

KENDRIYA VIDYALAYA SANGATHAN, ERNAKULAM REGION

PRE BOARD EXAMINATION 2025-26

CLASS : X

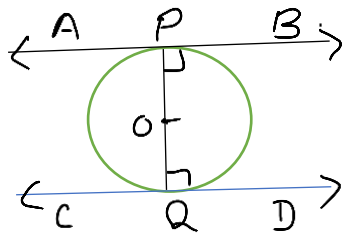
MATHEMATICS(BASIC)

Subject Code:241

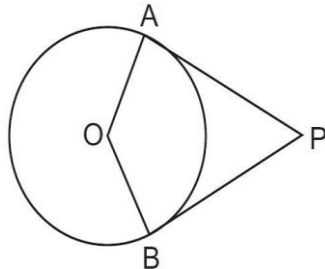
Duration : 3 hrs.

Marking Scheme

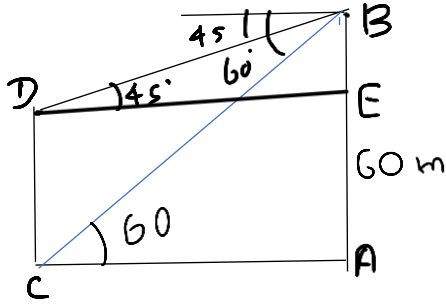
Maximum Marks : 80

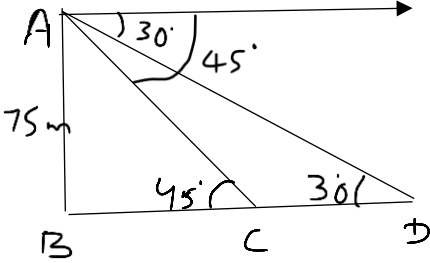
Question No	Solutions	Marks
	<u>SECTION A</u>	
1	(a) $5^2 \times 3^2$	1
2	(b) One solution	1
3	(b) 1	1
4	(b) $4x + 3y = 320$	1
5	(c) 8	1
6	(a) - 5	1
7	(c) 207	1
8	(d) 12	1
9	(d) countless	1
10	(a) 10 m	1
11	(a) 4.5 cm	1
12	(d) 5 cm	1
13	(a) 0	1
14	(d) 35	1
15	(c) Median = $\frac{\text{Mode} + 2\text{Mean}}{3}$	1
16	(c) 40°	1
17	(d) $\frac{44}{3}$ cm	1
18	(a) $\frac{2}{13}$	1
19	(d) Assertion (A) is false but reason (R) is true.	1
20	(a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A).	1
21	<p>Smallest two-digit composite number = 10 Greatest one-digit composite number = 9 LCM = $2 \times 3 \times 3 \times 5 = 90$</p> <p>OR</p> <p>Minimum distance each should walk = LCM of 40 cm ,42 cm ,45 cm = 2520 cm</p>	$\frac{1}{2}$ $\frac{1}{2}$ 1 1 1
22	<p>Correct Figure</p> <p>$\angle OPB = 90^\circ$</p> <p>$\angle OQD = 90^\circ$</p> <p>$\angle OPB + \angle OQD = 180^\circ$</p> <p>Therefore AB is parallel to CD</p> 	$\frac{1}{2}$ $\frac{1}{2}$ 1

