

Harmony of the spheres

Universal musical key

(The golden ratio and the Science of harmonics)



1st part: Introduction

If you love music, take a few minutes of your time and read attentively what is following and discover one of the greatest inventions based on a new musical perception. Everything started when the inventor associate together the diatonic scale and the chromatic scale by using numbers to indicate each degree (see Fig.1). By looking at the numbers that correspond to the intervals that constitute a Perfect Major Chord, you can see appear the legendary Fibonacci sequence (the golden section - PHI - or the divine proportion). With the discovery of a “Musical Universal Key”, M. Sylvain Lalonde, the inventor, demonstrates where this revolutionary easy approach method begin.

With the research of the harmony



The golden section influences the Western vision of the harmony
The sequence of Fibonacci... 1-1-2-3-5-8-13... applies to this rule

Ex: Perfect Majeur Chords: C,E,G,C

Tonic	Tone		Second	Tone		Third	Semitone	Tone		Fourth	Tone		Fifth	Tone		Sixth	Tone		Seventh	Semitone		Octave
	1	2		3	4		5	6	7		8	9		10	11		12	13				
1	C [#]	D ^b	2	D [#]	E ^b	3	E	F	F [#]	G ^b	4	G	G [#]	A ^b	5	A	A [#]	B ^b	6	B	7	C
C			D			E		F			G		G [#]		A		A [#]		B		C	
1	2	3	4	5	6	7	8	9	10	11	12	13										
Semitone		Semitone		Semitone		Semitone		Semitone		Semitone		Semitone		Semitone		Semitone		Semitone		Semitone		
A													B									

When $(A + B) / A = A / B$. The A / B ratio is then equal to the golden ratio.

$$8 / 5 = 1.6$$

Uclide d'Alexandrie

* For more details on natural harmonics see fig.6 & 7 section R&D
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2nd part: Diatonic scale vs Chromatic scale

12 Sounds = 12 Tones = 12 Tonalties

Let's look at the same graphics on a 360-degree platform.. The use of black and white is used to represent the notes of a piano, to help understand this new perception.

Select and print Fig. 3 (picture) cut the two discs, then cut down the 7 windows that correspond to the intervals on disc 1 (Item 32). Overlap disc 1 over the second disc (Item 30) and then position the 1st degree (“Tonic”) on C, you’ll get the “C-D-E-F-G-A-B” sequence.

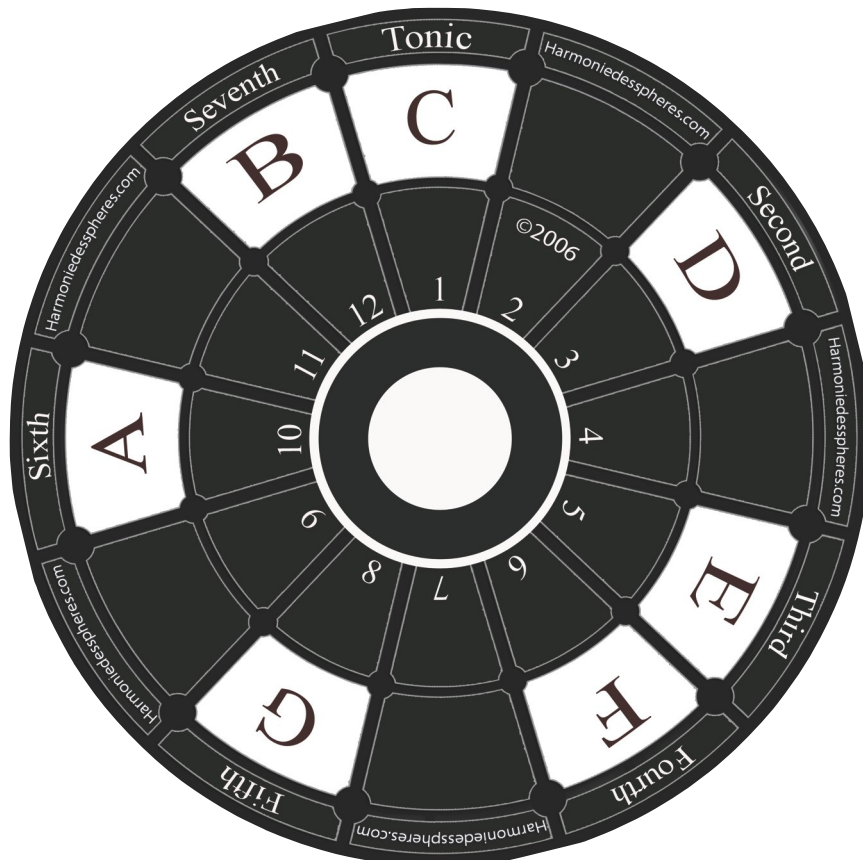
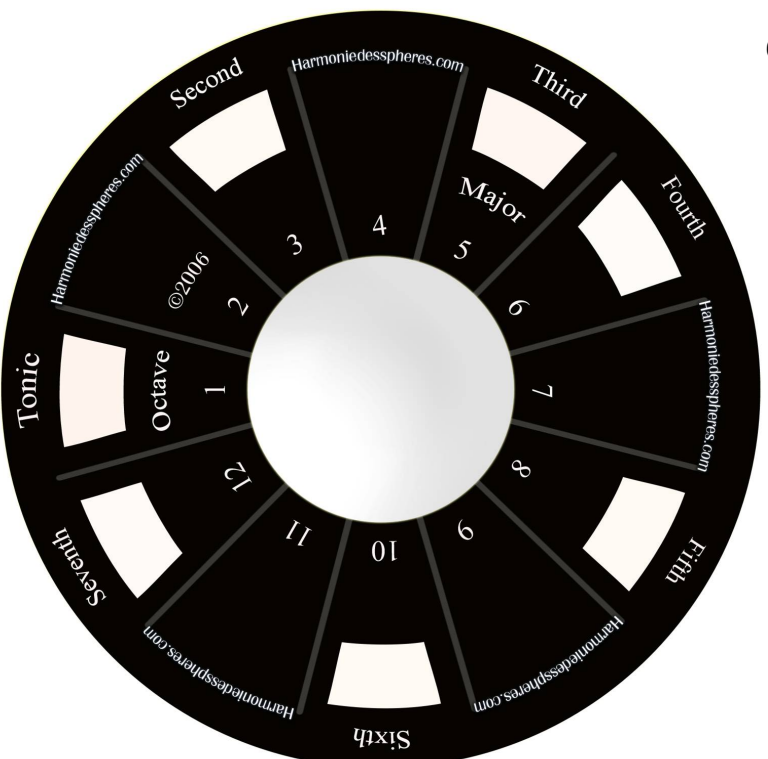


Fig.3



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Sylvain Lalonde founding president : Harmonie des sphères inc.

