

## New Book

### Arithmetic Mean:-

It is find similar as average.

It is defined as "a value obtained by dividing sum of observation by their number of observation".

$$A.M = \frac{\text{Sum of observation}}{\text{Number of observation}}$$

### Remember:-

→ If we have data in form of population then the value obtained i.e arithmetic will be called parameter & it will be denoted by  $\mu$  (mu).

$$\mu = \frac{x_1 + x_2 + \dots + x_N}{N} = \frac{\sum_{i=1}^N x_i}{N}$$

→ But if we have sample then the arithmetic mean obtained from that data will be called estimator / statistic  
→ Represented by  $\bar{x}$ .

$$\bar{x} = \frac{x_1 + x_2 + x_3 + \dots + x_n}{n} = \frac{\sum_{i=1}^n x_i}{n}$$

It should be noted that population mean is a fixed quantity where as  $\bar{x}$ , sample mean is variable because different sample from same population tend to have different mean.

Geometrically arithmetic mean represent a point at which the distribution or set of observation would be balanced.

### Example # 3.1

45, 32, 37, 46, 39, 36, 41, 48, 36

Find A.M?

Solution: Since we know;

$$A.M = \frac{\sum x_i}{n}$$

$$\bar{x} = \frac{45 + 32 + 37 + 46 + 39 + 36 + 41 + 48 + 36}{9}$$

$$\bar{x} = \frac{360}{9}$$

$$\boxed{\bar{x} = 40} \quad A.M.$$



## Weighted Arithmetic Mean:-

If we have data along with their importances are also given. So to find average of such numbers are called weighted arithmetic mean.

" When different items of the series are weighted according to their relative importance, the average of such data/series is called weighted A.M.

For e.g. GPA is weighted average of Mid, Final, Quizzes & assignment etc.

Mathematically:-

$$\bar{X}_w = \frac{\sum_{i=1}^n x_i w_i}{\sum_{i=1}^n w_i}$$

### Example:- 3.2

Calculate the weighted mean of the follow.

items	Expenditure (Rs)	Weight.
Food	290	7.5
Rent	<del>54</del> 98	2.0
Fuel & Lights	75	1.0
other	75	0.5
clothing	<del>54</del> 98	<del>2.0</del> 1.5

Sol:- The weighted mean can be calculated as,

Items	Expenditure ( $x_i$ )	Weights ( $w_i$ )	$x_i w_i$
Food	290	7.5	2175
Rent	54	2.0	108
Clothing	98	1.5	147
Fuel & light	75	1.0	75
Other Items	75	0.5	37
		$\Sigma w_i = 12.5$	$\Sigma w_i \cdot x_i = 2542.5$

Using formula;

$$\bar{x}_w = \frac{\sum w \cdot x_i}{\sum w} = \frac{2542.5}{12.5}$$

$$\boxed{\bar{x}_w = 203.4}$$

## (\*) Properties of Arithmetic mean:-

### Property #1

The sum of deviation of observation  $x_i$  from their mean  $\bar{x}$ , with their proper sign is zero.

Mathematically;  $\boxed{\sum (x_i - \bar{x}) = 0.}$

For e.g. consider exp #3.1.

Where data are.

$$45, 32, 37, 46, 39, 36, 41, 48, 36 \quad \Sigma \bar{x} = 40.$$

$$\begin{aligned} \text{So, } \sum (x_i - \bar{x}) &= (45-40) + (32-40) + (37-40) + (46-40) + (39-40) + (36-40) + (41-40) + (48-40) + (36-40) \\ &= 5 - 8 - 3 + 6 - 1 - 4 + 1 + 8 - 4 = 0 \quad \boxed{\text{proved}} \end{aligned}$$



### Proof of Property #1

$$= \sum (x_i - \bar{x})$$

$$= \sum_{i=1}^n x_i - \sum_{i=1}^n \bar{x}$$

$$= \sum_{i=1}^n x_i - n\bar{x}$$

$$= \sum_{i=1}^n x_i - n \frac{\sum_{i=1}^n x_i}{n}$$

$$\sum (x_i - \bar{x}) = \sum_{i=1}^n x_i - \sum_{i=1}^n \bar{x}$$

$$\boxed{\sum (x_i - \bar{x}) = 0}$$

As  $\bar{x}$  is constant so  
 $\sum \bar{x} = n\bar{x}$ .

