Homework: Expanding and Condensing Logarithmic Expressions

Completely expand each of the following logarithmic expressions.

1)
$$\log 2x^3$$

$$2) \ln \left(\frac{d}{f}\right)^2$$

3)
$$\log_3 27^4$$

4)
$$\ln \sqrt[4]{a^2 + b^2}$$

$$5) \log \left(\frac{(x+1)(x-5)}{10^x} \right)$$

Simplify each expression into one logarithm.

6)
$$\ln y + \frac{1}{2} \ln x$$

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 7) $2 \log_2 x - \log_2 7$

$$8)\log_p q + r\log_p s - t\log_p u$$

9)
$$\frac{1}{3}\ln(x-1)^3 + \frac{1}{2}[\ln x^4 - \ln(x+2)^2]$$
 10) $2(\log 8 + 5\log x - 3\log y)$

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11) Is the following equation true or false? Justify your answer.

$$\ln(x^2 - 1) - \ln(x + 1) = \ln(x - 1)$$

12) Is the following equation true or false? Justify your answer.

$$\log(x+y) = \log x + \log y$$

13) Completely simplify the following expression:

$$e^{\ln 2x^3 + \ln 4x^9}$$