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Now move the “Tonic” on the “Fifth”, the G, this way you obtain the alterations that constitutes the key frame of our tonal system and so on.
We call this:

« The Cycle of Fifths »

Ascending = Sharp order = F, C, G, D, A, E, B

Descending = Flat order = B, E, A, D, G, C, F

Fig.3B

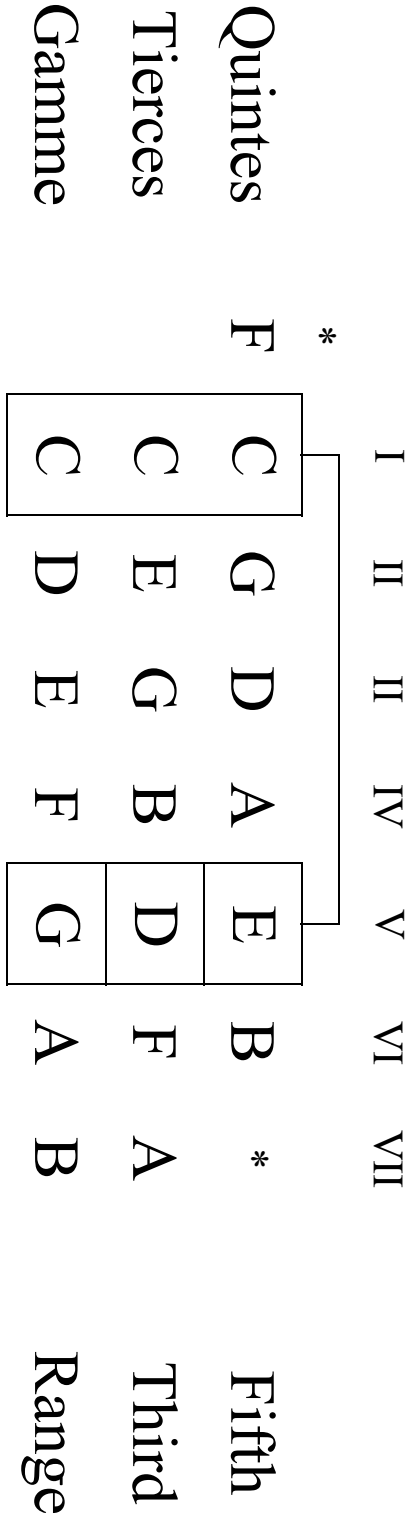
Note that the order of flats is the opposite of sharps

order of #		F	C	G	D	A	E	B	order of b	
Tonality										Major Range
C [#]	order of #	F [#]	C [#]	G [#]	D [#]	A [#]	E [#]	B [#]	order of b	↑ Cycle of Fifths ↓
F [#]	order of #	F [#]	C [#]	G [#]	D [#]	A [#]	E [#]	B	order of b	
B	order of #	F [#]	C [#]	G [#]	D [#]	A [#]	E	B	order of b	
E	order of #	F [#]	C [#]	G [#]	D [#]	A	E	B	order of b	
A	order of #	F [#]	C [#]	G [#]	D	A	E	B	order of b	
D	order of #	F [#]	C [#]	G	D	A	E	B	order of b	
G	order of #	F [#]	C	G	D	A	E	B	order of b	
C	order of #	F	C	G	D	A	E	B	order of b	
F	order of #	F	C	G	D	A	E	B ^b	order of b	
B ^b	order of #	F	C	G	D	A	E ^b	B ^b	order of b	
E ^b	order of #	F	C	G	D	A ^b	E ^b	B ^b	order of b	
A ^b	order of #	F	C	G	D ^b	A ^b	E ^b	B ^b	order of b	
D ^b	order of #	F	C	G ^b	D ^b	A ^b	E ^b	B ^b	order of b	
G ^b	order of #	F	C ^b	G ^b	D ^b	A ^b	E ^b	B ^b	order of b	
C ^b	order of #	F ^b	C ^b	G ^b	D ^b	A ^b	E ^b	B ^b	order of b	

Fig.3d

Cycles des quintes

Cycles of fifths



* Selon l'ordre des dièses / orders of sharps

3rd part: the natural harmonics vs temperate

Each note is made of natural multiples called harmonics

At each degree of the scale, there is a three fundamental sound chord

The chords of three sounds consists of a fundamental
a third party (major or minor) and a fifth just.

« THE THIRD CYCLE »

« C, E, G, B, D, F, A »

Harmonie des sphères



Clé universelle musicale
Musique Instrument Digital Interface
Codes

I	II	III	IV	V	VI	VII	VIII
Major	Minor	Minor	Major	Major	Minor	Diminished	Major
Sol	La	Si	Do	Ré	Mi	H	Sol
						Fa	
Mi			La	Si			Mi
	Fa	Sol		Do	Ré		
Do	Ré	Mi	Fa	Sol	La	Si	Do
Just	Just	Just	Just	Just	Just	Just	Just

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Harmony of the spheres



Universal musical key
Music Instrument Digital Interface
Codes

I	II	III	IV	V	VI	VII	VIII
Major	Minor	Minor	Major	Major	Minor	Diminished	Major
G	A	B	C	D	E	H	G
						F	
E			A	B			E
	F	G		C	D		
C	D	E	F	G	A	B	C
Just	Just	Just	Just	Just	Just	Just	Just

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The notes of a chord can be duplicated at the octave or arpeggiated without
altering the identity of the chord.

You can select and print Fig.3c (Codex) in legal format.

Cut the two parts (A and B) according to the language you want.

Also cut the twenty-four (24) windows (Part A) that correspond to the

« Music intervals »

I degree	C, E, G
II degree	D, F, A
III degree	E, G, B
IV degree	F, A, C
V degree	G, B, D
VI degree	A, C, E
VII degree	B, D, F
VIII degree	C, E, G

Then superimpose part A on part B and position the 1st degree on the C, you will obtain at each degree the notes of all the chords.

You can change the tone as you wish,

The results will be the same.

P.S. You can also use an ABS tube with a diameter of
1.5 inch or 3.81 cm to make it circular shape.

Fig.3c (Codex)

P
A
R
T
I
E
A

Harmonie des sphères



Clé universelle musicale
Musique Instrument Digital Interface
Codex

I	II	III	IV	V	VI	VII	VIII
Majeur	mineur	mineur	Majeur	Majeur	mineur	Diminuer	Majeur
Sol	La	Si	Do	Ré	Mi	H Fa	Sol
Mi	Fa	Sol	La	Si	Do	Ré	Mi
Do	Ré	Mi	Fa	Sol	La	Si	Do
	Ton	Ton	Demi-ton	Ton	Ton	Ton	Demi-ton

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Harmony of the spheres



Universal musical key
Music Instrument Digital Interface
Codex

I	II	III	IV	V	VI	VII	VIII
Majeur	mineur	mineur	Majeur	Majeur	mineur	Diminish	Majeur
G	A	B	C	D	E	H F	G
E	F	G	A	B	C	D	E
C	D	E	F	G	A	B	C
	Tone	Tone	Semi-tone	Tone	Tone	Tone	Semi-tone