But  $\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$

### Property #02

Sum of the square deviation of observation  $x_i$  means is minimum.

Mathematically;

$$\sum (x_i - \bar{x})^2 \text{ is minimum.}$$

$$\text{or } \sum (x_i - \bar{x})^2 \leq \sum (x_i - a)^2$$

Where  $a$  is any number.

Proof:-

$$\begin{aligned} \sum (x_i - a)^2 &= \sum (x_i - \bar{x} + \bar{x} - a)^2 \\ &= \sum ((x_i - \bar{x}) + (\bar{x} - a))^2 \end{aligned}$$

$$= \sum \left( (x_i - \bar{x})^2 - 2(x_i - \bar{x})(\bar{x} - a) + (\bar{x} - a)^2 \right)$$

Apply summation operator.

$$= \sum (x_i - \bar{x})^2 - 2(x_i - \bar{x}) \sum (\bar{x} - a) + \sum (\bar{x} - a)^2$$

$$= \sum (x_i - \bar{x})^2 - 2(\bar{x} - a) \sum (x_i - \bar{x}) + \sum (\bar{x} - a)^2$$

(property 1)

$$= \sum (x_i - \bar{x})^2 + \sum (\bar{x} - a)^2$$

$\therefore \sum (\bar{x} - a)$   
is constant  
no. so

$$= \sum (x_i - \bar{x})^2 + n(\bar{x} - a)^2$$

$$\sum (x_i - a)^2 = \sum (x_i - \bar{x})^2 + n(\bar{x} - a)^2$$

It is proved that  $\sum (x_i - a)^2 \geq \sum (x_i - \bar{x})^2$

By amount  $n(\bar{x} - a)^2$ .

∴ This property usually called minimum property of mean.

### Property # 043

If we have data or population having  $k$  sub groups

with their observations  $x_1, x_2, x_3, \dots, x_k$  and their corresponding means

are  $\bar{x}_1, \bar{x}_2, \bar{x}_3, \dots, \bar{x}_k$ . So the mean of





data can be calculated as;

$$\bar{X} = \frac{x_1 \bar{x}_1 + x_2 \bar{x}_2 + x_3 \bar{x}_3 + \dots + x_k \bar{x}_k}{x_1 + x_2 + x_3 + \dots + x_k}$$

### Property # 04

If you transform the observation (data given) then there will be also same transformation occurs in mean.

For e.g

If  $y_i = ax_i + b$  then;

$$\bar{y} = a\bar{x} + b.$$

This property is used when we have small number so we multiply (i.e. transform) for easing.

Proof:-

As;

$$y_i = ax_i + b.$$

Applying  $\Sigma$  operator on b/s.

$$\Sigma y_i = a \Sigma x_i + \Sigma b.$$

$$\frac{\Sigma y_i}{n} = \frac{a \Sigma x_i}{n} + \frac{n \cdot b}{n}$$

$\therefore$  divide by  $n$ .

$$\boxed{\bar{y} = a\bar{x} + b}$$

[Proved]

$$\frac{\Sigma y_i}{n} = \bar{y}$$

$$= \frac{\Sigma x_i}{n} = \bar{x}$$

Example:- 3.3

The mean height and the number of students in three sections of statistics class are given below.

Section	Number of boys	Mean height.
A	40	62"
B	37	58"
C	43	61"

Find overall height (mean) of 120 boys.

