

A prime producing quadratic expression.

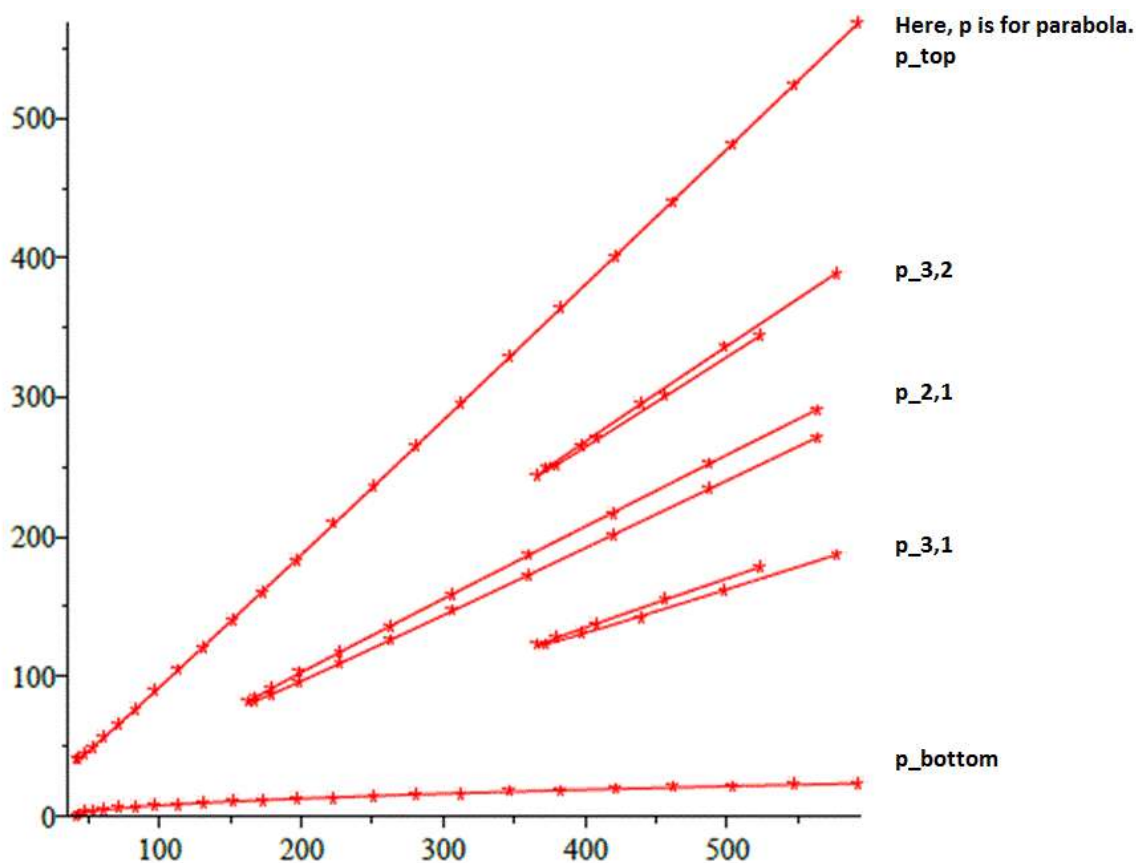
An exploration on the trinomial  $f(n) = n^2 + n + 41$ . Where  $n$  is a non-negative integer.

Apparently, all cases where  $f(n)$  is a composite number can be listed systematically.

Maple Code for exact curve fit parabolas. Parabolas are described parametrically.

```
> x[1, 1, bottom] := z^2+z+41; y[1, 1] := z;
> p2 := plot([x[1, 1, bottom], y[1, 1], z = 0 .. 20]);
> with(plots);
> display(p2);
>
> x[1, 1, top] := z^2+z+41; y[1, 1, top] := z^2+40;
> p3 := plot([x[1, 1, top], y[1, 1, top], z = 0 .. 20]);
> display(p3);
>
> y[2, 1] := 2*z^2+z+81; x[2, 1] := 4*z^2+163;
> p4 := plot([x[2, 1], y[2, 1], z = -10 .. 10]);
> display(p4);
>
> y[3, 1] := 3*z^2+2*z+122; x[3, 1] := 9*z^2+3*z+367;
> p5 := plot([x[3, 1], y[3, 1], z = -4 .. 3]);
>
> y[3, 2] := 6*z^2+z+244; x[3, 2] := 9*z^2+3*z+367;
> p6 := plot([x[3, 2], y[3, 2], z = -4 .. 3]);
```