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P
A
R
T
I
E
B

Do	Ré	Mi	Fa	Sol	La	Si	Do
Si	Ré ^b	Mi ^b	Fa ^b	Sol ^b	La ^b	Si ^b	Do
La	Do	Ré	Mi	Fa	Sol	La	Si
Sol	Si	Do	Ré	Mi	Fa	Sol	La
Fa	La	Si	Do	Ré	Mi	Fa	Sol
Mi	Sol	La	Si	Do	Ré	Mi	Fa
Ré	Fa	Sol	La	Si	Do	Ré	Mi
Do	Ré	Mi	Fa	Sol	La	Si	Do
Si	Do	Ré	Mi	Fa	Sol	La	Si
La	Si	Do	Ré	Mi	Fa	Sol	La
Sol	La	Si	Do	Ré	Mi	Fa	Sol
Fa	Sol	La	Si	Do	Ré	Mi	Fa
Mi	Sol	La	Si	Do	Ré	Mi	Fa
Ré	Mi	Sol	La	Si	Do	Ré	Mi
Do	Ré	Mi	Fa	Sol	La	Si	Do

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P
A
R
T
A

P
A
R
T
B

C	D	E	F	G	A	B	C
B	D ^b	E ^b	F ^b	G ^b	A ^b	B ^b	C
A	C	D	E	F	G	A	B
G	A	B	C	D	E	F	G
F	G	A	B	C	D	E	F
E	F	G	A	B	C	D	E
D	E	F	G	A	B	C	D
C	D	E	F	G	A	B	C
B	D ^b	E ^b	F ^b	G ^b	A ^b	B ^b	C
A	C	D	E	F	G	A	B
G	A	B	C	D	E	F	G
F	G	A	B	C	D	E	F
E	F	G	A	B	C	D	E
D	E	F	G	A	B	C	D
C	D	E	F	G	A	B	C

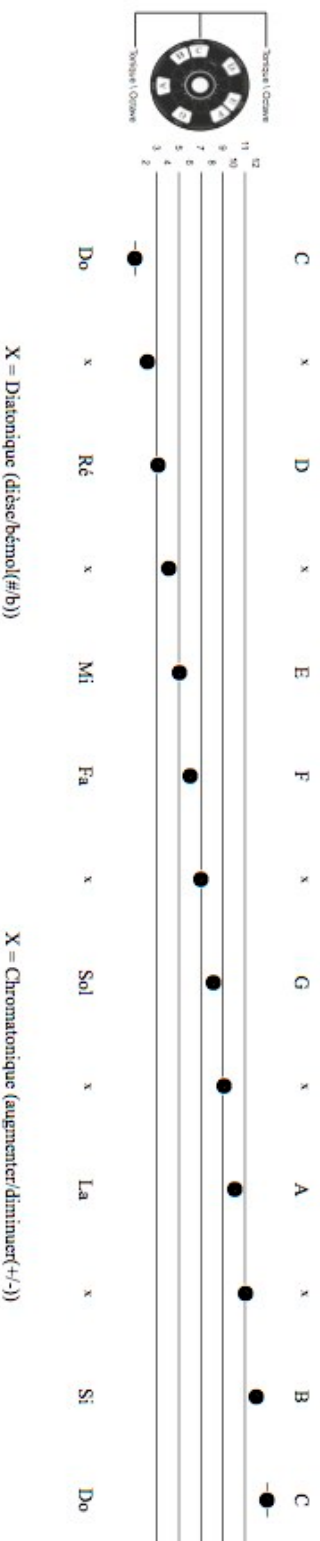
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Harmony of the spheres



Fig.4

**Musical universal key
Musical Instrument Digital Interface**



Select and print at legal format the Fig.4b (image) then cut the two rulers along the lines shown and also cut the eight (8) windows that correspond to the intervals of music.

Then superimpose the part of the center on the top of the rule that suits you and position the 1st degree (Tonic) on the C, you will obtain the sequence

“ C-D-E-F-G-A-B-C ”

You can repeat the exercise in fig.3
or simply move the ruler by tone or semitone.

What is important here is that no matter the tone (tonal height) in which you play, the intervals will always be the same :

Major (which constitute the key frame of our tonal system) or minor.



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Cut

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To fold

C

B

B^b

A[#]

A

A^b

G[#]

G

G^b

F[#]

F

E

E^b

D[#]

D

D^b

C[#]

C

B

B^b

A[#]

A

A^b

G[#]

G

G^b

F[#]

F

E

E^b

D[#]

D

D^b

C[#]

C

↑

To fold

Use a plastic ruler as a support print the sheet in legal size

Cut

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Couper

Octave

Couper

Couper

Septième

Couper

Sixième

Quinte

Couper

Couper

Quarte

Tierce

Couper

Seconde

Couper

Tonique

Couper

Solfège

Cut

Octave

Cut

Cut

Seventh

Cut

Sixth

Fifth

Cut

Cut

Fourth

Third

Cut

Second

Cut

Tonic

Cut

Solfège

Couper

Clé universelle musicale

Dessus de la règle

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Plier

Do

Si

Si^b

La[#]

La

La^b

Sol[#]

Sol

Sol^b

Fa[#]

Fa

Mi

Mi^b

Ré[#]

Ré

Ré^b

Do[#]

Do

↓

Do

Si

Si^b

La[#]

La

La^b

Sol[#]

Sol

Sol^b

Fa[#]

Fa

Mi

Mi^b

Ré[#]

Ré

Ré^b

Do[#]

Do

Plier

Utiliser une règle en plastique comme support imprimer la feuille en format légal

Couper

Tempered scale and various frequency of A

Fig.5b



HDS temperate scale Hz													
Progression %										5,94630943592953			
HDS	C	D		E		F		G		A	B		C
Do ¹²	16744	17739,688	18794,545	19912,127	21096,164	22350,607	23679,643	25087,708	26579,501	28160	29834,481	31608,531	33488
Do ¹¹	8372	8869,844	9397,273	9956,063	10548,082	11175,303	11839,822	12543,854	13289,750	14080	14917,240	15804,266	16744
Do ¹⁰	4186	4434,922	4698,636	4978,032	5274,041	5587,652	5919,911	6271,927	6644,875	7040	7458,620	7902,133	8372
Do ⁹	2093	2217,461	2349,318	2489,016	2637,020	2793,826	2959,955	3135,963	3322,438	3520	3729,310	3951,066	4186
Do ⁸	1046,50	1108,731	1174,659	1244,508	1318,510	1396,913	1479,978	1567,982	1661,219	1760	1864,655	1975,533	2093
Do ⁷	523,25	554,365	587,330	622,254	659,255	698,456	739,989	783,991	830,609	880	932,328	987,767	1046,50
Do ⁶	261,63	277,1826	293,66	311,13	329,63	349,23	369,99	392,00	415,30	440	466,16	493,88	523,25
Do ⁵	130,81	138,59	146,83	155,56	164,81	174,61	185,00	196,00	207,65	220,00	233,08	246,94	261,63
Do ⁴	65,41	69,30	73,42	77,78	82,41	87,31	92,50	98,00	103,83	110,00	116,54	123,47	130,81
Do ³	32,70	34,65	36,71	38,89	41,20	43,65	46,25	49,00	51,91	55,00	58,27	61,74	65,41
Do ²	16,35	17,32	18,35	19,45	20,60	21,83	23,12	24,50	25,96	27,50	29,14	30,87	32,70
Do ¹	8,18	8,66	9,18	9,72	10,30	10,91	11,56	12,25	12,98	13,75	14,57	15,43	16,35