Solution:- Given data.

$$n_1 = 40$$

$$\bar{x}_1 = 62"$$

$$n_2 = 37$$

$$\bar{x}_2 = 58"$$

$$n_3 = 43$$

$$\bar{x}_3 = 61"$$

$$\bar{x}_{\text{total}} = ?$$

$$\text{Since } \bar{x}_T = \frac{n_1 \bar{x}_1 + n_2 \bar{x}_2 + n_3 \bar{x}_3}{n_1 + n_2 + n_3}$$

$$\bar{x}_T = \frac{40(62) + 37(58) + 43(61)}{40 + 37 + 43}$$

$$\boxed{\bar{x}_T = 60.4"}$$



## Mean from Ungroup data:-

If we ungroup data then the mean can be find as;

$$\bar{x} = \frac{x_1 f_1 + x_2 f_2 + \dots + x_n f_n}{f_1 + f_2 + f_3 + \dots + f_n}$$

Q7

$$\bar{x} = \frac{\sum_{i=1}^n x_i f_i}{\sum_{i=1}^n f_i}$$

## Mean from group data;

In case of group data we will first find mid points from corresponding intervals and then use this relation;

$$\bar{x} = \frac{x_1 f_1 + x_2 f_2 + x_3 f_3 + \dots + x_n f_n}{f_1 + f_2 + f_3 + \dots + f_n}$$

$$\bar{x} = \frac{\sum_{i=1}^n x_i f_i}{\sum_{i=1}^n f_i}$$

Example #3.4 Calculate the mean weight from the given data

Weight (grams)	Frequency
65-84	9
85-104	10
105-124	17
125-144	10
145-164	5
165-184	4
185-204	5

Solution:-

Weights	Mid point	freq.	$\Sigma f_i x_i$
65-84	74.5	9	670.5
85-104	94.5	10	945
105-124	114.5	17	1946.5
125-144	134.5	10	1345
145-164	154.5	5	722.5
165-184	174.5	4	698
185-204	194.5	5	972.5
		$\Sigma f = 60$	$\Sigma f x_i = 7300$

So;

$$\bar{X} = \frac{\Sigma f x_i}{\Sigma f} = \frac{7300}{60}$$

$$\bar{X} = 121.67$$



Where as from other definition i.e.

$$\bar{x} = \frac{\text{Sum of actual observation}}{\text{No. of observation.}}$$

$$= \frac{7324}{60}$$

∵ 7324 is given.  
in questions.

$$\boxed{\bar{x} = 122.067} \quad \text{Ans}$$

Conclusion:-

As by calculating mean from midpoint method & actual observations are approximately same that's why we consider midpoint.

### Change of Origin & Scale:-

We use this process in order to transform given data and make it easy for calculation.

Let the given data is,

$x_1, x_2, x_3, \dots, x_n$  & corresponding frequencies are  $f_1, f_2, f_3, \dots, f_k$ .

$$\text{So, } u_i = \frac{x_i - a}{h} \quad \text{--- (1)}$$

Where  $a$  is number (data) whose frequency is maximum.

$h$  is class width.

$x_i$  is given corresponding data.

So the mean will be;

$$\bar{U} = \frac{\bar{x} - a}{h}$$

$$\boxed{\bar{x} = \bar{U}h + a}$$

Example #3.5 Given the following frequencies distribution of weights. Calculate mean by short method.

Weights (gram)	Mid points	f.
65-84	74.5	9
85-104	94.5	10
105-124	114.5	17
125-144	134.5	10
145-164	154.5	5
165-184	174.5	4
185-204	194.5	5