23	<p>Let the present age of Santhosh be x and present age of Son be y</p> $x = 3y$ $x + 5 = \frac{5}{2} (y + 5)$ <p>Simplifying $2x - 5y = 15$</p> <p>Solving to get $x = 45$ and $y = 15$</p> <p>OR</p> $7x - 2y = 5$ $8x + 7y = 15$ <p>Solve using algebraic method to get $x = 1$, $y = 1$</p> <p>For verification of both equations</p>	$\frac{1}{2}$ $\frac{1}{2}$ 1 1 1
24	$2\sqrt{2} \cos 45^\circ \sin 30^\circ + 2\sqrt{3} \cos 30^\circ$ $2\sqrt{2} \times \frac{1}{\sqrt{2}} \times \frac{1}{2} + 2\sqrt{3} \times \frac{\sqrt{3}}{2}$ $1 + 3$ 4 <p>OR</p> $\sin(A + B) = \sin A \cos B + \cos A \sin B$ <p>Put $A = 60^\circ$ and $B = 30^\circ$</p> $\sin(60^\circ + 30^\circ) = \sin 60^\circ \cos 30^\circ + \cos 60^\circ \sin 30^\circ$ $\sin 90^\circ = \sin 60^\circ \cos 30^\circ + \cos 60^\circ \sin 30^\circ$ $1 = \frac{\sqrt{3}}{2} \times \frac{\sqrt{3}}{2} + \frac{1}{2} \times \frac{1}{2}$ $1 = \frac{3}{4} + \frac{1}{4}$ $1 = 1, \text{verified}$	1 $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ 1 $\frac{1}{2}$
25	$ax^2 + bx + c = 0$ <p>For real and equal roots, $b^2 - 4ac = 0$</p> $b^2 = 4ac$ $c = b^2 / 2a$	1 1
26	<p>Prove that $\sqrt{3}$ is an irrational number.</p> <p>Let us assume that $\sqrt{3}$ is rational</p> <p>Then $\sqrt{3} = \frac{a}{b}$, where a and b are coprimes</p> <p>Squaring both sides</p> $3 = \frac{a^2}{b^2}$ $a^2 = 3b^2 \dots\dots\dots(1)$ <p>3 divides a^2</p> <p>3 divides a</p> <p>Put $a = 3c$ in Equation 1</p> $(3c)^2 = 3b^2$ $9c^2 = 3b^2$ $b^2 = 3c^2$ <p>3 divides b^2</p> <p>3 divides b</p> <p>3 is a common factor of a and b</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$

	<p>This is a contradiction to assumption that a and b are coprimes So, the assumption is wrong Therefore $\sqrt{3}$ is irrational</p>	$\frac{1}{2}$																																																	
27	<p>From an external point P, tangents PA and PB are drawn to a circle with centre O.If OP = 17 cm and radius = 8 cm,find the perimeter of quadrilateral OAPB</p> <div></div> <p>Correct figure $\angle A = \angle B = 90^\circ$ $OP^2 = OA^2 + AP^2$ $17^2 = 8^2 + AP^2$ $AP = 15$ cm Perimeter of OAPB = $15+8+8+15$ $= 46$ cm</p>	$\frac{1}{2}$ $\frac{1}{2}$ 1 1																																																	
28	<table><tr><th>Class Interval</th><th>Frequency</th><th>c f</th></tr><tr><td>0 - 10</td><td>8</td><td>8</td></tr><tr><td>10 - 20</td><td>16</td><td>24</td></tr><tr><td>20 - 30</td><td>36</td><td>60</td></tr><tr><td>30 - 40</td><td>34</td><td>94</td></tr><tr><td>40 - 50</td><td>6</td><td>100</td></tr><tr><td>Total</td><td>100</td><td></td></tr></table> <p>Median = $l + \left(\frac{\frac{n}{2} - c f}{f} \right) \times h$ $= 20 + \left(\frac{50 - 24}{36} \right) \times 10$ $= 20 + \frac{260}{36}$ $= 27.22$</p> <p>OR</p> <table><tr><th>Class Interval</th><th>Frequency</th><th>x_i</th><th>$f_i x_i$</th></tr><tr><td>0 – 20</td><td>12</td><td>10</td><td>120</td></tr><tr><td>20 – 40</td><td>15</td><td>30</td><td>450</td></tr><tr><td>40 – 60</td><td>32</td><td>50</td><td>1600</td></tr><tr><td>60 – 80</td><td>k</td><td>70</td><td>70 k</td></tr><tr><td>80 – 100</td><td>13</td><td>90</td><td>1170</td></tr><tr><td>Total</td><td>72 + k</td><td></td><td>3340 + 70 k</td></tr></table> <p>Arithmetic Mean = $\frac{\Sigma f_i x_i}{\Sigma f_i}$ $53 = \frac{3340 + 70 k}{72 + k}$</p>	Class Interval	Frequency	c f	0 - 10	8	8	10 - 20	16	24	20 - 30	36	60	30 - 40	34	94	40 - 50	6	100	Total	100		Class Interval	Frequency	x_i	$f_i x_i$	0 – 20	12	10	120	20 – 40	15	30	450	40 – 60	32	50	1600	60 – 80	k	70	70 k	80 – 100	13	90	1170	Total	72 + k		3340 + 70 k	1 1 $\frac{1}{2}$ $\frac{1}{2}$ $1\frac{1}{2}$ $\frac{1}{2}$
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	$53(72 + k) = 3340 + 70k$ $3816 + 53k = 3340 + 70k$ $3816 - 3340 = 70k - 53k$ $476 = 17k$ $k = 28$	$\frac{1}{2}$ $\frac{1}{2}$
29	<p>Let x be the monthly charges and y be the cost of food per day</p> $x + 22y = 1380$ $x + 28y = 1680$ <p>Solving to get x = 280 and y = 50</p> <p>OR</p> <p>The ratio of income of two persons is 9 : 7 and the ratio of their expenditure is 4 : 3, if each of them manage to save Rs. 2000/month. Find their monthly incomes.</p> <p>Incomes of two persons – 9x and 7x</p> <p>Expenditures of two persons – 4y and 3y</p> $9x - 4y = 2000$ $7x - 3y = 2000$ <p>Solving to get x = 2000 and y = 4000</p> <p>Monthly incomes are Rs 18000 and Rs14000 respectively</p>	1 2 1 1 $\frac{1}{2}$ $\frac{1}{2}$
30	$\text{LHS} = \frac{(1+\sin A)^2 + \cos^2 A}{\cos A(1+\sin A)}$ $= \frac{1+2\sin A + \sin^2 A + \cos^2 A}{\cos A(1+\sin A)}$ $= \frac{2+2\sin A}{\cos A(1+\sin A)}$ $= \frac{2(1+\sin A)}{\cos A(1+\sin A)}$ $= \frac{2}{\cos A} = 2 \sec A$	1 $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
31	$a_3 + a_8 = 7, a_7 + a_{14} = -3$ $a + 2d + a + 7d = 7$ $2a + 9d = 7$ $a + 6d + a + 13d = -3$ $2a + 19d = -3$ <p>Solving to get a = 8 and d = -1</p> $a_{15} = 8 + 14 \times (-1) = -6$	1 $\frac{1}{2}$ 1 $\frac{1}{2}$