Champ auditif

440,00000000000000000000000000000000

HDS temperate scale Hz													
Progression %										5,94630943592953			
HDS	C	D		E		F		G		A	B		C
Do ¹²	16820,15	17820,32	18879,97	20002,64	21192,06	22452,20	23787,28	25201,74	26700,32	28288,00	29970,09	31752,21	33640,29
Do ¹¹	8410,07	8910,16	9439,99	10001,32	10596,03	11226,10	11893,64	12600,87	13350,16	14144,00	14985,05	15876,10	16820,15
Do ¹⁰	4205,04	4455,08	4719,99	5000,66	5298,01	5613,05	5946,82	6300,44	6675,08	7072,00	7492,52	7938,05	8410,07
Do ⁹	2102,52	2227,54	2360,00	2500,33	2649,01	2806,53	2973,41	3150,22	3337,54	3536,00	3746,26	3969,03	4205,04
Do ⁸	1051,26	1113,77	1180,00	1250,16	1324,50	1403,26	1486,70	1575,11	1668,77	1768,00	1873,13	1984,51	2102,52
Do ⁷	525,630	556,89	590,00	625,08	662,25	701,63	743,35	787,55	834,38	884,00	936,57	992,26	1051,26
Do ⁶	262,815	278,44	295,00	312,54	331,13	350,82	371,68	393,78	417,19	442	468,28	496,13	525,630
Do ⁵	131,41	139,22	147,50	156,27	165,56	175,41	185,84	196,89	208,60	221,00	234,14	248,06	262,815
Do ⁴	65,70	69,61	73,75	78,14	82,78	87,70	92,92	98,44	104,30	110,50	117,07	124,03	131,41
Do ³	32,85	34,81	36,87	39,07	41,39	43,85	46,46	49,22	52,15	55,25	58,54	62,02	65,70
Do ²	16,43	17,40	18,44	19,53	20,70	21,93	23,23	24,61	26,07	27,63	29,27	31,01	32,85
Do ¹	8,213	8,70	9,22	9,77	10,35	10,96	11,61	12,31	13,04	13,81	14,63	15,50	16,43

Champ auditif

442,00000000000000000000000000000000

HDS temperate scale Hz													
Progression %										5,94630943592953			
HDS	C	D		E		F		G		A	B		C
Do ¹²	16896	17900,96	18965,40	20093,15	21287,95	22553,79	23894,91	25315,78	26821,13	28416	30105,70	31895,88	33793
Do ¹¹	8448	8950,48	9482,70	10046,57	10643,97	11276,90	11947,46	12657,89	13410,57	14208	15052,85	15947,94	16896
Do ¹⁰	4224	4475,24	4741,35	5023,29	5321,99	5638,45	5973,73	6328,94	6705,28	7104	7526,43	7973,97	8448
Do ⁹	2112	2237,62	2370,68	2511,64	2660,99	2819,22	2986,86	3164,47	3352,64	3552	3763,21	3986,99	4224
Do ⁸	1056	1118,81	1185,34	1255,82	1330,50	1409,61	1493,43	1582,24	1676,32	1776	1881,61	1993,49	2112
Do ⁷	528	559,40	592,67	627,91	665,25	704,81	746,72	791,12	838,16	888	940,80	996,75	1056
Do ⁶	264	279,70	296,33	313,96	332,62	352,40	373,36	395,56	419,08	444	470,40	498,37	528
Do ⁵	132	139,85	148,17	156,98	166,31	176,20	186,68	197,78	209,54	222	235,20	249,19	264
Do ⁴	66	69,93	74,08	78,49	83,16	88,10	93,34	98,89	104,77	111	117,60	124,59	132
Do ³	33	34,96	37,04	39,24	41,58	44,05	46,67	49,44	52,39	55,50	58,80	62,30	66
Do ²	16,50	17,48	18,52	19,62	20,79	22,03	23,33	24,72	26,19	27,75	29,40	31,15	33
Do ¹	8,25	8,74	9,26	9,81	10,39	11,01	11,67	12,36	13,10	13,88	14,70	15,57	16,50

Champ auditif

444,00000000000000000000000000000000

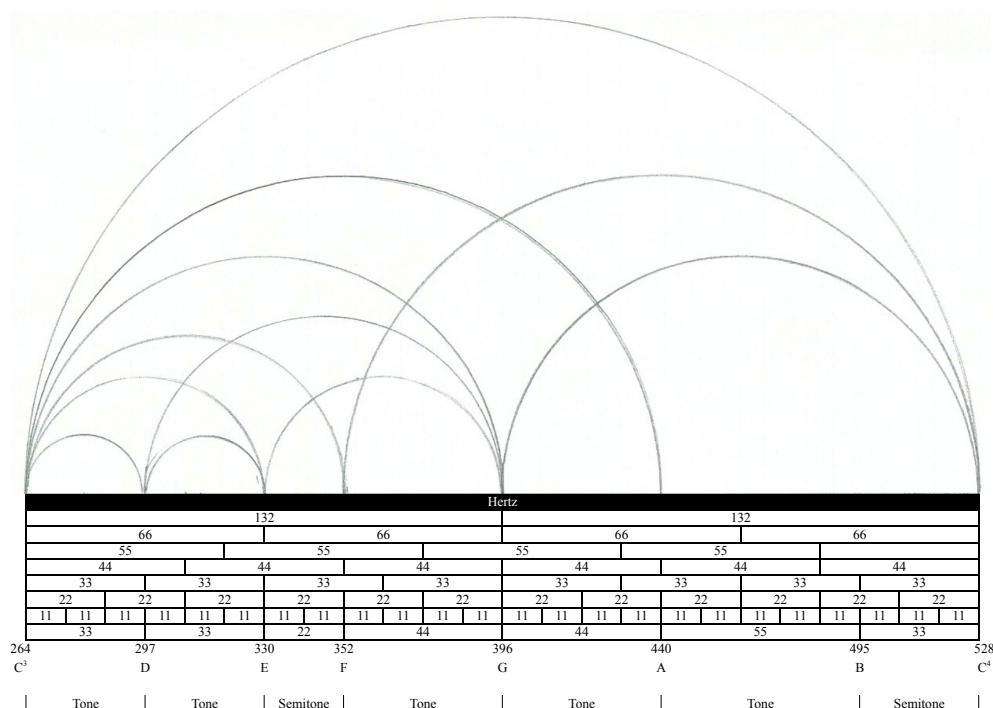
*** For more details on temperate scale see the section R/D

Pythagore and the harmony of the spheres

Fig.7

HARMONY OF THE SPHERES

MUSICAL UNIVERSAL KEY



HDS Universal Proportion

1,125	*	1,06666667	1,125	*	1,125	1,06666667
1,250			1,250		1,250	
1,500		1,33333333				
1,66666667		1,2				
1,33333333		1,500				
1,250		1,6				
1,875		1,06666667				