Solution:- As we know that; (short method)

$$\bar{x} = \bar{U}h + a \rightarrow (1)$$

$$\bar{U} = \frac{\sum f_i x_i}{\sum f_i} \rightarrow (2)$$



Weights	Mid point ( $x_i$ )	$f_i$	$x_i f_i$	$u_i$	$f_i u_i$
65-84	74.5	9	-2		-18
85-104	94.5	10	-1		-10
105-124	114.5	17	0		0
125-144	134.5	10	1		10
145-164	154.5	5	2		10
165-184	174.5	4	3		12
185-204	194.5	5	4		20
		$\Sigma f = 60$			$\Sigma f_i u_i = 24$

$$\bar{x} = \frac{\Sigma x_i f_i}{\Sigma f_i} = \frac{74.5 \times 9 + 94.5 \times 10 + 114.5 \times 17 + 134.5 \times 10 + 154.5 \times 5 + 174.5 \times 4 + 194.5 \times 5}{60}$$

Q (2)  $\Rightarrow$

$$\bar{u} = \frac{24}{60} \Rightarrow 0.4$$

$\therefore$  Mean of transfer data.

Q (3)  $\Rightarrow$

$$\bar{x} = \bar{u}h + a$$

$$\bar{x} = (0.4)(20) + 114.5$$

$$\bar{x} = 8 + 114.5$$

$$\boxed{\bar{x} = 122.5} \text{ Ans}$$

This is mean of actual data.

### Example 3.6

Compute the mean for the following frequency distribution of annual death rate.

Death rate	Frequency
3.5-4.4	1
4.5-5.4	4
5.5-6.4	5
6.5-7.4	13
7.5-8.4	12
8.5-9.4	19
9.5-10.4	13
10.5-11.4	10
11.5-12.4	6
12.5-13.4	4
13.5-14.4	1
	<u>88</u>

Consider  
 $a = 8.95$

$$\bar{Q}_1 = \frac{\sum f_i u_i}{n}$$

Solution:-

Death rate	Mid point	freq.	$u_i$	$f_i u_i$
3.5-4.4	3.95	1	-5	-5
4.5-5.4	4.95	4	-4	-16
5.5-6.4	5.95	5	-3	-15
6.5-7.4	6.95	13	-2	-26
7.5-8.4	7.95	12	-1	-12
8.5-9.4	8.95	19	0	0
9.5-10.4	9.95	13	1	13
10.5-11.4	10.95	10	2	20
11.5-12.4	11.95	6	3	18
12.5-13.4	12.95	4	4	16
13.5-14.4	13.95	1	5	5
		<u><math>\Sigma f = 88</math></u>		<u><math>\Sigma f_i u_i = -2</math></u>



$$\bar{U} = \frac{\sum f_i u_i}{\sum f}$$

$$= -\frac{2}{88}$$

$\bar{U} = 0.023 \rightarrow$  This is mean of transfer date.

Now use this eqn.

$$\bar{X} = \bar{U}h + a$$

$$\bar{X} = (0.023)(1) + 8.95$$

$$\boxed{\bar{X} = 8.973}$$

Mean of required date.

### Geometric mean:-

If we have data i.e.  $x_1, x_2, x_3, \dots, x_n$  that behave geometrically;

So;

$$G.M = (x_1 x_2 x_3 \dots x_n)^{1/n}$$

Taking log on b/s.

$$\log G.M = \frac{1}{n} \log (x_1 x_2 x_3 \dots x_n)$$

$$\log G.M = \frac{1}{n} (\log x_1 + \log x_2 + \dots + \log x_n)$$

$$\log G.M = \frac{1}{n} \sum_{i=1}^n \log x_i$$

$$\log G.M = \frac{\sum_{i=1}^n \log x_i}{n}$$

$$G.M = \text{Antilog} \left( \frac{\sum_{i=1}^n \log x_i}{n} \right)$$

So G.M is antilog of logarithm of Arithmetic data

For group data:-

Let we have grouped data  $x_1, x_2, \dots, x_k$  having frequencies  $f_1, f_2, \dots, f_k$ .

