

Analysis of the trinomial  $f(n) = n^2 + n + 17$ .

Abstract – Assuming that  $n$  is a non-negative integer, we find a pattern of when  $f(n) = n^2 + n + 17$  is a composite number. We assign  $n$  as  $n = A*x^2+B*x+C$ . Where  $A$ ,  $B$ , and  $C$  are determined by numerical evidence. The  $f(n)$  factors algebraically, and  $f(n)$  is a composite number.

We use the Maple program to calculate the values of 'n' where  $f(n)$  is a composite number. Then we graph these results. The graph shows some structure for the composite cases. See Maple code.

```
> # 6-29-2023
```

```
>
```

```
x := Vector[row](49) :
```

```
y := Vector[row](49) :
```

```
counter := 1 :
```

```
for a from 2 to 200 do
```

```
for b from 0 to a - 1 do
```

```
if mod( $b^2 + b + 17, a$ ) = 0
```

```
then x[counter] := a : y[counter] := b : counter := counter + 1;
```

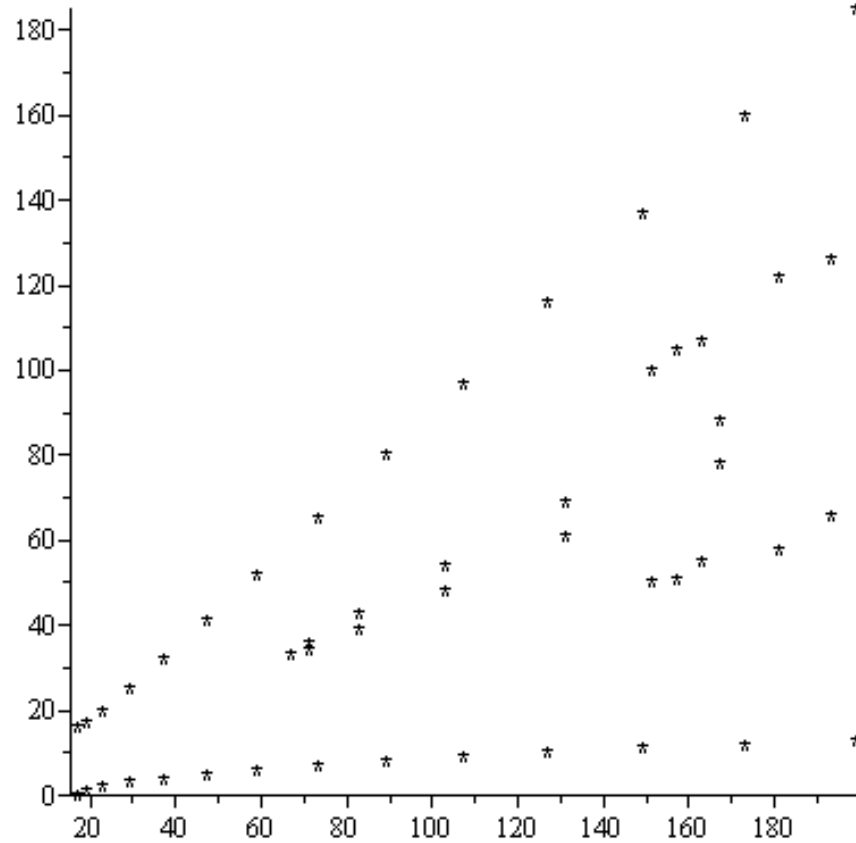
```
end if;
```

```
end do:
```

```
end do:
```

```
> counter
```

```
> plot(x, y, style = point, symbol = asterisk, color = black)
```



- > # this is a graph of 49 data points of  $y^2 + y + 17 \bmod x = 0$ .
  - > # It can be curve fit with parabolas.
  - > # This graph shows 5 parabolas
  - > # The names of the parabolas are  $p_{top}$ ;  $p_{bottom}$ ;  $p_{2,1}$ ;  $p_{3,2}$ ; and  $p_{3,1}$
  - >
- Hope you find this page interesting.