32	Figure, Given, to prove, Construction Correct Proof	2 3												
33	<p>Solutions of $3x + 2y = 12$</p> <table border="1"> <tr> <td>x</td><td>0</td><td>4</td></tr> <tr> <td>y</td><td>6</td><td>0</td></tr> </table> <p>solutions $5x - 2y = 4$</p> <table border="1"> <tr> <td>x</td><td>0</td><td>2</td></tr> <tr> <td>y</td><td>-2</td><td>3</td></tr> </table> <p>For drawing each correct graph Coordinates are $(0, -2)$, $(0, 6)$ and $(2, 3)$</p> <p>OR</p> <p>$x + y = 30$ $(x + 2)(y - 3) = 210$ Solving $x = 12$ or $x = 13$ When $x = 12$, $y = 18$ When $x = 13$, $y = 17$</p>	x	0	4	y	6	0	x	0	2	y	-2	3	1 1 2 1
x	0	4												
y	6	0												
x	0	2												
y	-2	3												
34	 <p> $\frac{AC}{AB} = \cot 60^\circ$ $\frac{AC}{60} = \frac{1}{\sqrt{3}}$ $AC = \frac{60}{\sqrt{3}}$ $\frac{BE}{DE} = \tan 45^\circ$ $BE = \frac{60}{\sqrt{3}}$ $AE = AB - BE$ $= 60 - \frac{60}{\sqrt{3}}$ $= \frac{60\sqrt{3} - 60}{\sqrt{3}}$ $= \frac{180 - 60 \times 1.73}{3}$ $= \frac{180 - 103.8}{3}$ $= \frac{76.2}{3}$ $= 25.4$ Height of building = 25.4 m </p> <p>OR</p>	1 1 1 $\frac{1}{2}$ 1 1 $\frac{1}{2}$												