$$\text{So } G.M = (x_1^{f_1} x_2^{f_2} x_3^{f_3} \dots x_k^{f_k})^{1/n}$$

$$\log G.M = \frac{1}{n} \log (x_1^{f_1} x_2^{f_2} x_3^{f_3} \dots x_k^{f_k})$$

$$= \frac{1}{n} (f_1 \log x_1 + f_2 \log x_2 + \dots + f_k \log x_k)$$

$$= \frac{1}{n} \sum_{i=1}^n \log f_i x_i$$

$$G.M = \text{Antilog} \left( \frac{1}{n} \sum_{i=1}^n \log x_i f_i \right)$$

For weighted mean:-

$$\log G.W = \frac{1}{\sum w_i} [\sum w_i \log x_i]$$



Exp #3.7 Find Geometric mean

45, 37, 32, 46, 39, 36, 41, 48, & 36.

Sol: As  $G.M = (x_1 \times x_2 \times x_3 \dots x_n)^{1/n}$

Where  $n = \text{no. of observation}$

$$G.M = (45 \cdot 37 \cdot 32 \cdot 46 \cdot 39 \cdot 36 \cdot 41 \cdot 48 \cdot 36)^{1/9}$$

$$\log G.M = \frac{1}{9} \log (45 \cdot 37 \cdot 32 \cdot 46 \cdot 39 \cdot 36 \cdot 41 \cdot 48 \cdot 36)$$

$$= \frac{1}{9} (\log 45 + \log 37 + \log 32 + \dots + \log 36)$$

$$G.M = \text{Antilog}(1.59856)$$

$$\boxed{G.M = 39.68}$$

Exp #3.8 Given the following frequency distribution of weights, calculate the G.M.

Weights (grams)	65-84	85-104	105-124	125-144	145-164	165-184	185-204
f	9	10	17	10	5	4	5

Sol: As we know that

$$G.M = \text{Antilog} \left( \frac{\sum f_i \log x_i}{n} \right)$$

First we will find  $\log x_i$  &  $f_i$

Weights	$x_i$ (M.P)	$f_i$	$\log x_i$	$f \log x_i$
65-84	74.5	9	1.872	16.848
85-104	94.5	10	1.970	19.75
105-124	114.5	17	2.0589	35
125-144	134.5	10	2.1287	21.287
145-164	154.5	5	2.1889	10.9445
165-184	174.5	4	2.2418	8.9672
185-204	194.5	5	2.2889	11.445
		<u>60</u>		<u>124.2412</u>

$$\Sigma f \log x_i = 124.2412$$

$$n = \Sigma f$$

$$= 60$$

$$\log G.M = \frac{1}{n} \Sigma f \log x_i$$

$$= \frac{124.2412}{60}$$

$$G.M = \text{Anti log}(2.0707)$$

$$G.M = 117.67 \quad \text{Ans.}$$

$$G.M = 117.67 \text{ gram}$$



## Harmonic Mean:-

Harmonic mean is defined as reciprocal of arithmetic mean of the reciprocal of the values.

$$H = \text{Reciprocal} \left( \frac{\frac{1}{x_1} + \frac{1}{x_2} + \dots + \frac{1}{x_n}}{n} \right)$$

or

$$H = \left( \frac{\frac{1}{x_1} + \frac{1}{x_2} + \dots + \frac{1}{x_n}}{n} \right)^{-1}$$

$$H = \left( \frac{\sum_{i=1}^n \frac{1}{x_i}}{n} \right)^{-1}$$

● Exp# 3.9 Find the harmonic mean from the following frequency distribution

Weight (gram)	65-84	85-104	105-124	125-144	145-164	165-184	185-204
f	9	10	17	10	5	4	5

Solution:-

As we know that;

$$H.M = \left( \frac{\sum_{i=1}^n f_i \frac{1}{x_i}}{n} \right)^{-1} \quad \text{--- (1)}$$

