances along with the clear field transmittance can be used to determine the overall heat flow for any size of wall or roof that use those components.

As with the clear field assemblies, there are additional information sources that have thermal performance values for common linear and point transmittances, albeit they are not as widely available. The performance catalogue in this guide, discussed in section 1.3, consolidates several of the linear and point transmittance as determined using the method set forth in 1365-RP. However, there are other sources available which are detailed further in section 1.3.3.

### Superimposing Heat Flows

Another way of looking at the basic concept of linear transmittance is by superimposing the heat flows from the full assembly, with an interface detail, and the clear field assembly, without the interface detail, over top of each other.

From this figure you can visualize the lateral heat flows to the path of least resistance through the interface detail assembly (i.e. through the slab). This results in a higher heat flow at the slab compared to if it was only the clear field. Far away enough from the slab and the heat flow reaches the same level as in the clear field. By subtracting the clear field from the total interface detail assembly leaves the additional heat flow from just the slab, from which we get the linear transmittance.

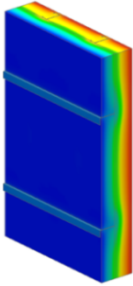


## 1.2.5 DETERMINING OVERALL THERMAL PERFORMANCE

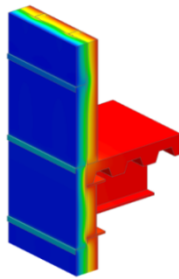
The thermal performance values of each of the envelope components can be used to calculate an overall thermal transmittance (U-value) for building envelope assemblies that include thermal bridging. Summarizing the approach so far, the thermal transmittances used in the calculations comprise of three separate categories:

- **Clear field transmittance** is the heat flow from the wall, floor or roof assembly. This transmittance includes the effects of uniformly distributed thermal bridging components, like brick ties, structural framing like studs, and structural cladding attachments that would not be practical to account for on an individual basis. The clear field transmittance is a heat flow per area, and is represented by a U-value denoted as the clear field ( $U_o$ ).
- **Linear transmittance** is the additional heat flow caused by details that are linear. This includes slab edges, corners, parapets, and transitions between assemblies. The linear transmittance is a heat flow per length, and is represented by psi ( $\Psi$ ).

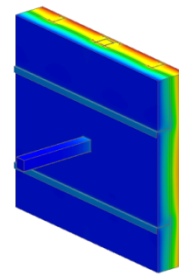
- **Point transmittance** is the heat flow caused by thermal bridges that occur only at single, infrequent locations. This includes building components such as structural beam penetrations and intersections between linear details. The point transmittance is a single additive amount of heat, represented by chi ( $\chi$ ).



**Figure 1.5:** Example clear field assembly



**Figure 1.6:** Example linear transmittance of a floor slab detail



**Figure 1.7:** Example point transmittance of a beam penetration detail

The overall U-value for any building envelope section is a simple addition and multiplication process. In straightforward terms this amounts to:

$$\text{Total Heat flow per area through the overall assembly} = \frac{\text{Heat flow through linear transmittances} + \text{Heat flow through point transmittances}}{\text{Total Area of assembly}} + \text{Heat flow per area through clear field assembly}$$

Or, in mathematical terms:

$$U_T = \frac{\Sigma(\Psi \cdot L) + \Sigma(\chi)}{A_{Total}} + U_o$$

Where:

$U_T$ =	total effective assembly thermal transmittance (Btu/hr·ft <sup>2</sup> ·°F or W/m <sup>2</sup> K)
$U_o$ =	clear field thermal transmittance (Btu/hr·ft <sup>2</sup> ·°F or W/m <sup>2</sup> K)
$A_{total}$ =	the total opaque wall area (ft <sup>2</sup> or m <sup>2</sup> )
$\Psi$ =	heat flow from linear thermal bridge (Btu/hr·ft °F or W/mK)
$L$ =	length of linear thermal bridge, i.e. slab width (ft or m)
$\chi$ =	heat flow from point thermal bridge (Btu/hr· °F or W/K)

There are multiple types and quantities of linear and point transmittances, but they are all added to the clear field heat flow to get the overall heat flow of an area of the building envelope. The length for the linear transmittance depends on the detail. For example, the length used in the calculation for a floor slab bypassing the thermal insulation could be the width of the building perimeter, if this slab detail occurs around the whole façade of the building. Alternatively, a corner detail length could be the height of the building envelope.



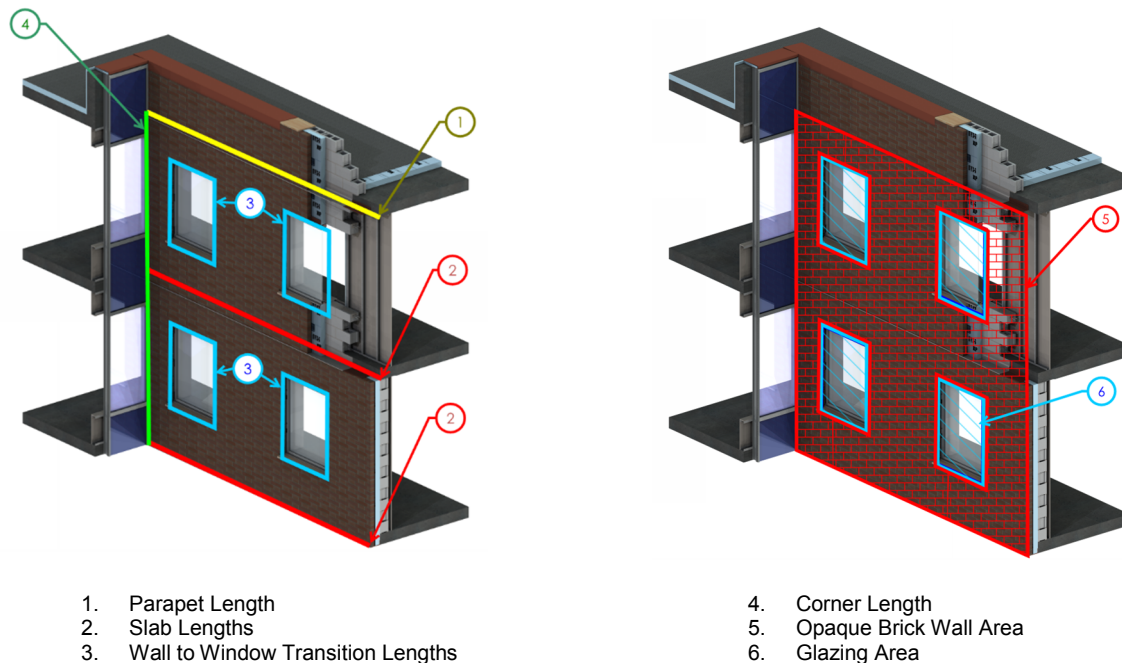
By finding the heat flows separately, each component can be evaluated to find their relative contribution to the overall heat flow.