HDS Fraction Pythagorean

1 1/8	
1 1/4	
1 1/3	
1 1/2	
1 2/3	
1 7/8	
2	

For more details on natural harmonics see the section R/D

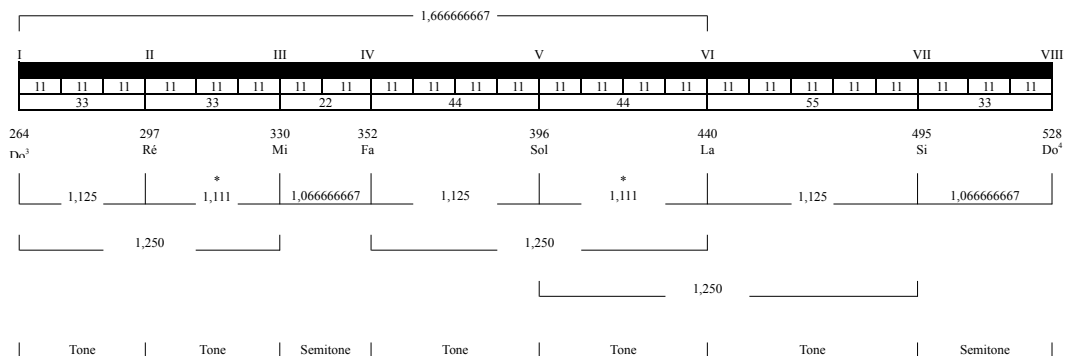
« Natural Harmonics »

Fig.7a



NATURAL HARMONICS

Starting from the fact that the natural resonance (harmonics) of each note are relatively all multiples of each of them and the frequency (Hz) is given by the simple arithmetic operation of fundamental sound F^0 multiplication by the rank number of it



II	X	=
11	1	11
11	2	22
11	3	33
11	4	44
11	5	55
11	6	66
11	7	77
11	8	88
11	9	99
11	10	110
11	11	121
11	12	132
11	13	143
11	14	154
11	15	165
11	16	176
11	17	187
11	18	198
11	19	209
11	20	220
11	21	231
11	22	242
11	23	253

Octave	11	24	264	C	1
	11	25	275		2
	11	26	286		3
Second	11	27	297	D	4
	11	28	308		5
	11	29	319		6
Third	11	30	330	E	7
	11	31	341		8
Fourth	11	32	352	F	9
	11	33	363		10
	11	34	374		11
	11	35	385		12
Fifth	11	36	396	G	13
	11	37	407		14
	11	38	418		15
	11	39	429		16
Sixth	11	40	440	A	17
	11	41	451		18
	11	42	462		19
	11	43	473		20
	11	44	484		21
Seventh	11	45	495	B	22
	11	46	506		23
	11	47	517		24
Octave	11	48	528	C	25

For more details on natural harmonics see figures 6 and 7 section R/D

Note that the ratio between A 440 Hz and C 264 Hz has a proportion of

$$1.66666666666667$$

$$\text{either: } 440/264 = 1.66666666666667$$

this proportion will never change ... whatever the frequency chosen:

$$\dots 328 - 426,7 - 432 - 440 - 442 - 444 \dots$$

it's a good way to find your C

then divide it by 24 to get what I call the unit of measure.

P: S. The tuning frequency of A at 426.7 Hz also called Scientific range
or Range of physicists, with a Do at 256 Hz

$$\text{either : } 426.666666666667 / 256 = 1.66666666666667.$$

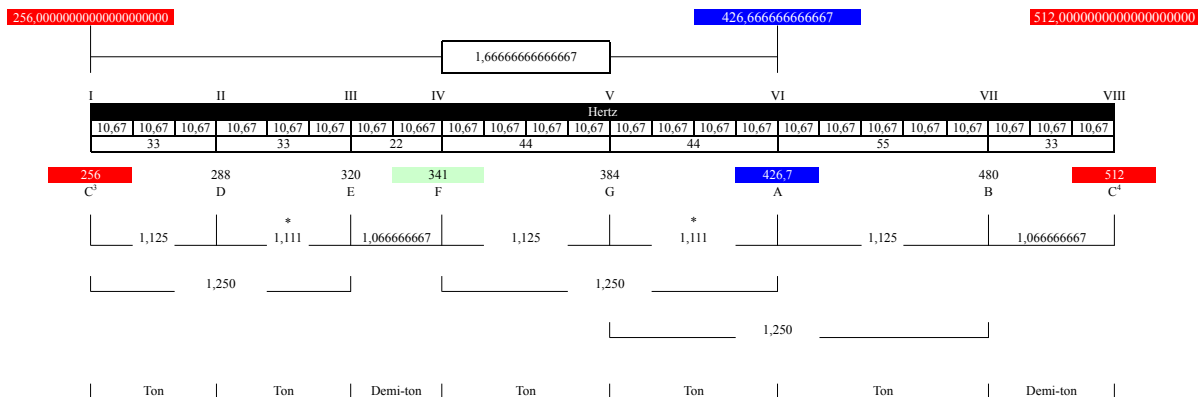
Fig.7f



NATURAL HARMONICS

426,7 Hz

Starting from the fact that the natural resonance (harmonics) of each note are relatively all multiples of each of them and the frequency (Hz) is given by the simple arithmetic operation of fundamental sound F0 multiplication by the rank number of it



10,666666666667

10,67 X =

10,67	1	10,67
10,67	2	21,33
10,67	3	32
10,67	4	42,67
10,67	5	53,33
10,67	6	64
10,67	7	74,67
10,67	8	85,33
10,67	9	96
10,67	10	106,7
10,67	11	117,3
10,67	12	128
10,67	13	138,7
10,67	14	149,3
10,67	15	160
10,67	16	170,7
10,67	17	181,3
10,67	18	192
10,67	19	202,7
10,67	20	213,3
10,67	21	224
10,67	22	234,7
10,67	23	245,3

Octave	10,67	24	256	C	1
	10,67	25	266,7		2
	10,67	26	277,3		3
Seconde	10,67	27	288	D	4
	10,67	28	298,7		5
	10,67	29	309,3		6
Tierce	10,67	30	320	E	7
	10,67	31	330,7		8
Quarte	10,67	32	341,3	F	9
	10,67	33	352		10
	10,67	34	362,7		11
	10,67	35	373,3		12
Quinte	10,67	36	384	G	13
	10,67	37	394,7		14
	10,67	38	405,3		15
	10,67	39	416		16
Sixième	10,67	40	426,7	A	17
	10,67	41	437,3		18
	10,67	42	448		19
	10,67	43	458,7		20
	10,67	44	469,3		21
Septième	10,67	45	480	B	22
	10,67	46	490,7		23
	10,67	47	501,3		24
Octave	10,67	48	512	C	25