Weight (grams)	$x_i$ (Mid Point)	$f_i$	$f (1/x_i)$
65-84	74.5	9	0.1208
85-104	94.5	16	0.10582
105-124	114.5	17	0.14847
125-144	134.5	10	0.07435
145-164	154.5	5	0.03236
165-184	174.5	4	0.02292
185-204	194.5	5	0.02571

$$\sum f (1/x_i) = 0.53044$$

$$n = \sum f$$

$$H.M = \left( \frac{0.53044}{60} \right)^{-1}$$

$$= (8.84067 \times 10^{-3})^{-1}$$

$$\boxed{H.M = 113.11 \text{ gram}}$$

### Example 3.10

Compute the Geometric and Harmonic mean for the following distribution annual

$x_i$	3.95	4.95	5.95	6.95	7.95	8.95	9.95	10.95	11.95	12.95	13.95
$f_i$	1	4	5	13	12	19	13	10	6	4	1

Solution:-

As we know the geometric and harmonic mean are



$$G.M = \text{Antilog} \left( \frac{1}{n} \sum_{i=1}^n f_i \log x_i \right) \rightarrow \textcircled{1}$$

$$\{ H.M = \left( \frac{\sum_{i=1}^n \frac{1}{f_i \log x_i}}{n} \right)^{-1} \rightarrow \textcircled{2}$$

First we will construct a table.

$x_i$	$f_i$	$f_i (\frac{1}{x_i})$	$\log x_i$	$f \log x_i$
3.95	1	0.25316	0.5966	0.59660
4.95	4	0.80808	0.69461	2.77844
5.95	5	0.84035	0.77452	3.87260
6.95	13	1.87044	0.84198	10.94574
7.95	12	1.56948	0.9037	10.80444
8.95	19	2.12287	0.95182	18.08458
9.95	13	1.30650	0.99782	12.97166
10.95	10	0.91320	1.03945	10.39450
11.95	6	0.50208	1.0774	6.46440
12.95	4	0.30888	1.11229	4.44916
13.95	1	0.07168	1.14459	1.1446

$$n = \sum f_i = 88 \quad \sum f_i (\frac{1}{x_i}) = 10.50672$$

$$\sum f_i \log x_i = 82.50$$

$$n = \sum f_i$$

Using  $\textcircled{1}$  &  $\textcircled{2}$ .

$$G.M = \text{Antilog} \left( \frac{1}{88} (82.50) \right) \Rightarrow \sqrt{G.M = 8.65}$$

$$H.M = \left( \frac{10.50672}{88} \right)^{-1} \Rightarrow \sqrt{H.M = 8.37}$$

Ans  
2

## Median:-

Consider if we have such like data  
1, 2, 3, 70, 80, 90 & 1000

$$\text{So } A.M = \frac{1+2+3+70+80+90+1000}{7}$$

$$A.M = 178.$$

Which is not exact or appropriate central tendency. So in order to get appropriate mean we used median.

"Median of data is a number at or below which 50% of ordered data lies."

→ Usually mean tells about that value which lie in mid of given data while median also locate that value from data.

### Rules:- (For Raw data)

If  $\frac{n}{2}$  is not integer then the median is  $\left(\frac{n+1}{2}\right)$  while if  $\frac{n}{2}$  is integer then median is average of

$$\frac{n}{2} \text{ \& } \frac{n+1}{2}$$

→ Note:- In order to find median the data should be arranged in ascending order.



### Example # 3.11

Find the median & Quartile?

45, 32, 37, 46, 39, 36, 41, 48 & 36.

Solution:- First arrange data in ascending order

32, <sup>36,</sup> 36, 37, 39, 41, 45, 46, 48.

No. of data = 9.

$$\frac{n}{2} = \frac{9}{2} = 4.5 \quad \text{as not Integer}$$

So therefore the median will be;

$$\frac{n+1}{2} \Rightarrow \frac{9+1}{2} \Rightarrow (5).$$

The 5<sup>th</sup> position data is 39.

So median is 39.