The overall U-value for a building section can be found as long as the thermal performance values for the clear field, linear and point transmittances are known along with the quantities determined by architectural drawings. These transmittances can be calculated using the procedures put forth in 1365-RP; however, modeling every detail on a project would be impractical. As such, this guide provides an extensive catalogue of assemblies where the thermal performance values have already been calculated for designers. This catalogue is discussed in more detail in section 1.3.

### 1.2.6 FINDING LENGTH AND AREA TAKEOFFS

Determining the overall U-value of a building section using length and area takeoffs can be fairly straight forward i.e. slab lengths along the face of a building, or corner heights; however, there are some nuances when it comes to certain interface details. The following example shows the lengths and areas for a simple brick wall section.

**Example:** The overall opaque wall U-value is required for the brick wall section of a building that is adjacent to a curtain-wall system. From the analysis, the designer has determined that the brick wall section contains a parapet, slab, wall to window transition and corner detail. The designer finds the thermal performance values for the brick clear wall assembly and the linear transmittances for the interface details in a thermal performance catalogue. The length and area takeoffs are shown in Figure 1.8.



**Figure 1.8:** Example building length and area takeoffs

The glazing area above shows the differences between the glazing and opaque wall areas; however, glazing is not included with the opaque wall U-value calculations.

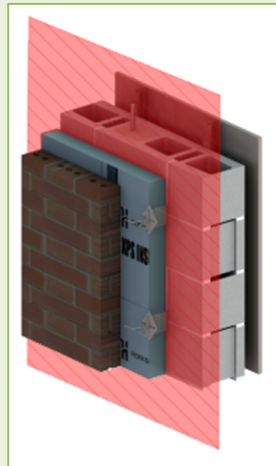
Once the thermal performance values of the clear wall and interface details are known, and the lengths and areas found, the overall U-value for the brick wall can be determined:

$$U_{overall} = \frac{\Psi_{parapet} \cdot L_{parapet} + \Psi_{slab} \cdot L_{slab} + \Psi_{transition} \cdot L_{transition} + \Psi_{corner} \cdot L_{corner}}{A_{Opaque\ Brick\ Wall\ Area}} + U_{brick\ clear\ wall}$$

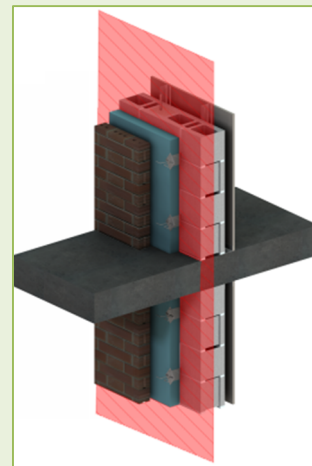
For some of the interface details, there are additional considerations as to where to assign the extra heat flow. In the above example, the brick wall was connected to a curtain-wall system with spandrel. The corner interface detail is connected to both assemblies, and in the above calculation, the heat flow through the corner was assigned entirely to the brick wall. Alternatively, it could have been assigned entirely to the brick wall or the curtain-wall or split evenly between the two. It is up to the designer to decide how they wish to divide up the building U-values. This matters mostly for energy models as the heat flow through each envelope section gets assigned to a particular building thermal zone. This same concept applies to a parapet as it acts as a corner between the roof and the walls. However, it may not matter if the heat flow through the parapet is assigned to the wall or to the roof as both are connected to the same interior thermal zone. For wall to glazing transitions, the additional heat flow is assigned to the wall and not the glazing, thereby NFRC standards can be utilized for determining the U-value of glazing separately (Mitchell, et al., Rev 2013). When there are slabs, the clear wall area includes the projected area of slab edges, including balcony slabs.

## Length and Area Takeoffs and the Plane of Heat Transfer

The plane of heat transfer for the building envelope is a theoretical projected area between the interior and exterior conditions through which heat flows. In order for there to be a heat loss or heat gain through the building envelope, energy must pass through this plane of heat transfer. A building assembly may have some elaborate features that extend out past the building envelope; however, all that is important for thermal performance is where the heat flow passes the plane of heat transfer into or out of the building.

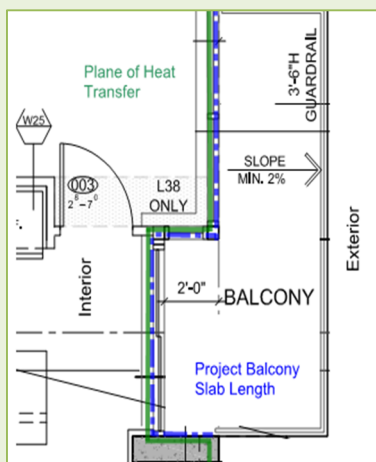


Plane of heat transfer  
through a wall

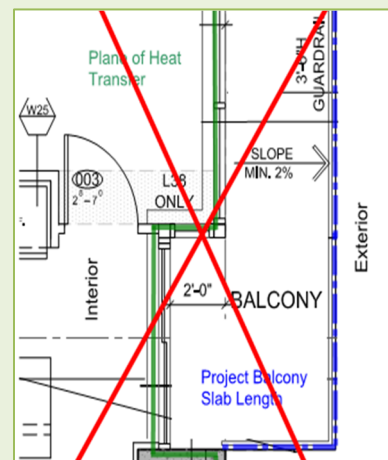


Plane of heat transfer  
through a projected  
balcony

For flat objects (i.e. walls) the plane of heat transfer is easy to visualize. With projections, such as balcony slabs, it may not be immediately intuitive where the plane is; however, since it is only important where the heat flows through the building envelope, the plane of heat transfer is the same as the flat wall. The areas of details that project out of the building envelope are not necessary for calculations. The heat flows as a result of these projections are accounted for in the linear transmittance of that detail. If there was a significant difference in heat flow as a result of the distance of the projection (i.e. a balcony that projected 1m from the wall compared to one that projects 3m from the wall) then there would be a different linear transmittance value. However, it should be noted that for the details in this guide, the projected distances of the balconies had minimal effect on the linear transmittance values for the projected slabs. When determining length takeoffs for projections for use in overall thermal performance calculations, only the lengths along the plane of heat transfer should be used. For example, for balcony slabs, use the length where the balcony intersects the wall and NOT the outside perimeter length of the balcony. Similarly for parapets, the length around the parapet is not needed.