341,333333333334

426,66666666667

For more details on natural harmonics see figures 6 and 7 section R/D

Fig.7H



LES HARMONIQUES NATURELLES - NATURAL HARMONICS

F 352	C 264	G 391,111	D 293,333																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																
<table> <tr><td>1</td><td>14,6666667</td><td>1</td><td>11</td></tr> <tr><td>2</td><td>29,3333333</td><td>2</td><td>22</td></tr> <tr><td>3</td><td>44</td><td>3</td><td>33</td></tr> <tr><td>4</td><td>58,6666667</td><td>4</td><td>44</td></tr> <tr><td>5</td><td>73,3333333</td><td>5</td><td>55</td></tr> <tr><td>6</td><td>88</td><td>6</td><td>66</td></tr> <tr><td>7</td><td>102,6666667</td><td>7</td><td>77</td></tr> <tr><td>8</td><td>117,3333333</td><td>8</td><td>88</td></tr> <tr><td>9</td><td>132</td><td>9</td><td>99</td></tr> <tr><td>10</td><td>146,6666667</td><td>10</td><td>110</td></tr> <tr><td>11</td><td>161,3333333</td><td>11</td><td>121</td></tr> <tr><td>12</td><td>176</td><td>12</td><td>132</td></tr> <tr><td>13</td><td>190,6666667</td><td>13</td><td>143</td></tr> <tr><td>14</td><td>205,3333333</td><td>14</td><td>154</td></tr> <tr><td>15</td><td>220</td><td>15</td><td>165</td></tr> <tr><td>16</td><td>234,6666667</td><td>16</td><td>176</td></tr> <tr><td>17</td><td>249,3333333</td><td>17</td><td>187</td></tr> <tr><td>18</td><td>264</td><td>18</td><td>198</td></tr> <tr><td>19</td><td>278,6666667</td><td>19</td><td>209</td></tr> <tr><td>20</td><td>293,3333333</td><td>20</td><td>220</td></tr> <tr><td>21</td><td>308</td><td>21</td><td>231</td></tr> <tr><td>22</td><td>322,6666667</td><td>22</td><td>242</td></tr> <tr><td>23</td><td>337,3333333</td><td>23</td><td>253</td></tr> <tr><td>24</td><td>352</td><td>24</td><td>264</td></tr> <tr><td>25</td><td>366,6666667</td><td>25</td><td>275</td></tr> <tr><td>26</td><td>381,3333333</td><td>26</td><td>286</td></tr> <tr><td>27</td><td>396</td><td>27</td><td>297</td></tr> <tr><td>28</td><td>410,6666667</td><td>28</td><td>308</td></tr> <tr><td>29</td><td>425,3333333</td><td>29</td><td>319</td></tr> <tr><td>30</td><td>440</td><td>30</td><td>330</td></tr> <tr><td>31</td><td>454,6666667</td><td>31</td><td>341</td></tr> <tr><td>32</td><td>469,3333333</td><td>32</td><td>352</td></tr> <tr><td>33</td><td>484</td><td>33</td><td>363</td></tr> <tr><td>34</td><td>498,6666667</td><td>34</td><td>374</td></tr> <tr><td>35</td><td>513,3333333</td><td>35</td><td>385</td></tr> <tr><td>36</td><td>528,6666667</td><td>36</td><td>396</td></tr> <tr><td>37</td><td>542,6666667</td><td>37</td><td>407</td></tr> <tr><td>38</td><td>557,3333333</td><td>38</td><td>418</td></tr> <tr><td>39</td><td>572</td><td>39</td><td>429</td></tr> <tr><td>40</td><td>586,6666667</td><td>40</td><td>440</td></tr> <tr><td>41</td><td>601,3333333</td><td>41</td><td>451</td></tr> <tr><td>42</td><td>616,6666667</td><td>42</td><td>462</td></tr> <tr><td>43</td><td>630,6666667</td><td>43</td><td>473</td></tr> <tr><td>44</td><td>645,3333333</td><td>44</td><td>484</td></tr> <tr><td>45</td><td>660</td><td>45</td><td>495</td></tr> <tr><td>46</td><td>674,6666667</td><td>46</td><td>506</td></tr> <tr><td>47</td><td>689,3333333</td><td>47</td><td>517</td></tr> <tr><td>48</td><td>704</td><td>48</td><td>528</td></tr> </table>	1	14,6666667	1	11	2	29,3333333	2	22	3	44	3	33	4	58,6666667	4	44	5	73,3333333	5	55	6	88	6	66	7	102,6666667	7	77	8	117,3333333	8	88	9	132	9	99	10	146,6666667	10	110	11	161,3333333	11	121	12	176	12	132	13	190,6666667	13	143	14	205,3333333	14	154	15	220	15	165	16	234,6666667	16	176	17	249,3333333	17	187	18	264	18	198	19	278,6666667	19	209	20	293,3333333	20	220	21	308	21	231	22	322,6666667	22	242	23	337,3333333	23	253	24	352	24	264	25	366,6666667	25	275	26	381,3333333	26	286	27	396	27	297	28	410,6666667	28	308	29	425,3333333	29	319	30	440	30	330	31	454,6666667	31	341	32	469,3333333	32	352	33	484	33	363	34	498,6666667	34	374	35	513,3333333	35	385	36	528,6666667	36	396	37	542,6666667	37	407	38	557,3333333	38	418	39	572	39	429	40	586,6666667	40	440	41	601,3333333	41	451	42	616,6666667	42	462	43	630,6666667	43	473	44	645,3333333	44	484	45	660	45	495	46	674,6666667	46	506	47	689,3333333	47	517	48	704	48	528	<table> <tr><td>1</td><td>11</td><td>1</td><td>11</td></tr> 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</table>	1	11	1	11	2	22	2	22	3	33	3	33	4	44	4	44	5	55	5	55	6	66	6	66	7	77	7	77	8	88	8	88	9	99	9	99	10	110	10	110	11	121	11	121	12	132	12	132	13	143	13	143	14	154	14	154	15	165	15	165	16	176	16	176	17	187	17	187	18	198	18	198	19	209	19	209	20	220	20	220	21	231	21	231	22	242	22	242	23	253	23	253	24	264	24	264	25	275	25	275	26	286	26	286	27	297	27	297	28	308	28	308	29	319	29	319	30	330	30	330	31	341	31	341	32	352	32	352	33	363	33	363	34	374	34	374	35	385	35	385	36	396	36	396	37	407	37	407	38	418	38	418	39	429	39	429	40	440	40	440	41	451	41	451	42	462	42	462	43	473	43	473	44	484	44	484	45	495	45	495	46	506	46	506	47	517	47	517	48	528	48	528	