#### Notes: Solving Inequalities

**Do Now:** Solve the following inequality. Draw a number line to represent the answer.

4h - 7 > -11

# > Greater Than

- $\geq$  Greater Than or Equal To
- < Less Than

## Set Less Than or Equal To

What inequality represents each verbal expression? 1) All real numbers x less than or equal to -7 2) All real numbers at most 47

3) 6 is less than a number k is less than 13

Solve the following inequality:

$$-\frac{1}{3}k+9 > -6$$

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 $\frac{1}{3}k + 9 > -6$ 

Interval Notation:

Set Builder Notation:

Write the following solutions in interval notation and set builder notation.

**1)** *x* < 8

**2)**  $-5x + 7 \le 17$ 

Before we go on ...

Determine the smallest integer that makes -3x + 7 - 5x < 15 true.

Connor wants to attend the town carnival. The price of admission to the carnival is \$4.50, and each ride costs an additional 79 cents. If he can spend at most \$16.00 at the carnival, which inequality can be used to solve for r, the number of rides Connor can go on, and what is the maximum number of rides he can go on?

- (1)  $0.79 + 4.50r \le 16.00$ ; 3 rides
- (2)  $0.79 + 4.50r \le 16.00$ ; 4 rides
- (3)  $4.50 + 0.79r \le 16.00$ ; 14 rides
- (4)  $4.50 + 0.79r \le 16.00$ ; 15 rides

Given the set  $\{x \mid -2 \le x \le 2$ , where x is an integer}, what is the solution of -2(x-5) < 10?

- (1) 0, 1, 2 (3) -2, -1, 0
- (2) 1, 2 (4) -2, -1

## Vocab Breakdown

### Compound Inequalities:

## **Compound Inequalities**

How about....

-3 < m - 4 < -1

a) How would I verbally say this inequality?

b) Now solve it.

And...

 $16 \le -2x + 6 < 20$ 

#### **Compound Inequalities**

#### AND

#### OR

All real numbers that are greater than or equal to -4 AND less than 6

All real numbers that are less than or equal to 2 OR greater than 6

a) Represent each scenario with a number line.

b) Write each scenario as an inequality.

c) Represent each inequality in interval notation.

d) Represent each inequality in set builder notation.

#### Before the Classwork...

Given that a > b, solve for x in terms of a and b:

 $b(x-3) \ge ax + 7b$ 

#### **Classwork: Solving Inequalities**

1)

Which value would be a solution for *x* in the inequality 47 - 4x < 7?

- (1) -13 (3) 10
- (2) -10 (4) 11

2) The inequality  $7 - \frac{2}{3}x < x - 8$  is equivalent to (1) x > 9 (3) x < 9(2)  $x > -\frac{3}{5}$  (4)  $x < -\frac{3}{5}$ 

#### 3)

The acidity in a swimming pool is considered normal if the average of three pH readings, p, is defined such that 7.0 . If the first two readings are 7.2 and 7.6, which value for the third reading will result in an overall rating of normal?

- (1) 6.2 (3) 8.6
- (2) 7.3 (4) 8.8

4)

Solve the inequality below to determine and state the smallest possible value for x in the solution set.

$$3(x+3) \le 5x-3$$

<sup>5)</sup> Solve the inequality below:

$$1.8 - 0.4y \ge 2.2 - 2y$$

Provide your answer in inequality form, interval notation, and set builder notation.

6) Solve for *x* algebraically:  $7x - 3(4x - 8) \le 6x + 12 - 9x$ 

If x is a number in the interval [4,8], state all integers that satisfy the given inequality. Explain how you determined these values.

7)

Sarah wants to buy a snowboard that has a total cost of \$580, including tax. She has already saved \$135 for it. At the end of each week, she is paid \$96 for babysitting and is going to save three-quarters of that for the snowboard.

Write an inequality that can be used to determine the *minimum* number of weeks Sarah needs to babysit to have enough money to purchase the snowboard.

Determine and state the *minimum* number of full weeks Sarah needs to babysit to have enough money to purchase this snowboard.

8)

Given  $7x + 2 \ge 58$ , which number is *not* in the solution set?

- (1) 6 (3) 10
- (2) 8 (4) 12