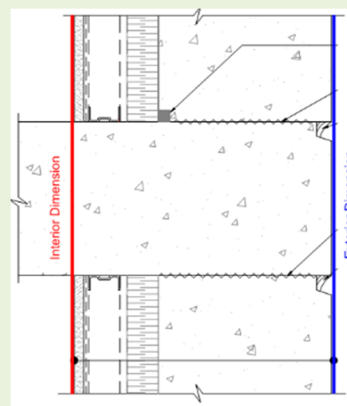
Correct Projected  
Balcony Slab  
Length for  
Calculations



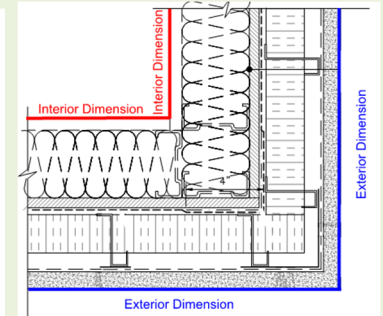
Incorrect Project  
Balcony Slab Length  
for Calculations

## A Note on Length and Area Takeoffs for the Detail Oriented

The lengths for linear transmittances are usually easiest to find using building elevation drawings, which are exterior dimensions. Some further investigation for take offs may be required, such as looking at interior section views, when a detail is obstructed by other building features (i.e. the cladding). However, getting the takeoff lengths and areas from the exterior or the interior dimensions will result in slight differences on the overall U-value, depending on how the linear transmittances are reported. The way in which the linear transmittances are reported for this guide are such that if mixed interior and exterior dimensions are used, then the U-values will be slightly more conservative. This is typically not a concern as the differences from mixing interior and exterior dimensions are minor and there are already inherent discrepancies between architectural drawings and what is built on site. The following information is for those designers who want that extra level of precision.



Interior/Exterior Dimensions  
for a single plane  
assembly



Interior/Exterior  
Dimensions for a multi-  
plane assembly

The formulation of linear transmittance values is dependent on the area of the plane of heat transfer through the modeled assembly. In most cases, figuring out the plane of heat transfer is straight forward. For straight building objects, like a wall, heat transfer between the interior and the exterior is in a single plane, through the wall, so the interior and exterior dimensions will be the same. However, for an angled detail like an outside corner, the heat transfer is in more than one plane and the interior and exterior dimensions are different.

Remembering that the linear transmittance is an extra heat flow caused by an interference detail compared to the clear field heat flow, the calculation of  $\Psi$  is dependent on the area of the clear field used in the calculation. Due to conservation of energy, the heat flow in equals the heat flow out, and the overall amount is the same regardless of the dimension chosen. However, assigning the degree of that heat flow between the clear field and the detail is where the issue lies.

**Example:** For the outside corner shown above, if the clear field area is assumed to be the interior dimensions, which are smaller, then the heat flow contribution from the clear field will be smaller and the rest is assigned to the corner. If the clear field is assumed to be the exterior dimensions, then the heat flow contribution through the clear field will be larger, with a smaller amount assigned to the corner. This results in a smaller or larger calculated linear transmittance depending on the dimension used, however, the resultant heat flow **should be identical** when the correct lengths are used in U-value calculations.

If a linear transmittance for a multi-plane assembly was determined using interior dimensions, and the takeoff lengths for the detail use exterior dimensions, then the heat flow through that detail will be slightly overestimated for outside corners and parapets since the exterior dimensions are typically larger than the interior dimensions. This overestimation is the same magnitude as using exterior dimensions for any U-value calculation and is equal to the clear field U-value multiplied by the difference in area between the interior and exterior dimensions.

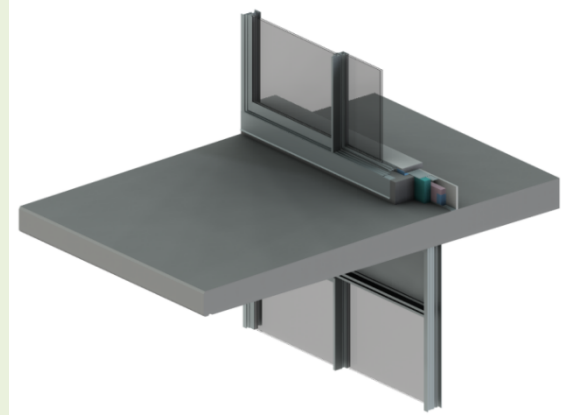
To be most precise, the locations for the takeoffs in multi-plane assemblies should match with how the linear transmittance is reported. Alternatively, the difference between the interior and exterior dimensions on either side of the corner is actually just the wall thickness. The heat flow through a section of clear wall the size of the wall thickness could be subtracted from the overall heat flow in order to remove the overestimation. However, it should be noted that multi-plane assemblies are typically parapets and corners and this may only be a consideration in smaller buildings (less than four storeys) if the parapet or corner details have a high linear transmittance.

ISO 14683 (CEN, 2007) reports multiple linear transmittances for interface details based on different dimensioning systems. While this is thorough, the intent of the methodology in ASHRAE 1365-RP (Morrison Hershfield Ltd, 2011) was to simplify calculations; therefore only one transmittance value, reported from interior dimensions, is given per insulation level per interface detail in this guide. Differences in exterior and interior dimensions with linear transmittances are further discussed in (Janssens, et al., 2007).

## Dealing with Floor to Ceiling Glazing

An issue that arises when determining lengths and areas for heat loss calculations is glazing that spans floor to ceiling. In the methodology presented in the guide, glazing and opaque envelope areas are accounted for separately when calculating heat loss, with additional heat loss from interface details added to the opaque areas. Thus, a situation arises when there is floor to ceiling glazing from slab to slab and there is no discernible opaque clear wall area.

In calculating the linear transmittance of a detail, the value is based on an additive amount of heat flow from the detail to the clear field assembly associated with that detail. For example, the linear transmittance of a balcony going through an interior insulated concrete wall is the difference in heat loss between the same sized assembly with and without the balcony there. In the calculations for the overall U-value, we prescribe an area to the total assembly, and a portion of that assembly is interrupted by details. We calculate the total U-value by adding the heat loss associated with thermal bridging at interface details to the clear field heat loss. However, with floor to ceiling glazing, the slab is flanked by glazing assemblies, which presents a situation where there is not an obvious clear wall thermal transmittance.



**Assembly without an opaque clear field**

The linear transmittances for the details in section 8.0 Balcones and Doors in Appendix A and B were calculated by subtracting out the glazing heat flow above and below the slab. There are many possible wall assemblies that can be adjacent to the balcony sliding door and balcony slab.