For Quartile:-

$$\frac{n}{4} = \frac{9}{4} = 2.25 \quad \text{not integer.}$$

$$\text{So, } \frac{n}{4} + 1 \Rightarrow \frac{9}{4} + 1 = 2.25 + 1 = 3.25.$$

So marks obtain by 2<sup>nd</sup> student is  
quartile  
median = 36. Ans

## Median of ungroup frequency distributions:-

→ First organized data in ascending order.

(\*) find cumulative frequency.

(\*) Now if  $\frac{n}{2}$  is ~~not~~ integer for e.g. let the value that we get is 17. So we will see in Cum. freq. column the value if not found. So we take its range that this value which is lie b/w 15 & 20. So take 20 C. frequency & in front of that C. freq. we get the median of that value.

### Second Case:-

If we find  $\frac{n}{2}$  and then give such value which present in C. frequency then we will take average of that value which is in front of that found value and preceding value. Note those average values should be in x-column.

If  $\frac{n}{2}$  is <sup>not</sup> Integer:- (odd).

If we have odd number or we get number i.e. not integer then we use  $\frac{n+1}{2}$  if we get such value which



is not c. freq. column so we will consider range and take preceding one as median.  
E if it is present in c. freq. column  
So we will consider that value which is in front of that c. freq.

### For group frequency Distribution:-

- 1st step is to introduce class boundaries.
- 2- Find cumulative frequency column.
3. Find  $n/2$  and locate in c. freq. column to find median class.

Then used this formula for median class

$$\begin{array}{l} \text{Median Class} \\ \text{(Class boundary)} \\ \text{(LB - UB)} \end{array} = l + \frac{h}{f} \left( \frac{n}{2} - c \right)$$

$\therefore l =$  lower boundary

$h =$  class width

$f =$  frequency of median class.

$c =$  c. frequency of previous or preceding class.

### Example 3.12

The following distribution relates to the number of assistants in 50 total establishments.

No. of Assistants	0	1	2	3	4	5	6	7	8	9
f	3	4	6	7	10	6	5	5	3	1

Find the median number of assistants.

Also compute quartile & 7th decile.

Sol<sup>n</sup>: As this is example of ungrouped frequency distribution. So first we will find c. freq. row.

No. of Assistants	0	1	2	3	4	5	6	7	8	9
Frequency	3	4	6	7	10	6	5	5	3	1
c. frequency	3	7	13	20	30	36	41	46	49	50

Since

$$\frac{n}{2} = \frac{50}{2} = 25 \rightarrow \text{Integer.}$$

As there is 25 in c. frequency. So will consider c. freq. 30 column. In front of 30 we have 4.

So median is = 4.

For quartile =  $\frac{n}{4} = \frac{50}{4} = 12.5$  Not integer.

So consider 13th c. freq. by  $\frac{n+1}{2}$  rule So quartile is 2.



### Example # 3.13 :-

Find the median, quartiles and 8th decile for distribution of marks given below.

Marks	30-39	40-49	50-59	60-69	70-79	80-89
No. of students	8	87	190	304	211	85

90-99

20

### Solution:-

For grouped frequency distribution we need class boundaries, cumulative frequencies.

Class Boundaries	Frequency	Com. Frequency
29.5 - 39.5	8	8
39.5 - 49.5	87	95
49.5 - 59.5	190	285
59.5 - 69.5	304	589
69.5 - 79.5	211	800
79.5 - 89.5	85	885
89.5 - 99.5	20	905

Median will be lie in.

$$= \frac{905}{2} = 452.5^{th}$$

which is non integer so by  $\frac{n+1}{2}$  rule

The median class will be 59.5 - 69.5

Now use formula, i.e.

$$\text{Median} = l + \frac{h}{f} \left( \frac{n}{2} - c \right)$$

$$l = 59.5$$

$$h = 10$$

$$f = 304$$

$$\frac{n}{2} = 452.5$$

$$c = 285$$

— By putting values.

$$\text{Median} = 59.5 + \frac{10}{304} (452.5 - 285)$$

$\text{Median} = 65$

Ans  
✓