# ADHIKAANSH ACADEMY (IITJEE NEET IX X XI XII)

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## MATHS NOTES (CLASS 12<sup>TH</sup>)



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#### **Chapter-3**

#### **Matrices**

- A matrix is an ordered rectangular array of numbers or functions.
- A matrix having m rows and n columns is called a matrix of order m × n.
- $[a_{ij}]_{m \times l}$  is a column matrix.
- $[a_{ii}]_{l \times n}$  is a row matrix.
- An m × n matrix is a square matrix if m = n.
- $A = A = [a_{ij}]_{m \times n}$  is a diagonal matrix if  $a_{ij} = 0$ , when  $i \neq j$
- $A = \left[a_{ji}\right]_{n \times n}$  is a scalar matrix if  $a_{ij} = 0$  when  $i \neq j$ ,  $a_{ij} = k$  (k is some constant), when I = j.
- $A = \left[a_{ij}\right]_{n \times n}$  is an identity matrix, if  $\cdots_{ij} = 1$ , when i = j,  $a_{ij} = 0$ , when  $i \neq j$ .
- A zero matrix has all its elements as zero.
- $A = [a_{ij}] = [b_{ij}] = B$  if (i) A and B are of same order, (ii) for all possible values of *i* and *j*.
- $kA = k \left[ a_{ij} \right]_{m \times n} = \left[ k \left( a_{ij} \right) \right]_{m \times n}$
- - A = (-1)A
- A B = A + (–1) B
- A + B = B + A
- (A + B) + C = A + (B + C), where A, B and C are of same order.
- k(A + B) = kA + kB, where A and B are of same order, k is constant.
- (k + l) A = kA + lA, where k and l are constant.
- If  $A = [a_{ij}]_{m \times n}$  and  $B = [b_{jk}]_{n \times p}$ , then  $AB = C = [c_{ik}]_{m \times p}$ , where  $C_{tl} = \sum_{j=i}^{n} a_{ij} b_{jk}$ 
  - (i) A(BC) = (AB)C,

- (ii) A(B + C) = AB + AC,
- (iii) (A + B)C = AC + BC
- If  $A = \begin{bmatrix} a_{ij} \end{bmatrix}_{m \times n}$ , then A' or  $A^{T} = \begin{bmatrix} a_{ji} \end{bmatrix}_{n \times m}$
- (i) (A')' = A,
- (ii) (kA)' = kA',
- (iii) (A + B)' = A' + B',
- (iv) (AB)' = B'A'
- A is a symmetric matrix if A' = A.
- A is a skew symmetric matrix if A' = -A.
- Any square matrix can be represented as the sum of a symmetric and a skew symmetric matrix.
- Elementary operations of a matrix are as follows:
- (i)  $\mathbf{R}_1 \leftrightarrow \mathbf{R}_j$  or  $\mathbf{C}_1 \leftrightarrow \mathbf{C}_j$

(i)  $\mathbf{R}_1 \rightarrow \mathbf{k} \mathbf{R}_i$  or  $\mathbf{C}_1 \leftrightarrow \mathbf{k} \mathbf{C}_1$ 

- (i)  $\mathbf{R}_1 \leftrightarrow \mathbf{R}_j + \mathbf{k}\mathbf{R}_j$  or  $\mathbf{C}_1 + \mathbf{k}\mathbf{C}_j$
- If A and B are two square matrices such that AB = BA = I, then B is the inverse matrix of A and is denoted by A<sup>-1</sup> and A is the inverse of B.
- Inverse of a square matrix, if it exists, is unique.

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