Using the linear transmittance values directly and including the areas of the slabs between the floor to ceiling glazing as clear field area may result in a more conservative overall U-value since the clear field area is being over accounted for. The results for the balcony details presented in Appendix B are presented in a few alternative formats than for the other interface details. The reason for this deviation is to allow the data to be applied broadly to many variations and to make the information easy and flexible to use. Balconies can be factored into U-value calculations using the following approaches.

### 1) U-value Approach

U-values of the opaque area of balconies are presented in the thermal performance data sheets in Appendix B. These U-values can be treated as its own wall assembly, or averaged into the adjacent assembly using an area weighted calculation. If using area weighted calculations, then the total projected area of the slabs need to be determined separately from the area of the adjacent walls.

### 2) Linear Transmittance without Area

Linear transmittances are provided in section 8.0 of Appendix B for balconies where it has been assumed there is no clear field. These values are essential a delta U that can be added to any adjacent wall assembly. However, in the calculations the clear wall heat loss should not include the area of the slabs. In the U-value equation given in section 1.25, the clear field  $U_o$  term should be corrected by multiplying it by the following factor,  $A_{\text{adjacent wall}} / A_{\text{total}}$ , where the area of the adjacent wall is the total area minus the area over the slab edge at the floor the floor glazing.

In each assembly where choosing one of these approaches in necessary, it has been indicated in the thermal performance results sheets in Appendix B.

## 1.3 SUMMARY OF THE THERMAL PERFORMANCE CATALOGUE

### 1.3.1 CATALOGUE BREAKDOWN

The catalogue prepared for this guide contains extensive thermal performance information on numerous common details, along with details intended to mitigate thermal bridging, including some emerging technologies and products. This data was calculated using the methodology from 1365-RP (including air films), as summarized in Section 1.2. The catalogue also contains thermal performance information from ASHRAE 1365-RP, along with other details previously analyzed by Morrison Hershfield Ltd. The catalogue is broken into two main sections:

- **Appendix A** contains an overview of the assemblies and interface details. This includes isometric drawings, dimensions and material properties.
- **Appendix B** contains the thermal performance information. This includes clear field, linear and point transmittance values, where applicable, along with overall U-values for the modeled assembly sizes and temperature indices.

For the catalogue, the details have been arranged first by construction type (steel framed, mass wall etc.), then by transmittance type (clear field, slabs, parapets, etc.). Table 1.1 shows how the catalogue is arranged. Table 1.2 summarizes the basic outline of what types of details are featured in the catalogue. A more detailed discussion on the catalogue information is given at the beginning of Appendices A and B.

**Table 1.1: Catalogue Index**

BC Thermal Study Catalogue
1. Window-wall
2. Conventional Curtain-wall
3. Unitized Curtain-wall
4. High Performance Curtain-wall
5. Steel Stud Construction
6. Concrete Construction
7. Wood Frame Construction
8. Doors and Balconies
9. Roofs

**Table 1.2: Thermal Performance Catalogue Index**

Detail Type	Detail Sub-Category
Clear Field Assemblies	wall, roof, spandrel section, cladding attachment method, insulation strategy
At-grade Transitions	exposed, exterior insulated, wood
Floor and Balcony Slab Transitions	exposed, under-insulated, shelf angle, manufactured thermal break, exterior insulated, wood
Glazing Transitions	un-insulated, misaligned insulation, efficiently aligned
Interior Wall Intersections	exposed, exterior insulated
Corners	interior insulated, exterior insulated
Parapets	exposed, under-insulated, manufactured thermal break, exterior insulated, wood
Roofs	penetrations, transitions
Structural Beams	through beam, manufactured thermal break



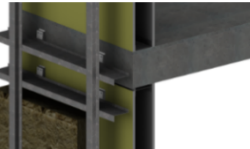
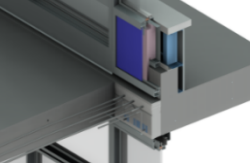
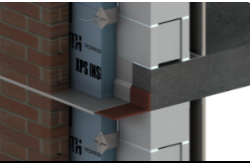

The beginning of Appendix B also includes a visual summary of the catalogue details. This includes a brief summary of each detail and key thermal performance values. These are arranged first by transmittance type ( $U$ ,  $\Psi$ ,  $\chi$ ) then by transmittance value. The inclusion of this visual summary is to facilitate faster navigation through the catalogue and provide another option for disseminating details for designers.

Many projects have architectural packages that can contain an overwhelming number of details (150+), and accounting for every interface detail can be time consuming and impractical. An intent of providing a catalogue is that by becoming familiar with the assemblies and interface details included here, designers will be able to estimate when interface details will have an impact on the building envelope and when similar details can be grouped together. As with any estimating process, good judgment will always be required.

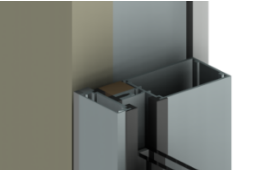
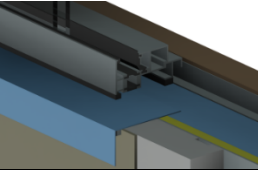
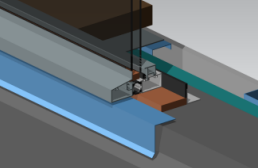
### 1.3.2 THERMAL PERFORMANCE CATEGORIES

Previous work has been done (Janssens, et al., 2007) to categorize thermal transmittances in terms of performance in order to help designers compare details and set expectations for details that have not been explicitly modeled. All the details in this catalogue have been assigned a rating, from poor to efficient, based on the range of thermal transmittances between similar types of details. Due to the large number of slab, parapet and glazing transition details analyzed in preparation for this guide (approximately 30+ for each), separate linear transmittance ranges were created for each of those detail types. For other details, such as corners and partition walls, there are too few variations to create a performance range for that specific detail type. As such, they are all included in “Other Interface Details”. The ranges for Slabs, Glazing Transitions, Parapets and Other Interface Details are given in Tables 1.3, 1.4, 1.5 and 1.6 respectively. The visual summary, shown at the beginning of Appendix B, includes the performance categories within each detail summary.