Now see plot on next page

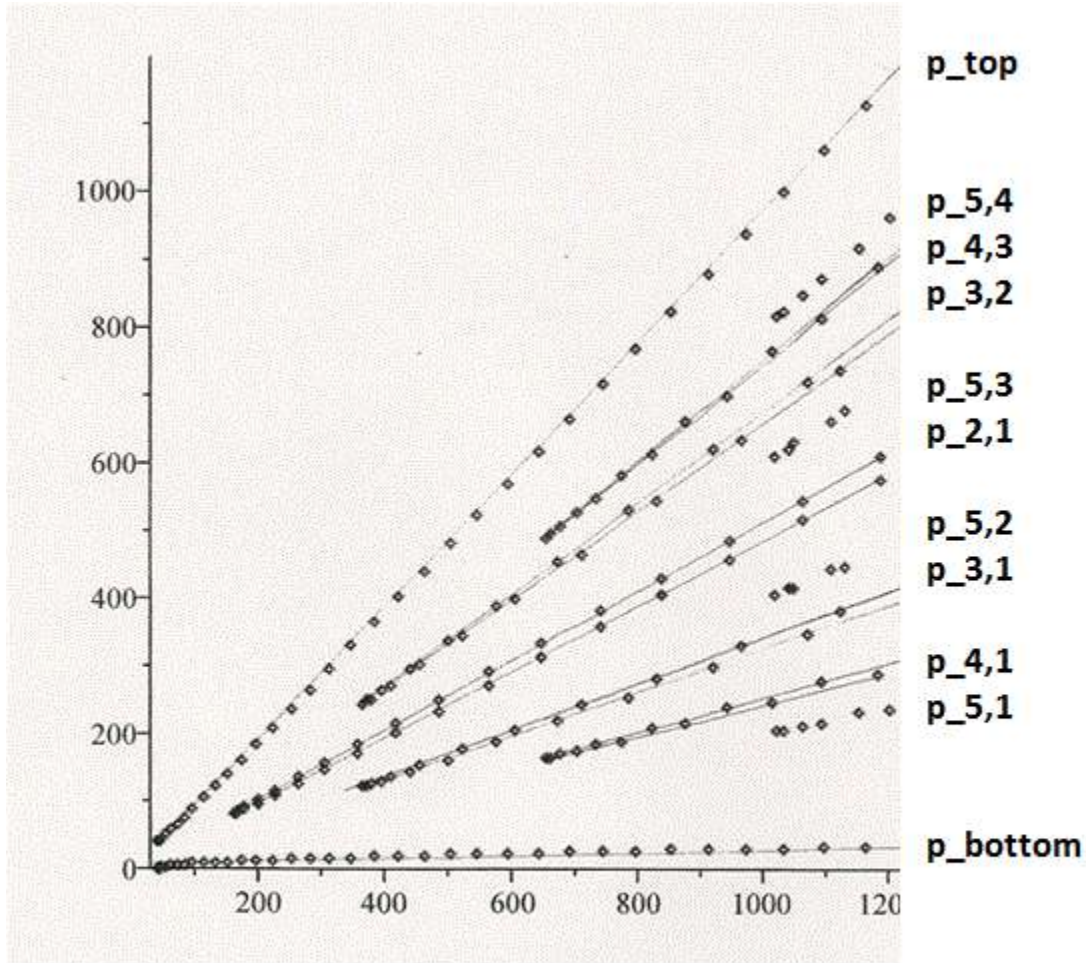


Data points of  $y^2 + y + 41 \equiv 0 \pmod{x}$ . Also, parabolic exact curve fit of this data.

Rules for naming parabolas

$p_{r,c}$  with  $p$  for parabola,  $r$  for row and  $c$  for column. Require that  $r$  and  $c$  are positive integers. Also,  $0 < r < c$  and  $\gcd(r,c) = 1$ . Where  $\gcd$  stands for greatest common divisor. Also, the count of the number of  $c$  parabolas for a given  $r$  is Euler's phi function  $\phi(r)$ . This enumerates as  $\phi(r) = 1, 2, 2, 4, 2, \dots$  see [oeis.org/A10](http://oeis.org/A10).

Here is a zoomed out view of the same graph.



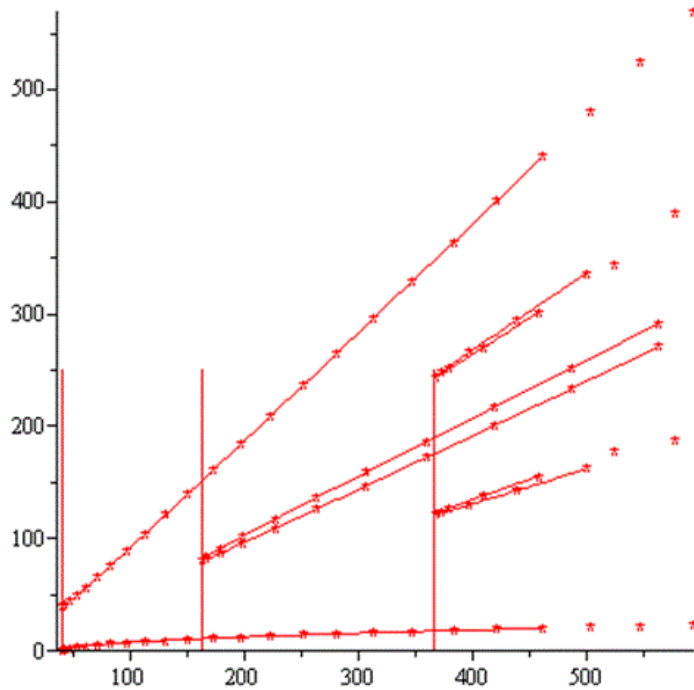
**$y^2+y+41 \pmod x$  is congruent to 0.**

Horizontal minimum of parabolas (not including  $p_{top}$  and  $p_{bottom}$ ) is  $163 \cdot (x^2)/4$ . For some reason, the parabolas line up. Such is the nature of the integers.

A prime producing polynomial graph again with more analysis.

# Graph of divisibility

Vertical lines at  
 $163 \cdot n^2/4$



Notice the vertical lines are tangent to the parabolas.

See that  $163 \cdot 1/4 = 40.75$ . And,  $163 \cdot (2^2)/4 = 163$ . And  $163 \cdot (3^2)/4 = 366.75$ . So we have 3 vertical lines. The x minimum of the curve fit graphs line up exactly with the vertical lines. The parabolas are tangent there.