	 <p> $\frac{BD}{AB} = \cot 30^\circ$ $\frac{BD}{75} = \sqrt{3}$ $BD = 75\sqrt{3} \text{ m}$ $\frac{BC}{AB} = \cot 45^\circ$ $\frac{BC}{75} = 1$ $BC = 75 \text{ m}$ $CD = BD - BC$ $= 75\sqrt{3} - 75$ $= 75(\sqrt{3} - 1) = 75(0.73) = 54.75$ Distance between the ships = 54.75 m </p>	1 1 $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ 1 $\frac{1}{2}$
35	<p>Volume of model = Volume of cylinder + volume of two cones</p> $= \pi r^2 H + 2 \times \frac{1}{3} \pi r^2 h$ $= \pi r^2 \left(H + \frac{2h}{3} \right)$ $= \frac{22}{7} \times \frac{3}{2} \times \frac{3}{2} \left(8 + \frac{4}{3} \right)$ $= \frac{22}{7} \times \frac{3}{2} \times \frac{3}{2} \times \frac{28}{3}$ $= 66 \text{ cm}^3$	1 1 1 1 1
36	<p>(i) Coordinates of P are P(2 , 5) and coordinates of R are R(8 , 3)</p> $PR = \sqrt{(8 - 2)^2 + (3 - 5)^2}$ $= \sqrt{6^2 + (-2)^2}$ $= \sqrt{36 + 4}$ $= \sqrt{40}$ <p>(ii) Coordinates of midpoint of PR = $\left(\frac{2+8}{2}, \frac{5+3}{2} \right)$</p> $= \left(\frac{10}{2}, \frac{8}{2} \right)$ $= (5, 4)$ <p>(iii) (a) Let A(x, 0) be the point on the X axis</p> $AP = AR$	1 1

	$\sqrt{(x-2)^2 + (0-2)^2} = \sqrt{(x-8)^2 + (0-3)^2}$ $x^2 - 4x + 4 + 4 = x^2 - 16x + 64 + 9$ $12x = 44$ $x = \frac{11}{3}$ <p>Therefore the point is $(\frac{11}{3}, 0)$</p> <p>(b) $Q(x,y) = \left(\frac{1 \times 8 + 2 \times 2}{1+2}, \frac{1 \times 3 + 2 \times 5}{1+2} \right)$</p> $= \left(\frac{12}{3}, \frac{13}{3} \right) = \left(4, \frac{13}{3} \right)$	<p>1</p> <p>1</p> <p>1</p> <p>1</p>
37	<p>(i) $\text{Area} = \frac{90}{360} \times 3.14 \times 5 \times 5$</p> $= 19.625 \text{ m}^2$ <p>(ii) $\text{Area} = \frac{90}{360} \times 3.14 \times 10 \times 10$</p> $= 78.5 \text{ m}^2$ <p>(iii) (a) $\text{Ratio} = \frac{19.625}{78.5} = \frac{1}{4}$</p> $= 1:4$ <p>(b) $\text{Area not covered} = 400 - (19.625 + 78.5)$</p> $= 400 - (98.125)$ $= 301.875 \text{ m}^2$	<p>1</p> <p>1</p> <p>2</p> <p>1</p> <p>1</p>
38	<p>(i) Favourable outcomes are (1,6),(2,5),(3,4),(4,3),(5,2),(6,1)</p> <p>Probability of winning the game $= \frac{6}{36} = \frac{1}{6}$</p> <p>(ii) Favourable outcomes are (2,6),(3,5),(4,4),(5,3),(6,2)</p> <p>Probability of winning $= \frac{5}{36}$</p> <p>(iii) (a) Favourable outcomes are (1,1),(2,2),(3,3),(4,4),(5,5),(6,6)</p> <p>Probability of doublet $= \frac{6}{36} = \frac{1}{6}$</p> <p>(b) Favourable outcomes are (1,1),(1,2),(1,4),(1,6),(2,1),(2,3), (2,5),(3,2),(3,4),(4,1),(4,3),(5,2),(5,6),(6,1),(6,5)</p> <p>Probability(prime number) $= \frac{15}{36} = \frac{5}{12}$</p>	<p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p>