**Table 1.3:** Performance Categories and Default Transmittances for Floor and Balcony Slabs

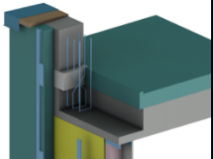
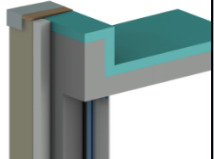
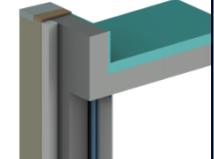
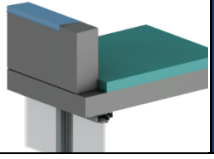
	Performance Category		Description and Examples	Linear Transmittance	
				$\frac{\text{Btu}}{\text{hr ft}^2 \text{F}}$	$\frac{\text{W}}{\text{m}^2 \text{K}}$
FLOOR AND BALCONY SLABS		Efficient	<b>Fully insulated with only small conductive bypasses</b> Examples: exterior insulated wall and floor slab.	0.12	0.2
		Improved	<b>Thermally broken and intermittent structural connections</b> Examples: structural thermal breaks, stand-off shelf angles.	0.20	0.35
		Regular	<b>Under-insulated and continuous structural connections</b> Examples: partial insulated floor (i.e. firestop), shelf angles attached directly to the floor slab.	0.29	0.5
		Poor	<b>Un-insulated and major conductive bypasses</b> Examples: un-insulated balconies and exposed floor slabs.	0.58	1.0

**Table 1.4:** Performance Categories and Default Transmittances for Glazing Transitions

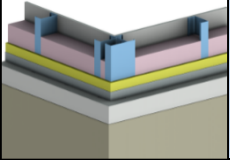

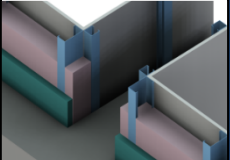
	Performance Category		Description and Examples	Linear Transmittance	
				$\frac{\text{Btu}}{\text{hr ft}^2 \text{F}}$	$\frac{\text{W}}{\text{m}^2 \text{K}}$
GLAZING TRANSITIONS		Efficient	<b>Well aligned glazing without conductive bypasses</b> Examples: wall insulation is aligned with the glazing thermal break. Flashing does not bypass the thermal break.	0.12	0.2
		Regular	<b>Misaligned glazing and minor conductive bypasses</b> Examples: wall insulation is not continuous to thermal break and framing bypasses the thermal insulation at glazing interface.	0.20	0.35
		Poor	<b>Un-insulated and conductive bypasses</b> Examples: metal closures connected to structural framing. Un-insulated concrete opening (wall insulation ends at edge of opening).	0.29	0.5



**Table 1.5:** Performance Categories and Default Transmittances for Parapets

PARAPETS	Performance Category		Description and Examples	Linear Transmittance	
				$\frac{\text{Btu}}{\text{hr ft F}}$	$\frac{\text{W}}{\text{m K}}$
		Efficient	<b>Roof and Wall Insulation Meet at the Roof Deck</b> Examples: structural thermal break at roof deck, wood-frame parapet.	0.12	0.2
		Improved	<b>Fully Insulated Parapet</b> Examples: insulation wraps around the parapet to the same insulation level as the roof and wall.	0.17	0.3
		Regular	<b>Under-insulated Parapets</b> Examples: concrete parapet is partially insulated (less than roof insulation), insulated steel framed parapet, concrete block parapet.	0.26	0.45
		Poor	<b>Un-insulated and major conductive bypasses</b> Examples: exposed parapet and roof deck.	0.46	0.8

**Table 1.6:** Performance Categories and Default Transmittances for Other Interface Details

OTHER INTERFACE DETAILS	Performance Category		Description and Examples	Linear Transmittance	
				$\frac{\text{Btu}}{\text{hr ft F}}$	$\frac{\text{W}}{\text{m K}}$
		Efficient	<b>Minor Thermal Bridging at Miscellaneous Details</b> Examples: extra framing at corners of steel framed walls, wood-frame to foundation wall interface.	0.12	0.2
		Regular	<b>Moderate Thermal Bridging at Miscellaneous Details</b> Examples: insulation returns into a concrete shear wall, exterior insulated wall at interface with insulated footing.	0.26	0.45
		Poor	<b>Major Thermal Bridging at Miscellaneous Details</b> Examples: un-insulated concrete shear wall, exposed footing at exterior insulated wall with insulation below floor slab.	0.49	0.85

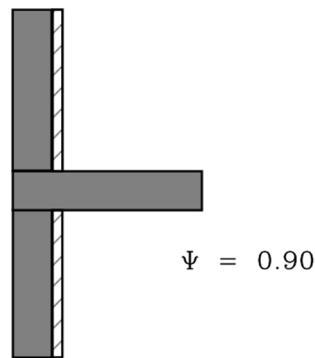
Rating details based on expected transmittance ranges has several uses:

1. Not every common interface detail has been evaluated and cataloged in this guide. Ranges help with estimating the order of magnitude of transmittance values for interface details that are not directly covered by the catalogue, without the need for further evaluation.
2. Some project specific interface details will still require further evaluation. The ranges for transmittances help set expectations for evaluating other interface details.
3. Ratings can establish default assumptions and/or set prescriptive requirements for the inclusion of interface details in codes and energy standards.
4. Similarly, ratings can establish values for the baseline buildings of the performance compliance paths in energy standards and/or performance rating programs (for example LEED).
5. Ranges for interface details can help set thermal performance targets for the building envelope early in design. When included with a preliminary energy model (before details are even chosen) the ranges can show what can be expected from the building envelope based on a given construction type.

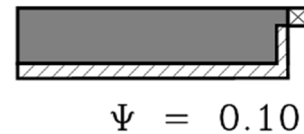
### 1.3.3 OTHER SOURCES OF INFORMATION

While the catalogue provided with this guide is extensive, there are additional sources to find thermal performance data for clear field assemblies and linear and point transmittances. Here are a few examples:

- Appendix A of **ASHRAE 90.1 “Energy Standard for Buildings Except Low-Rise Residential”** (ASHRAE, 2010) contains several tables of thermal performance values for a variety of clear field constructions, including walls, roofs and floors for concrete, steel framed and wood framed constructions. The values for many of the exterior insulated structures assume continuous insulation and do not account for cladding attachments which interrupt the exterior insulation.
- **Manufacturers of proprietary systems**, such as structural cladding attachments or curtain-wall systems, often have thermal performance data of their products. Upon request they can provide designers with the information. However, be aware that different manufacturers may calculate thermal performance using various procedures, sometimes making it difficult to compare different systems appropriately. If the manufacturer does not provide a full report on their thermal performance values, it may be prudent to request further information.
- In the absence of more specific information, **ISO 14683:2007 “Thermal Bridges in Building Construction”** (CEN, 2007) provides generic linear transmittances for simplified constructions. This standard outlines the methods of calculating linear transmission used in the European standards and provides an Annex with default  $\Psi$  values for many of the common interface details. The default values are based on very basic geometric shapes representing building components, as shown in Figures 1.9 and 1.10, resulting in conservative transmittance values. For example, complex heat flow paths created by misaligned glazing thermal breaks or flashing are not captured by these values. This standard also provides multiple linear transmittances based on different dimensioning procedures. See the breakout box “A Note on Linear Length and Area Takeoffs for the Detail Oriented” in section 1.2.6 for more information.



