ADHIKAANSH ACADEMY (IITJEE NEET IX X XI XII)

RUN BY: DEEPAK SAINI SIR

B.TECH, M.TECH (N.S.I.T. DELHI UNIVERSITY) Ex. Faculty of Resonance Kota, Career Point Kota Aakash Institute Mumbai

MATHS NOTES (CLASS 11TH)



Adhikaansh Academy

225/5, Panchsheel Colony, Apposite to Nandini Plaza , Garh Road Meerut. Contact no: 7665186856

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CHAPTER 7

PERMUTATIONS (Arrangements) AND COMBINATIONS (selections)

In permutation **order is important**, since 27 & 72 are different numbers(arrangements). In combination order is not important.

• Fundamental principle of counting (FPC)



then by FPC there are mn ways to go from station A to station C

The number of permutations of n different things taken r at a time, where repetition is not allowed is given by ⁿP_r = n(n-1)(n-2).....(n-r+1) where 0<r<n.

eg
$${}^{5}P_{2} = 5 \times 4$$

 ${}^{7}P_{3} = 7 \times 6 \times 5 = 210$

= 20

• Factorial notation: $\mathbf{n!} = 1 \times 2 \times 3 \times \dots \times \mathbf{n}$, where **n** is a natural number eg 5! = 1 x 2 x 3 x 4 x 5

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we define 0! = 1
also n! = n(n-1)!
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$$= n(n-1)(n-2)!$$

- ${}^{n}P_{r} = \underline{\underline{n!}}_{(n-r)!}$ Where $0 \le r \le n$
- Number of permutations of n different things, taken r at a time, where repetition is allowed is **n**^r
- Number of permutations of n objects taken all at a time, where P₁ objects are of first kind, P₂ objects are of second kind.....P_k objects are of the kth kind and rest, if any, are all different is <u>n!</u> (eg 9)

$$P_1!.P_2!...P_k!$$

• The number of combinations of n different things taken r at a time is given by

ⁿC_r = n(n-1)(n-2)....(n-r+1), where 0< r≤n
1.2.3.....r
eg ⁵C₃ =
$$\frac{5 \times 4 \times 3}{1 \times 2 \times 3}$$
 = ⁵C₂

• ${}^{n}C_{r} = {}^{n}C_{n-r}$ $eg {}^{5}C_{3} = {}^{5}C_{2}$ $^{7}C_{5} = ^{7}C_{2}$ ⁿ $C_r = n!$, where $0 \le r \le n$. **r!(n-r)!** ${}^{n}C_{r} = {}^{n}C_{s}$ implies r = s or n = r+s (eg 17*) 1 mark ${}^{n}C_{n} = {}^{n}C_{0} = 1$ • ${}^{n}C_{1} = n$ $eg {}^{5}C_{1} = 5$ • ${}^{n}C_{r} + {}^{n}C_{r-1} = {}^{n+1}C_{r}$ Ex 7.1 1, 2, 4 Ex 7.2 $4^*, 5^*$ (1 mark) eg 8* (1 mark), eg 11*, 12**, 13**, 14**, 16** (4 marks) Ex 7.3 7*, 8*, 9**, 10**, 11** Theorm 6 to prove (4 marks)* eg 17* (1 mark) use direct formula n = 9+8 = 17 since ${}^{n}C_{r} = {}^{n}C_{s}$ implies r = s or n = r+s eg 19** **Ex 7.4**

2**,3*,5*,6*,7**,8*,9*

eg 21**, eg 23*(HOT), eg 24*

Misc Ex

1**,2**,3**,4*,5*,7**,10**,11**

EXTRA/HOT QUESTIONS

- 1) How many permutations can be made with letters of the word MATHEMATICS ? In how many of them vowels are together?
- 2) In how many ways can 9 examination papers be arranged so that the best and the worst papers are never together. (HOT)
- 3) How many numbers greater than 56000 can be formed by using the digits 4,5,6,7,8; no digit being repeated in any number.
- 4) Find the number of ways in which letters of the word ARRANGEMENT can be arranged so that the two A's and two R's do not occur together. (HOT)
- 5) If C(2n,3): C(n,3):: 11:1 find n.
- 6) If P(11,r) = P(12,r-1) find r.

- 7) Five books, one each in Physics, Chemistry, Mathematics, English and Hindi are to be arranged on a shelf. In how many ways can this be done?
- 8) If ${}^{n}P_{r} = {}^{n}P_{r+1}$ and ${}^{n}C_{r} = {}^{n}C_{r-1}$ find the values of n and r.
- 9) A box contains five red balls and six black balls. In how many ways can six balls be selected so that there are at least two balls of each color.
- 10) A group consist of 4 girls and 7 boys in how many ways can a committee of five members be selected if the committee has i) no girl ii) atleast 1 boy and 1 girl
 - iii) atlest 3 girls.

Note : at least means \geq

Answers

- 1) 4989600, 120960
- 2) 282240 Hint (consider the best and the worst paper as one paper)
- 3) 90
- 4) 1678320
- 5) 6
- 6) 9
- 7) 120
- 8) n = 3, r = 2
- 9) 425
- 10) i) 21
 - ii) 441
 - iii) 91

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