<table> <tr><td>1</td><td>16,2962963</td><td>1</td><td>16,2962963</td></tr> <tr><td>2</td><td>32,5925926</td><td>2</td><td>32,5925926</td></tr> <tr><td>3</td><td>48,8888889</td><td>3</td><td>48,8888889</td></tr> <tr><td>4</td><td>65,1851852</td><td>4</td><td>65,1851852</td></tr> <tr><td>5</td><td>81,4814815</td><td>5</td><td>81,4814815</td></tr> <tr><td>6</td><td>97,7777778</td><td>6</td><td>97,7777778</td></tr> <tr><td>7</td><td>114,0740741</td><td>7</td><td>114,0740741</td></tr> <tr><td>8</td><td>130,3703704</td><td>8</td><td>130,3703704</td></tr> <tr><td>9</td><td>146,6666667</td><td>9</td><td>146,6666667</td></tr> <tr><td>10</td><td>162,962963</td><td>10</td><td>162,962963</td></tr> <tr><td>11</td><td>179,2592593</td><td>11</td><td>179,2592593</td></tr> <tr><td>12</td><td>195,5555556</td><td>12</td><td>195,5555556</td></tr> <tr><td>13</td><td>211,8518518</td><td>13</td><td>211,8518518</td></tr> <tr><td>14</td><td>228,1481481</td><td>14</td><td>228,1481481</td></tr> <tr><td>15</td><td>244,4444444</td><td>15</td><td>244,4444444</td></tr> <tr><td>16</td><td>260,7407407</td><td>16</td><td>260,7407407</td></tr> <tr><td>17</td><td>277,0370371</td><td>17</td><td>277,0370371</td></tr> <tr><td>18</td><td>293,3333333</td><td>18</td><td>293,3333333</td></tr> <tr><td>19</td><td>309,6296296</td><td>19</td><td>309,6296296</td></tr> <tr><td>20</td><td>325,9259259</td><td>20</td><td>325,9259259</td></tr> <tr><td>21</td><td>342,2222222</td><td>21</td><td>342,2222222</td></tr> <tr><td>22</td><td>358,5185185</td><td>22</td><td>358,5185185</td></tr> <tr><td>23</td><td>374,8148148</td><td>23</td><td>374,8148148</td></tr> <tr><td>24</td><td>391,1111111</td><td>24</td><td>391,1111111</td></tr> <tr><td>25</td><td>407,4074074</td><td>25</td><td>407,4074074</td></tr> <tr><td>26</td><td>423,7037037</td><td>26</td><td>423,7037037</td></tr> <tr><td>27</td><td>440</td><td>27</td><td>440</td></tr> <tr><td>28</td><td>456,2962963</td><td>28</td><td>456,2962963</td></tr> <tr><td>29</td><td>472,5925926</td><td>29</td><td>472,5925926</td></tr> <tr><td>30</td><td>488,8888889</td><td>30</td><td>488,8888889</td></tr> <tr><td>31</td><td>505,1851852</td><td>31</td><td>505,1851852</td></tr> <tr><td>32</td><td>521,4814815</td><td>32</td><td>521,4814815</td></tr> <tr><td>33</td><td>537,7777778</td><td>33</td><td>537,7777778</td></tr> <tr><td>34</td><td>554,0740741</td><td>34</td><td>554,0740741</td></tr> <tr><td>35</td><td>569,3703704</td><td>35</td><td>569,3703704</td></tr> <tr><td>36</td><td>585,6666667</td><td>36</td><td>585,6666667</td></tr> <tr><td>37</td><td>601,9629629</td><td>37</td><td>601,9629629</td></tr> <tr><td>38</td><td>618,2592593</td><td>38</td><td>618,2592593</td></tr> <tr><td>39</td><td>634,5555556</td><td>39</td><td>634,5555556</td></tr> <tr><td>40</td><td>650,8518518</td><td>40</td><td>650,8518518</td></tr> <tr><td>41</td><td>667,1481481</td><td>41</td><td>667,1481481</td></tr> <tr><td>42</td><td>683,4444444</td><td>42</td><td>683,4444444</td></tr> <tr><td>43</td><td>699,7407407</td><td>43</td><td>699,7407407</td></tr> <tr><td>44</td><td>716,0370371</td><td>44</td><td>716,0370371</td></tr> <tr><td>45</td><td>732,3333333</td><td>45</td><td>732,3333333</td></tr> <tr><td>46</td><td>748,6296296</td><td>46</td><td>748,6296296</td></tr> <tr><td>47</td><td>764,9259259</td><td>47</td><td>764,9259259</td></tr> <tr><td>48</td><td>781,2222222</td><td>48</td><td>781,2222222</td></tr> </table>	1	16,2962963	1	16,2962963	2	32,5925926	2	32,5925926	3	48,8888889	3	48,8888889	4	65,1851852	4	65,1851852	5	81,4814815	5	81,4814815	6	97,7777778	6	97,7777778	7	114,0740741	7	114,0740741	8	130,3703704	8	130,3703704	9	146,6666667	9	146,6666667	10	162,962963	10	162,962963	11	179,2592593	11	179,2592593	12	195,5555556	12	195,5555556	13	211,8518518	13	211,8518518	14	228,1481481	14	228,1481481	15	244,4444444	15	244,4444444	16	260,7407407	16	260,7407407	17	277,0370371	17	277,0370371	18	293,3333333	18	293,3333333	19	309,6296296	19	309,6296296	20	325,9259259	20	325,9259259	21	342,2222222	21	342,2222222	22	358,5185185	22	358,5185185	23	374,8148148	23	374,8148148	24	391,1111111	24	391,1111111	25	407,4074074	25	407,4074074	26	423,7037037	26	423,7037037	27	440	27	440	28	456,2962963	28	456,2962963	29	472,5925926	29	472,5925926	30	488,8888889	30	488,8888889	31	505,1851852	31	505,1851852	32	521,4814815	32	521,4814815	33	537,7777778	33	537,7777778	34	554,0740741	34	554,0740741	35	569,3703704	35	569,3703704	36	585,6666667	36	585,6666667	37	601,9629629	37	601,9629629	38	618,2592593	38	618,2592593	39	634,5555556	39	634,5555556	40	650,8518518	40	650,8518518	41	667,1481481	41	667,1481481	42	683,4444444	42	683,4444444	43	699,7407407	43	699,7407407	44	716,0370371	44	716,0370371	45	732,3333333	45	732,3333333	46	748,6296296	46	748,6296296	47	764,9259259	47	764,9259259	48	781,2222222	48	781,2222222	