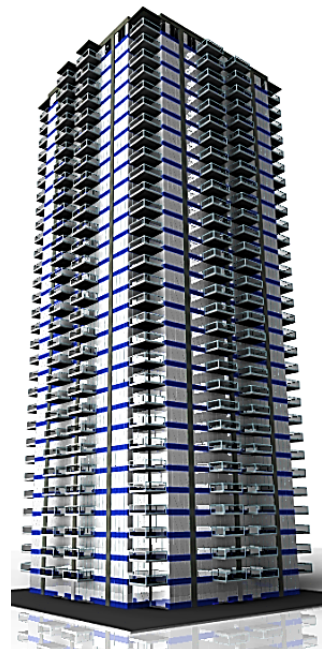
**Figure 1.9:** A reproduction of a simplified concrete wall assembly with interior insulation at through wall slab from ISO 14683:2007



**Figure 1.10:** A reproduction of a simplified concrete wall assembly at a window jamb from ISO 14683:2007

## 1.4 EXAMPLE UTILIZATION OF THE CATALOGUE

In order to demonstrate how to utilize the catalogue in calculating overall U-values for a building, the following is a step-by-step example for a common Vancouver residential high-rise building.



**Figure 1.11:** Example High-Rise MURB with 60% glazing

**Example:** A designer wishes to find the overall U-value for each construction type for a High-Rise Multi-unit Residential Building with 60% glazing.

The building (illustrated in Figure 1.11) is concrete construction, with an R-11 (RSI-1.94) interior insulated concrete wall between window-wall sections. The window-wall sections include a glazed section (U-0.4, USI-2.3) and spandrel section with R-8.4 (RSI-1.48) insulated backpan. The roof contains an R-20 (RSI-3.52) insulated deck that has several beam penetrations and curbs to support an architectural feature. There are balconies, exposed concrete slab edges and window-wall bypasses. All details are typical and assumed to be contained within an architectural drawing package.

### Step 1: Determine How to Divide Up the Building

In calculating building envelope U-values, first it should be known how the U-values will be used. U-values can be calculated for different areas depending on how the U-value will be utilized or level of detail required. For example, the building envelope performance could be divided by zone to find specific zone heating loads, by construction type for whole building energy analysis or kept as one value for the whole building for preliminary design. The methodology to find the different U-values are the same and it is up to the judgment of the designer on what they require.

*In this example, the designer chooses to divide the building by construction type.*

## Step 2: Determine Clear Field Assemblies

The construction types can be determined through the clear field assemblies, which can be found from wall/roof/floor schedules, as shown in Figure 1.12, but also by sorting through the elevations and detail drawings. There may be multiple clear field assemblies for a single construction type (i.e. several steel stud assemblies), but if they are similar enough in thermal transmittance, with good judgment they can be combined and considered one assembly.

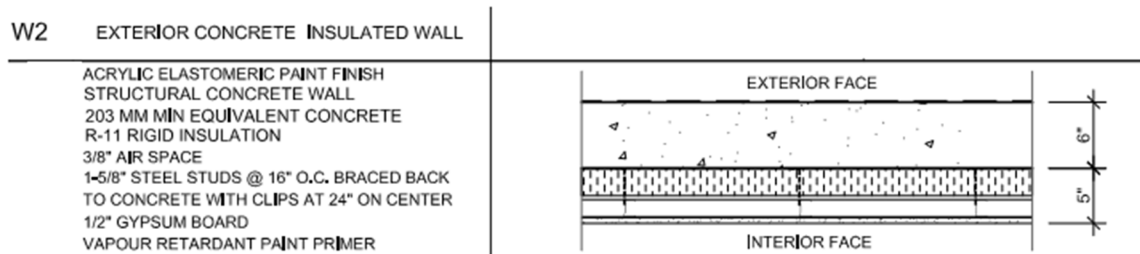


Figure 1.12: Example concrete clear field wall assembly

For this example, from the architectural drawings, the designer finds there are three distinct construction types in the wall and roof schedules: Concrete Wall, Concrete Roof and Window-wall Spandrel.

## Step 3: Determine Linear and Point Details

After determining the clear field assemblies, the types of linear and point details need to be found. In architectural drawings, these can be found through elevations, plans and detail drawings, as shown in Figures 1.13 and 1.14.

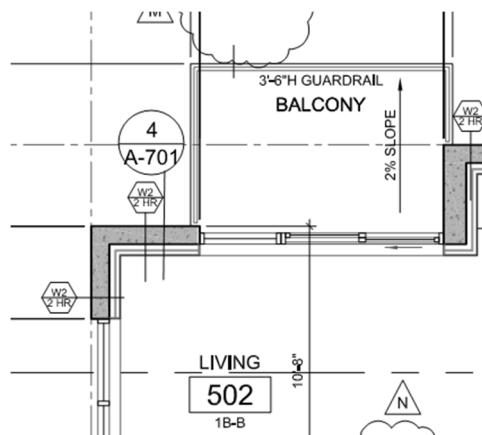


Figure 1.13: Exposed Floor Slab in Plan 4/A701

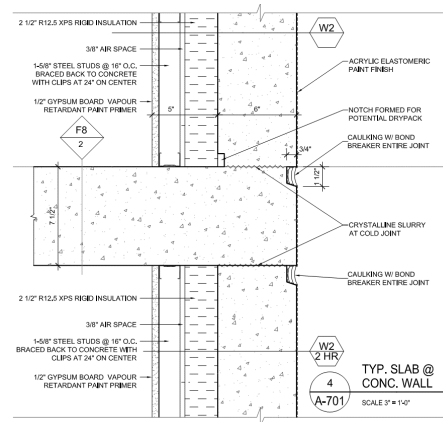


Figure 1.14: Exposed Floor Slab detail 4/A701

When dividing by construction type, the interface details can also be divided in the same way and can be assigned to specific clear field assemblies. For each clear field assembly there will be a set of linear and/or point details associated with it. For transitions between different clear field assemblies (such as a parapet transition between wall and roof) it is up to the designer to choose which assembly to assign the heat loss to.

For this example, an isometric floor plan is given in Figure 1.15. From the architectural drawings, the designer determines there are several standard details and assigns them to the concrete wall, the window-wall spandrel or the roof. In this case, the designer assigns the parapets to the walls. In the drawings, the designer finds there are only balcony slabs at the spandrel sections. The transmittance types are summarized in Table 1.7. For the simplicity of this example, other miscellaneous details have been omitted.

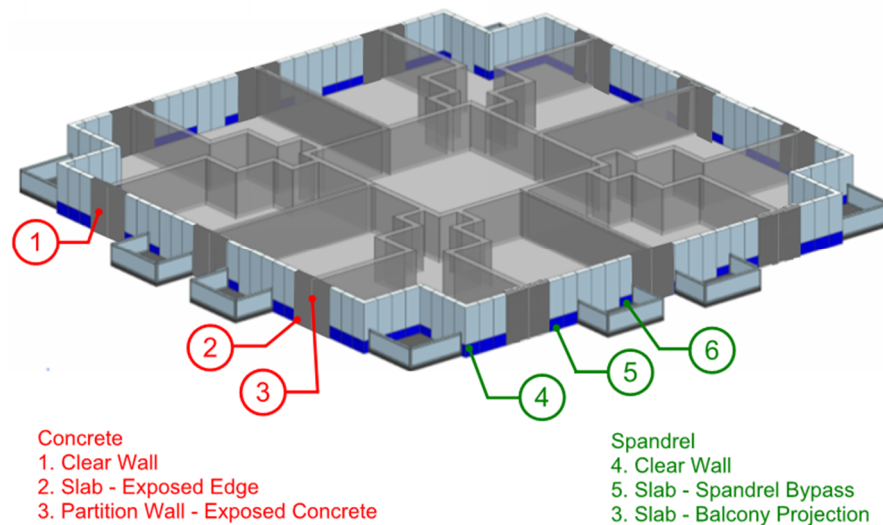
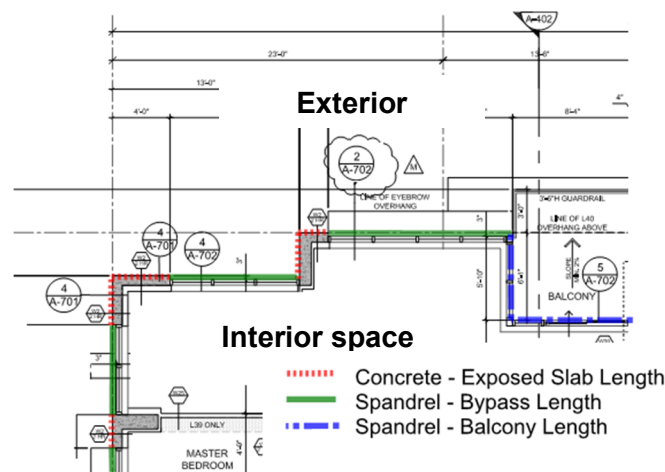


Figure 1.15: Example building typical floor plan

Table 1.7: Summary of Steps 1-3 for Example building

Step 1-2	Step 3
Transmittance Type	
Concrete Wall	Clear Field – Concrete Wall
	Parapet – Exposed Concrete
	Slab - Exposed Concrete Edge
	Slab - At Grade Transition
	Partition Wall - Exposed Concrete
Window-wall Spandrel	Clear Field – Spandrel
	Parapet – Partially insulated by Spandrel
	Slab – Spandrel Bypass
	Slab – Spandrel with Balcony projection
	Slab - At Grade Transition
Roof	Clear Field – Roof
	Curb – Uninsulated
	Point Penetrations – Structural Beams

With the types of transmittances (clear field, linear and point) found, the area, lengths and number of instances should be determined. Information on takeoffs is given in section 1.2.6. Areas for the clear field can typically be easiest to determine from elevation drawings. Lengths for slabs, parapets and other horizontal linear details can be found through plans, while lengths for vertical linear details (such as corners) can be found in the elevations. An example takeoff for slab edges is shown in Figure 1.16.



**Figure 1.16:** Example slab length takeoff

Using the floor plans and elevations, the designer determines the appropriate takeoffs for each detail they determined in Table 1.7. Using the elevations, the areas of the clear fields (including areas over the slab edges) are found. The slab edge lengths for a single floor are calculated, and then are multiplied by the amount of similar floors in the building. Each of the partition walls are found to extend the height of the building. The parapet lengths and curb lengths and number of beam penetrations are found using the roof plan and the at-grade transitions are found using the ground floor plan. Takeoff areas and lengths for this example are given in Table 1.8.

Thermal performance data for clear field, linear and point details can be found in the catalogue provided with this guide, or through other sources (outlined in section 1.3.3). The project specific interface details can be matched up with the catalogue details in Appendix A and the thermal values are given in Appendix B. If a specific project detail cannot be found in the catalogue, judgment will be required to estimate the thermal performance by comparing similar details or by using the ranges in section 1.3.2. If that cannot be done with certainty, then further modeling may be necessary.

*For this example, the designer matches as many clear field assemblies and interface details to the catalogue as they can. The designer first looks at the visual summary in Appendix B, then narrows down to the specific details. The designer finds the following:*

- For the concrete wall clear field and interface details, the designer finds appropriate matching details in Appendix A.6 – Mass Walls and the thermal values for those details in Appendix B.6, except for the at-grade transition.



- The designer finds an appropriate linear transmittance for the concrete at-grade transition in ISO 14863.
- For the spandrel wall clear field and interface details, the designer finds appropriate matching details in Appendix A.1 – Window-wall and Appendix A.8 – Balconies and Doors, along with the thermal data in Appendix B.1 and B.8, except for the at-grade transition.
- The designer estimates the at-grade transition by comparing their project detail to a similar conventional curtain-wall Detail 2.5.1.
- The designer finds matching roof details in Appendix A.9 – Roofs along with the matching thermal data in Appendix B.9.
- The designer decides not enough information is available to estimate the roof penetrations and decides to have that detail modeled.

Detail references and transmittances for this example are given in Table 1.8.

### Step 6 (Optional): Calculate Individual Transmittance Heat Flow

While not necessary to calculate the overall U-value, it may be advantageous for designers to calculate the individual heat flows associated with specific details to help make better design decisions and identify details that should be targeted. Recognizing components of the U-value equation given in section 1.2.5, the individual heat flows can be calculated using the following:

- Clear Field Heat Flow =  $U_o \cdot A$
- Linear Transmittance Heat Flow =  $\Psi \cdot L$
- Point Transmittance Heat Flow =  $\chi \cdot \text{number of occurrences}$

For this example, the designer calculates the heat flow through the individual details to see which interface details have the largest impact on thermal performance. From that analysis the designer is able to determine which details should be a priority to improve. Individual heat flows for this example are given in Table 1.8.