<table> <tr><td>1</td><td>12,2222222</td><td>1</td><td>12,2222222</td></tr> <tr><td>2</td><td>24,4444444</td><td>2</td><td>24,4444444</td></tr> <tr><td>3</td><td>36,6666667</td><td>3</td><td>36,6666667</td></tr> <tr><td>4</td><td>48,8888889</td><td>4</td><td>48,8888889</td></tr> <tr><td>5</td><td>61,1111111</td><td>5</td><td>61,1111111</td></tr> <tr><td>6</td><td>73,3333333</td><td>6</td><td>73,3333333</td></tr> <tr><td>7</td><td>85,5555556</td><td>7</td><td>85,5555556</td></tr> <tr><td>8</td><td>97,7777778</td><td>8</td><td>97,7777778</td></tr> <tr><td>9</td><td>110</td><td>9</td><td>110</td></tr> <tr><td>10</td><td>122,222222</td><td>10</td><td>122,222222</td></tr> <tr><td>11</td><td>134,4444444</td><td>11</td><td>134,4444444</td></tr> <tr><td>12</td><td>146,6666667</td><td>12</td><td>146,6666667</td></tr> <tr><td>13</td><td>158,8888889</td><td>13</td><td>158,8888889</td></tr> <tr><td>14</td><td>171,111111</td><td>14</td><td>171,111111</td></tr> 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<tr><td>43</td><td>525,555556</td><td>43</td><td>525,555556</td></tr> <tr><td>44</td><td>537,777778</td><td>44</td><td>537,777778</td></tr> <tr><td>45</td><td>550</td><td>45</td><td>550</td></tr> <tr><td>46</td><td>562,222222</td><td>46</td><td>562,222222</td></tr> <tr><td>47</td><td>574,444444</td><td>47</td><td>574,444444</td></tr> <tr><td>48</td><td>586,666667</td><td>48</td><td>586,666667</td></tr> 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<tr><td>16</td><td>293,3333333</td><td>16</td><td>293,3333333</td></tr> <tr><td>17</td><td>311,6666667</td><td>17</td><td>311,6666667</td></tr> <tr><td>18</td><td>330</td><td>18</td><td>330</td></tr> <tr><td>19</td><td>348,3333333</td><td>19</td><td>348,3333333</td></tr> <tr><td>20</td><td>366,6666667</td><td>20</td><td>366,6666667</td></tr> <tr><td>21</td><td>385</td><td>21</td><td>385</td></tr> <tr><td>22</td><td>403,3333333</td><td>22</td><td>403,3333333</td></tr> <tr><td>23</td><td>421,6666667</td><td>23</td><td>421,6666667</td></tr> <tr><td>24</td><td>440</td><td>24</td><td>440</td></tr> <tr><td>25</td><td>458,3333333</td><td>25</td><td>458,3333333</td></tr> <tr><td>26</td><td>476,6666667</td><td>26</td><td>476,6666667</td></tr> <tr><td>27</td><td>495</td><td>27</td><td>495</td></tr> <tr><td>28</td><td>513,3333333</td><td>28</td><td>513,3333333</td></tr> <tr><td>29</td><td>531,6666667</td><td>29</td><td>531,6666667</td></tr> <tr><td>30</td><td>550</td><td>30</td><td>550</td></tr> <tr><td>31</td><td>568,3333333</td><td>31</td><td>568,3333333</td></tr> <tr><td>32</td><td>587</td><td>32</td><td>587</td></tr> <tr><td>33</td><td>605,6666667</td><td>33</td><td>605,6666667</td></tr> <tr><td>34</td><td>623,3333333</td><td>34</td><td>623,3333333</td></tr> <tr><td>35</td><td>641,6666667</td><td>35</td><td>641,6666667</td></tr> <tr><td>36</td><td>660</td><td>36</td><td>660</td></tr> <tr><td>37</td><td>678,3333333</td><td>37</td><td>678,3333333</td></tr> <tr><td>38</td><td>696,6666667</td><td>38</td><td>696,6666667</td></tr> <tr><td>39</td><td>715</td><td>39</td><td>715</td></tr> <tr><td>40</td><td>733,3333333</td><td>40</td><td>733,3333333</td></tr> <tr><td>41</td><td>751,6666667</td><td>41</td><td>751,6666667</td></tr> <tr><td>42</td><td>770</td><td>42</td><td>770</td></tr> <tr><td>43</td><td>788,3333333</td><td>43</td><td>788,3333333</td></tr> <tr><td>44</td><td>806,6666667</td><td>44</td><td>806,6666667</td></tr> <tr><td>45</td><td>825</td><td>45</td><td>825</td></tr> <tr><td>46</td><td>843,3333333</td><td>46</td><td>843,3333333</td></tr> <tr><td>47</td><td>861,6666667</td><td>47</td><td>861,6666667</td></tr> <tr><td>48</td><td>880</td><td>48</td><td>880</td></tr> </table>	1	18,3333333	1	18,3333333	2	36,6666667	2	36,6666667	3	55	3	55	4	73	4	73	5	91,6666667	5	91,6666667	6	110	6	110	7	128,3333333	7	128,3333333	8	146,6666667	8	146,6666667	9	165	9	165	10	183,3333333	10	183,3333333	11	201,6666667	11	201,6666667	12	220	12	220	13	238,3333333	13	238,3333333	14	256,6666667	14	256,6666667	15	275	15	275	16	293,3333333	16	293,3333333	17	311,6666667	17	311,6666667	18	330	18	330	19	348,3333333	19	348,3333333	20	366,6666667	20	366,6666667	21	385	21	385	22	403,3333333	22	403,3333333	23	421,6666667	23	421,6666667	24	440	24	440	25	458,3333333	25	458,3333333	26	476,6666667	26	476,6666667	27	495	27	495	28	513,3333333	28	513,3333333	29	531,6666667	29	531,6666667	30	550	30	550	31	568,3333333	31	568,3333333	32	587	32	587	33	605,6666667	33	605,6666667	34	623,3333333	34	623,3333333	35	641,6666667	35	641,6666667	36	660	36	660	37	678,3333333	37	678,3333333	38	696,6666667	38	696,6666667	39	715	39	715	40	733,3333333	40	733,3333333	41	751,6666667	41	751,6666667	42	770	42	770	43	788,3333333	43	788,3333333	44	806,6666667	44	806,6666667	45	825	45	825	46	843,3333333	46	843,3333333	47	861,6666667	47	861,6666667	48	880	48	880	<table> 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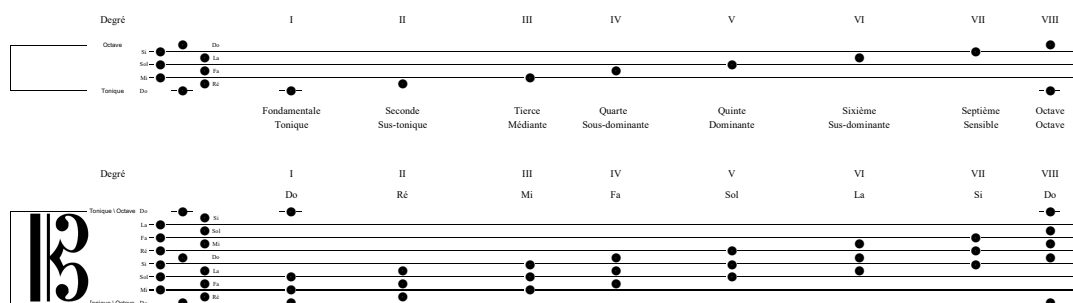
Fig.8

Harmonie des sphères



Clé universelle musicale

Le Diatonisme



Harmonie des sphères inc.

Mission

Promote the universal musical key throughout the world,
research and develop simple and accessible applications
to all, in order to facilitate the understanding of musical notions.

« Music it's of space-time »

Sylvain Lalonde founding president : Harmonie des sphères inc.

To contact us : sylvain.lalonde@me.com

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In memory of an exceptional mind

« Life is not a mystery but a science undisclosed »

« The Genesis of reality, Bernard de Montréal »

Last update: 8 November 2023