### Step 7: Calculate Overall U-Value

With all the transmittance values and takeoff areas/lengths known, the overall Wall/Roof U-values can be calculated using the equation given in section 1.2.5.

$$U_T = \frac{\Sigma(\Psi \cdot L) + \Sigma(\chi)}{A_{Total}} + U_o$$

If the individual heat flows have already been determined in Step 6, then all of the heat flows can be summed together and divided by the total opaque area (in this case, the clear field area) to get the overall U-value that includes the effects of thermal bridging at interface details.

The designer calculates the overall U-values for each construction type, along with an overall Opaque Wall U-value and Opaque Roof U-value separately. The summary of all steps for the example building is given in Table 1.8 and 1.9 for the walls and roof respectively.

**Table 1.8:** Summary of Calculation Steps 1-7 for Example Building Opaque Wall

Step 1-2	Step 3	Step 4	Step 5		Step 6-7	
Transmittance Type		Quantity	Detail Ref.	Transmittance	Heat Flow (W/K)	% of Total Heat Flow
Concrete Wall	Clear Field	2987 m <sup>2</sup>	6.2.2	0.42 W/m <sup>2</sup> K	1254	16%
	Parapet	27 m	6.5.3	0.78 W/mK	21	<1%
	Exposed Floor Slab	1090 m	6.2.5	1.00 W/mK	1085	14%
	At Grade Transition	27 m	ISO-14863	0.75 W/mK	20	<1%
	Partition Wall	1315 m	6.2.2	0.67 W/mK	876	11%
Overall Concrete Wall U-value, BTU / hr ft <sup>2</sup> °F (W/m <sup>2</sup> K)					<b>0.192 (1.09)</b>	
Overall Concrete Wall R-value, hr ft <sup>2</sup> °F/ BTU (m <sup>2</sup> K/W)					<b>5.2 (0.92)</b>	
Window-wall Spandrel	Clear Field	1792 m <sup>2</sup>	1.1.1	1.07 W/m <sup>2</sup> K	1917	24%
	Parapet	82 m	1.3.2	0.72 W/mK	59	<1%
	Slab Bypass	1635 m	1.2.1	0.58 W/mK	945	12%
	Balcony Slab	1635 m	8.1.9	1.11 W/mK	1815	23%
	At Grade Transition	82 m	2.5.1 (est.)	0.86 W/mK	70	<1%
Overall Spandrel Wall U-value, BTU / hr ft <sup>2</sup> °F (W/m <sup>2</sup> K)					<b>0.472 (2.68)</b>	
Overall Spandrel Wall R-value, hr ft <sup>2</sup> °F/ BTU (m <sup>2</sup> K/W)					<b>2.11 (0.37)</b>	
Total (W/K)					<b>8063</b>	<b>100%</b>
Overall Opaque Wall U-value, BTU / hr ft <sup>2</sup> °F (W/m <sup>2</sup> K)					<b>0.297 (1.68)</b>	
Overall Opaque Wall R-value, hr ft <sup>2</sup> °F/ BTU (m <sup>2</sup> K/W)					<b>3.4 (0.59)</b>	

**Table 1.9:** Summary of Calculation Steps 1-7 for Example Building Opaque Roof

Transmittance Type		Quantity	Detail Ref.	Transmittance	Heat Flow (W/K)	% of Total Heat Flow
Roof	Clear Field	743 m <sup>2</sup>	9.2.2	0.27 W/m <sup>2</sup> K	200	82%
	Curbs	20 m	9.2.2	0.93 W/m K	19	8%
	Beam Penetrations	#20	Modelled	1.2 W/K	24	10%
Overall Roof U-value, BTU / hr ft <sup>2</sup> °F (W/m <sup>2</sup> K)					<b>0.058 (0.33)</b>	
Overall Roof R-value, hr ft <sup>2</sup> °F/ BTU (m <sup>2</sup> K/W)					<b>17.3 (3.05)</b>	

*Even though it takes up less area of opaque wall than the concrete, the designer can see that the largest amount of heat flow is associated with the spandrel section clear field, but the heat flow through the window-wall bypass and the balconies is also significant.*



## 1.5 INPUTTING THERMAL VALUES INTO ENERGY MODELS

Determining overall building performance, including the combined interaction between envelope, mechanical and electrical systems, is often termed “whole building energy analysis” and is often assessed using computer simulation and is used for multiple purposes, including:

- Design decision making through parametric analysis, by considering the energy and cost impact of design decisions to reduce energy or meet code
- Demonstrating compliance with energy codes
- Comparing a proposed building to a reference building for green building rating systems (LEED, Green Globes, etc.)
- Estimating energy use in new or existing buildings
- Estimating the impact of operational improvements or capital investments in existing buildings
- Heat loss calculations for mechanical system sizing

One of the main drivers for creating this guide was to provide more accurate thermal values and a methodology for designers to assist in creating more precise energy models.

Currently, there are few energy modeling programs that allow linear transmittance values to be input directly into energy simulations. While this feature is being considered for development for common building energy simulation software, at the moment this ability is not widely available. Thermal transmittances are either directly inputted as wall, roof or floor U-values or determined by using construction layers to build up the building envelope assemblies. For either case, the overall U-value that includes the effects of linear and points transmittances must first be determined without the assistance of the energy modeling software to ensure that the correct thermal transmittances will be processed by the model.

It is important to emphasize that air leakage and dynamic thermal responses are accounted for by separate functions in typical whole building energy models. Thermal bridging is accounted for only in the thermal transmittances that are processed by the energy model. See Appendix C for an explanation of how energy models take into account thermal mass separately from thermal transmittances.

Many modeling programs use construction layers to build up the building envelope assemblies based on material properties. To account for thermal bridging, all the material properties should be left as is, while only the insulating layer R-value should be de-rated such that the correct overall U-value determined from calculation is matched and output by the software. This method allows for the functions that account for thermal mass to be approximated by the software.

**Example:** a section of concrete wall with R-15 exterior insulation contains a balcony slab and is calculated to have an overall U-value of U-0.16. The energy modeling program being used requires construction layers as the inputs. The layers are input with default values for the air films, cladding, airspaces, concrete and interior finishes and the simulation output shows a U-value of U-0.05. The exterior insulation R-value is edited and decreased from R-15 such that in the simulation output, the U-value for the overall wall assembly matches U-0.16.

One final note on model inputs, the clear field U-values given in the thermal performance catalogue in this guide are based on the ASHRAE 1365-RP methodology, which include air films. Many energy modeling programs calculate air films separately. The air films for the modeled details in this guide are listed with the material properties in each of the details in Appendix A. The thermal resistance of these air films may need to be subtracted out before entering R- or U-values into an energy modeling program.

## 1.6 REFERENCES

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